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## MATHS

## BOOKS - FULL MARKS MATHS (TAMIL ENGLISH)

## COORDINATE GEOMETRY

## Progress Check

1. $A(0,4), B(5,0)$ and $C(-4,-7)$ are vertices of a triangle then its centroid will be at $\qquad$ .
2. The vertices of $\triangle P Q R$ are $\mathrm{P}(0,-4), \mathrm{Q}(3,1)$ and R(-8,1)


Draw $\triangle P Q R$ on a graph paper .

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3. Given $a$ quadrilateral $A B C D$ with vertices
$A(-3,-8), B(6,-6), C(4,2)$ and $D(-8,2)$.


Find the area of $\triangle A B C$.

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## 4. Fill the missing boxes

| S.No. | Points | Slope |
| :---: | :---: | :---: |
| 1 | $\mathrm{~A}(-a, b), \mathrm{B}(3 a,-b)$ |  |
| 2 | $\mathrm{~A}(2,3), \mathrm{B}(\ldots, \ldots \ldots)$ | 2 |
| 3 |  | 0 |
| 4 |  | undefined |

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## 5. Fill the details In respective boxes

| Form | When to use? |  |
| :---: | :---: | :---: |
| $y=m x+c$ | Slope $=m$, <br> Intercept $=c$ are given | Slope intercept form |
| $\frac{y-y_{1}}{y_{2}-y_{1}}=\frac{x-x_{1}}{x_{2}-x_{1}}$ | Two points $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right)$ <br> are given | Two points form |
| $\frac{x}{a}+\frac{y}{b}=1$ | The intercepts are given | Intercept form |

6. Fill the details in respective boxes

| S.No. | Equations | Parallel or <br> perpendicular |
| :---: | :---: | :---: |
| 1. | $5 x+2 y+5=0$ <br> $5 x+2 y-3=0$ |  |
| 2. | $3 x-7 y-6=0$ <br> $7 x+3 y+8=0$ |  |


| S.No. | Equations | Parallel or <br> perpendicular |
| :---: | :---: | :---: |
| 3. | $8 x-10 y+11=0$ <br> $4 x-5 y+16=0$ |  |
| 4. | $2 y-9 x-7=0$ <br> $27 y+6 x-21=0$ |  |

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## Thinking Corner

1. If the area of a quandrilateral formed by the points
(a,a),(-a,a),(a,-a) and (-a,-a), where $a \neq 0$ is 64 square
units, then identify the type of the quadrilateral.

## Exercise 51

1. Find the area of the triangle formed by the points.
$(1,-1),(-4,6),(-3,-5)$

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2. Determine whether the sets of points at collinear?
$(a, b+c),(b, c+a)$ and $(c, a+b)$

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3. Vertices of given triangles are taken in order and their areas are provided aside. In each case, find the value of ' p '.
S.No. Vertices Area(sq. units )
(i) $\quad(0,0),(\mathrm{p}, 8),(6,2) \quad 20$
(ii) $\quad(\mathrm{p}, \mathrm{p}),(5,6),(5-2) \quad 32$

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4. In the each of the following, find the value of 'a' for which the given points are collinear.
$(2,3),(4, a)$ and $(6,-3)$
5. Find the area of the quadrilateral whose vertices are at
$(-9,-2),(-8,-4),(2,2)$ and $(1,-3)$

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6. Find the value of $k$, if the area of a quadrilateral is

> 28 sq.units, whose vertices are
> $(-4,-2),(-3, k),(3,-2)$ and $(2,3)$

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7. If the points $A(-3,9), B(a, b)$ and $C(4,-5)$ are collinear and if $a+b=1$, find the a and b .

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8. Let $P(11,7), Q(13.9,4)$ an $d R(9.5,4)$ be the mid points of the sides $A B, B C$ and $A C$ respectively of $\triangle A B C$. Find the coordinates of the vertices $\mathrm{A}, \mathrm{B}$, and C . Hence find the area of $\triangle A B C$ and compare this with area of $\triangle P Q R$.
9. In the figure, the quadrilateral swimming pool shown is surrounded by concrete patio. Find the area of the patio.
$D(-10,6)$
$C(6,10)$
$H(-6,4) \quad$ G(3.7)
$F(3,-6) \quad F(6,-2)$
$\mathrm{A}(-4,-8) \quad \mathrm{B}(8,-4)$

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10. A triangle shaped glass with vertices at
$A(-5,-4), B(1,6)$ and $C(7,-4)$ has to be painted. If one bucket of paint covers 6 square feet,
how many buckets of paint will be required paint is applied.

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11. In the figure, find area of

## triangle FED



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1. What is the slope of a line whose inclination with positive direction of $x$-axis is
2. What is the inclination of a line whose slope is

0

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3. Find the slope of a line joining the points
$(\sin \theta,-\cos \theta)$ and $(-\sin \theta, \cos \theta)$ with the origin

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4. What is the slope of a line perpendicular to the line joining $A(5,1)$ and P where P is the mid-point of the segment joining (4, 2)) and ( $-6,4$ ).

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5. Show that the given points are collinear, $(-3,-4)$, $(7,2)$ and $(12,5)$

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6. If the three points $(3,-1)(a, 3)$ and $(1,-3)$ are collinear, find the vlaue of a .

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7. The line through the points $(-2, a)$ and $(9,3)$ has slope $\frac{-1}{2}$. Find the value of $a$.

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8. The line thorugh the point $(-2,6)$ and $(4,8)$ perpendicular to the line through the points $(8,12)$ and $(x, 24)$. Find the value of x .
9. Show that the given points form a right angled triangle and check whether they satisfies pythagoras theorem.
$A(1,-4), B(2,-3)$ and $C(4,-7)$

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10. Show that the given points form a parallelogram:

$$
A(2.5,3.5), B(10,-4), C(2.5,-2.5) \text { and } D(-5,5)
$$

11. 

$A(2,2), B(-2,-3), C(1,-3)$ and $D(x, y)$
form a parallelogram then find the value of $x$ and $y$.

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12. 

$A(3,-4), B(9,-4), C(5,-7)$ and $D(7,-7)$.
Show that $A B C D$ is a trapezium.
13. A quadrilateral has vertices at
$A(-4,-2), B(5,-1), C(6,5)$ and $D(-7,6)$.
Show that the mid-point of its sides form a parallelogram.

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14. $P Q R S$ is a rhombus. Its diagonals $P R$ and $Q S$ intersect at the points $M$ and satisfy $Q S=2 P R$. If the coordinates of $S$ and $M$ are $(1,1)$ and $(2,-1)$ respectively , find the coordinates of $P$.

# 1. Find the equation of a straight line passing 

 through the mid-point of a line segment joining the points $(1,-5),(4,2)$ and parallel to $X$ axis
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2. The equation of a straight line is $2(x-y)+5=0$. Find its slope, inclination and intercept on the Y axis.

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## 3. Find the equation of a line whose inclination is

 $30^{\circ}$ and making an intercept -3 on the $Y$ axis.
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4. Find the slope and $y$ intercept of
$\sqrt{3} x+(1-\sqrt{3}) y=3$.

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5. Find the value of 'a' if the line through ( $-2,3$ ) and
$(8,5)$ is perpendicular to $y=a x+2$.
6. The hill in the form of a right triangle has its foot at (19, 2). The inclination of the hill to the ground is
$45^{\circ}$. Find the equation of the hill joining the foot and top.

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7. Find the equation of a line through the given pair of points $\left(x_{1}, y_{1}\right),\left(x_{2}, y_{2}\right)$
$\left(2, \frac{2}{3}\right)$ and $\left(\frac{-1}{2},-2\right)$

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8. A cat is located at the point $(-6,-4)$ in $x y$ plane. A bottle of milk is kept at (5,11).The cat wishes to consume the milk travelling through shortest possible distance. Find the equation of the path it needs to take its milk.

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9. Find the equation of the median and altitude of
$\triangle A B C$ through A where the vertices are $A(6,2), B(-5,-1)$ and $C(1,9)$.
10. Find the equation of a straight line which has slope $\frac{-5}{4}$ and passing through the point ( $-1,2$ ) .

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11. You are downloading a song. The percent $y$ (in decimal form) of mega bytes remaining to get downloaded in x seconds is given by $y=0.1 x+1$. find the total $M B$ of the song.
12. Find the equation of a line whose intercepts on the $x$ and $y$ axes are given below.
(i) $4,-6$ and (ii) $-5, \frac{3}{4}$

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13. Find the intercepts made by the following lines on the coordinate axes.
(i) $3 x-2 y-6=0$
(ii) $4 x+3 y+12=0$

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14. Find the equation of a straight line

Passing through (1,-4) and has intercepts which are in the ratio 2:5

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Exercise 54

1. Find the slope of the following straight lines.
(i) $5 y-3=0$
(ii) $7 x-\frac{3}{17}=0$
2. Find the slope of the line which is
parallel to $\mathrm{y}=0.7 \mathrm{x}-11$
perpendicular to the line $x=-11$

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3. Check whether the given lines are parallel or perpendicular

$$
\frac{x}{3}+\frac{y}{4}+\frac{1}{7}=0 \text { and } \frac{2 x}{3}+\frac{y}{2}+\frac{1}{10}=0
$$

4. 

If the straight
lines

$$
12 y=-(p+3) x+12,12 x-7 y=16
$$

perpendicular find ' p '.

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5. Find the equation of a straight line passing through the point $P(-5,2)$ and parallel to the line joining the points $Q(3,-2)$ and $R(-5,4)$.
6. Find the equation of a line passing thorugh ( $6,-2$ ) and perpendicular to the line joining the point $(6,7)$ and $(2,-3)$.

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7. $A(-3,0), B(10,-2)$ and $C(12,3)$ are the vertices of $\triangle A B C$. Find the equation of the altitude through A and B .
8. Find the equation of the perpendicular bisector of the line joinging the point
$A(-4,2)$ and $B(6,-4)$.

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9. Find the equation of a straight line through the intersection of lines $7 x+3 y=10,5 x-4 y=1$ and parallel to the lines $13 x+5 y+12=0$.
10. Find the equation of a straight line through the intersection of lines $3 x+2 y=10$ and $5 x-6 y=2$ and perpendicular to the line $4 x-7 y+13=0$.

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11. Find the equation of a straight line joining the
point of intersection of
$3 x+y+2=0$ and $x-2 y-4=0$ to the point of intersection of $7 x-3 y=-12$ and $2 y=x+3$.
12. Find the equation of a straight line through the point of intersection of the lines $8 x+3 y=18,4 x+5 y=9$ and bisecting the line segment joining the points $(5,-4)$ and $(-7,6)$.

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## Exercise 55

1. The area of triangle formed by the points
$(-5,0),(0,-5)$ and $(5,0)$ is
A. 0 sq. units
B. 25 sq. units
C. 5 sq.units
D. none of these

Answer: B

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2. A man walks near a wall, such that the distance between him and the wall is 10 units. Consider the wall to be the $Y$ axix. The path travelled by the man is
A. $x=10$
B. $y=10$
C. $x=0$
D. $y=0$

## Answer: A

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3. The straight line given by the equation $x=11$ is
A. parallel to $x$ axis
B. parallel to $y$ axis
C. passing through the origin
D. passing through the point $(0,11)$

## Answer: B

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4. If $(5,7),(3, p)$ and $(6,6)$ are collinear, then the value of
$p$ is
A. 3
B. 6
C. 9
D. 12

## Answer: C

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# 5. The point <br> of intersection $3 x-y=4$ and $x+y=8$ is 

A. $(5,3)$
B. $(2,4)$
C. $(3,5)$
D. $(4,4)$

Answer: C
6. The slope of the line joining $(12,3)(4, a)$ is $\frac{1}{8}$. The value of 'a' is ...........
A. 1
B. 4
C. -5
D. 2

Answer: D

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7. The slope of the line which is perpendicular to a line joining the points $(0,0)$ and $(-8,8)$ is

$$
\text { A. }-1
$$

B. 1
C. $\frac{1}{3}$
D. -8

Answer: B
8. If slope of the line $P Q$ is $\frac{1}{\sqrt{3}}$ then slope of the perpendicular bisector of $P Q$ is
A. $\sqrt{3}$
B. $-\sqrt{3}$
C. $\frac{1}{\sqrt{3}}$
D. 0

Answer: B
9. If $A$ is a points on the $Y$ axis whose ordinate is 8 and $B$ is a point on the $x$ axis whose abscissae is 5 then the equation of the line $A B$ is .......
A. $8 x+5 y=40$
B. $8 x-5 y=40$
C. $x=8$
D. $y=5$

Answer: A
(D) Watch Video Solution

## 10. The equation of a line passing through the origin

 and perpendicular to the line $7 x-3 y+4=0$ isA. $7 x-3 y+4=0$
B. $3 x-7 y+4=0$
C. $3 x+7 y=0$
D. $7 x-3 y=0$

Answer: C

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11. Consider four straight lines
(i) $l_{1}=3 y=4 x+5$ (ii) $l_{2}: 4 y=3 x-1$
(iii) $l_{3}: 4 y+3 y=7$ (iv) $l_{4} 4 x+3 y=2$
A. $l_{1}$ and $l_{2}$ are perpendicular
B. $l_{1}$ and $l_{4}$ are parallel
C. $l_{2}$ and $l_{4}$ are perpendicular
D. $l_{2}$ and $l_{3}$ are parallel

Answer: C

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12. $A$ straight line has equation $8 y=4 x+21$.
which of the following is true.
A. The slope is 0.5 and the $y$ intercept is 2.6
B. The slope is 5 and the $y$ intercept is 1.6
C. The slope is 0.5 and the $y$ intercept is 1.6
D. The slope is 5 and the y intercept is 2.6

Answer: A

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13. When proving that quadrilateral is a trapezium it is neccesary to show $\qquad$ .
A. Two sides are parallel
B. Two parallel and two non-parallel sides
C. Opposite sides are parallel
D. All sides are of equal length.

Answer: B

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14. When proving that $a$ quadrilateral is $a$ parallelogram by using slopes you must find
A. the slopes of two sides
B. The slopes of two pair of opposite sides
C. The lengths of all sides
D. Both the lengths and slopes of two sides

## Answer: B

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15. $(2,1)$ is the points of intersection of two lines
A. $x-y=3=0,3 x-y-7=0$
B. $x+y=3,3 x+y=7$
C. $3 x+y=3, x+y=7$
D. $x+3 y-3=0, x-y-7=0$

Answer: B

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## Unit Exercise 5

1. PQRS is a rectangle formed by joining the points

$$
P(-1,-1), Q(-1,4), R(5,4) \text { and } S(5,-1)
$$

$A, B, C$ and $D$ are the mid points of $P Q, Q R, R S$ and $S R$ respectively. Is the quadrilateral $A B C D$ a square, a rectangle or a rhombus? Justify your answer.

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2. The area of triangle is 5 sq . units. Two of its vertices are $(2,1)$ and $(3,-2)$. The third vertex is ( $x, y$ ) where $y=x+3$. Find the coordinates of the third vertex.
3. Find the area of a triangle formed by lines $3 x+y-2=0,5 x+2 y-3=0$ and $2 x-y-3=0$

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4. If vertices of a quadrilateral are at

$$
A(-5,7), B(-4, k), C(-1,-6) \text { and } D(4,5)
$$

and its area is 72 sq . units. Find the value of $k$.

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5. Without using distance formula, show that the points $(-2,-1),(4,0),(3,3)$ and $(-3,2)$ is
vertices of a parallelogram.

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6. Find the equations of the lines, whose sum and product of intercepts are 1 and -6 respectively.

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7. The owner of a milk store finds that, he can sell 980
litres of milk each week at ₹ $14 /$ /litres and 1220 litres of milk each week at ₹16/litre. Assuming a linear
relationship between selling price and demand, how many litres could he sells weekly at ₹17/litres?

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8. Find the image of the points $(3,8)$ with respect to the line $x+3 y=7$ assuming the line to be a plane mirror.

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9. Find the equation of a line passing through the
point of intersection of the lines
$4 x+7 y-3=0$ and $2 x-3 y+1=0$ that has equal intercepts on the axes.

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10. A person standing at a junction (crossing) of two straight paths represented by the equations
$2 x-3 y+4=0$ and $3 x+4 y-5=0$ seek to reach the path whose equation is $6 x-7 y+8=0$ in the least times. Find the equation of the path that he should follow.

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## Additional Questions Solved Multiple Questions

1. If the three points $(-3,7),(a, 1),(-3,2)$ are collinear then the value of ' $a$ ' is
A. 0
B. -1
C. -3
D. 1

Answer: C

## Additional Questions Solved Multiple Choice Questions

1. If $A(5,5), B(-5,1), C(10,7)$ lie in a straight line, the area of $\triangle A B C$ is
A. $\frac{13}{2}$ sq.units
B. 9 sq. units
C. 25 sq.units
D. 0

Answer: D
2. In a rectangle $A B C D$ area of $\triangle A B C$ is $\frac{31}{2}$ Sq. units. Then the area of rectangle is
A. 62 sq. units
B. 31 sq. units
C. 60 sq. units
D. 30 sq. units

Answer: B

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3. If the points ( $k, 2 k$ ) , $3 \mathrm{k}, 3 \mathrm{k}$ ) and ( 3,1 ) are collinear, then k is

$$
\begin{aligned}
& \text { A. } \frac{1}{3} \\
& \text { B. }-\frac{1}{3} \\
& \text { C. } \frac{2}{3} \\
& \text { D. }-\frac{2}{3}
\end{aligned}
$$

## Answer: B

4. If the area of the triangle formed by the points $(x, 2 x),(-2,6)$ and $(3,1)$ is 5 square units then $x=$
A. 2
B. $\frac{3}{5}$
C. 3
D. 5

Answer: A

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5. The slope of a line parallel to $y$-axis is equal to
A. 0
B. -1
C. 1
D. not defined

Answer: D

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6. In a rectangle PQRS , the slope of $\mathrm{PQ}=\frac{5}{6}$ then the slope of RS is
A. $\frac{-5}{6}$
B. $\frac{6}{5}$
C. $\frac{-6}{5}$
D. $\frac{5}{6}$

## Answer: D

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7. The $y$-intercept of the line $y=2 x$ is
A. 1
B. 2
C. $\frac{1}{2}$
D. 0

## Answer: D

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8. The straight line given by the equation $y=5$ is
A. parallel to $x$ axis
B. parallel to $y$ axis
C. passing through the origin
D. none of these
9. The $x$-intercept of the line $2 x-3 y+5=0$ is
A. $\frac{5}{2}$
B. $\frac{-5}{2}$
C. $\frac{2}{5}$
D. $\frac{-2}{5}$

Answer: B
10. The lines $3 x-5 y+1=0$ and $5 x+k y+2=0$ are perpendicular if the value of $k$ is
A. -5
B. 3
C. -3
D. 5

Answer: B
11. if $x-y=3$ and $x+2 y=6$ ae the diameters of a circle then the centre is at the point.........
A. $(0,0)$
B. $(1,2)$
C. $(1,-1)$
D. $(4,1)$

Answer: D
12. The line $4 x+3 y-12=0$ meets the $x$-axis at the point..........
A. $(4,0)$
B. $(3,0)$
C. $(-3,0)$
D. $(-4,0)$

Answer: B
13. The equation of a straight line passing through the point $(2,-7)$ and parallel to $x$-axis is
A. $x=2$
B. $x=-7$
C. $y=-7$
D. $y=2$

Answer: C

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14. The equation of a straight line having slope 3 and y intercept -4 is
A. $3 x-y-4=0$
B. $3 x+y-4=0$
C. $3 x-y+4=0$
D. $3 x+y+4=0$

Answer: A

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## Additional Questions Solved Answer The Following

1. If the points $(3,-4)(1,6)$ and $(-2,3)$ are the vertices of a triangle ,find its area.

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2. If the area of the triangle formed by the points
$(1,2)(2,3)$ and $a, 4)$ is 8 sq. units find $a$.

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3. If the points $A(2,5), B(4,6)$ and $C(8, a)$ are collinear find the value of 'a' using slope concept .

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4. If ( $x, y$ ) is any point on the line joining the points
$\mathrm{A}(\mathrm{a}, 0)$ and $\mathrm{B}(0, \mathrm{~b})$, then show that $\frac{x}{a}+\frac{y}{b}=1$

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5. A straight line passes through $(1,2)$ and has the equation $y-2 x-k=0$. Find $k$.

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6. If a line passes through the mid point of $A B$ where

A is $(3,0)$ and B is $(5,4)$ and makes an angle $60^{\circ}$ with $x$-axis find its equation.

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7. Find the equation of the line through $(3,2)$ and perpendicular to the line joining (4,5) and (1,2)

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8. $P$ and $Q$ trisect the line segment joining the points
$(2,1)$ and $(5,-8)$. If the point $P$ lies on $2 x-y+k=0$, then
find the value of $k$.

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9. Find the equation of the line passing through $(4,5)$ and making equal intercept in the axes.

## D Watch Video Solution

10. Find the equation of the line passing through
$(2,-1)$ and whose intercepts on the axes are equal in magnitude but opposite in sign.
11. The straight line cuts the coordinate axes at $A$ and B. if the mid point of $A B$ is $(3,2)$ the find the equation of $A B$.

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12. If the coordinates of two points $A$ and $B$ are $(3,4)$
and $(5,-2)$ respectively. Find the coordinates of any
point ' $c$ ', if $A C=B C$ and area of triangle $A B C=10$ sq.
units.


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13. The four vertices of a quadrilateral are (1,2) (-5,6)
( $7,-4$ ) and ( $k,-2$ ) taken in order.
if the area of the quadrilateral is 9 sq . units find the value of $k$.

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14. Find the area of a triangle whose three sides are having the equations $x+y=2, x-y=0$ and $x+2 y-6=0$.

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15. Verify the Median of a triangle divides into two triangles of the equal whose vertices are $A(4,-6), B(3,-2)$ and $C(5,2)$
16. Find the area of the $\Delta A B C$ with $\mathrm{A}(1,-4)$ and the mid points of sides through $A$ being ( $2,-1$ ) and ( $0,-1$ )

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17. Find the equation of the straight lines passing through $(-3,10)$ whose sum of the intercepts is 8 .
18. Find the equation of the straight line passing through the point of intersection of the lines $5 x$ $8 y+23=0$ and $7 x+6 y-71=0$ and is perpendicular to the line joining the points (5,1) and ( $-2,2$ ).

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19. Find the equation of the line passing through the points of intersection of $4 x-y-3=0$ and $x+y-2=0$ and perpendicular to $2 x-5 y+3=0$.
20. Find the equation of the line through the point of intersection of the lines $2 x+y-5=0$ and $x+y-3=0$ and bisecting the line segment joining the points (3,-2) and (-5,6).

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