

# MATHS

# **BOOKS - UNITED BOOK HOUSE**

# **MODEL QUESTION PAPER SET 10**

#### Exercise

**1.** CHOOSE the correct answer from the following alternative : the domain for which the functions  $f(x)=3x^2 - 2x$  and g(x)=3(3x-2) are equal, will be -

A. {1,2/3}

B. {1,3}

C. {2/3,3}

D. {2/3,0}

#### Answer:

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2. choose the correct alternative :(ii) state which of the foll. Is the

value of 
$$\tan\left(\left(\frac{1}{3}\right)\left(\tan^{-1}x + \tan^{-1}\left(\frac{1}{x}\right)\right)\right)$$
 (x>0)?

A. 
$$\frac{1}{\sqrt{3}}$$

B. 
$$\sqrt{3}$$

C. 1

D. 0

#### Answer:

**3.** choose the correct answer from the given alternative : if A ia a square matrixof oreder 3 x 3, then the value of |KA| will be-

A. k|A|

 $\mathsf{B.}\,K^2|A|$ 

 $\mathsf{C}.\,K^3|A|$ 

D. 3K|A|

#### Answer:

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**4.** choose the correct alternative : (iv) the deriavtive of  $x^2$  w.r.t log

x is

B. 2

C. 2x

D.  $2x^3$ 

#### Answer:



5. choose the correct alternative : (v) the value of  $\int_{-1}^1 |x| dx$  is

A. 1

B. 2

C. 4

D. 44228

Answer:



6. choose the correct alternative :(viii) the perpendicular distance

of the point(1,2,3,) from the x-axis is -

A.  $\sqrt{5}$  units

B.  $\sqrt{13}$  units

C. 9 units

D. 13 units

#### Answer:



7. Three events A,B and C are mutually exclusive and exhaustive ,

if P(A)=3/5 and P(B)=1/6, then the value of P(C) is

A. 23/30

B. 
$$\frac{7}{30}$$
  
C.  $\frac{1}{10}$   
D.  $\frac{9}{10}$ 

#### Answer:



8. If f(x) is the probability distribution function of a random variable X and X can assume only two values  $x_1$  and  $x_2$  then the value of  $f(x_1) + f(x_2)$  is

A.  $\geq 1$ 

B.  $\leq 1$ 

 $\mathsf{C}. \ \geq 0$ 

#### Answer:

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9. answerer any one of the foll. :(ii) if two angles of a triangle are

$$\tan^{-1}\left(\frac{1}{2}\right)$$
 and  $\tan^{-1}\left(\frac{1}{3}\right)$ , then find the third angle.

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10. (b) answer any one of the foll.: (i) prove without expanding

$$egin{array}{c|c} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \end{array} = 0$$
 wher w is an imaginary cube root of unity.

11. answer any three of the foll. : (i) evaluate :  

$$\lim_{x \to \infty} \frac{e^{ax} + e^{\beta x} - 2}{x}$$
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12. find dy/dx, when  $e^{xy} - 4xy = 4$ 
  
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13. evaluate:  $\int \frac{dx}{\sin^2 x \cos^2 x}$ 
  
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() Watch Video Solution

14. Show that , the equation of all circles touchung the y -axis at the origin is  $2xy\frac{dy}{dx}=y^2-x^2.$ 

15. Find the interval in which the function  $f(x) = x^x (x > 0)$  is

decreasing.

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16. if a and b are any two constants, then prove that  $Var(aX+b) = a^2 Var(X).$ 

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17. prove that , 
$$an \left( 2 an^{-1} \sqrt{rac{1+\cos heta}{1-\cos heta}} 
ight) + an heta$$
 =0

**18.** answer the following : (ii) prove that,  $\begin{vmatrix} 2ab & a^2 & b^2 \\ a^2 & b^2 & 2ab \\ b^2 & 2ab & a^2 \end{vmatrix}$  =- $(a^3 + b^3)^2$ 

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19. answeer the following : (i) if  $y\sqrt{x^2+1}=\log\Bigl(\sqrt{x^2+1}-x\Bigr)$  , show that ,  $\bigl(x^2+1\bigr)rac{dy}{dx}+xy+1=0$ 

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20.

$$x=a( heta-\sin heta),y=a(1-\cos heta),showt,\ 2yrac{d^2y}{dx^2}+\cos ec^2rac{ heta}{2}=0$$

**21.** answer the following: (ii)evaluate:

$$\int\!\!rac{e^x(x-4)}{\left(x-2
ight)^3}dx$$

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22. evaluate : 
$$\int \frac{dx}{x^4 + x^2 + 1}$$

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23. answer the following : (iii) solve:  $rac{dy}{dx} = 1 + e^{2x-y}$  , given y=2

when x=2



**24.** evaluate : 
$$\int_{-1}^{2} \left|1-x^{2}\right| dx$$

**25.** Evaluate (with the help of definite integral):  $\lim_{n \to \infty} \left\{ \left( 1 + \frac{1}{n} \right) \left( 1 + \frac{2}{n} \right) \dots \left( 1 + \frac{n}{n} \right) \right\}^{\frac{1}{n}}$ Watch Video Solution

**26.** a problem on mathematics is given to three students A,B,C whose probabilities of solving it are 1/3,2/5and 3/4 . Find the probability that the problem is solved.

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**27.** the overall percentage of failures in a certain examination is 40 what is the probability that out of a group of 6 candidates at least 4 passed the examination ?



**28.** Prove that the equation of the palne which passes through the point (-1,3,2) and is perpendicular to the planes x+2y+2z=5 and 3x+3y+2z=8 is 2x-4y+3z+8=0.

