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## MATHS

## BOOKS - MODERN PUBLICATION MATHS (KANNADA ENGLISH)

## FAMILY OF LINES

Multiple Choice Question Level I

1. Area of the triangle formed by the lines $x+y$
$=2$ and angel bisectors of the pair of st lines
$x^{2}+2 y=1$ is
A. 2 sq units
B. 4 sq units
C. 6 sq units
D. 8 sq units

Answer: A

- View Text Solution

2. If 'a' is a parameter then the equation of family of lines having y interecept 4 is

$$
\begin{aligned}
& \text { A. } \frac{x}{a}-\frac{y}{4}=1 \\
& \text { B. } \frac{x}{a}+\frac{y}{4}=1 \\
& \text { C. } \frac{x}{a}-\frac{y}{4}-1=0 \\
& \text { D. } \frac{x}{a}+\frac{y}{4}-1=0
\end{aligned}
$$

Answer: B

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3. If $k$ is a parameter then the equation of
family of lines parallel to the line $3 x+4 y+5=0$ is
A. $4 x-3 y+k=0$
B. $3 x-4 y+k=0$
C. $3 x+4 y+k=0$
D. $4 x+3 y=0$

Answer: C

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4. If ' $k$ ' is parameter then the equation of family of lines perpendicular to the line $3 x+4 y+7-k=0$ is
A. $4 x+3 y+k=0$
B. $4 x-3 y+k=0$
C. $3 x+4 y+k=0$
D. $3 x-4 y+k=0$

Answer: B

D Watch Video Solution
5. If k is parameter then the equation of family of lines passing through $(3,4)$ is
A. $k x-y-4 k=0$
B. $k x-y-3 k+4=0$
C. $k x+y-3 k+4=0$
D. none of these

Answer: B

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6. If ' $k$ ' is a parameter then the equation of
family of lines through the intersetion of the lines
$x+2 y=5$ and $x-3 y=7$ is :

$$
\begin{aligned}
& \text { A. }(1+k) x-(2-3 k) y-(5+7 k)=0 \\
& \text { B. }(1+k) x+(2-3 k) y-(5+7 k)=0 \\
& \text { C. }(1+k) x-(2-3 k) y+(5+7 k)=0 \\
& \text { D. }(1+k) x+(2-3 k)+(5+7 k)=0
\end{aligned}
$$

## Answer: B

7. The equation of the straight line joining the origin to the point of intersection of $y-x+7=0$ and $y+2 x-2=0$ is
A. $3 x+4 y=0$
B. $3 x-4 y=0$
C. $4 x-3 y=0$
D. $4 x+3 y=0$

## Answer: D

8. The equation of the straight line passing
through the intersectio of the lines $x-2 y=1$ and
$x+3 y=2$ and parallel to $3 x+4 y=0$ is
A. $3 x+4 y+5=0$
B. $3 x+4 y-10=0$
C. $3 x+4 y-5=0$
D. $3 x+4 y+6=0$

Answer: C
9. The equatio $y^{2}-x^{2}+2 x-1=0$
represents
A. a pair of st line
B. a circle
C. a parabola
D. an ellipse

Answer: A

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10. Angle between the lines
$2 x^{2}-7 x y+3 y^{2}=0$ is
A. $60^{\circ}$
B. $45^{\circ}$
C. $\tan ^{-1}\left(\frac{7}{6}\right)$
D. $30^{\circ}$

Answer: B
11. The angle between the pair of straight lines
$y^{2} \sin ^{2} \theta-x y \sin ^{2} \theta+x^{2}\left(\cos ^{2} \theta-1\right)=0$ is
A. $\frac{\pi}{4}$
B. $\frac{\pi}{3}$
C. $\frac{2 \pi}{3}$
D. $\frac{\pi}{2}$

## Answer: D

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12. If the angle between two st lines
represented
$2 x^{2}+5 x y+3 y^{2}+7 y+4=0$ is $\tan ^{-1} \mathrm{~m}$
then $m$ equals
A. 1
B. 7
C. $\frac{1}{5}$
D. $\frac{7}{5}$

Answer: C
13. The lines represented by the equation
$A x^{2}+2 B x y+H y^{2}=0$ are perpendicular if
A. $A+H=0$
B. $B+H=0$
C. $A H=-1$
D. $A+B=0$

Answer: A

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14. If the slope of one of the lines represented by $a x^{2}-6 x y+y^{2}=0$ is the square of the other then
A. $a=1$
B. $a=4$
C. $a=6$
D. $a=8$

Answer: D

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15. If the slope of one of the lines represented
by $a x^{2}+10 x y+y^{2}=0$ is four times the slope of the other then
A. $a=1$
B. $a=4$
C. $a=8$
D. $a=16$

Answer: D

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16. The angle between the pari of lines
represented by $x^{2}-7 x y+12 y^{2}=0$ is :

$$
\begin{aligned}
& \text { A. } \sin ^{-1} \frac{1}{12} \\
& \text { B. } \sin ^{-1} \frac{1}{13} \\
& \text { C. } \sin ^{-1} \frac{1}{\sqrt{170}} \\
& \text { D. } \sin ^{-1} \frac{1}{\sqrt{85}}
\end{aligned}
$$

Answer: C

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17. If one of the lines $a x^{2}+2 h x y+b y^{2}=0$ bisects the angle between the aaxes in the first quadrant then

$$
\begin{aligned}
& \text { A. } h^{2}-a b=0 \\
& \text { B. } h^{2}+a b=0 \\
& \text { C. }(a+b)^{2}=h^{2} \\
& \text { D. }(a+b)^{2}=4 h^{2}
\end{aligned}
$$

## Answer: D

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18. Area of the triangle formed by the lines
$y^{2}-9 x y+18 x^{2}=0$ and $\mathrm{y}=\mathrm{a}$ is
A. $\frac{27}{4}$
B. 0
C. $\frac{a}{3}$
D. $\frac{a^{2}}{12}$

## Answer: D

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19. Orthocentre of the triangle formed by the
lines $\mathrm{x}+\mathrm{y}+\mathrm{p}=0$ and $2 x^{2}+y^{2}+x+2 y-1=0$ is
A. $(0,1)$
B. $(-1,0)$
C. $(-1,1)$
D. $(1,1)$

Answer: B

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20. Centroid of the triangle formed by the sides $\mathrm{y}-1=0$ and $x^{2}+7 x y+2 y^{2}=0$ is
A. $\left(-\frac{7}{3}, \frac{2}{3}\right)$
B. $\left(\frac{7}{3}, \frac{2}{3}\right)$
C. $\left(\frac{2}{3}, 0\right)$
D. $\left(-\frac{2}{3}, 0\right)$

Answer: A

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21. Circumcentre of the triangle formed by the
lines $x y+2 x+2 y+4=0$ and $x+y+2=0$ is
A. $(0,0)$
B. $(-2,-2)$
C. $(-1,-1)$
D. $(-1,-2)$

Answer: C

D Watch Video Solution
22. Area of the triangle formed by the following lines : $y=|x|$ and $x+2 y=2$ is
A. 4 sq units
B. $\frac{4}{3}$ sq units
C. $\frac{8}{3}$ sq units
D. $\frac{16}{3}$ sq units

Answer: B

D Watch Video Solution
23. Area of triangle formed by :
$2 x^{2}+x y-3 y^{2}=0$ and $\mathrm{x}+\mathrm{y}=3$ is

> A. $\frac{39}{4}$
> B. $\frac{41}{4}$
> C. $\frac{43}{4}$
> D. $\frac{45}{4}$

Answer: D

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24. The difference of the tangents of the angles which the lines
$x^{2}\left(\sec ^{2} \theta-\sin ^{2} \theta\right)-2 x y \tan \theta+y^{2} \sin ^{2} \theta=0$ makes with x axis is
A. 2
B. $2 \tan \theta$
C. $\sin 2 \theta$
D. $2 \cot \theta$

Answer: A
25.
$x^{2}+y^{2}+2 g x+2 f y+1=0$ represents a pair of lines then
A. $f^{2}-g^{2}=1$
B. $f^{2}+g^{2}=1$
C. $g^{2}-f^{2}=1$
D. $f^{2}+g^{2}=\frac{1}{2}$

Answer: B
26. If $a x^{2}+2 h x y+b y^{2}+2 g x+2 f y+c=0$ represents parallel lines then
A. $h f=b g$
B. $h^{2}=b c$
C. $a^{2} f=b^{2} g$
D. none of these

Answer: A
$x^{2}+(\lambda+\mu) x y+\lambda \mu y^{2}+x+\mu y=0$
represent two parallel straight lines if
A. $\lambda+\mu=0$
B. $\lambda=\mu$
C. $\lambda=2 \mu$
D. $\lambda=4 \mu$

Answer: B
28. If the equation
$12 x^{2}+7 x y-p y^{2}-18 x+q y+6=0$
represents a pair of perpendicular lines then

$$
\begin{aligned}
& \text { A. } p=12, q=1 \\
& \text { В. } p=-12, q=-1 \\
& \text { C. } p 12, q=-1 \\
& \text { D. } p=-12, q=1
\end{aligned}
$$

29. If the lines joining the origin to the points
of intersection of the line $y=m x+2$ and the
curve $x^{2}+y^{2}=1$ are right angles then
A. $m^{2}=1$
B. $m^{2}=3$
C. $m^{2}=5$
D. $m^{2}=7$
30. If the lines joining the origin to the points of intersection of the line $2 x+y-1=0$ and the curve $3 x^{2}+\lambda x y-4 x+1=0$ are at right angles then
A. $\lambda=-4$
B. $\lambda=4$
C. $\lambda=7$
D. all value of $\lambda$

## Answer: D

## - Watch Video Solution

31. Area of the parallelogram formed by
$2 x^{2}+5 x y+3 y^{2}=0$
$2 x^{2}+5 x y+3 y^{2}+3 x+4 y+1=0$ is
A. 1
B. -1
C. 2
D. -2

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32. The quadrilateral by pairs of lines
$x y+x+y+1=0, x y+3 x+4 y+9=0$ is
A. a rectangle
B. a square
C. a parallelogram
D. a rhombus

Answer: B

## - View Text Solution

33. If two lines represented by
$a x^{3}+b x^{2} y+c x y^{2}+d y^{3}=0$ are at right
anlges then $a^{2}+d^{2}+a c+b d$ equals
A. 0
B. 1
C. -1
D. $a b+c d$

## D View Text Solution

# 34. The three lines represented by <br> $y^{3}-4 x^{2} y=0$ form a triangle which is 

A. isosceles
B. equilateral
C. right angled
D. none of these

## Answer: D

## D Watch Video Solution

35. If the sum of the slopes of the lines given
by $x^{2}-2 c x y-7 y^{2}=0$ is four times their product then chas the value
A. 1
B. -1
C. 2
D. -2

## Answer: C

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## Multiple Choice Question Level li

1. If $4 a^{2}+9 b^{2}-c^{2}+12 a b=0$, then the family of straight lines $a x+b y+c=0$ is concurrent at
A. $(-2,3)$ or $(2,-3)$
B. $(-2,3)$ or $(-2,-3)$
C. $(2,3)$ or $(2,-3)$
D. $(2,3)$ or $(-2,-3)$

## Answer: D

## D Watch Video Solution

## 2. The distance between the parallel lines

given by
$(x+7 y)^{2}+4 \sqrt{2}(x+7 y)-42=0$ is
A. 2
B. $\frac{4}{7}$
C. $4 \sqrt{2}$
D. $8 \sqrt{2}$

## Answer: A

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3. The pair of st lines perpendicular to the pari
$a x^{2}+2 h x y+b y^{2}=0$ has the equation
A. $a x^{2}-2 h x y+b y^{2}=0$
B. $a y^{2}+2 h x y+b x^{2}=0$
C. $b x^{2}+2 h x y+a y^{2}=0$

$$
\text { D. } b x^{2}-2 h x y+a y^{2}=0
$$

## Answer: D

## - Watch Video Solution

4. The equation $3 x^{2}+2 h x y+y^{2}=0$ represent a pair of st lines passing thro the origin the two lines are
A. real and distinct if $h t(2)>3$
B. real and distinct if $h^{2}>+9$
C. real and coincident if $h^{2}=7$
D. real and coincident if $h^{2}>3$

Answer: A

## D Watch Video Solution

5. The sum of the slopes of the lines
represented by $4 x^{2}+2 h x y-7 y^{2}=0$ is
equal to the product of the slopes then $h$ is
A. -4
B. 4
C. -6
D. -2

Answer: D

## - Watch Video Solution

6. If one of the lines of the pair $a x^{2}+2 h x y+b y^{2}=0$ bisects the angle
between positive directions of the axies then

## $a, b, h$ satisfy the relation

A. $a+b=2|h|$
B. $a+b=-2 h$
C. $a-b=2|h|$
D. $(a-b)^{2}=4 h^{2}$

Answer: B

## 7. If the pairs of lines

$3 x^{2}-2 p x y-3 y^{2}=0$
$5 x^{2}-2 q x y-5 y^{2}=0$ are such that each pair bisects the angle between the other pair then pq equals
A. -1
B. -7
C. -9
D. -15

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8. If pair of st lines
$a x^{2}+2 h x y-a y^{2}-a y^{2}=0$ and
$b x^{2}+2 g x y-b y^{2}=0$ be such that each bisects the angle between the other then
A. $a b+g h=0$
B. $h^{2}-a b=0$
C. $a h+b g=0$
D. $a g+b h=0$

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9. Let $P Q R$ be a right angled isosceles triangle right angled at $P(2,1)$ if the equation of the line
$Q R$ is $2 x+y=3$ then the equation repersenting $P Q$ and $P R$ is
A.

$$
3 x^{2}-3 y^{2}+8 x y+20 x+10 y+25=0
$$

B.

$$
3 x^{2}-3 y^{2}+8 x y-20 x-10 y+25=0
$$

C.

$$
3 x^{2}-3 y^{2}+8 x y+10 x+15 y+20=0
$$

D.

$$
3 x^{2}-3 y^{2}-8 x y-10 x-15 y-20=0
$$

## Answer: B

## D Watch Video Solution

10. If the pair of lines $a x^{2}+2 h x y+b y^{2}=0$
is rotated about the origin through $90^{\circ}$, then
their equation in the new position is given by

$$
\begin{aligned}
& \text { A. } a x^{2}-2 h x y-b y^{2}=0 \\
& \text { B. } a x^{2}-2 h x y+b y^{2}=0 \\
& \text { C. } b x^{2}+2 h x y+a y^{2}=0 \\
& \text { D. } b x^{2}-2 h x y+a x^{2}=0
\end{aligned}
$$

## Answer: D

11. The equation of the image of the pair of
lines $y=|x|$ by the line $x=1$ is
A. $|y|+2=0$
B. $|y|=x+2$
C. $y=|1 x-2|$
D. $y=|x-1|$

Answer: C
( Watch Video Solution
12. If $x^{2}-k x y+y^{2}+2 y+2=0$ represent a pair of st lines then $k$ equals
A. 2
B. $\frac{1}{\sqrt{2}}$
C. $2 \sqrt{2}$
D. $\sqrt{2}$

Answer: D

- Watch Video Solution

13. 

The
equation
$8 x^{2}+8 x y+2 y^{2}+26 x+13 y+15=0$
represents a pair of parallel st lines the distance between them is:

> A. $\frac{7}{\sqrt{5}}$
> B. $\frac{7}{2 \sqrt{5}}$
> C. $\frac{2}{\sqrt{5}}$
D. none of these

Answer: B
14. If $a x^{2}+2 h x y+b y^{2}+2 g x+2 f y+c=0$ represents parallel lines then
A. $\frac{\sqrt{g^{2}-a c}}{h^{2}+a^{2}}$
B. $\frac{\sqrt{g^{2}-a c}}{h^{2}+a^{2}}$
C. $2 \frac{\sqrt{g^{2}-a c}}{a(a+b)}$
D. $\frac{\sqrt{g^{2}+a c}}{a(a+b)}$

Answer: C
15. The lines joining the origin to the point of intersection of the curves
$x^{2}+y^{2}+2 g x+c=0$
$x^{2}+y^{2}+2 f y-c=0$ are at right angles if
A. $g^{2}-f^{2}=c$
B. $g^{2}+f^{2}=c$
C. $g^{2}+f^{2}=c^{2}$
D. $g^{2}-f^{2}=2 c$

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16. The lines joining the origin to the points of intersectio of the curves
$a x^{2}+2 h x y+b y^{2}+2 g x=0$
and
$a x^{2}+2 h x y+b y^{2}+2 g x=0$ are at right angles if
A. $a(h+g)=a(h+g)$
B. $h(a+b)=h(a+b)$
C. $g(a+b)=g(a+b)$

## D. $g(a+b)=g(a+b)$

## Answer: C

## D Watch Video Solution

17. The equation $\mathrm{x}-\mathrm{y}=4$ and $x^{2}+4 x y+y^{2}=0$ represent the sides of
A. an isosceles triangle
B. an equilateral triangle
C. a right angled triangle

## D. none of these

## Answer: C

## D Watch Video Solution

18. A diagonal of the rectangle formed by the
lines
$x^{2}-7 x+6=0$ and $y^{2}-14 y+40=0$ is
A. $5 x-6 y=0$
B. $5 x+6 y=0$
C. $6 x-5 y-14=0$
D. $6 x-5 y+14=0$

## Answer: D

## D Watch Video Solution

19. 

If
two
of
the
lines
$a x^{3}+b x^{2} y+c x y^{2}+d y^{3}=0$
make
complementary angles with the $x$ in
anticlockwise sense then
A. $a(c-d)=b(b-c)$
B. $a(a-c)=d(d-b)$
C. $a(b-c)=d(a-b)$
D. $a(b-d)=c(c-d)$

Answer: B

D Watch Video Solution
20. If the pairs of lines $x^{2}-2 p x y-y^{2}=0$
and $x^{2}-2 q x y-y^{2}=0$ be such that each
pair bisects the angle between the other pair then

$$
\begin{aligned}
& \text { A. } p=-q \\
& \text { B. } p q=1 \\
& \text { C. } p q=-1 \\
& \text { D. } \mathrm{p}=\mathrm{q}
\end{aligned}
$$

Answer: C
( Watch Video Solution
21. A square is formed by following two pairs
of $\quad$ st lines $y^{2}-14 y+45=0 \quad$ and
$x^{2}-8 x+12=0 \mathrm{~A}$ circle is inscribed in it the centre of the circle is
A. $(7,4)$
B. $(4,7)$
C. $(3,7)$

$$
\text { D. }\left(\frac{3}{8}, 4\right)
$$

Answer: B
22. If one of the lines given by
$6 x^{2}-x y+4 c y^{2}=0$ is $3 \mathrm{x}+4 \mathrm{y}=0$ then c equals
A. 1
B. -1
C. 3
D. -3

Answer: D

D Watch Video Solution
23. Out of two st lines represented by an equation $a x^{2}+2 h x y+b y^{2}=0$ if one will be $y=m x$ then other is :
A. $a+2 h m+b m^{2}=0$
B. $b+2 h m+a m^{2}=0$
C. $h+2 a m+b m^{2}=0$
D. $h+2 h m+a m^{2}=0$

Answer: A
24. The line parallel to the $x$ axis and passing through the intersection of the lines
$a x+2 b y+3 b=0$ and $b x-2 a y-3 a=0$
where $(a, b) \neq(0,0)$ is
A. below the $x$ axis at a distance of $\frac{2}{3}$ from
it
B. below the $x$ axis at a distance of $\frac{3}{2}$ from
it
C. above the $x$ axis at a distance of $\frac{2}{3}$ from it
D. above the $x$ axis at a distance of $\frac{3}{2}$ from it

## Answer: B

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25. If one of the lines of
$m y^{2}+\left(1-m^{2}\right) x y-m x^{2}=0$
is a bisector of the angle between the lines
$x y=0$ then $m$ is
A. 2
B. 1
C. 2
D. $-\frac{1}{2}$

Answer: B

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1. Locus of the image of the point $(2,3)$ in the line $(2 x-3 y+4)+k(x-2 y+3)=0, k \in R$ is a
A. straight line parallel to $x$ axis
B. straight line parallel to $y$ axis
C. circle of radius $\sqrt{2}$
D. circle of radius $\sqrt{3}$

Answer: C

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## Question From Karnataka Cet Comed

1. If $m$ is the slope of one of the lines
represented by
$a x^{2}+2 h x y+b y^{2}=0$ then $(h+b m)^{2}=$
A. $h^{2}-a b$
B. $h^{2}+a b$
C. $(a-b)^{2}$
D. $(a+b)^{2}$
2. The perpendicular distance between the lines
$9 x^{2}-24 x y+16 y^{2}+21 x-28 y+10=0$ is
A. $\frac{7}{5}$
B. $\frac{3}{5}$
C. $\frac{4}{5}$
D. $\frac{1}{5}$
3. 

If
the
line
$6 x-7 y+8+\lambda(3 x-y+5)=0$ is parallel to y -axis, then $\lambda=$
A. -7
B. -2
C. 7
D. 2

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4. If the line $\mathrm{px}+\mathrm{qy}=0$ coincides with one of the lines given by
$a x^{2}+2 h x t y+b y^{2}=0$ then
A. $a p^{2}+2 g p q+b q^{2}=0$
B. $a p^{2}+2 h p q+b p^{2}=0$
C. $a q^{2}-2 h p q+b p^{2}=0$
D. none of these

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5. Let a and b non zero reals such that $a \neq b$
then the equation of the line passing through
the origin and the point of intersection of
$\frac{x}{a}+\frac{y}{b}=1$ and $\frac{x}{b}+\frac{y}{a}=1$ is
A. $a x+b y=0$
B. $b x+a y=0$
C. $y-x=0$
D. $x+y=0$

Answer: C
(D) Watch Video Solution

