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India's Number 1 Education App

## MATHS

## BOOKS - FULL MARKS MATHS (TAMIL ENGLISH)

## TRIGONOMETRY

## Progress Check

1. The number of trigonometry ratio is $\qquad$ .

D Watch Video Solution
2. $1-\cos ^{2} \theta$ is

0
Watch Video Solution
3. $(\sec \theta+\tan \theta)(\sec \theta-\tan \theta)=$

## D Watch Video Solution

4. $(\cot \theta+\operatorname{cosec} \theta)(\cot \theta-\operatorname{cosec} \theta)$ is

## - Watch Video Solution

5. $\operatorname{co6} 0^{\circ} \sin 30^{\circ}+\cos 30^{\circ} \sin 60^{\circ}=$ $\qquad$

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6. $\tan 60^{\circ} \cos 60^{\circ}+\cot 60^{\circ} \sin 60^{\circ}=$ _ $_{-}$.

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7. $\left(\tan 45^{\circ}+\cot 45^{\circ}\right)+\left(\sec 45^{\circ} \operatorname{cosec} 45^{\circ}\right)$ is $\qquad$

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8. (i) $\sec \theta=\operatorname{cosec} \theta$ if $\theta$ is ........... . (ii) $\cot \theta=\tan \theta$ if $\theta$ is $\qquad$

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## Thinking Corner

1. What type of triangle is used to calculate heights and distances?

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2. When the height of the building and distances from the foot of the building is given, which trigonometric ratio is used to find the

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3. If the line of sight and angle of elevation is given, then which trigonometric ratio is used to find the height of the building,

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## Exercise 61

1. Prove the below identities
$\cot \theta+\tan \theta=\sec \theta \operatorname{cosec} \theta$
2. Prove that following identities

$$
\frac{1-\tan ^{2} \theta}{\cot ^{2} \theta-1}=\tan ^{2} \theta
$$

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3. Prove that following identities
$\sqrt{\frac{1+\sin \theta}{1-\sin \theta}}=\sec \theta+\tan \theta$

## - Watch Video Solution

4. Prove that following identities

$$
\sec ^{6} \theta-\tan ^{6} \theta-3 \tan ^{2} \theta \sec ^{2} \theta=1
$$

5. Prove that following identities $\sec ^{4} \theta\left(1-\sin ^{4} \theta\right)-2 \tan ^{2} \theta=1$

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6. Prove that following identities $\frac{\sin A-\sin B}{\cos A+\cos B}+\frac{\cos A-\cos B}{\sin A+\sin B}=0$

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7. If $\sqrt{3} \sin \theta-\cos \theta=0$, then show that $\tan 3 \theta=\frac{3 \tan \theta-\tan ^{3} \theta}{1-3 \tan ^{3} \theta}$

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8. If $\cot \theta+\tan \theta=x$ and $\sec \theta-\cos \theta=y$ then prove that $\left(x^{2} y\right)^{\frac{2}{3}}-\left(x y^{2}\right)^{\frac{2}{3}}=1$

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9. If $\sin \theta\left(1+\sin ^{2} \theta\right)=\cos ^{2} \theta$, then prove that $\cos ^{6} \theta-4 \cos ^{2} \theta+8 \cos ^{2} \theta=4$

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10. If $\frac{\cos \theta}{1+\sin \theta}=\frac{1}{a}$ then prove that $\frac{a^{2}-1}{a^{2}+1}=\sin \theta$.

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Exercise 62

1. Find the angle of elevation of the top of a tower from a point on the ground, which is 30 m away the foot of a tower of height $10 \sqrt{3} \mathrm{~m}$.
2. A road is flanked on either side by continuous rows of house of height $4 \sqrt{3} \mathrm{~m}$ with no space in between them. A pedestrain is standing on the median of the road facing a row house. The angle of elevationn from the pedestrain to the top of the house is $30^{\circ}$. Find the width of the road.

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3. To a man standing outside his house. The angles of elevation of the top and bottom of a window are $60^{\circ}$ and $45^{\circ}$ respectively. If the height of the man is 180 cm and if he is 5 m away from the wall. What is the height of the window? $(\sqrt{3}=1.732)$.

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4. A statue 1.6 m tall stands on the top of a pedestal. From a point on the ground, the angle of elevation of the top of the statue is $60^{\circ}$ and from the same point angle of elevation of the top of the pedestal is $40^{\circ}$. Find the height of the pedestal. $\left(\tan 40^{\circ}=0.8361, \sqrt{3}=1.732\right)$

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5. A flog pole ' $h$ ' metres is on the top of the hemispherical dome of radius ' $r$ ' metres. A man is standing 7 m away form the dome. Seeing the top of the pole at an angle $45^{\circ}$ and moving 5 m away from the dome and seeing the bottom of the pole at angle $30^{\circ}$. Find the height of the pole

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6. The top of a 15 m high tower make an angle of elevation of $60^{\circ}$ with the bottom of an electronic pole and angle of elevation of $30^{\circ}$ with the top of the pole. What is the height of the electric pole?

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7. A vertical pole fixed to the ground is divided in the ratio 1:9 by a mark on it with lower part shorter than the upper part. If the two parts subtend equal angles at a place on the ground, 25 m away from the base of the pole, what is the height of the pole?

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8. A traveler approaches a mountain on highway. He measures the angle of elevation to the peak at each milestone. At two consecutive milestones the angles measured are $4^{\circ}$ and $8^{\circ}$. What is the height
of the peak if the distance between consecutive milestones is 1 mile.
$\left(\tan 4^{\circ}=0.0699, \tan 8^{\circ}=0.14405\right)$

## D Watch Video Solution

## Exercise 63

1. From the top of a rock $50 \operatorname{sqr}(3) \mathrm{m}$ high, the angle of depression of car on the ground is observed to be $30^{\circ}$. Find the distance of the car from the rock.

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2. The horizontal distance between two building is 70 m . The angle of depression of the top of the first building when seen from the top of the second building is $45^{\circ}$. If the height of the second building is 120 $m$, find the height of the first building.
3. From the top of the tower 60 m high the angles of depression of the top and bottom of a vertical lamp post are observed to be $38^{\circ}$ and $60^{\circ}$ respectively. Find the height of the lamp post. $\left(\tan 38^{\circ}=0.7813, \sqrt{3}=1.732\right)$

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4. An aeroplane at an altitude of 1800 m finds that two boats are selling towards it in the same direction. The angles of depressionn of the boats as obversed from the aeroplane are $60^{\circ}$ and $30^{\circ}$ respectively. Find the distance between the two boats. $(\sqrt{3}=1.732)$
5. From the top of a lighhouse, the angles of depression of two ships on the opposite sides of it are observed to be $30^{\circ}$ and $60^{\circ}$. If the height of the lighthouse is $h$ meters and thhe line joining the ships passes through the foot of the lighthouse. show that the distance between the ships is $\frac{4 h}{\sqrt{3}} \mathrm{~m}$.

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6. A lift in a building of height 90 feet with transparent glass walls is descending from the top of the building. At the top of the building, the angles of depression to a fountain in the garden is $60^{\circ}$. Two minutes later, the angle of depression reduces to $30^{\circ}$. If the fountain is $30 \sqrt{3}$ feet from the entrace of the lift, find the speed of the lift, and the speed of the lift which is descending.

## D Watch Video Solution

1. From the top of tree of height 13 m the angle of elevation and depression of the top and bottom of another tree are $45^{\circ}$ and $30^{\circ}$ respectively. Find the height of the seconds tree. $(\sqrt{3}=1.732)$.

## D Watch Video Solution

2. A man is standing on the deck of a ship, which is 40 m above water level. He observes the angle of elevation of the top of a hill as $60^{\circ}$ and the angle depression of the base of the hill as $30^{\circ}$. Calculate the distance of the hill from the ship and the height of the hill, $(\sqrt{3}=1.732)$.
3. If the angle of elevation of a cloud from a point ' $h$ ' meterss above a take is $\theta_{1}$ and the angle of depression of its reflection in the take is $\theta_{2}$. Prove that the height that the cloud is located from the ground is $\frac{h\left(\tan \theta(1)+\tan \theta_{2}\right)}{\tan \theta_{2}-\tan \theta_{2}}$.

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4. The angle of elevation of the top of cell phone tower from the foot of a high apartment is $60^{\circ}$ and the angle of depression of the foot of the tower from the top of the apartment is $30^{\circ}$. If the height of the apartment is 50 m , find the height of the cell tower. According to radiations control norms, the minimum height of the cell phone tower should be 120 m . State if the height of the above mentioned cell phone tower meets the radiation norms.
5. The angles of elevation and depression of the top and bottom of a lamp post from the top of a 66 m high apartment are $60^{\circ}$ and $30^{\circ}$ respectively, find

The height of the lamp post.

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6. Three villagers A, B and C can see each other across a valley. The horizontal distance between $A$ and $B$ is 8 km and the horizontal distance between $B$ and $C$ is 12 km . The angle of depression of $B$ from

A is $20^{\circ}$ and the angle of elevation of C from B is $30^{\circ}$. Calculate: the vertical between $A$ and $B$.

## D Watch Video Solution

1. The value of $\sin ^{2} \theta+\frac{1}{1+\tan ^{2} \theta}$ is equal to
A. $\tan ^{2} \theta$
B. 1
C. $\cot ^{2} \theta$
D. 0

Answer: 2

D Watch Video Solution
2. $\tan \theta \operatorname{cosec} 2-\tan \theta$ is equal to
A. $\sec \theta$
B. $\cot ^{2} \theta$
C. $\sin \theta$
D. $\cot \theta$

## D Watch Video Solution

3. 

$(\sin \propto+\operatorname{cosec} \propto)^{2}+(\cos \propto+\sec \propto)^{3}=k+\tan ^{2} \propto+\cot ^{2} \propto$, then the value of $\mathrm{k}=$ $\qquad$ .
A. 9
B. 7
C. 5
D. 3

Answer: 2
4. If $\sin \theta+\cos \theta=a$ and $\sec \theta+\operatorname{cosec} \theta=b$, then the value of $b\left(a^{2}-1\right)$ is equal to
A. 2 a
B. 3 a
C. 0
D. $2 a b$

## Answer: 1

## - Watch Video Solution

5. If $5 x=\sec \theta$ and $\frac{5}{x}=\tan \theta$, then $x^{2}-\frac{1}{x^{2}}$ is equal to
A. 25
B. $\frac{1}{25}$
C. 5
D. 1

Answer: 2

D Watch Video Solution
6. If $\sin \theta=\cos \theta$ then $2 \tan ^{2} \theta+\sin ^{2} \theta-1={ }_{-}$.
A. $\frac{-3}{2}$
B. $\frac{3}{2}$
C. $\frac{2}{3}$
D. $\frac{-2}{3}$

Answer: B

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7. If $x=a \tan \theta$ and $y=b \sec \theta$ then
A. $\frac{y^{2}}{b^{2}}-\frac{x^{2}}{a^{2}}=1$
B. $\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=1$
C. $\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=0$
D. $\frac{y^{2}}{b^{2}}-\frac{x^{2}}{a^{2}}=0$

## Answer: A

D Watch Video Solution
8. $(1+\tan \theta+\sec \theta)(1+\cot \theta-\operatorname{cosec} \theta)$ is equal to
A. 0
B. 1
C. 2
D. -1

## Answer: C

## D Watch Video Solution

9. $a \cot \theta+b \operatorname{cosec} \theta=p$ and $b \cot \theta+a \operatorname{cosec} \theta=q$ then $p^{2}-q^{2}$ is equal to
A. $a^{2}-b^{2}$
B. $b^{2}-a^{2}$
C. $a^{2}+b^{2}$
D. $b-a$

## Answer: B

10. If the ratio of the height of a tower and the length of its shadow is $\sqrt{3}: 1$, then the angle of elevation of the sum had measure.
A. $45^{\circ}$
B. $30^{\circ}$
C. $90^{\circ}$
D. $60^{\circ}$

## Answer: D

## D Watch Video Solution

11. The electric pole subtends an angle of $30^{\circ}$ at a point on the same level as its foot. At a second point ' $b$ ' metres above the first, the depression of the foot of the tower is $60^{\circ}$. The height of the tower (in towers) is equal to
A. $\sqrt{3} b$
B. $\frac{b}{3}$
C. $\frac{b}{2}$
D. $\frac{b}{\sqrt{3}}$

## Answer: C

## - Watch Video Solution

12. A tower is 60 m height. Its show is x metres shorter when the sun's altitude is $45^{\circ}$ than when it has been $30^{\circ}$, then x is equal to
A. 41.92 m
B. 43.92 m
C. 43 m
D. 45.6 m

## ( Watch Video Solution

13. The angle of depression of the top and bottom of 20 m tall building from the top of a multistoried building are $30^{\circ}$ and $60^{\circ}$ respectively. The height of the multi storied building and the distance between two building (in meters) is $\qquad$ .
A. $20,10 \sqrt{3}$
B. $10,5 \sqrt{3}$
C. 20,10
D. $30,10 \sqrt{3}$

## Answer: D

14. Two persons are standing ' $x$ ' metres apart from each other and the height of the first person is double that of the other. If from the middle points of the linejoining their their feet an observe finds the angular elevations of their tops to be complementary, then the height of the shorter person (in metres) is
A. $\sqrt{2} x$
B. $\frac{x}{2 \sqrt{2}}$
C. $\frac{x}{\sqrt{2}}$
D. $2 x$

Answer: B

## D Watch Video Solution

15. The angle of elevation of a cloud from a point $h$ metres above a lake is $\beta$. The angle of depression of its reflection in the lake is $45^{\circ}$.

The height of location of the cloud from the lake is
A. $\frac{(1+\tan \beta)}{1-\tan \beta}$
B. $\frac{h(1-\tan \beta)}{1+\tan \beta}$
C. $h \tan \left(45^{\circ}-\beta\right)$
D. none of these

## Answer: A

## D Watch Video Solution

## Unit Exercise

1. Prove that
$\cot ^{2} A((\sec A-1) /(1+\sin A))+\sec ^{2} A\left(\frac{\sin A-1}{1+\sec A}\right)=0$
2. Prove that $\left(\frac{1+\sin \theta-\cos \theta}{1+\sin \theta+\cos \theta}\right)^{2}=\frac{1-\cos \theta}{1+\cos \theta}$

## D Watch Video Solution

3. If $x \sin ^{3} \theta+y \cos ^{3} \theta=\sin \theta \cos \theta$ and $x \sin \theta=y \cos \theta$, then prove that $x^{2}+y^{2}=1$.

## D Watch Video Solution

4. If $\mathrm{a} \cos \theta-\mathrm{b} \sin \theta=\mathrm{c}$, show that $\mathrm{a} \sin \theta+\mathrm{b} \cos$ $\theta= \pm \sqrt{a^{2}+b^{2}-c^{2}}$

## D Watch Video Solution

5. A bird is sitting on the top of a 80 m high tree. From a point on the ground, the angle of elevation of the bird is $45^{\circ}$. The bird flies away
horizontallly in such away that it remained at a constant height from the ground. After 2 seconds, the angle

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6. An aeroplane is flying parallel to the Earth's surface at a speed of
$175 \mathrm{~m} / \mathrm{sec}$ and at a height of 600 m . The anlge elevation of the aeroplane from a point on the Earth's surface is $37^{\circ}$ at a given point.

After what period of time does the angle of elevation increase to $53^{\circ}$ $?\left(\tan 53^{\circ}=1.3270, \tan 37^{\circ}=0.7536\right)$.

## D Watch Video Solution

7. $A$ bird is flying from $A$ towards $B$ at an angle of $35^{\circ}$, a point 30 km away from A. At B it charges its course of flight and heads towards C on a bearing of $48^{\circ}$ and distance 32 km away.

How far is B to the North of $A$ ?
8. Two ships are sailing in the sea on either side of the lighthouse.

The angles of depression of two ships as observed from the top of the lighthouse are $60^{\circ}$ and $45^{\circ}$ respectively. If the distance between the ships is $200\left(\frac{\sqrt{3+1}}{\sqrt{3}}\right)$ metres, find the height of the lighthouse.

## (D) Watch Video Solution

9. A building and a statue are in opposite side of a street from each other 35 m apart. From a point on the roof of building the angle of elevationof the top of statue is $24^{\circ}$ and the angle of depression of base of base of the statue is $34^{\circ}$. Find the height of the statue.

$$
\left(\tan 24^{\circ}=0.4452, \tan 34^{\circ}=0.6745\right)
$$

Additional Questions Solved

1. $\left(1-\sin ^{2} \theta\right)\left(\sec ^{2} \theta\right)=. . . . . . . . . .$.
A. 0
B. 1
C. $\tan ^{2} \theta$
D. $\cos ^{2} \theta$

## Answer: B

## - Watch Video Solution

2. $\left(1+\tan ^{2} \theta\right) \sin ^{2} \theta=$
A. $\sin ^{2} \theta$
B. $\cos ^{2} \theta$
C. $\tan ^{2} \theta$
D. $\cot ^{2} \theta$

## Answer: C

## - Watch Video Solution

3. $\left(1-\cos ^{2} \theta\right)\left(1+\cot ^{2} \theta\right)=. . . . . . . . .$.
A. $\sin ^{2} \theta$
B. 1
C. 0
D. $\tan ^{2} \theta$

Answer: B
4. $\sin \left(90^{\circ}-\theta\right) \cos \theta+\cos \left(90^{\circ}-\theta\right) \sin \theta=\ldots . . . . . . . . .$.
A. 1
B. 0
C. 2
D. -1

## Answer: A

## - Watch Video Solution

$5.1-\frac{\sin ^{2} \theta}{1+\cos \theta}=\ldots . . . . . . . .$.
A. $\cos \theta$
B. $\tan \theta$
C. $\cot \theta$
D. $\cos e c \theta$

## D Watch Video Solution

6. $\cos ^{4} x-\sin ^{4} x=\ldots \ldots \ldots .$.
A. $2 \sin ^{2} x-1$
B. $2 \cos ^{2} x-1$
C. $1+2 \sin ^{2} x$
D. $1-2 \cos ^{2} x$

## Answer: B

## - Watch Video Solution

7. If $\tan \theta=\frac{a}{x}$, then the value of $\frac{x}{\sqrt{a^{2}+x^{2}}}=$
A. $\cos \theta$
B. $\sin \theta$
C. $\cos e c \theta$
D. $\sec \theta$

## Answer: A

## - Watch Video Solution

8. If $x=a \sec \theta, y=b \tan \theta$, then the value of $\frac{x^{2}}{a^{2}}-\frac{y^{2}}{b^{2}}=\ldots . . .$. .
A. 1
B. -1
C. $\tan ^{2} \theta$
D. $\cos ^{2} e c^{2} \theta$
9. $\frac{\sec \theta}{\cot \theta+\tan \theta}=\ldots \ldots . . . . .$.
A. $\cot \theta$
B. $\tan \theta$
C. $\sin \theta$
D. $-\cot \theta$

## Answer: C

## (D) Watch Video Solution

10. $\frac{\sin \left(90^{\circ}-\theta\right) \sin \theta}{\tan \theta}+\frac{\cos \left(90^{\circ}-\theta\right) \cos \theta}{\cot \theta}=\ldots \ldots . . . . .$.
A. $\tan \theta$
B. 1
C. -1
D. $\sin \theta$

## Answer: B

Watch Video Solution
11. In the adjoining figure, $\mathrm{AC}=$ $\qquad$
A. 25 m
B. $25 \sqrt{3} m$
C. $\frac{25}{\sqrt{3}}$
D. $25 \sqrt{2} m$

## Answer: B

12. In the adjoining figure, $\angle A B C=$ $\qquad$
A. $45^{\circ}$
B. $30^{\circ}$
C. $60^{\circ}$
D. $50^{\circ}$

## Answer: C

## - View Text Solution

13. A man is 28.5 m away from a tower. His eye level above the ground is 1.5 m . The angle of elevation of the tower from his eyes is $45^{\circ}$. Then the height of the tower is $\qquad$
A. 30 m
B. 27.5 m
C. 28.5 m
D. 27 m

## Answer: A

Watch Video Solution
14. In the adjoining figure, $\sin \theta=\frac{15}{17}$. Then $B C=$

## - Watch Video Solution

15. $\left(1+\tan ^{2} \theta\right)(1-\sin \theta)(1+\sin \theta)=$
A. $\cos ^{2} \theta-\sin ^{2} \theta$
B. $\sin ^{2} \theta-\cos ^{2} \theta$
C. $\sin ^{2} \theta+\cos ^{2} \theta$
D. 0

## - Watch Video Solution

16. $\left(1+\cot ^{2} \theta\right)(1-\cos \theta)(1+\cos \theta)=$
A. $\tan ^{2} \theta-\sec ^{2} \theta$
B. $\sin ^{2} \theta-\cos ^{2} \theta$
C. $\sec ^{2} \theta-\tan ^{2} \theta$
D. $\cos ^{2} \theta-\sin ^{2} \theta$

Answer: C

## - Watch Video Solution

17. $\left(\cos ^{2} \theta-1\right)\left(\cot ^{2} \theta+1\right)+1=$
A. 1
B. -1
C. 2
D. 0

## Answer: D

## - Watch Video Solution

18. $\frac{1+\tan ^{2} \theta}{1+\cot ^{2} \theta}=$
A. $\cos ^{2} \theta$
B. $\tan ^{2} \theta$
C. $\sin ^{2} \theta$
D. $\cot ^{2} \theta$
19. The value of $\sin ^{2} \theta+\frac{1}{1+\tan ^{2} \theta}$ is equal to
A. $\cos e c^{2} \theta+\cot ^{2} \theta$
B. $\cos e c^{2} \theta-\cot ^{2} \theta$
C. $\cot ^{2} \theta-\cos ^{2} c^{2} \theta$
D. $\sin ^{2} \theta-\cos ^{2} \theta$

## Answer: B

(D) Watch Video Solution
20. $9 \tan ^{2} \theta-9 \sec ^{2} \theta=$
A. 1
B. 0
C. 9
D. -9

## Answer: D

21. If the ratio of the height of a tower and the length of its shadow is $\sqrt{3}: 1$, then the angle of elevation of the sum had measure.
A. $45^{\circ}$
B. $30^{\circ}$
C. $60^{\circ}$
D. $90^{\circ}$

Answer: B
22. A ladder makes an anglesof $60^{\circ}$ with the ground when placed against a wall. If the foot of the ladder is $2 m$ away from the wall, the length of the ladder is
A. $\frac{4}{\sqrt{2}}$
B. $4 \sqrt{3}$
C. $2 \sqrt{2} m$
D. 4 m

## Answer: D

## (D) Watch Video Solution

23. The angle of depression of a car parked on the road from the top of the 150 m high tower is $30^{\circ}$. Find the distance of the car from the
A. $150 \sqrt{3} m$
B. $150 \sqrt{2} m$
C. 75 m
D. $50 \sqrt{3} m$

## Answer: D

## D Watch Video Solution

24. the angle of elevation of the top of a tower at a point on the ground 50 m away from the foot of the tower is $45^{\circ}$. Then the height of the tower (in meters) is $\qquad$
A. $50 \sqrt{3} m$
B. 50 m
C. $\frac{50}{\sqrt{2}} m$
D. $\frac{50}{\sqrt{3}} m$

Answer: B

## - Watch Video Solution

25. If $x=a \cos \theta$ and $y=b \sin \theta$ then $b^{2} x^{2}+a^{2} y^{2}=\ldots \ldots \ldots \ldots .$.
A. $a^{2} b^{2}$
B. $a b$
C. $a^{4} b^{4}$
D. $a^{2}+b^{2}$

## Answer: A

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Additional Questions Solved li

1. Prove that : $\sec ^{2} \theta+\operatorname{cosec}^{2} \theta=\sec ^{2} \theta \cdot \operatorname{cosec}^{2} \theta$

## D Watch Video Solution

2. Prove that $\frac{\sin \theta}{1-\cos \theta}=\operatorname{cosec} \theta+\cot \theta$

## - Watch Video Solution

3. Prove that $\sec \theta(1-\sin \theta)(\sec \theta+\tan \theta)=1$

## - Watch Video Solution

4. Prove that $\frac{\sin \theta}{\operatorname{cosec} \theta+\cot \theta}=1-\cos \theta$
5. Prove that identity $\frac{\sin \theta}{\cos e c \theta}+\frac{\cos \theta}{\sec \theta}=1$

## - Watch Video Solution

6. Prove that identity $\sqrt{\frac{1-\cos \theta}{1+\cos \theta}}=\operatorname{cosec} \theta-\cot \theta$

## D Watch Video Solution

7. 

Prove
that
identity
$\left[\operatorname{cosec}\left(90^{\circ}-\theta\right)-\sin \left(90^{\circ}-\theta\right)\right][\operatorname{cosec} \theta-\sin \theta][\tan \theta+\cot \theta]=1$

## - Watch Video Solution

8. A kite is flying at a height of 60 m above the ground.The string attached to the kite is tied at the ground it makes an angle of $60^{\circ}$.

Assuming that the string is straight, find the length of the string . $(\sqrt{3}=1.732)$

## ( Watch Video Solution

9. Find the angle of elevation of the top of a tower from a point on the ground, which is 30 m away the foot of a tower of height $10 \sqrt{3} \mathrm{~m}$.

## D Watch Video Solution

10. A ramp for unloading a moving truck, has an angle of elevation of
$30^{\circ}$. If the top of the ramp is 0.9 m above the ground level, then find the length of the ramp.
11. A girl of height 150 cm stands in front of a lamp-post and casts a shadow of length $150 \sqrt{3} \mathrm{~cm}$ on the ground. Find the angle of elevation of the top of the lamp-post.

## - Watch Video Solution

12. Prove that $\sqrt{\cot ^{2} \theta-\cos ^{2} \theta}=\cot \theta \cdot \cos \theta$

## - Watch Video Solution

13. Prove that $\frac{1+\sin \theta}{\cos \theta}+\frac{\cos \theta}{1+\sin \theta}=2 \sec \theta$

## D Watch Video Solution

14. A tower is $100 \sqrt{3}$ metres high. Find the angle of elevation of its top from a point 100metres away from its foot.
15. If $\sin \theta=x$ and $\sec \theta=y$ then find the value of $\cot \theta$

## D Watch Video Solution

16. A circus artist is climbing a 20 m long rope, which is tightly stretched and tied from the top of a vertical pole to the ground. Find the height of the pole, if the angle made by the rope with the ground level is $30^{\circ}$ ( see figure).

## D Watch Video Solution

17. A kite is flying at a height of 60 m above the ground.The string attached to the kite is tied at the ground it makes an angle of $60^{\circ}$.

Assuming that the string is straight, find the length of the string . $(\sqrt{3}=1.732)$
18. Prove that $\sin ^{6} \theta+\cos ^{6} \theta+3 \sin ^{2} \theta \cos ^{2} \theta=1$

## D Watch Video Solution

Additional Questions Solved lii

1. Prove that $\sqrt{\frac{\sec \theta-1}{\sec \theta+1}}+\sqrt{\frac{\sec \theta+1}{\sec \theta-1}}=2 \operatorname{cosec} \theta$

## D Watch Video Solution

2. Prove that $\frac{1+\cos A}{\sin A}+\frac{\sin A}{1+\cos A}=2 \cos e c A$
3. Express the following sum or difference as a product
(ii) $\cos 6 \theta+\cos 2 \theta$

## Watch Video Solution

4. Prove that $\frac{\sin \left(90^{\circ}-\theta\right)}{1+\sin \theta}+\frac{\cos \theta}{1-\cos \left(90^{\circ}-\theta\right)}=2 \sec \theta$

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5. Prove that $\frac{\tan \theta}{1-\cot \theta}+\frac{\cot \theta}{1-\tan \theta}=1+\sec \theta \operatorname{cosec} \theta$

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6. Prove that $\frac{\sin \left(90^{\circ}-\theta\right)}{1-\tan \theta}+\frac{\cos \left(90^{\circ}-\theta\right)}{1-\cot \theta}=\cos \theta+\sin \theta$
7. Prove that $\frac{\tan \left(90^{\circ}-\theta\right)}{\operatorname{cosec} \theta+1}+\frac{\operatorname{cosec} \theta+1}{\cot \theta}=2 \sec \theta$

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8. Prove that $\frac{\cot \theta+\cos e c \theta-1}{\cot \theta-\cos e c \theta+1}=\cos e c \theta+\cot \theta$

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9. Prove that $(1+\cot \theta-\operatorname{cosec} \theta)(1+\tan \theta+\sec \theta)=2$

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10. Prove that $\frac{\sin \theta-\cos \theta+1}{\sin \theta+\cos \theta-1}=\frac{1}{\cos \theta-\tan \theta}$. using the identity $\sec ^{2} \theta=1+\tan ^{\circ}$.

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11. Prove that $\frac{1}{\operatorname{cosec} \theta-\cot \theta}-\frac{1}{\sin \theta}=\frac{1}{\sin \theta}-\frac{1}{\cos e c \theta+\cot \theta}$

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12. If $\tan \theta=n \tan \alpha$ and $\sin \theta=m \sin \alpha$ then prove that $\cos ^{2} \theta=\frac{m^{2}-1}{n^{2}-1}, n \neq \pm 1$.

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13. If $\sin \theta, \cos \theta$ and $\tan \theta$ are in G.P., then prove that $\cot ^{6} \theta-\cot ^{2} \theta=1$

## D Watch Video Solution

14. Find the value of $\cos 60^{\circ}+\sin 60^{\circ}$
15. Find the value of $\cos 90^{\circ}+\sin 90^{\circ}$

## D Watch Video Solution

16. A1.5 m tall boy is standing at some distance from a 30 m tall building. The angle of elevation from his eyse to the top of the building increase from $30^{\circ}$ to $60^{\circ}$ as he walks towards the building. Find the distance he walked towards the building.

## D Watch Video Solution

17. Find the value of $\cos 120^{\circ}$
