



MATHS

BOOKS - MODERN PUBLICATION MATHS (KANNADA ENGLISH)

APPLICATION OF DERIVATIVES

Multiple Choice Questions Level I Select The Correct Answer

1. The value of 'c' in Rolle's theorem for the function

$f(x) = x^3 - 3x$ in the interval $[0, \sqrt{3}]$ is :

A. 1

B. -1

C. $\frac{3}{2}$

D. $\frac{1}{3}$

Answer: A



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2. The abscissa of the point on the curve $3y = 6x - 5x^3$, the normal at which passes through origin is :

A. 1

B. $\frac{1}{3}$

C. 2

D. $\frac{1}{2}$

Answer: A



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3. The two curves $x^3 - 3xy^2 + 2 = 0$ and $3x^2y - y^3 - 2 = 0$

A. touch each other

B. cut at right angle

C. cut at an angle $\frac{\pi}{3}$

D. cut at an angle $\frac{\pi}{4}$

Answer: B



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4. The tangent to the curve given by :

$$x = e^t \cos t, y = e^t \sin t \text{ at } t = \frac{\pi}{4}$$

makes with x-axis an angle :

A. 0

B. $\frac{\pi}{4}$

C. $\frac{\pi}{3}$

D. $\frac{\pi}{2}$

Answer: D



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5. The equation of the normal to the curve $y = \sin x$ at $(0, 0)$ is :

A. $x = 0$

B. $y = 0$

C. $x + y = 0$

D. $x - y = 0$

Answer: C

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6. The point on the curve $y^2 = x$, where the tangent makes an angle of $\frac{\pi}{4}$ with x-axis is :

A. $\left(\frac{1}{2}, \frac{1}{4}\right)$

B. $\left(\frac{1}{4}, \frac{1}{2}\right)$

C. $(4, 2)$

D. $(1, 1)$

Answer: B

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7. The maximum value of $\sin x + \cos x$ is :

A. $\frac{1}{4}$

B. $\frac{1}{2}$

C. $\sqrt{2}$

D. $2\sqrt{2}$

Answer: C



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8. At $x = \frac{5\pi}{6}$, $f(x) = 2 \sin 3x + 3 \cos 3x$ is :

A. maximum

B. minimum

C. zero

D. neither maximum nor minimum.

Answer: D



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9. $f(x) = x^x$ has a stationary point at :

A. $x = e$

B. $x = \frac{1}{e}$

C. $x = 1$

D. $x = \sqrt{e}$

Answer: B



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10. The largest interval for which :

$$x^{12} - x^9 + x^4 - x + 1 > 0 \text{ is :}$$

A. $-4 < x \leq 0$

B. $0 < x < 1$

C. $-100 < x < 100$

D. $-\infty < x < \infty$

Answer: D



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11. Let f and g be increasing and decreasing functions respectively from $[0, \infty)$ to $[0, \infty)$, Let $h(x) = f(g(x))$. If $h(0) = 0$, then $h(x) - h(1)$ is :

- A. less than $-h(1)$
- B. always +ve
- C. always -ve
- D. strictly increasing.

Answer: A



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12. If the line $ax + by + c = 0$ is a normal to the curve $xy = 1$, then :

- A. $a > 0, b > 0$
- B. $a > 0, b < 0$ or $a < 0, b > 0$
- C. $a < 0, b < 0$
- D. None of these.

Answer: B



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13. The curve $y = x^{1/5}$ has at $(0, 0)$:

- A. a vertical tangent
- B. a horizontal tangent
- C. an oblique tangent
- D. no tangent.

Answer: A



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14. If $y = a \log x + bx^2 + x$ has its extreme values at $x = -1$ and $x = 2$, then :

A. $a = 2, b = -1$

B. $a = -2, b = \frac{1}{2}$

C. $a = 2, b = \frac{-1}{2}$

D. None of these.

Answer: C



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15. Let $P(x) = a_0 + a_1x^2 + a_2x^4 + a_3x^6 + \dots + a_nx^{2n}$ be a polynomial in a real variable x with $0 < a_0 < a_1 < a_2 < \dots < a_n$. The function $P(x)$ has :

- A. neither max. nor min.
- B. only on max.
- C. only one max. and one mini.
- D. only one minima.

Answer: D



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16. The maximum value of $\frac{\log x}{x}$ is :

- A. 1
- B. $2/e$
- C. e
- D. $\frac{1}{e}$

Answer: D



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17. If the slope of the normal to the curve $x^3 = 8a^2y$, $a > 0$ at a point in the first quadrant is $-\frac{2}{3}$, then the point is :

A. $(2a, -a)$

B. $(2a, a)$

C. $(a, 2a)$

D. $(-a, a)$.

Answer: B



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18. If a differentiable function $f(x)$ has a relative minimum at $x = 0$, then the function $y = f(x) + ax + b$ has a relative minimum at $x = 0$ for :

A. all a and all b

B. all $b > 0$

C. all b if $a = 0$

D. all $a > 0$

Answer: C



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19. The function $f(x) = x^3 - 3x$ is :

- A. increasing in $(-\infty, -1) \cup [1, \infty)$ and decreasing in $(-1, 1)$
- B. decreasing in $(-\infty, -1) \cup [1, \infty)$ and increasing in $(-1, 1)$
- C. increasing in $(0, \infty)$ and decreasing in $(-\infty, 0)$
- D. decreasing in $(0, \infty)$ and increasing in $(-\infty, 0)$.

Answer: A



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20. The number of values of k for which the equation $x^3 - 3x + k = 0$ has two distinct roots lying in the interval $(0, 1)$ is :

A. 3

B. 2

C. infinitely many

D. no value of k satisfies the requirement.

Answer: D



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21. The point on the curve $y = (x - 3)^2$, where the tangent is parallel to the chord joining $(3, 0)$ and $(4, 1)$ is :

A. $(-7/2, 1/4)$

B. $(5/2, 1/4)$

C. $(-5/2, 1/4)$

D. $(7/2, 1/4)$

Answer: D



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22. The length of the tangent of the curve $y = x^2 + 2$ at $(1, 3)$ is

(A) $\sqrt{5}$

(B) $3\sqrt{5}$

(C) $\frac{3}{2}$

(D) $\frac{3\sqrt{5}}{2}$



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23. The slope of the normal to the curve :

$$x = a(\cos \theta + \theta \sin \theta), y = a(\sin \theta - \theta \sin \theta)$$

at any point ' θ ' is :

A. $-\cot \theta$

B. $-\tan \theta$

C. $\cot \theta$

D. $\tan \theta$

Answer: A



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24. A stone is projected vertically upwards moves under the action of gravity alone and its motion is described by $x = 49t - 4.9t^2$. It is at a maximum height when :

A. $t = 0$

B. $t = 5$

C. $t = 10$

D. None of these.

Answer: B



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25. The function $f(x) = ax + b$, is strictly decreasing for all $x \in R$ iff :

A. $a = 0$

B. $a < 0$

C. $a > 0$

D. None of these.

Answer: B



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26. Tangents to the curve $y = x^3$ at points (1, 1) and (-1, -1) are :

A. intersecting but not at rt. angles

B. parallel

C. perpendicular

D. None of these.

Answer: C



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27. Let $f(x)$ be continuous in a neighbourhood of 'a' and $g(a) \neq 0$

g is continuous at $x=a$. Let f be a function such that

$f'(x) = g(x)(x - a)^2$, then :

A. f is decreasing at a if $g(a) > 0$

B. f is increasing at a if $g(a) > 0$

C. f is increasing at a if $g(a) < 0$

D. None of these.

Answer: B



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28. The slope of the tangent to the curve :

$$x = a \sin t, y = a \left(\cos t + \log \tan \frac{t}{2} \right)$$

at the point 't' is :

A. $\tan \frac{t}{2}$

B. $\cot t$

C. $\tan t$

D. None of these.

Answer: B



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29. Rolle's Theorem is not applicable to the function :

$f(x) = |x|$ in the interval $[-3, 3]$ because :

A. f is not derivable in $(-3, 3)$

B. $f(x) \geq 0 \forall x$ in $[-3, 3]$

C. $f(3) \neq f(-3)$

D. f is continuous in $(-3, 3)$

Answer: A



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30. Rolle's theorem holds for the function $f(x) = x^3 + bx^2 + cx$, $1 \leq x \leq 2$ at the point $\frac{4}{3}$, the values of b and c are :

- A. $b = 8, c = -5$
- B. $b = -5, c = 8$
- C. $b = 5, c = -8$
- D. $b = -5, c = -8$

Answer: B



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31. There exists a function $f(x)$ satisfying $f(0) = 1, f'(0) = -1, f(x) > 0$, for all x, then :

A. $f''(x) < -2$, for all x

B. $-2 \leq f''(x) \leq -1$, for all x

C. $1 \leq f''(x) < 0$ for all x

D. $f''(x) > 0$, for all x .

Answer: C



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32. Let $f(x) = x^3 - 6x^2 + 9x + 18$, then $f(x)$ is strictly decreasing in :

A. $(1, 3)$

B. $(-\infty, 1] \cup [3, \infty)$

C. $[3, \infty)$

D. $(-\infty, 1]$

Answer: A



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33. Let $f(x) = x^4 - 4x$, then :

A. f is increasing in $(-\infty, 1]$

B. f is increasing in $[1, \infty)$

C. f is decreasing in $[1, \infty)$

D. None of these

Answer: B



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34. If the graph of a differentiable function $y = f(x)$ meets the lines $y = -1$ and $y = 1$, then the graph :

- A. does not meet the line $y = 0$
- B. meets the line $y = 0$ atleast thrice
- C. meets the line $y = 0$ atleast twice
- D. meets the line $y = 0$ at least once.

Answer: D



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35. The equation of the tangent to the curve $y^2 = 4ax$ at the point $(at^2, 2at)$ is :

A. $tx + y = at^3$

B. $ty = x - at^2$

C. $ty = x + at^2$

D. None of these

Answer: C



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36. Let $f(x) = \frac{x}{1+x} - \log(1+x)$, when $x > 0$, then f is :

A. a decreasing function

B. neither increasing nor decreasing

C. an increasing function

D. None of these.

Answer: A

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37. In case of strictly increasing function, slope of the tangent and hence derivative is :

- A. zero
- B. either positive or zero
- C. negative
- D. positive.

Answer: B

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38. Let $f(x) = x^3 + \frac{3}{2}x^2 + 3x + 3$, then $f'(x)$ is :

- A. a decreasing function
- B. an increasing function
- C. an odd function
- D. an even function.

Answer: B



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39. Let $f(x) = x - \cos x, x \in R$, then f is :

- A. a decreasing function
- B. an increasing function
- C. an odd function
- D. None of these.

Answer: B



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40. The acceleration of a moving particle whose space time equation is given by $s = 3t^2 + 2t - 5$ is :

A. 6

B. 5

C. 0

D. 1

Answer: A



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41. The normal to a given curve is parallel to x-axis if :

A. $\frac{dx}{dy} = 1$

B. $\frac{dx}{dy} = 0$

C. $\frac{dy}{dx} = 0$

D. $\frac{dy}{dx} = 1$

Answer: B



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42. The equation of the normal at the point 't' to the curve

$x = at^2, y = 2at$ is :

A. $tx + y = 2at + at^3$

B. $tx + y = 2at$

C. $tx + y = at^2$

D. None of these.

Answer: A



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43. The function $f(x) = \frac{x}{|1 + |x||}$ is :

A. not differentiable at $x = 0$

B. strictly increasing

C. strictly decreasing

D. neither increasing nor decreasing.

Answer: B



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44. The point on the curve $y = x^2$, where slope of the tangent is equal to the x-coordinate of the point is :

A. $\left(-\frac{1}{2}, \frac{1}{2}\right)$

B. $(0, 0)$

C. $(2, 0)$

D. $(0, 2)$

Answer: B



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45. The equation of the horizontal tangent to the curve $y = e^x + e^{-x}$ is :

A. $y = -2$

B. $y = -3$

C. $y = 2$

D. None of these.

Answer: C



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46. The points on the curve $y = 12x - x^3$, the tangents at which are parallel to x-axis are :

A. $(-2, 16)$ and $(2, -16)$

B. $(2, 16)$ and $(-2, -16)$

C. $(2, 16)$ and $(-2, 16)$

D. None of these.

Answer: B



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47. Let $f(x) = \frac{\log x}{x} + \log 51$, then $f(x)$ is :

- A. $f'(x) = 0$ for $x = 2e^3$
- B. decreasing for $2 < x < e$
- C. increasing for $x > e$
- D. decreasing for $x > e$.

Answer: D



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48. The function $f(x) = \tan x$ for all real

$x \neq \pm \frac{\pi}{2}, \pm \frac{3\pi}{2}, \dots$ is :

- A. increasing
- B. decreasing
- C. neither decreasing nor increasing
- D. None of these.

Answer: A



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49. Rolle's theorem is applicable in case of $f(x) = a^{\sin x}$ in :

- A. interval $(0, \pi/2)$
- B. any interval

C. interval $(0, \pi)$

D. None of these.

Answer: D



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50. The value of k in order that $f(x) = \sin x - \cos x - kx + b$ decrease for all real values is given by :

A. $k < \sqrt{2}$

B. $k \geq \sqrt{2}$

C. $k < 1$

D. $k \geq 1$

Answer: B

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51. A particle moves so that the space described in time 't' is square root of a quadratic function of 't', then

A. acc. varies as s^3

B. acc. varies as $\frac{1}{s}$

C. acc. varies as $\frac{1}{s^3}$

D. None of these.

Answer: C

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52. Maximum value of $f(x) = \sin x + \cos x$ is :

A. 1

B. 2

C. $\frac{1}{\sqrt{2}}$

D. $\sqrt{2}$

Answer: D



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53. The function $f(x) = \sum_{k=1}^5 (x - k)^2$ assumes minimum value

for x given by:

A. 5

B. $5/2$

C. 3

D. 2

Answer: C



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54. Let x and y be two variables such that $x > 0$ and $xy = 1$. Then the minimum value of $x+y$ is

A. 2

B. -2

C. 1

D. None of these.

Answer: C



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55. On uniform heating, the side of a square sheet of metal is increasing at the rate of 0.02 cm/sec. The rate at which the area is increasing when the side is 10 cm long is :

A. $0.4\text{cm}^2 / \text{sec}$

B. $0.2\text{cm}^2 / \text{sec}$

C. $4.0\text{cm}^2 / \text{sec}$

D. $40\text{cm}^2 / \text{sec}.$

Answer: A



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56. The greatest value of

$f(x) = \cos\left(xe^{[x]} + 7x^2 - 3x\right), x \in [-1, \infty)$ is :

A. -1

B. 1

C. 0

D. None of these.

Answer: B



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57. The function $f(x) = x + \frac{4}{x}$ has :

A. a local maxima at $x = 2$ and a local minima at $x = -2$

B. local minima at $x = 2$ and a local maxima at $x = -2$

C. absolute maxima at $x = 2$ and absolute minima at $x = -2$

D. absolute minima at $x = 2$ and absolute maxima at $x = -2$.

Answer: B



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58. Let $f(x) = (x^2 - 4)^{1/3}$, then f has a :

- A. local maxima at $x = 0$
- B. local minima at $x = 0$
- C. point of inflexion at $x = 0$
- D. None of these.

Answer: B



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59. The function $f(x) = 2 + 4x^2 + 6x^4 + 8x^6$ has :

- A. only one maxima
- B. only one minima
- C. no maxima and minima
- D. many maxima and minima.

Answer: B



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60. The function $f(x) = |x|$ has:

- A. only one minima
- B. only one maxima
- C. no maxima or minima
- D. None of these.

Answer: A



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61. If $f(x) = x + \frac{1}{x}$, then :

- A. relative minimum gt relative maximum
- B. relative maximum gt relative minimum
- C. relative maximum does not exist
- D. relative minimum does not exist.

Answer: A



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62. Let $f(x) = \cos x \sin 2x$, then :

A. $\min. f(x) > -\frac{2}{9}$ for $x \in (-\pi, \pi)$

B. $\min. f(x) > -\frac{1}{9}$ for $x \in [-\pi, \pi]$

C. $\min. f(x) = -\frac{1}{3\sqrt{3}}$ for $x \in [-\pi, \pi]$

D. $\min. f(x) > \frac{-9}{7}$ or $\frac{-7}{9}$ for $x \in [-\pi, \pi]$.

Answer: D



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63. Let $f(x)$ have second derivative at c such that $f'(c) = 0$ and $f''(c) > 0$, then c is a point of :

A. inflexion

B. local maxima

C. local minima

D. None of these.

Answer: C



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64. The function $f(x) = 2x^3 - 3x^2 - 12x + 4$ has :

- A. no maxima and minima
- B. two maxima
- C. two minima
- D. one maxima and one minima.

Answer: D



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65. A circle of radius unity is inscribed in an isosceles triangle.

The least perimeter of the triangle is :

A. $6\sqrt{3}$

B. 9

C. $2\sqrt{3}$

D. $3\sqrt{3}$

Answer: A



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66. The greatest value of :

$$f(x) = \cos \left[x e^{[x]} + 7x^2 - 3x \right], x \in [-1, \infty) \text{ is :}$$

A. 0

B. -1

C. 1

D. None of these.

Answer: C



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67. If $f'(x) = (x - a)^{2n}(x - b)^{2p+1}$, when n and p are positive integers, then :

A. $x = a$ is a point of maxima

B. $x = a$ is a point of minima

C. $x = a$ is neither a point of maxima nor a point of minima

D. None of these.

Answer: C



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68. If $f'(x) = (x - a)^{2n}(x - b)^{2m+1}$, where $m, n \in N$, then :

- A. $x = b$ is a point of inflexion
- B. $x = b$ is a point of minima
- C. $x = b$ is a point of maxima
- D. None of these.

Answer: B



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69. The minimum value of $2(x^2 - 3)^3 + 27$ is :

A. 2^{27}

B. 2

C. 1

D. None of these.

Answer: C



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70. A stone is thrown vertically upwards and the height x ft, reached by the stone in t seconds is given by $x = 80t - 16t^2$.

The stone reaches the maximum height in

A. 2

B. 4

C. 3

D. 2.5.

Answer: D



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71. A particle moves along x-axis so that its position is given by $x = 2t^3 - 3t^2$ at times t seconds. What is the time interval during which the particle will be on the negative half of the axis ?

A. $0 < t < \frac{2}{3}$

B. $0 < t < 1$

C. $0 < t < 3/2$

D. $\frac{1}{2} < t < 1.$

Answer: C



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72. The velocity v m/sec of particle is proportional to the cube of the time. If the velocity after 2 secs is 4m/sec, then v is equal to :

A. t^3

B. $\frac{t^3}{2}$

C. $\frac{t^3}{3}$

D. $\frac{t^3}{4}$

Answer: B



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73. Maximum slope of the curve $y = -x^3 + 3x^2 + 9x - 27$ is :

A. 0

B. 12

C. 16

D. 32

Answer: B



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74. Let $f(x) = 2x^3 - 3x^2 - 12x + 5$ on $[-2, 4]$. The relative maxima occurs at $x =$

A. -2

B. -1

C. 2

D. 4

Answer: D



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75. The function which is neither decreasing nor increasing in $(\pi/2, 3\pi/2)$, is :

A. $\cos x$

B. $\tan x$

C. x^2

D. $|x - 1|$

Answer: A



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76. The maximum value of $f(x) = \frac{x}{1 + 4x + x^2}$ on $[-1, 1]$ is :

A. $-\frac{1}{4}$

B. $-\frac{1}{3}$

C. $\frac{1}{6}$

D. $\frac{1}{5}$

Answer: C



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77. The abscissae of the points of the curve $y = x(x - 2)(x - 4)$, where tangents are parallel to x-axis, is obtained as :

A. $x = 2 \pm \frac{2}{\sqrt{3}}$

B. $x = 1 \pm \frac{1}{\sqrt{3}}$

C. $x = 2 \pm \frac{1}{\sqrt{3}}$

D. $x = \pm 1$

Answer: A



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78. Let $f(x) = [e^x(x-1)(x-2)]$. Then f decrease in the interval :

A. $(-\infty, -2)$

B. $(-2, -1)$

C. $(1, 2)$

D. $(2, +\infty)$

Answer: C



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79. For all $x \in (0, 1)$:

A. $e^x < 1 + x$

B. $\log(1 + x) < x$

C. $\sin x > x$

D. $\log_e x > x$

Answer: B



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80. The function $f(x) = \cot^{-1} x + x$ increases in the interval :

A. $(1, \infty)$

B. $(-1, \infty)$

C. $(-\infty, \infty)$

D. $(0, \infty)$

Answer: C



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81. The real number x when added to its inverse gives the minimum value of the sum at x equal to :

A. 1

B. -1

C. -2

D. 2

Answer: A



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82. Find which function does not obey Mean Value Theorem in $[0, 1]$:

$$\text{A. } f(x) = \begin{cases} \frac{1}{2} - x, & x < \frac{1}{2} \\ \left(\frac{1}{2} - x\right)^2, & x \geq \frac{1}{2} \end{cases}$$

$$\text{B. } f(x) = \begin{cases} \frac{\sin x}{x}, & x \neq 0 \\ 1, & x = 0 \end{cases}$$

$$\text{C. } f(x) = x|x|$$

$$\text{D. } f(x) = |x|$$

Answer: A



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83. A point on the parabola $y^2 = 18x$ at which the ordinate increases at twice the rate of the abscissa is :

A. (2, 4)

B. (2, -4)

C. $\left(-\frac{9}{8}, \frac{9}{2}\right)$

D. $\left(\frac{9}{8}, \frac{9}{2}\right)$

Answer: D



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84. The normal to the curve $x = a(1 + \cos \theta)$, $y = a \sin \theta$ at ' θ ' always passes through the fixed point :

A. (a, 0)

B. (0, a)

C. (0, 0)

D. (a, a)

Answer: A



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85. A function $y = f(x)$ has a second order derivative $f''(x) = 6(x - 1)$. If its graph passes thro' the point (2, 1) and at the point the tangent to the graph is $y = 3x - 5$, then the function is :

A. $(x + 1)^3$

B. $(x - 1)^3$

C. $(x - 1)^2$

D. $(x + 1)^2$

Answer: B



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86. If $f(x) = x^3 + bx^2 + cx + d$ and $0 < b^2 < c$, then in $(-\infty, \infty)$, $f(x)$:

A. is increasing

B. has real maximum

C. is decreasing

D. is bounded.

Answer: A



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87. If $f(x) = x^\alpha \log x$ and $f(0) = 0$, then the value of α for which Roll's theorem can be applied in $[0, 1]$ is :

A. -2

B. -1

C. 0

D. $\frac{1}{2}$

Answer: D



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88. If $f(x)$ is differentiable increasing function, then

$\lim_{x \rightarrow 0} \frac{f(x^2) - f(x)}{f(x) - f(0)}$ equals :

A. 1

B. 0

C. -1

D. 2

Answer: C



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89. The normal to the curve :

$$x = a(\cos \theta + \theta \sin \theta), y = a(\sin \theta - \theta \cos \theta)$$

at any point ' θ ' is such that:

A. it makes angle $\frac{\pi}{2} + \theta$ with the x-axis

B. it passes through the origin

C. it is at a constant distance from the origin

D. it passes through $\left(\frac{a\pi}{2}, -a\right)$

Answer: A



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90. A function is matched below against an interval where it is supposed to be increasing. Which of the following parts is incorrectly matched?

A.

Interval	Function
$[2, \infty)$	$2x^3 - 3x^2 - 12x + 6$

B.

Interval	Function
$(-\infty, \infty)$	$x^3 - 3x^2 + 3x + 3$

C.

Interval	Function
$(-\infty, -4]$	$x^3 + 6x^2 + 6$

D.

Interval	Function
$\left(-\infty, \frac{1}{3}\right]$	$3x^3 - 2x + 1$

Answer: D



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91. Let f be differentiable for all x . If $f(1) = -2$, $f'(x) \geq 2$ for all $x \in [1, 6]$, then :

A. $f(6) < 8$

B. $f(6) \geq 8$

C. $f(6) = 5$

D. $f(6) = 5$

Answer: B



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92. The function $f(x) = \frac{x}{2} + \frac{2}{x}$ has a local minimum at :

A. $x = 2$

B. $x = -2$

C. $x = 0$

D. $x = 1$

Answer: A



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93. Angle between the tangents to the curve $y = x^2 - 5x + 6$ at the points $(2, 0)$ and $(3, 0)$ is :

A. $\pi / 2$

B. $\pi / 3$

C. $\pi / 6$

D. $\pi / 4$

Answer: A

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94. The function $f(x) = \tan^{-1}(\sin x + \cos x)$ is an increasing function in :

A. $\left(-\frac{\pi}{2}, \frac{\pi}{4}\right)$

B. $\left(0, \frac{\pi}{2}\right)$

C. $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

D. $\left(\frac{\pi}{4}, \frac{\pi}{2}\right)$

Answer: A

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95. A value of c for which the conclusion of Mean Value Theorem holds for the function $f(x) = \log_e x$ on the interval $[1, 3]$ is :

A. $\frac{1}{2}\log_e^3$

B. $\log_3 e$

C. \log_e^3

D. $2\log_3 e$

Answer: D



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Multiple Choice Questions Level II

1. Let $f(x)$ satisfy the requirements of Lagrange's Mean Value Theorem in $[0, 2]$. If $f(0) = 0$ and $|f'(x)| \leq \frac{1}{2}$, for all x in $[0, 2]$, then :

A. $f(x) \leq 2$

B. $|f(x)| \leq 1$

C. $f(x) = 2x$

D. $f(x) = 3$, for at least one x in $[0, 2]$

Answer: B



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2. AB is a diameter of a circle and C is any point on the circumference of the circle, then :

A. the area of $\triangle ABC$ is max. when it is isosceles

B. the area of $\triangle ABC$ is minimum when it is isosceles

C. the perimeter of ABC is minimum when it is isosceles

D. None of these.

Answer: A



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3. Two towns A and B are 60 km apart. A school is to be built to serve 150 students in town A and 50 students in town B. If the total distance to be travelled by all 200 students is to be as small as possible, then the school should be built at :

- A. town B
- B. 45 km from town A
- C. town A
- D. 45 km from town B

Answer: C



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4. Let $f(x)$ be a quadratic expression, which is positive for all real

x . If $g(x) = f(x) + f'(x) + f''(x)$, then for any real x :

A. $g(x) < 0$

B. $g(x) > 0$

C. $g(x) \leq 0$

D. $g(x) \geq 0$

Answer: B



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5. The normal to the curve :

$$x = a(\cos \theta + \theta \sin \theta), y = a(\sin \theta - \theta \cos \theta)$$

at any point ' θ ' is such that:

- A. it makes a constant angle with x-axis
- B. it passes through the origin
- C. it is at a constant distance from the origin
- D. None of these.

Answer: C



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6. The line $\frac{x}{a} + \frac{y}{b} = 1$ touches the curves $y = be^{-x/a}$ at the point :

- A. $(a, b/a)$
- B. $(-a, ba)$
- C. $(a, a/b)$
- D. None of these.

Answer: D



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7. The curves $y = x^2$ and $6y = 7 - x^3$ intersect at the point (1, 1) at an angle :

A. $\pi / 4$

B. $\pi / 3$

C. $\pi / 2$

D. None of these.

Answer: C



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8. The curve $\left(\frac{x}{a}\right)^n + \left(\frac{y}{b}\right)^n = 2$ touches the straight line $\frac{x}{a} + \frac{y}{b} = 2$ at the point (a, b) :

- A. for $x = 3$
- B. for $x = 2$
- C. for any value of n
- D. for no value of n .

Answer: C



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9. Let $f(x)$ and $g(x)$ be differentiable for $0 \leq x \leq 1$ such that $f(0) = 0, g(0) = 0, f(1) = 6$. Let there exist a real number c in $(0, 1)$ such that $f'(c) = 2g'(c)$, then the value of $g(1)$ must be :

A. 1

B. 3

C. -2

D. -1

Answer: B



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10. A cannon ball is fired at an angle θ , $0 < \theta < \pi/2$, with the horizontal. If v is the initial velocity of the cannon ball, the height h of the ball at time t , ignoring the air resistance, is given by :

$$h = (v \sin \theta)t - 4.9t^2.$$

The value of θ so that the horizontal range of the ball is maximum is :

A. $\pi / 6$

B. $\pi / 6$

C. $\pi / 3$

D. $3\pi / 4$

Answer: B



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11. The area of the triangle formed by the co-ordinate axes and a tangent to the curve $xy = a^2$ at the point (x_1, y_1) on it is :

A. $\frac{a^2 x_1}{y_1}$

B. $\frac{a^2 y_1}{x_1}$

C. $2a^2$

D. $4a^2$

Answer: C



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12. If $a + b + c = 0$, then the equation $3ax^2 + 2bx + c = 0$ has :

- A. at least one real root in $(0, 1)$
- B. one root is $(-1, 0)$ and other in $(1, 2)$
- C. both imaginary roots
- D. two coincident roots.

Answer: A



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13. Let $f(x)$ be twice differentiable on $[1, 3]$, and let $f(1) = f(3)$.

Further if $|f''(x)| \leq 2$, then for all x in $[1, 3]$:

A. $-1 \leq f'(x) \leq 1$

B. $-4 < f'(x) < 4$

C. $|f'(x)| > 2$

D. $|f'(x)| < 4$

Answer: D



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14. Let f be a real valued function defined on $(0, 1) \cup (2, 4)$, such that $f(x) = 0$, for every x , then :

A. f is a constant function if $f\left(\frac{1}{2}\right) = 0$

B. f is not a constant function

C. f is a constant function $f(1/2) = f(3)$

D. f is a constant function.

Answer: C



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15. If $x \in (0, \pi/2)$, then :

A. $\tan x < x < \sin x$

B. $x < \sin x < \tan x$

C. $\sin x < x < \tan x$

D. None of these.

Answer: C

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16. The curve $y = ax^3 + bx^2 + cx$ is inclined at 45° to X-axis at $(0, 0)$, but it touches X-axis at $(1, 0)$, then the values of a, b, c are given by:

A. $a = -1, b = 2, c = 1$

B. $a = 1, b = -2, c = 1$

C. $a = 1, b = 1, c = -2$

D. $a = -2, b = 1, c = 1$

Answer: B

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17. If $\log_{0.3}(x - 1) < \log_{0.09}(x - 1)$, then x lies in the interval :

A. $(-2, -1)$

B. $(1, 2)$

C. $(2, \infty)$

D. None of these.

Answer: C



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18. The angle of intersection of the two curves $xy = a^2$ and $x^2 - y^2 = 2b^2$ is :

A. $\pi/3$

B. $\pi/6$

C. $\pi/4$

D. None of these.

Answer: D



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19. The length of subtangent to the curve $x^2 + xy + y^2 = 7$ at $(1, -3)$ is :

A. $3/5$

B. 3

C. $5/3$

D. 15

Answer: D



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20. The equation $3x^2 + 4ax + b = 0$ has atleast one root in $(0, 1)$ if :

A. $b = 0, a = -4/3$

B. $4a + b + 3 = 0$

C. $2a + b + 1 = 0$

D. None of these.

Answer: C



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21. The curve $y - e^{xy} + x = 0$ has a vertical tangent at the point :

A. $(1, 0)$

B. (0, 0)

C. (1, 1)

D. at no point

Answer: A



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22. If the normal to the curve $y = f(x)$ at the point $(3, 4)$ makes an angle $3\pi/4$ with the positive x-axis, then $f'(3)$ is :

A. -1

B. $\frac{-3}{4}$

C. $\frac{4}{3}$

D. 1

Answer: D



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23. If $x + y = k$ is normal to $y^2 = 12x$, then k is :

A. 3

B. 9

C. -9

D. -3

Answer: B



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24. The two curves $x^3 - 3xy^2 + 2 = 0$ and $3x^2y - y^3 - 2 = 0$:

A. cut at right angles

B. touch each other

C. cut at an angle $\frac{\pi}{3}$

D. cut at an angle $\frac{\pi}{4}$

Answer: A



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25. The greatest distance of the point P(10, 7) from the circle

$$x^2 + y^2 - 4x - 2y - 20 = 0 \text{ is :}$$

A. 10

B. 15

C. 5

D. None of these.

Answer: B



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26. The greatest value of $f(x) = (x + 1)^{1/3} - (x - 1)^{1/3}$ on $[0, 1]$ is :

A. 1

B. 2

C. 3

D. $\frac{1}{3}$

Answer: B



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27. The point(s) on the curve $y^3 + 3x^2 = 12y$, where the tangent is vertical, is (are) :

A. $\left(\pm \frac{4}{\sqrt{3}}, -2 \right)$

B. $\left(\pm \sqrt{\frac{11}{3}}, 1 \right)$

C. (0, 0)

D. $\left(\pm \frac{4}{\sqrt{3}}, 2 \right)$

Answer: D



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28. If the function $f(x) = 2x^3 - 9ax^2 + 12a^2x + 1$, where $a > 0$ attains its maximum and minimum at p and q respectively such their $p^2 = q$, then a equals :

A. 1

B. 2

C. $\frac{1}{2}$

D. 3

Answer: B



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29. If minimum value of $f(x) = x^2 + 2bx + 2c^2$ is greater than maximum value of $g(x) = -x^2 - 2cx + b^2$, then for x is real :

A. $|c| > |b|\sqrt{2}$

B. $|c|\sqrt{2} > b$

C. $0 < c < \sqrt{2}b$

D. no real value of a.

Answer: A



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30. The line $2x + \sqrt{6}y = 2$ is a tangent to the curve $x^2 - 2y^2 = 4$. The point of contact is :

A. $(4, -\sqrt{6})$

B. $(7, -2\sqrt{6})$

C. $(2, 3)$

D. $(\sqrt{6}, 1)$

Answer: A



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31. A spherical iron ball 10 cm in radius is coated with a layer of ice of uniform thickness that melts at a rate of $50\text{cm}^3/\text{min}$. When the thickness of ice is 5 cm, then the rate at which the thickness of ice decreases, is :

A. $\frac{1}{18\pi}$ cm/min

B. $\frac{1}{36\pi}$ cm/min

C. $\frac{5}{6\pi}$ cm/min

D. $\frac{1}{54\pi}$ cm/min

Answer: A



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32. Suppose the cubic $x^3 - px + q$ has three distinct real roots, where $p > 0$ and $q > 0$. Then which one of the following holds ?

- A. The cubic has maxima at both $\sqrt{\frac{p}{3}}$ and $-\sqrt{\frac{p}{3}}$
- B. The cubic has minima at $\sqrt{\frac{p}{3}}$ and maxima at $-\sqrt{\frac{p}{3}}$
- C. The cubic has minima at $-\sqrt{\frac{p}{3}}$ and maxima at $\sqrt{\frac{p}{3}}$
- D. The cubic has minima at both $\sqrt{\frac{p}{3}}$ and $-\sqrt{\frac{p}{3}}$.

Answer: B



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33. The total number of local maxima and local minima of the function :

$$f(x) = \begin{cases} (2+x)^3, & -3 < x \leq -1 \\ x^{\frac{2}{3}}, & -1 < x < 2 \end{cases} \text{ is :}$$

A. 0

B. 1

C. 2

D. 3

Answer: C



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34. Let the function $g: (-\infty, \infty) \rightarrow \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$ be given by $g(u) = 2 \tan^{-1}(e^u) - \frac{\pi}{2}$. Then g is :

A. even and is strictly increasing in $(0, \infty)$

B. odd and is strictly decreasing in $(-\infty, \infty)$

C. odd and is strictly increasing in $(-\infty, \infty)$

D. neither even nor odd, but is strictly increasing in $(-\infty, \infty)$

Answer: C



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35. Given $P(x) = x^4 + ax^3 + bx^2 + cx + d$ such that $x = 0$ is the only real root of $P'(x) = 0$. If $P(-1) < P(1)$, then in the interval $[-1, 1]$:

- A. $P(-1)$ is the minimum and $P(1)$ is the maximum of P
- B. $P(-1)$ is not the minimum and $P(1)$ is the maximum of P
- C. $P(-1)$ is the minimum but $P(1)$ is not the maximum of P
- D. neither $P(-1)$ is the minimum nor $P(1)$ is the maximum of P .

Answer: B

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1. The equation of the tangent to the curve $y = x + \frac{4}{x^2}$, that is parallel to the x-axis, is :

A. $y = 0$

B. $y = 1$

C. $y = 2$

D. $y = 3$

Answer: D



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2. Let $f: R \rightarrow R$ be a positive increasing function with

$$\lim_{x \rightarrow \infty} \frac{f(3x)}{f(x)} = 1. \text{ Then } \lim_{x \rightarrow \infty} \frac{f(2x)}{f(x)} =$$

A. 1

B. $\frac{2}{3}$

C. $\frac{3}{2}$

D. 3

Answer: A



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3. Let $f: R \rightarrow R$ be defined by :

$$f(x) = \begin{cases} k - 2x, & \text{if } x \leq -1 \\ 2x + 3, & \text{if } x > -1 \end{cases}.$$

If f has a local maximum at $x = -1$, then a possible value of k is :

A. 1

B. 0

C. $-\frac{1}{2}$

D. -1

Answer: D



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4. Let f, g and h be real-valued functions defined on the interval $[0, 1]$ by:

$$f(x) = e^{x^2} + e^{-x^2}, g(x) = xe^{x^2} + e^{-x^2} \text{ and } h(x) = x^2e^{x^2} + e^{-x^2}$$

.

If a, b and c denote respectively the absolute maximum of f, g and h on $[0, 1]$, then :

A. $a = b$ and $c \neq b$

B. $a = c$ and $a \neq b$

C. $a \neq b$ and $c \neq b$

D. $a = b = c$.

Answer: D



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5. The shortest distance between $y - x = 1$ and curve $x = y^2$ is :

A. $\frac{\sqrt{3}}{4}$

B. $\frac{3\sqrt{2}}{8}$

C. $\frac{8}{3\sqrt{2}}$

D. $\frac{4}{\sqrt{3}}$

Answer: B



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6. The shortest distance between $y - x = 1$ and curve $x = y^2$ is :

A. $\frac{3\sqrt{2}}{8}$

B. $\frac{2\sqrt{3}}{8}$

C. $\frac{3\sqrt{2}}{5}$

D. $\frac{\sqrt{3}}{4}$

Answer: A



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7. A spherical balloon is filled with 4500π cubic metres of helium gas. If a leak in the balloon causes the gas to escape at the rate of 72π cubic metres per minute, then the rate (in metres per

minute) at which the radius of the balloon decreases 49 minutes after the leakage begins is :

A. $\frac{9}{7}$

B. $\frac{7}{9}$

C. $\frac{2}{9}$

D. $\frac{9}{2}$

Answer: C



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8. The real number k for which the equation :

$2x^3 + 3x + k = 0$ has two distinct real roots in $[0, 1]$:

A. lies between 2 and 3

B. lies between -1 and 0

C. does not exist

D. lies between 1 and 2.

Answer: C



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9. The number of points in $(-\infty, \infty)$, for which $x^2 - x \sin x - \cos x = 0$, is :

A. 6

B. 4

C. 2

D. 0

Answer: C

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10. If f and g are differentiable functions in $[0, 1]$ satisfying $f(0) = 2 = g(1)$, $g(0) = 0$ and $f(1) = 6$, then for some $c \in [0, 1]$:

A. $2f'(c) = 3g'(c)$

B. $f'(c) = g'(c)$

C. $f'(c) = 2g'(c)$

D. $2f'(c) = g'(c)$

Answer: C

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11. If $x = -1$ and $x = 2$ are extreme points of :

$f(x) = \alpha \log|x| + \beta x^2 + x$, then :

A. $\alpha = -6, \beta = -\frac{1}{2}$

B. $\alpha = 2, \beta = -\frac{1}{2}$

C. $\alpha = 2, \beta = \frac{1}{2}$

D. $\alpha = -6, \beta = \frac{1}{2}$

Answer: B



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12. The normal to the curve, $x^2 + 2xy - 3y^2 = 0$, at $(1, 1)$:

A. does not meet the curve again

B. meets the curve again in the second quadrant

C. meets the curve again in the third quadrant

D. meets the curve again in the fourth quadrant.

Answer: D



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13. Let $f(x)$ be a polynomial of degree four having extreme values

at $x = 1$ and $x = 2$. If $\lim_{x \rightarrow 0} \left[1 + \frac{f(x)}{x^2} \right] = 3$, then $f(2)$ is equal to :

A. -8

B. -4

C. 0

D. 4

Answer: C

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1. P is the point of contact of the tangent from the origin to the curve $y = \log_e^x$. the length of the perpendicular drawn from the origin to the normal at P is

A. $\sqrt{e^2 + 1}$

B. $2\sqrt{e^2 + 1}$

C. $\frac{1}{e}$

D. $\frac{1}{2e}$

Answer: A

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2. For the curve $4x^5 = 5y^4$, the ratio of the cube of the sub-tangent at a point on the curve to the square of the sub-normal at the same point is :

A. $\left(\frac{5}{4}\right)^4$

B. $\left(\frac{4}{5}\right)^4$

C. $y\left(\frac{5}{4}\right)^4$

D. $x\left(\frac{4}{5}\right)^5$

Answer: B



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3. The set of real values of x for which $f(x) = \frac{x}{\log x}$ is increasing is :

A. $\{1\}$

B. $\{x : x < e\}$

C. empty

D. $\{x : x \geq e\}$

Answer: D



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4. A wire of length 20 cm is bent in the form of a sector of a circle. The maximum area that can be enclosed by the wire is

A. 30 sq. cm

B. 10 sq. cm

C. 25 sq. cm

D. 20 sq. cm

Answer: C



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5. If for the curve $y = 1 + bx - x^2$ the tangent at $(1, -2)$ is parallel to x-axis, then $b =$

A. 2

B. -2

C. 1

D. -1

Answer: D



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6. The slopes of the tangent and normal at $(0, 1)$ for the curve $y = \sin x + e^x$ are respectively :

A. 1 and -1

B. $-\frac{1}{2}$ and 2

C. 2 and $-\frac{1}{2}$

D. -1 and 1

Answer: C



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7. A stone is thrown vertically upwards and the height x ft, reached by the stone in t seconds is given by $x = 80t - 16t^2$.

The stone reaches the maximum height in

A. 2 secs

B. 2.5 secs

C. 3 secs

D. 3.5 secs.

Answer: B



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8. If $\sin^{-1} a$ is the acture angle between the curves

$x^2 + y^2 = 4x$ and $x^2 + y^2 = 8$ at $(2,2)$, then $a =$

A. 1

B. 0

C. $\frac{1}{\sqrt{2}}$

D. $\frac{\sqrt{3}}{2}$

Answer: C



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9. The maximum area of rectangle that can be inscribed in a circle of radius 2 units is :

A. 8π sq. units

B. 4 sq. units

C. 5 sq. units

D. 8 sq. units

Answer: D



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10. A stone is dropped into a quiet lake and waves in circles at the speed of 5 cm/s. At the instant when the radius of the circular wave is 8 cm, how fast is the enclosed area increasing?

A. $8xcm^2 / s$

B. $80\pi cm^2 / s$

C. $6\pi cm^2 / s$

D. $\frac{8}{3}cm^2 / s$

Answer: B



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11. A gardener is digging a plot of land. As he gets tired, he works more slowly, After 't' minutes he is digging at a rate of $\frac{2}{\sqrt{t}}$

square metres per minute. How long will it take him to dig an area of 40 square metres ?

- A. 10 minutes
- B. 40 minutes
- C. 100 minutes
- D. 30 minutes.

Answer: C



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12. If $f(x) = x^3$ and $g(x) = x^3 - 4x$ in $-2 < x < 2$, then consider the statements :

- (a) $f(x)$ and $g(x)$ satisfy Mean Value Theorem
- (b) $f(x)$ and $g(x)$ both satisfy Rolle's theorem

(c) Only $g(x)$ satisfies Rolle's theorem.

OF THE STATEMENTS

- A. (a) alone is correct
- B. (a) and (c) are correct
- C. (a) and (b) are correct
- D. None is correct.

Answer: B



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13. The tangent to the curve $y = x^3 + 1$ at $(1, 2)$ makes an angle θ with y-axis, then the value of $\tan \theta$ is

A. 3

B. $\frac{1}{3}$

C. $-\frac{1}{3}$

D. -3

Answer: B



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14. The maximum value of $\left(\frac{1}{x}\right)^{2x^2}$ is :

A. $e^{1/2}$

B. $(e)^{1/e}$

C. 1

D. e^2

Answer: B



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15. Let x be a number which exceeds its square by the greatest possible quantity, then $x =$

A. $\frac{1}{2}$

B. $\frac{1}{4}$

C. $-\frac{3}{4}$

D. $\frac{1}{3}$

Answer: A



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16. The sub tangent at $x = \frac{\pi}{2}$ on the curve $y = \sin x$ is :

A. 0

B. 1

C. $\frac{\pi}{2}$

D. None of these.

Answer: A



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17. A balloon which always remains spherical is being inflated by pumping in 10 cubic centimeters of gas per second . Find the rate at which the radius 15 cm .

A. $\frac{1}{90\pi}$ cm/sec

B. $\frac{1}{9\pi}$ cm/sec

C. $\frac{1}{30\pi}$ cm/sec

D. $\frac{1}{\pi}$ cm/sec.

Answer: A



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18. The two curves $x^3 - 3xy^2 + 2 = 0$ and $3x^2y - y^3 = 2$

A. touch each other

B. cut at right-angle

C. cut at an angle $\frac{\pi}{3}$

D. cut at an angle $\frac{\pi}{4}$

Answer: B



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19. If x is real, the minimum value of $x^2 - 8x + 17$ is :

A. 1

B. 2

C. 3

D. 4

Answer: A



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20. The slant height of a cone is fixed at 7 cm. If the rate of increase of its height is 0.3 cm/sec., then the rate of increase of its volume when its height is 4 cm is :

A. $\frac{\pi}{2}$ cm/sec.

B. π cm/sec.

C. $\frac{\pi}{5}$ cm/sec.

D. $\frac{\pi}{10}$ cm/sec.

Answer: D



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21. If $S^2 = at^2 + 2bt + c$, then the acceleration is :

- A. Directly proportional to S
- B. Inversely proportional to S
- C. Directly proportional to S^2
- D. Inversely proportional to S^3 .

Answer: D



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22. The value of 'c' in Lagrange's Theorem for the function

$f(x) = \log(\sin x)$ in the interval $\left[\frac{\pi}{6}, \frac{5\pi}{6}\right]$ is :

A. $\frac{\pi}{4}$

B. $\frac{\pi}{2}$

C. $\frac{2\pi}{3}$

D. None of these.

Answer: B



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23. A ladder 5 m long is leaning against a wall. The bottom of the ladder is pulled along the ground, away from the wall, at the rate of 2 m/s. How fast is its height on the wall decreasing when the foot of the ladder is 4m away from the wall?

A. $\frac{3}{8}$ m/sec.

B. $\frac{8}{3}$ m/sec.

C. $\frac{5}{3}$ m/sec.

D. $\frac{2}{3}$ m/sec.

Answer: B



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24. The angle between the curves :

$y^2 = 4ax$ and $ay = 2x^2$ is :

A. $\tan^{-1} \frac{3}{4}$

B. $\tan^{-1} \frac{3}{5}$

C. $\tan^{-1} \frac{4}{3}$

D. $\tan^{-1} \frac{5}{3}$.

Answer: B



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25. The maximum area in square units of an isosceles triangle inscribed in an ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ with its vertex at one end of the major axis is :

A. $\sqrt{3}ab$

B. $\frac{3\sqrt{3}}{4}ab$

C. $\frac{5\sqrt{3}}{4}ab$

D. None of these.

Answer: B



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