# ©゙doubtnut 

India's Number 1 Education App

## PHYSICS

## BOOKS - FULL MARKS PHYSICS (TAMIL

## ENGLISH)

## OSCILLATIONS

## In Text Book Example Problems

1. Classify the following motions as periodic and non-periodic motions?
(a) Motion of Halley's comet.
(b) Motion of clouds.
(c ) Moon revolving around the Earth.

## D Watch Video Solution

2. Which of the following functions of time represent periodic and non-periodic motion?
(a) $\sin \omega t+\cos \omega t$ (b) $e-\omega t$

## D Watch Video Solution

3. Which of the following represent simple harmonic motion?

# $x=A \sin \omega t+B \cos 2 \omega t$ <br> (iii) $x=A e^{i \omega t}$ <br> $x=A \ln \omega t$ 

## D Watch Video Solution

4. Consider a particle undergoing simple
harmonic motion. The velocity of the particle at position $x_{1}$ is $v_{1}$ and velocity of the particle at position $x_{2}$ is $v_{2}$. Show that the ratio of time period and amplitude is
$\frac{T}{A}=2 \pi \sqrt{\frac{x_{2}^{2}-x_{1}^{2}}{v_{1}^{2} x_{2}^{2}-v_{2}^{2}-x_{1}^{2}}}$
5. A nurse measured the average heart beats of a patient and reported to the doctor in terms of time period as $0.8 s$. Express the heart beat of the patient in terms of number of beats measured per minute.

## D Watch Video Solution

6. Calculate the amplitude, angular frequency,
frequency, time period and initial phase for the
simple harmonic oscillation given below:
(a) $y=0.3 \sin (40 \pi t+1.1)$
(b) $y=2 \cos (\pi t)$ (c)
$y=3 \sin (2 \pi t-1.5)$

## D Watch Video Solution

7. Show that for a simple harmonic motion, the phase difference between.
(a) displacement and velocity is $\frac{\pi}{2}$ radian or
(b) velocity and acceleration is $\frac{\pi}{2}$ radian or $90^{\circ}$.
(c) displacement and acceleration is $\pi$ radian or $180^{\circ}$
8. A spring balance has a scale which ranges from

0 to 25 kg and the length of the scale is 0.25 m . It
is taken to an unknown planet X where the acceleration due to gravity is $11.5 m s^{-1}$. Suppose a body a mass M kg is suspended in this spring and made to oscillate with a period of 0.50 s .

Compute the gravitational force acting on the body.
9. Consider two springs whose force constants are $1 \mathrm{Nm}^{-1}$ and $2 \mathrm{Nm}^{-1}$ which are connected in series. Calculate the effective spring constant $\left(k_{s}\right)$ and comment on $k_{s}$.

## (D) Watch Video Solution

10. Consider two springs with force constants
$1 \mathrm{Nm}^{-1}$ and $2 \mathrm{Nm}^{-1}$ connected in parallel.
Calculate the effective spring constant $\left(k_{p}\right)$ and comment on $k_{p}$.
11. Calculate the equivalent spring constant for the following system and also compute if all the spring constants are equal:

## - View Text Solution

12. A mass $m$ moves with $a$ speed $v$ on $a$ horizontal smooth surface and collides with a nearly massless spring whose spring constant is
k. If the mass stops after collision, compute the maximum compression of the spring.

## (D) Watch Video Solution

13. In simple pendulum experiment, we have used small angle approximation.

## D View Text Solution

14. If the length of the simple pendulum is increased by $44 \%$ from its original length,
calculate the percentage increase in time period of the pendulum.

## (D) Watch Video Solution

15. Write down the kinetic energy and total energy expressions in terms of linear momentum, For one-dimensional case.

## D Watch Video Solution

16. Compute the position of an oscillating particle when its kinetic energy and potential energy are
equal.

## ( Watch Video Solution

## Textual Evaluation Solved Multiple Choice Questions

1. In a simple harmonic oscillation, the acceleration against displacement for one complete oscillation will be.
A. an ellipse
B. a circle
C. a parabola

## D. a straight line

## Answer: D

## - Watch Video Solution

2. A particle executing SHM crossed points $A$ and B with the same velocity. Having taken 3 s in passing from $A$ to $B$, it returns to $B$ after another 3s. The time period is :
A. 15s
B. 6 s
C. 12s
D. 9 s

## Answer: C

## D Watch Video Solution

3. The length of a second's pendulum on the surface of the Earth is 0.9 m . The length of the
same pendulum of surface of planet $X$ such that the acceleration of planet X is n times greater than the Earth is :
A. $0.9 n$
B. $\frac{0.9}{n} m$
C. $0.9 n^{2} m$
D. $\frac{0.9}{n^{2}}$

Answer: A

## - Watch Video Solution

4. A simple pendulum is suspended from the roof of a school bus which movies in a horizontal
direction with an acceleration $a$, then the time period is :
А. $T=\propto \frac{1}{g^{2}+a^{2}}$
B. $T=\propto \frac{1}{\sqrt{g^{2}+a^{2}}}$
C. $T \propto \sqrt{g^{2}+a^{2}}$
D. $T \propto\left(g^{2}+a^{2}\right)$

Answer: A
5. Two bodies $A$ and $B$ whose masses are in the ratio 1:2 are suspended from two separate massless springs of force constants $k_{A}$ and $k_{B}$ respectively. If the two bodies oscillate vertically
such that their maximum velocities are in the ratio $1: 2$ the ratio of the amplitude $A$ to that of $B$ is :
A. $\sqrt{\frac{k_{B}}{2 k_{A}}}$
B. $\sqrt{\frac{k_{B}}{8 k_{A}}}$
C. $\sqrt{\frac{2 k_{B}}{k_{A}}}$
D. $\sqrt{\frac{8 k_{B}}{k_{A}}}$

## Answer: B

## (D) Watch Video Solution

6. A spring is connected to a mass $m$ suspended
from it and its time period for vertical oscillation
is T . spring is now cut into two equal halved and
the same mass is suspended fron one of the havles. The period of vertical oscillation is:
A. $T^{\prime}=\sqrt{2} T$
B. $T^{\prime}=\frac{T}{\sqrt{2}}$
C. $T^{\prime}=\sqrt{2 T}$
D. $T^{\prime}=\sqrt{\frac{T}{2}}$

## Answer: B

## D Watch Video Solution

7. A simple pendulum has a time period $T_{1}$. When its point of suspension is moved vertically upwards according as $y=k t^{2}$, where y is vertical
covered and $k=1 m s^{-2}$, its time period
becomes $T_{2}$ then $\frac{T_{1}^{2}}{T_{2}^{2}}$ is $\left(\mathrm{g}=10 \mathrm{~ms}^{-2}\right)$

$$
\frac{5}{6}
$$

B. $\frac{11}{10}$
C. $\frac{6}{5}$
D. $\frac{4}{5}$

## Answer: C

## D Watch Video Solution

8. An ideal spring of spring constant $k$, is suspended from the ceiling of a room and a blok of mass $m$ is fastened to its lower end. If the block is released when the spring is un-stretched, then then maximum extension in the spring is :
A. $4 \frac{M g}{k}$
B. $\frac{M g}{k}$
C. $2 \frac{M g}{k}$
D. $\frac{M g}{2 k}$

## Answer: C

## D Watch Video Solution

9. A pendulum is hung in a very high building and is moving freely to and fro like a simple harmonic oscillator. If the acceleration of the bob is
$16 \mathrm{~ms}^{-1}$ at a distance of 4 m from the mean position, then the time period is
A. 2 s
B. 1s
C. $2 \pi s$
D. $\pi s$

Answer: D
(D) Watch Video Solution
10. A hollow sphere is filled with water. It is hung by a long thread. As the water flows out of a hole at the bottom, the period of oscillation will
A. first increase and then decrease
B. first decrease and then increase
C. increase continuously
D. decrease continuously

Answer: A

## D Watch Video Solution

11. The damping force on an oscillator is directly proportional to the velocity. The units of the constant of proportionality are
A. $\mathrm{kgms}^{-1}$
B. $k g m s^{-2}$
C. $k g s^{-1}$
D. kgs

Answer: C
12. When a damped harmonic oscillator completes 100 oscillations, its amplitude is reduced to $\frac{1}{3}$ of its initial value. What will be its amplitude when it completes 200 oscillations ?
A. $\frac{1}{5}$
B. $\frac{2}{3}$
C. $\frac{1}{6}$
D. $\frac{1}{9}$

Answer: D
13. Which of the following different equations
represents a damped harmonic oscillator?
A. $\frac{d^{2} y}{d t^{2}}+y=0$
B. $\frac{d^{2} y}{d t^{2}}+\gamma \frac{d y}{d t}+y=0$
C. $\frac{d^{2} y}{d t^{2}}+k^{2} y=0$
D. $\frac{d y}{d t}+y=0$

Answer: B
(D) Watch Video Solution
14. If the inertial mass and gravitational mass of
the simple pendulum of length I are not equal,
then the time period of the simple pendulum is :
A. $T=2 \pi \sqrt{\frac{m_{i} l}{m_{g} g}}$
B. $T=2 \pi \sqrt{\frac{m_{g} l}{m_{i} g}}$
C. $T=2 \pi \frac{m_{g}}{m_{i}} \sqrt{\frac{l}{g}}$
D. $T=2 \pi \frac{m_{i}}{m_{g}} \sqrt{\frac{l}{g}}$

## Answer: A

## Textual Evaluation Solved li Short Answer Question

1. What is meant by periodic and non-periodic motion ? Give any two examples, for each motion ?

## - Watch Video Solution

2. What is meant by mean by force constant of a spring ?

D Watch Video Solution
3. Define time period of simple harmonic motion.
(D) Watch Video Solution
4. Define frequency of simple harmonic motion.

## (D) Watch Video Solution

5. what is an epoch ?
6. Write short notes on two springs connected in series.

- Watch Video Solution

7. Write short notes on two springs connected in parallel.

## D Watch Video Solution

8. Write down the time period of simple pendulum.

## - Watch Video Solution

9. State the laws of simple pendulum.

- Watch Video Solution

10. Write down the equation of time period for
linear harmonic oscillator?
(D) Watch Video Solution
11. What is meant by free oscillation ?
12. Explain damped oscillation. Give an example.

## - Watch Video Solution

13. Define forced oscillation. Give an example.

## - Watch Video Solution

14. What is meant by maintained oscillation ?

Given an example.

## - Watch Video Solution

15. Explain resonance. Give an example .
(D) Watch Video Solution

## Textual Evaluation Solved lii Long Answer Questions

1. What is meant by simple harmonic oscillation?

Give example
2. Describe Simple Harmonic Motion as a projection of uniform circular motion. The projection of uniform circular motion on a diameter of SHM

## (D) Watch Video Solution

3. What is meant by angular harmonic oscillations? Compute the time period of angular harmonic oscillation.

Time period and frequency of angular SHM:
4. Write down the difference between simple harmonic motion and angular simple harmonic motion.

## D Watch Video Solution

## 5. Discuss the simple pendulum in detail.

## - Watch Video Solution

6. Explain the horizontal oscillations of a spring.
7. Describe the vertical oscillations of a spring.
(D) Watch Video Solution
8. Write shorts notes on the oscillations of liquid column in U-tube.

- Watch Video Solution


## 9. Discuss in detail the energy in simple harmonic

 motion.
## D Watch Video Solution

10. Explain in detail the four different types of oscillations.

## D Watch Video Solution

1. Consider the Earth as a homogenous sphere of radius R and a straight hole is bored in it through its centre. Show that a particle dropped into the hole will execute a simple harmonic motion such
that its time period is $T=2 \pi \sqrt{\frac{R}{g}}$

## (D) Watch Video Solution

2. Calculate the time period of the oscillation of a particle of mass $m$ moving in the potential
defined as $U(x)= \begin{cases}\frac{1}{2} k x^{2}, & x<0 \\ m g x, & g>0\end{cases}$
3. Consider a simple pendulum of length I = 0.9 m which is properly placed on a trolley rolling down on a inclined plane which is at $0=45^{\circ}$ with the horizontal. Assuming that the inclined plane is frictionless. Assuming that the time period of oscillation of the simple pendulum is T . Find the value of $T$.

## D Watch Video Solution

4. A piece of wood of mass $m$ is floating erect in a liquid whose density is $\rho$. If it is slightly pressed down and released, then executes simple harmonic motion. Show that its time period of oscillation is $T=2 \pi \sqrt{\frac{m}{A \rho g}}$

## D Watch Video Solution

5. Consider two simple harmonic motion along $x$ and $y$ - axis having same frequencies but different amplitudes as $x=A \sin (\omega t+\varphi)$ (along $\mathbf{x}$ axis) and $y=B \sin \omega t$ ( along y axis).
then show that $\frac{x^{2}}{A^{2}}+\frac{y^{2}}{B^{2}}-\frac{2 x y}{A B} \cos \varphi=\sin ^{2} \varphi$ and also discuss the special cases when
$\varphi=\frac{\pi}{2}$ and $A=B$
Note : when a particle is subjected to two simple harmonic motion at right angle to each other the particle may move along different paths.

## - Watch Video Solution

6. Show that for a particle executing simple
harmonic motion the average value of kinetic energy is equal to the average value of potential energy.

## 7. Match the following :

| Column I | Column II |
| :--- | :--- |
| 1. Atto | (i) $10^{-15}$ |
| 2. Fermi | (ii) $10^{18}$ |
| 3. Femto | (iii) $10^{6}$ |
| 4. Micro | (iv) $10^{-13}$ |
|  | (v) $10^{-18}$ |
|  | (vi) $10^{-6}$ |

## - Watch Video Solution

Additional Questions Solved

# 1. The total energy of a particle vibrating in SHM 

 is proportional to the square of its.A. velocity

B. acceleration

C. amplitude

## D. none of these

Answer: A
2. Write down the time period of simple pendulum.

# A. its length should doubled 

B. its length should be quadrupled
C. the mass of its bob should be doubled
D. the mass of its bob should be quadrupled

Answer: B
3. A simple harmonic oscillator has amplitude A
and time period T . Its maximum speed is.................

$$
\begin{aligned}
& \text { A. } \frac{4 A}{T} \\
& \text { B. } \frac{2 A}{T} \\
& \text { C. } \frac{4 \pi A}{T} \\
& \text { D. } \frac{2 \pi A}{T}
\end{aligned}
$$

Answer: D
4. A simple harmonic oscillator has a period of 0.01 s and an amplitude of 0.2 m . The magnitude of the velocity in $\mathrm{m} / \mathrm{s}$ at the centre of oscillation is is..................
A. $20 \pi$
B. $40 \pi$
C. $60 \pi$
D. $80 \pi$

Answer: B

## 5. A particle is executing SHM. Then the graph of

 acceleration as a function of displacement isA. straight line
B. circle
C. ellipse
D. hyperbola

Answer: A
6. A particle is executing SHM. Then the graph of velocity as a function of displacement is.

A. straight line

B. circle
C. ellipse
D. hyperbola

Answer: C

D Watch Video Solution
7. The amplitude of a vibrating body situated in a resisting medium
A. decreases linearly with time
B. decreases exponentially with time
C. decreases with time in some other manner
D. remains constant with time

Answer: B

- Watch Video Solution

8. The frequency of a vibrating body situated in air.
A. is the same as its nautral frequency
B. is higher than its natural frequency
C. is lower than its natural frequency
D. can have any value

Answer: C
9. The equation $\frac{d^{2} y}{d t^{2}}+b \frac{d y}{d t}+\omega^{2} y=0$ represents the equation of motion for a....................vibration.
A. free

## B. damped

C. forced
D. resonant

Answer: B

## 10. The displacement equation of an oscillator is

 $y=5 \sin (0.2 \pi t+0.5 \pi)$ in $\mathbf{S I}$ units. The time period of oscillation is.A. 10 s
B. 1 s
C. 0.2 s
D. 0.5 s

Answer: A
11. A loaded spring vibrates with a period $T$. The spring is divided into four equal parts and the same load is suspended from one as these parts.

The new time period is.
A. $\frac{T}{4}$
B. $\frac{T}{2}$
C. 2 T
D. 4 T

Answer: B
12. The vertical extension in a light spring by a weight of 1 kg , in equilibrium is 9.8 cm . The period of oscillation of the spring, in seconds, will be.

> A. $\frac{2 \pi}{10}$
> B. $\frac{2 \pi}{100}$
C. $20 \pi$
D. $200 \pi$

Answer: A
13. A particle executing SHM has an acceleration of $64 \mathrm{~cm} / \mathrm{s}^{2}$ with its displacement is 4 cm . Its time period, in seconds is.
A. $\frac{\pi}{2}$
B. $\frac{\pi}{4}$
C. $\pi$
D. $2 \pi$

Answer: A
14. A body describes simple harmonic motion with an amplitude of 5 cm and a period of 0.2 s .

Find the acceleration and velocity of the body when the displacement is 5 cm .
A. $\frac{A}{3}$
B. $\frac{A}{2}$
C. $\frac{A}{\sqrt{2}}$
D. $\frac{A}{2 \sqrt{2}}$

Answer: C
15. The maximum displacement of a particle executing SHM is 1 cm and the maximum acceleration is $(1.57)^{2} \mathrm{~cm} / \mathrm{s}^{2}$. Its time period is. S.................
A. 0.25 s
B. 4.0s
C. 1.57s
D. 3.14 s

Answer: B
16. The velocity of a particle, undergoing SHM is v at the position. If its amplitude is doubled, the velocity at the mean position will be.
A. 2 v
B. 3 v
C. $2 \sqrt{2} v$
D. $4 v$

Answer: A
17. A girl is swinging on a swing in the sitting position. How will the period of swing be affected if she stands up?
A. The period will now be shorter
B. The period will now be longer
C. The period will remain unchanged
D. The period may become longer or shorter depending upon the height of the girl
18. The equation of SHM of a particle is $\frac{d^{2} y}{d t^{2}}+k y=0$, where $\mathbf{k}$ is a positive constant.

## The time period of motion is given by................

$$
\begin{aligned}
& \text { A. } \frac{2 \pi}{\sqrt{k}} \\
& \text { B. } \frac{2 \pi}{k} \\
& \text { C. } \frac{k}{2 \pi} \\
& \text { D. } \frac{\sqrt{k}}{2 \pi}
\end{aligned}
$$

Answer: A

## 19. The amplitude of a damped oscillator becomes

half in one minute. The amplitude after 3 minutes
will be $\frac{1}{x}$ time the original, where x is
A. $2 \times 3$
B. $2^{3}$
C. $3^{2}$
D. $3 \times 2^{2}$

Answer: B
20. When the potential energy of a particle executing simple harmonic motion is one-fourth of its maximum value during the oscillation, the displacement of the particle from the equilibrium position in terms of its amplitude a is
A. $\frac{a}{4}$
B. $\frac{a}{3}$
C. $\frac{a}{2}$
D. $\frac{2 a}{3}$

Answer: C

## (D) Watch Video Solution

21. A massless spring, having force constant $k$, oscillates with a frequency $n$ when a mass $m$ is
suspended from it. The spring is cut into two
equal halves and a mass $2 m$ is suspended from one of the parts. The frequency of oscillation will now be.
A. $n$
B. $n \sqrt{2}$
C. $\frac{n}{\sqrt{2}}$
D. $2 n$

Answer: A

## (D) Watch Video Solution

22. For a simple pendulum the graph between
length and time period will be a..............
A. hyperbola
B. Parabola
C. Straight line

## D. none of these

Answer: B

## - Watch Video Solution

23. A particle is executing simple harmonic motion given by $x=5 \sin \left(4 t-\frac{\pi}{6}\right)$. The velocity of the particle when its displacement is 3 units is

A. $\frac{2 \pi}{3}$ units
B. $\frac{5 \pi}{6}$ units

## C. 20 units

D. 16 units

Answer: D

## (D) Watch Video Solution

24. When a particle oscillates simple harmonically, its potential energy varies periodically. If the frequency of oscillation of the particle is $n$, the frequency of potential energy variation is.
A. $\frac{n}{2}$
B. $n$
C. 2n
D. 4 n

Answer: C

## D Watch Video Solution

25. A particle, moving along the $x$-axis, executes simple harmonic motion when the force acting on it is given by ( $A$ and $k$ are positive constant.).................
A. $-A k x$
B. $A \cos (k x)$
C. $A \exp (-k x)$
D. $A k x$

Answer: A

## - Watch Video Solution

26. The motion of a particle is expressed by the
equation $a=-b x$, where $\mathbf{x}$ is the displacement
from the mean position, $a$ is the acceleration and b is a constant. The periodic time is..............
A. $\frac{2 \pi}{b}$
B. $\frac{2 \pi}{\sqrt{b}}$
C. $2 \pi \sqrt{b}$
D. $2 \sqrt{\frac{\pi}{b}}$

Answer: B

- Watch Video Solution

27. The angular velocity and the amplitude of a simple pendulum are $\omega$ and a , respectively. The ratio of its kinetic and potential energies at a displacement $x$ from the mean position is.

$$
\begin{aligned}
& \text { A. } \frac{x^{2} \omega^{2}}{a^{2}-x^{2} \omega^{2}} \\
& \text { B. } \frac{x^{2}}{a^{2}-x^{2}} \\
& \text { C. } \frac{a^{2}-x^{2} \omega^{2}}{x^{2} \omega^{2}} \\
& \text { D. } \frac{a^{2}-x^{2}}{x^{2}}
\end{aligned}
$$

Answer: D
28. A particle is oscillating according to the equation $x=5 \cos (0.5 \pi t)$ where $t$ is in seconds.

The particle moves from the position of equilibrium to the position of maximum displacement in time.
A. 1 s
B. 2 s
C. 0.5 s
D. 4 s

## - Watch Video Solution

29. A seconds pendulum is placed in a space laboratory orbiting around the Earth at a height 3R from the Earth's surface where $R$ is the radius of the Earth. The time period of the pendulum will be.
A. zero
B. $2 / 3 s$
C. 4 s
D. inifinite

Answer: D

## D Watch Video Solution

30. A mass $m$ is vertically suspended from a spring of negligible mass, the system oscillates with a frequency $n$. What will be the frequency of
the system, if a mass 4 m is suspended from the same spring?
A. $\frac{n}{2}$
B. 2n
C. $\frac{n}{4}$

## D. 4 n

Answer: A

## - Watch Video Solution

31. Two simple pendulums of lengths 0.5 m and
2.0m respectively are given small linear displacement in one direction at the same time.

They will again be in phase when the pendulum of shorter length has
completed..............oscillations.
A. 5
B. 3
C. 1
D. 2

Answer: D

D Watch Video Solution
32. A body is executing simple harmonic motion with an angular frequency 2 rad/sec. The velocity
of the body at 20 mm displacement, when the amplitude of motion is 60 mm , is
A. $90 \mathrm{~mm} / \mathrm{s}$
B. $113 \mathrm{~mm} / \mathrm{s}$
C. $118 \mathrm{~mm} / \mathrm{s}$
D. $131 \mathrm{~mm} / \mathrm{s}$

Answer: B

- Watch Video Solution

33. If the displacement of a particle executing

SHM, is given by $y=0.30 \sin (220 t+0.64)$ in metre, then the frequency and the maximum velocity of the particle are ( $t$ is in seconds)
A. $35 \mathrm{~Hz}, 66 \mathrm{~m} / \mathrm{s}$
B. $45 \mathrm{~Hz}, 66 \mathrm{~m} / \mathrm{s}$
C. $58 \mathrm{~Hz}, 113 \mathrm{~m} / \mathrm{s}$
D. $35 \mathrm{~Hz}, 132 \mathrm{~m} / \mathrm{s}$

Answer: A
34. The kinetic energy of a particle, executing SHM, is 16 J when it is at its mean position. If the amplitude of oscillations is $\mathbf{2 5} \mathbf{~ c m}$, and the mass of the particle is 5.12 kg , the time period of its oscillation is
A. $\pi / 5 s$
B. $2 \pi s$
C. $20 \pi s$
D. $5 \pi s$

## - Watch Video Solution

35. A particle of mass $m$ is executing oscillations
about the origin on the $x$-axis. Its potential energy is $V(x)=k x^{2}$. Where $\mathbf{k}$ is a positive constant. If the amplitude of oscillation is a, then its time period T is.
A. Proportional to $\frac{1}{\sqrt{a}}$
B. independent of a
C. proportional to $\sqrt{a}$
D. proportional to $a^{3 / 2}$

Answer: B

## D Watch Video Solution

36. The amplitude of a damped oscillation reduces to one third of its original value $a_{0}$ in 20s. The amplitude of such oscillation after a period of 40 s will be.
A. $a_{0} / 9$
B. $a_{0} / 6$
C. $a_{0} / 2$

## D. $a_{0} / 27$

Answer: A

## - Watch Video Solution

37. Masses $m_{A}$ and $m_{B}$ hanging from the ends of strings of lengths $l_{A}$ and $l_{B}$ are executing.

Simple harmonic motions. If their frequencies are
related as $f_{A}=2 f_{B}$, then.
A. $l_{A}=2 l_{B}$ and $m_{A}=m_{B}$ ?
B. $l_{A}=4 l_{B}$ regardless of masses.

## C. $l_{A}=l_{B} / 4$ regardless of masses

D. $l_{A}=2 l_{B}$ and $m_{A}=2 m_{B}$

Answer: C

## D Watch Video Solution

38. Two simple harmonic motions act on a particle. These harmonic motions are
$x=A \cos (\omega t+\delta), y=A \cos (\omega t+\alpha)$
When $\delta=\alpha+\frac{\pi}{2}$, the resulting motion is.
A. A circle and the actual motion is clockwise
B. an ellipse and the actual motion is counter clockwise
C. a ellipse and the actual motion is clockwise
D. a circle and the actual motion is counter clockwise

Answer: D

## (D) Watch Video Solution

39. A metal bob is suspended from a coiled spring. When set into vertical vibrations on the
earth. It oscillates up and down with frequency f.
If the same experiment is carried out in a satellite
circling the Earth the frequency of vibration will be.
A. f
B. zero
C. infinite
D. depend on the distance of the satellite from the earth

Answer: A
40. In forced oscillations of a particle, the amplitude is maximum for a frequency $\omega_{1}$ of the
force, while the energy is maximum for a frequency $\omega_{2}$ of the force. Then.
A. $\omega_{1}<\omega_{2}$
B. $\omega_{1}<\omega_{2}$ when damping is small and
$\omega_{1}>\omega_{2}$ when damping is large
C. $\omega_{1}>\omega_{2}$
D. $\omega_{1}=\omega_{2}$

Answer: D

## (D) Watch Video Solution

41. Which one of the following statements is true
for the speed $v$ and the acceleration $a$ of $a$ particle executing simple harmonic motion?
A. When $v$ is maximum, $a$ is maximum
B. Value of a is zero, whatever may be the
value of $v$
C. When $v$ is zero, a is zero

D. When $v$ is maximum, $a$ is zero

Answer: D

## D Watch Video Solution

42. The function $\sin ^{2}(\omega t)$ represents
A. a simple harmonic motion with a period
$\pi / \omega$
B. a simple harmonic motion with a period
$2 \pi / \omega$

# C. a periodic, but not simple harmonic motion 

## with a period $\pi / \omega$

D. a periodic, but not simple harmonic motion
with a period $2 \pi / \omega$

Answer: A

## D Watch Video Solution

43. A particle executing simple harmonic motion
has a kinetic energy $K_{o} \cos ^{2} \omega t$. The maximum
values of the potential energy and the total energy are, respectively............
A. $k_{0} / 2$ and $k_{0}$
B. $k_{0}$ and $2 k_{0}$
C. $k_{0}$ and $k_{0}$
D. 0 and $2 k_{0}$

Answer: C
( Watch Video Solution
44. A particle executing simple harmonic motion of amplitude 5 cm has maximum speed of 31.4 $\mathrm{cm} / \mathrm{s}$. The frequency of its oscillation is.
A. 3 Hz
B. 4 Hz
C. 2 Hz
D. 1 Hz

Answer: D

- Watch Video Solution

45. The phase difference between the instantaneous velocity \& acceleration of a particle executing simple harmonic motion is
A. $0.5 \pi$
B. $\pi$
C. $0.707 \pi$
D. zero

Answer: A
46. Which one of the following equations of motion represents simple harmonic motion?
A. Acceleration $=-k_{0} x+k_{1} x^{2}$
B. Acceleration $=-k(x+a)$
C. Acceleration $=k(x+a)$
D. Acceleration $=k x$

Answer: B

D Watch Video Solution
47. Which of the following functions represent

## SHM?

I. $y=\sin \omega t-\cos \omega t$ II. $y=\sin ^{3} t$
III. $Y=5 \cos \left(\frac{3 \pi}{4}-3 \omega t\right)$

A. I and III

## B. I and II

C. only I
D. I, II and III

Answer: A
48. Two simple harmonic motions of angular frequencies 100 and $1000 \mathrm{rad} / \mathrm{s}$ have the same displacement amplitude. The ratio of their maximum acceleration is.
A. $1: 10$
B. $1: 10^{2}$
C. $1: 10^{3}$
D. $1: 10^{4}$

Answer: B
49. The period of oscillation of a simple pendulum is $\mathbf{T}$ in a stationary lift. If the lift moves upwards with an acceleration of 8 g , the period will.
A. remain the same
B. decrease by $\mathrm{T} / 2$
C. increase by $\mathrm{T} / 3$
D. none of these
50. A simple harmonic oscillator consist of a particle of mass $m$ and an ideal spring with spring constant k . The particle oscillates with a time period T . The spring is cut into two equal parts.

If one part oscillates with the same particle, the time period will be.
A. $T / 2$
B. $\frac{T}{\sqrt{2}}$
C. $\sqrt{2} T$
D. $2 T$

Answer: B

## (D) Watch Video Solution

51. A particle executing simple harmonic motion of amplitude 5 cm has maximum speed of 31.4 $\mathrm{cm} / \mathrm{s}$. The frequency of its oscillation is.
A. 3 Hz
B. 4 Hz

## C. 2 Hz

D. 1 Hz

## Answer: D

## - Watch Video Solution

## Additional Questions Solved 2 Marks Questions

## 1. What is Oscillatory motion?

D Watch Video Solution

## 2. Define simple harmonic motion (S.H.M)

## - Watch Video Solution

## 3. What is meant by displacement in SHM?

D Watch Video Solution
4. Define velocity in SHM.

D Watch Video Solution

## 5. Define acceleration.

## - Watch Video Solution

6. What is meant by phase of a particle executing SHM ?
(D) Watch Video Solution
7. What is meant by angular oscillation?

D Watch Video Solution

## 8. Define amplitude of the wave.

## - Watch Video Solution

## Additional Questions Solved 3 Marks Questions

1. Derive the expression for resultant spring constant when two springs having constant $k_{1}$ and $k_{2}$ are connected in series.

D Watch Video Solution
2. Derive the expression for resultant spring constant when two springs having constant $k_{1}$ and $k_{2}$ are connected in parallel.

## D Watch Video Solution

## Additional Questions Solved Iv Numerical Problems

1. A pendulum is hung from the roof of $a$ sufficiently high building and is moving freely to
and fro like a simple harmonic oscillator. The acceleration of the bob of the pendulum is
$20 \mathrm{~ms}^{-2}$ at a distance of 5 m from the mean position. To find the time period of oscillation.

## ( Watch Video Solution

2. The acceleration dula to gravity on the surface of moon is $1.7 \mathrm{~ms}^{-2}$. What is the time period of a simple pendulum on the surface of moon if its time period on the surface of earth is 3.5 s ?
3. A particle executes linear simple harmonic motion with an amplitude of 3 cm . When the particle is at 2 cm from the mean position, the magnitude of its velocity is equal to that of its acceleration. Then find its time period in seconds.

## D Watch Video Solution

4. A body of mass $m$ is attached to lower end of a spring whose upper end is fixed. The spring has negligible mass. When the mass $m$ is slightly pulled down and released, it oscillates with a time
period of 3 s . When the mass $m$ is increased by 1 kg , the time period of oscillations becomes 5 s . Find the value of m is kg .

## D Watch Video Solution

5. Two simple harmonic motions are represented
by the equations:
$x_{1}=5 \sin \left(2 \pi t+\frac{\pi}{4}\right), x^{2}=5 \sqrt{2}(\sin 2 \pi t+\cos 2 \pi t)$
What is the ratio of their amplitudes?

- Watch Video Solution

6. A block whose mass is 1 kg is fastened to a spring. The spring has a spring constant of $50 \mathrm{Nm}^{-1}$. The block is pulled to a distance $\mathrm{x}=10$ cm from its equilibrium position at $\mathrm{x}=0$ on a frictionless surface from rest at $\mathbf{t}=0$. Calculate the kinetic, potential and total energies of the block when it is 5 cm away from the mean position.

## Watch Video Solution

7. A $5 \mathbf{~ k g ~ c o l l a r ~ i s ~ a t t a c h e d ~ t o ~ a ~ s p r i n g ~ o f ~ s p r i n g ~}$ constant $500 \mathrm{~N} \mathrm{~m}^{-1}$. It slides without friction over a horizontal rod. The collar is displaced from its equilibrium position by 10.0 cm and released.

Calculate
(a) the period of oscillation,
(b) the maximum speed and
(c) maximum acceleration of the collar.

- Watch Video Solution

8. A 0.2 kg of mass hangs at the end of a spring.

When 0.02 kg more mass is added to the end of
the spring, it stretches 7 cm more. If the 0.02 kg mass is removed, what will be the period of
vibration of the system?

## (D) Watch Video Solution

9. A mass $M$ is suspended from a spring of negligible mass. The spring is pulled a little and
then released so that the mass executes SHM of
time period $T$. If the mass is increased by $m$, the
time period becomes $5 \mathrm{~T} / 3$. What is the ratio $m / M ?$
(D) Watch Video Solution
10. A body describes simple harmonic motion with an amplitude of 5 cm and a period of 0.2 s .

Find the acceleration and velocity of the body
when the displacement is 5 cm .

- Watch Video Solution

