



MATHS

BOOKS - FULL MARKS MATHS (TAMIL ENGLISH)

APPLICATIONS OF INTEGRATION

Example

1. Estimate the value of $\int_0^{0.5} x^2 dx$ using the Riemann sums corresponding to 5

subintervals of equal width and applying (i) left-end rule (ii) right-end rule (iii) the midpoint rule.



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2. Evaluate $\int_0^1 x dx$, as the limit of a sum.



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3. Evaluate $\int_0^1 x^3 dx$, as the limit of a sum.



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4. Evaluate $\int_1^4 (2x^2 + 3) dx$, as the limit of a sum



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5. Evaluate $\int_0^3 (3x^2 - 4x + 5) dx$.



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6. Evaluate $\int_0^1 \frac{2x + 7}{5x^2 + 9} dx$,



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7. Evaluate, $\int_0^1 [2x] dx$ where $[.]$ is the greatest integer function .



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8. Evaluate $\int_0^{\frac{\pi}{3}} \frac{\sec x \tan x}{1 + \sec^2} x dx$



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9. Evaluate $\int_0^9 \frac{1}{x + \sqrt{x}} dx$.

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10. $\int_1^2 \frac{x dx}{(x + 1)(x + 2)}$.

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11. Evaluate: $\int_0^{\frac{\pi}{2}} \frac{\cos \theta}{(1 + \sin \theta)(2 + \sin \theta)} d\theta$.



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12. Evaluate: $\int_0^{\frac{1}{\sqrt{2}}} \frac{\sin^{-1} x}{(1-x^2)^{\frac{3}{2}}} dx.$



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13. Evaluate: $\int_0^{\frac{\pi}{2}} (\sqrt{\tan x} + \sqrt{\cot x}) dx.$



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14. Evaluate: $\int_0^{1.5} [x^2] dx$, where $[x]$ is the greatest integer function.



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15. Evaluate: $\int_{-4}^4 |x + 3| dx$.



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16. Show that $\int_0^{\frac{\pi}{2}} \frac{dx}{4 + 5 \sin x} = \frac{1}{3} \log_e 2$



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17. Prove that
$$\int_0^{\frac{\pi}{4}} \frac{\sin 2x dx}{\sin^4 x + \cos^4 x} = \frac{\pi}{4}$$



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18.

Evaluate:

$$\int_0^{\frac{\pi}{4}} \frac{dx}{a^2 \sin^2 x + b^2 \cos^2 x} = \frac{1}{ab} \tan^{-1} \left(\frac{a}{b} \right),$$

where $a, b > 0$



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19. Evaluate: $\int_0^{\frac{\pi}{4}} \frac{1}{\sin x + \cos x} dx$.



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20. Show that

$$\int_0^{\pi} g(\sin x) dx = 2 \int_0^{\frac{\pi}{2}} g(\sin) dx,$$

where $g(\sin x)$ is a function of $\sin x$.



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21. Evaluate $\int_0^{\pi} \frac{x}{1 + \sin x} dx$.





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22.

Show

that

$$\int_0^{2\pi} g(\cos x) dx = 2 \int_0^{\pi} g(\cos x) dx,$$

where

$g(\cos x)$ is a function of $\cos x$.



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23.

If $\int_a^b f(x) dx = \int_a^b f(a+b-x) dx$,

then

$$\int_0^{2a} f(x) dx = \int_0^a f(x) dx + \int_a^{2a} f(x) dx = 2 \int_0^a f(x) dx$$



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24. Evaluate : $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} x \cos x dx$.



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25. Evaluate: $\int_{-\log 2}^{\log 2} e^{-|x|} dx$.



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26. Evaluate $\int_0^a \frac{f(x)}{f(x) + f(a-x)} dx$.



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27. Prove that $\int_0^{\frac{\pi}{4}} \log(1 + \tan x) dx = \frac{\pi}{8} \log 2$.



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28. Show that

$$\int_0^1 \tan^{-1} x + \tan^{-1}(1 - x) dx = \frac{\pi}{2} - \log_e 2$$



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29. Evaluate: $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x} + \sqrt{x}} dx.$

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30. Evaluate $\int_{-\pi}^{\pi} \frac{\cos^2 x}{1 + a^x} dx.$

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31. Evaluate $\int_0^{\pi} x^2 \cos nx dx,$ where n is positive integer.

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32. Evaluate: $\int_0^1 e^{-2x} (1 + x - 2x^3) dx$.



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33. Evaluate: $\int_0^{2\pi} x^2 \sin nx dx$, where n is positive integer.



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34. Evaluate: $\int_{-1}^1 e^{-\lambda x} (1 - x^2) dx$.



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35. Evaluate: $\int_b^\infty \frac{1}{a^2 + x^2} dx, a > 0, \text{in } \mathbb{R}$.



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36. Evaluate: $\int_0^{\frac{\pi}{2}} \frac{dx}{4 \sin^2 x + 5 \cos^2 x}$



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37. Evaluate $\int_0^{\frac{\pi}{2}} (\sin^2 x + \cos^4 x) dx$



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38. Evaluate: $\int_0^{\frac{\pi}{2}} \left| \begin{array}{cc} \cos^4 x & 7 \\ \sin^5 x & 3 \end{array} \right| dx.$



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39. Find the values of the following: (i)

$$\int_0^{\frac{\pi}{2}} \sin^5 x \cos^4 x dx$$

(ii) $\int_0^{\frac{\pi}{2}} \sin^4 x \cos^6 x dx$



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40. Evaluate: $\int_0^{2a} x^2 \sqrt{2ax - x^2} dx.$



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41. Evaluate: $\int_0^1 x^5 (1 - x^2)^5 dx.$



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42. Evaluate: $\int_0^1 x^3(1-x)^4 dx$.



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43. Prove that $\int_0^{\infty} x^n e^{-x} dx = n!$, Where n is a positive integer.



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44. Evaluate : $\int_0^{\infty} e^{-ax} x^n dx$, where $a > 0$.



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45. Show that $\Gamma(n) = 2 \int_0^{\infty} e^{-x^2} x^{2n-1} dx$.



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46. Evaluate $\int_0^{\infty} \frac{x^n}{n^x} dx$, where n is a positive integer.



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47. Find the area of the region bounded by the line $6x+5y=30$, x-axis and the lines $x=-1$ and $x=3$.



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48. Find the area of the region bounded by the line $7x-5y=35$, x-axis and the lines $x=-2$ and $x=3$.



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49. Find the area of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$.



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50. Find the area of the parabola $y^2 = 4ax$ and its latus rectum.



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51. Find the area of the region bounded by y axis and the parabola $x = 5 - 4y - y^2$.



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52. Find the area of the region bounded by x -axis, the sine curve $y = \sin x$, the lines $x = 0$ and $x = 3\pi$.



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53. Find the area of the region bounded by x -axis, the curve $y = |\cos x|$, the lines $x = 0$ and $x = \pi$.



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54. Find the area of the region bounded by the parabolas $y^2 = 4x$ and $x^2 = 4y$.



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55. Find the area of the region bounded between the parabola $x^2 = y$ and the curve $y = |x|$.



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56. Find the area of the region bounded by

$y = \cos x$, $y = \sin x$, the lines

$$x = \frac{\pi}{4} \text{ and } x = \frac{5\pi}{4}.$$



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57. The region enclosed by the circle

$x^2 + y^2 = a^2$ is divided into two segments by

the line $x=h$. Find the area of the smaller

segment.



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58. Find the area of the region in the first quadrant bounded by the parabola $y^2 = 4x$, the line $x+y=3$ and the y-axis.



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59. Find by integration, the area of the region bounded by the lines $5x - 2y = 15$, $x + 4 = 0$ and the x-axis.



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60. Using integration find the area of the region bounded by triangle ABC, whose vertices A,B and C are $(-1,1)$, $(3,2)$, and $(0,5)$ respectively.



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61. Using integration find the area of the region which is bounded by x-axis the tangent and normal to the circle $x^2 + y^2 = 4$ drawn at $(1, \sqrt{3})$.





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62. Find the volume of the sphere of radius a .



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63. Find the volume of a right-circular cone of base radius r and height h .



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64. Find the volume of the spherical cap of height h cut off from a sphere of radius r .

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65. Find the volume of the solid formed by revolving the region bounded by the parabola $y = x^2$, x -axis, ordinates $x=0$ and $x=1$ about the x -axis.

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66. Find the volume of the solid formed by revolving the region bounded by the ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1, a > b \text{ about the major x-axis,}$$



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67. Evaluate the volume of the solid generated by revolving about y axis the region bounded between the parabola $y^2 = x + 1$, the y axis and the lines $y = 1$ and $y = -1$.



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68. Find, by integration, the volume of the solid generated by revolving about y-axis the region bounded between the curve $y = \frac{3}{4}\sqrt{x^2 - 16}$, $x \geq 4$, the y-axis and the lines $y=1$ and $y=6$



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69. Find, by integration, the volume of the solid generated by revolving about y axis, the

region bounded by the curve

$y = \log x$, $y = 0$, $x = 0$ and $y = 2$.



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Exercise 9 1

1. Find an approximate value of $\int_1^{1.5} x dx$ by applying the left-end rule with the partition $\{1.1, 1.2, 1.3, 1.4, 1.5\}$



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2. Find an approximate value of $\int_1^{1.5} x dx$ by applying the left-end rule with the partition $\{1.1, 1.2, 1.3, 1.4, 1.5\}$

A.

B.

C.

D.

Answer: 0.855



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3. Find an approximate value of

$$\int_1^{1.5} (2 - x) dx$$
 by applying the mid-point rule

with the partition $\{1.1, 1.2, 1.3, 1.4, 1.5\}$



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Exercise 9 2

1. Evaluate the following integrals as the limits

of sum: (i) $\int_0^1 (5x + 4) dx$.

(ii) $\int_1^2 (4x^2 - 1) dx$.



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Exercise 9 3

1. Evaluate the following definite integrals :

$$\int_{-1}^1 \frac{dx}{x^2 + 2x + 5}$$



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Exercise 9 4

1. Evaluate $\int_0^1 x e^{-2x} dx$



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2. Evaluate the following :

$$\int_0^1 \frac{\sin(3 \tan^{-1} x) \tan^{-1} x}{1 + x^2} dx$$



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3. Evaluate the following :

$$\int_0^{\frac{1}{\sqrt{2}}} \frac{e^a \sin^{-1} x \sin^{-1} x}{\sqrt{1 - x^2}} dx$$



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4. Evaluate : $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} x \cos x dx.$



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Exercise 9 5

1. Evaluate the following :

$$\int_0^{\frac{\pi}{2}} \frac{dx}{1 + 5 \cos^2 x}$$



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Exercise 9 6

1. Evaluate the following :

$$\int_0^{\frac{\pi}{2}} \sin^{10} x dx$$



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Exercise 9 7

1. Evaluate the following :

$$\int_0^{\infty} x^5 e^{-3x} dx$$



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2. If $\int_0^{\infty} e^{-ax^2x^3} dx = 32, \alpha > 0$, find α .



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Exercise 9 8

1. Find the area of the region bounded by $3x - 2y + 6 = 0$, $x = -3$, $x = 1$ and x-axis.



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2. Find the area of the region bounded by $2x - y + 1 = 0$, $y = -1$, $y = 3$ and y-axis.



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3. Find the area of the region bounded by the curve $2 + x - x^2 + y = 0$, x-axis, $x = -3$ and $x = 3$



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4. Find the area of the region bounded by the line $y = 2x + 5$ and the parabola $y = x^2 - 2x$



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5. Find the area of the region bounded between the curves $y = \sin x$ and $y = \cos x$ and the lines $x = 0$ and $x = \pi$.



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6. Find the area of the region bounded by $y = \tan x$, $y = \cot x$ and the line $x = 0$, $x = \frac{\pi}{2}$, $y = 0$



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7. Find the area of the region bounded by the parabola $y^2 = x$ and the line $y = x - 2$



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8. Father of a family wishes to divide his square field bounded by $x = 0$, $x = 4$, $y = 4$, and $y = 0$ along the curve $y^2 = 4x$ and $x^2 = 4y$ into three equal parts for his wife, daughter and son. Is it possible to divide ? If so, find the area to be divided among them.



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9. The curve $y = (x - 2)^2 + 1$ has a minimum point at P. A point Q on the curve is such that the slope of PQ is 2. Find the area bounded by the curve and the chord PQ.



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10. Find the area of the region common to the circle $x^2 + y^2 = 16$ and the parabola $y^2 = 6x$.



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Exercise 9 9

1. Find, by integration, the volume of the solid generated by revolving about the x-axis, the region enclosed by $y = 2x^2$, $y = 0$ and $x = 1$.



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2. Find, by integration, the volume of the solid generated by revolving about the x-axis, the

region enclosed by $y = e^{-2x}$, $y = 0$, $x = 0$ and $x = 1$



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3. Find, by integration, the volume of the solid generated by revolving about the y -axis, the region enclosed by $x^2 = 1 + y$ and $y = 3$.



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4. The region enclosed between the graphs of $y = x$ and $y = x^2$ is denoted by R, Find the volume generated when R is rotated through 360° about x - axis.



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5. find the integration, the volume of the container which is in the shape of a right circular conical frustum as shown in the figure.



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6. A watermelon has an ellipsoid shade which can be obtained by revolving an ellipse with major-axis 20 cm and minor-axis 10 cm about its major-axis. Find its volume using integration.



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Exercise 9 10

1. The value of $\int_0^{\frac{2}{3}} \frac{dx}{\sqrt{4-9x^2}}$ is

A. $\frac{\pi}{6}$

B. $\frac{\pi}{2}$

C. $\frac{\pi}{4}$

D. π

Answer: A



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2. The value of $\int_{-1}^2 |x| dx$

A. $\frac{1}{2}$

B. $\frac{3}{2}$

C. $\frac{5}{2}$

D. $\frac{7}{2}$

Answer: C



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3. For any value of

$n \in Z$, $\int_0^\pi e^{\cos^2 x} \cos^3[(2n + 1)x] dx$ is

A. $\frac{\pi}{2}$

B. (π)

C. 0

D. 2

Answer: C



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4. The value of $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \sin^2 x \cos x dx$ is

A. $\frac{3}{2}$

B. $\frac{1}{2}$

C. 0

D. $\frac{2}{3}$

Answer: D



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5. The value of

$$\int_{-4}^4 \left[\tan^{-1} \left(\frac{x^2}{x^4 + 1} \right) + \tan^{-1} \left(\frac{x^4 + 1}{x^2} \right) \right] dx$$

is

A. π

B. 2π

C. 3π

D. 4π

Answer: D



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6. The value of

$$\int_{-\frac{\pi}{4}}^{\frac{\pi}{4}} \left(\frac{2x^7 - 3x^5 + 7x^3 - x + 1}{\cos^2 x} \right) dx \text{ is}$$

A. 4

B. 3

C. 2

D. 0

Answer: B



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7. If $f(x) = \int_0^x t \cos t dt$, then $\frac{df}{dx}$

A. $\cos x - x \sin x$

B. $\sin x + x \cos x$

C. $x \cos x$

D. $x \sin x$

Answer: C



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8. The area between $y^2 = 4x$ and its latus rectum is

A. $\frac{2}{3}$

B. $\frac{4}{3}$

C. $\frac{8}{3}$

D. $\frac{5}{3}$

Answer: C



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9. The value of $\int_0^1 x(1-x)^{99} dx$ is

A. $\frac{1}{11000}$

B. $\frac{1}{10100}$

C. $\frac{1}{10010}$

D. $\frac{1}{10001}$

Answer: B



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10. The value of $\int_0^\pi \frac{dx}{1+5^{\cos x}}$ is.....

A. $\frac{\pi}{2}$

B. π

C. $\frac{3\pi}{2}$

D. 2π

Answer: A



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11. The value of $\frac{r(n+2)}{r(n)} = 90$ then n is

A. 10

B. 5

C. 8

D. 9

Answer: D



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12. The value of $\int_0^{\frac{\pi}{6}} \cos^3 3x dx$

A. $\frac{2}{3}$

B. $\frac{2}{9}$

C. $\frac{1}{9}$

D. $\frac{1}{3}$

Answer: B



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13. The value of $\int_0^{\pi} \sin^4 x dx$ is

A. $\frac{3\pi}{10}$

B. $\frac{3\pi}{8}$

C. $\frac{3\pi}{4}$

D. $\frac{3\pi}{2}$

Answer: B



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14. The value of $\int_0^{\infty} e^{-3x} x^2 dx$ is

A. $\frac{7}{27}$

B. $\frac{5}{27}$

C. $\frac{4}{27}$

D. $\frac{5}{27}$

Answer: D



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15. If $\int_0^a \frac{1}{4+x^2} dx = \frac{\pi}{8}$ then a is

A. 4

B. 1

C. 3

D. 2

Answer: D



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16. The volume of solid of revolution of the region bounded by $y^2 = x(a - x)$ about x -axis is

A. $(\pi a)^2$

B. $\frac{\pi a^3}{4}$

C. $\frac{\pi a^3}{5}$

D. $\frac{\pi a^3}{6}$

Answer: D



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17. If $f(x) = \int_1^x \frac{e^{\sin u}}{u} du, x > 1$ and

$\int_1^3 \frac{e^{\sin x^2}}{x} dx = \frac{1}{2}[f(a) - f(1)]$, then one of

the possible value of a is

A. 3

B. 6

C. 9

D. 5

Answer: C



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18. The value of $\int_0^1 (\sin^{-1} x)^2 dx$ is

A. $\frac{(\pi)^2}{4} - 1$

B. $\frac{(\pi)^2}{4} + 2$

C. $\frac{(\pi)^2}{4} + 1$

D. $\frac{(\pi)^2}{4} - 2$

Answer: D



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19. The value of $\int_0^a \left(\sqrt{a^2 - x^2}\right)^3 dx$ is..... .

A. $\frac{\pi a^3}{16}$

B. $\frac{3\pi a^4}{16}$

C. $\frac{3\pi a^2}{8}$

D. $\frac{3\pi a^4}{8}$

Answer: B



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20. If $\int_0^x f(t) dt = x + \int_x^1 t f(t) dt$, then the value of $f(1)$ is

A. $\frac{1}{2}$

B. 2

C. 1

D. $\frac{3}{4}$

Answer: A



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Additional Problems

1. Evaluate as the limit of sums : $\int_1^3 (2x^2 + 5) dx$



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2. Evaluate as the limit of sums:

$$\int_1^2 (x^2 - 1) dx$$



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3. Evaluate : $\int_0^2 (x^2 + x + 2) dx$.



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4. Evaluate: $\int_{-\pi/4}^{\pi/4} x^3 \sin^2 x dx$.



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5. Evaluate $\int_{-1}^1 \log\left(\frac{3-x}{3+x}\right) dx$.



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6. Evaluate: $\int_{-\pi/2}^{\pi/2} x \sin x \, dx$



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7. Evaluate: $\int_0^1 x(1-x)^n \, dx$.



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8. Evaluate: $\int_{\pi/6}^{\pi/3} \frac{dx}{1 + \sqrt{\cot x}}$.



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9. Evaluate: $\int_0^{2\pi} \frac{\cos x}{\sqrt{4 + 3 \sin x}} dx$

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10. Evaluate: $\int_0^{\pi/4} \frac{\sin^3 x}{\cos^5 x} dx$

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11. Evaluate: $\int_0^{\pi/2} \sqrt{\sin \theta} \cos^5 \theta d\theta$

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12. Evaluate: $\int_0^{\pi/3} \frac{\sec x \tan x}{1 + \sec^2 x} dx$



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13. Evaluate, $\int_0^{\pi/2} \frac{dx}{5 + 4 \sin x}$.



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14. Evaluate: $\int_0^{\pi/4} \frac{dx}{4 + 5 \cos^2 x}$.



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15. Evaluate: $\int_0^{\pi/2} \frac{dx}{4 + 9 \cos^2 x}$

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16. $\int_0^{\pi/2} \sin^7 x dx$ is :

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17. Evaluate $\int_0^{\pi/2} \sin^4 x \cos^2 x dx$.



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18. Find the area of the region bounded by

$$y^2 = 4ax \text{ and } x = |y|.$$



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19. Find the area of bounded by the curve

$$y = x^3 \text{ and the line } y=x.$$



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20. Find the area of the loop and the curve

$$3ay^2 = x(x - a)^2.$$



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21. Find the area between the line $y = x + 1$

and the curve $y = x^2 - 1$



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22. The volume of the solid that results when the region enclosed by $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ is revolved about the minor axis is :

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23. Find the volume of the solid generated when the region enclosed by $y = \sqrt{x}$, $y = 3$ and $x = 0$ is revolved about y axis.

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24. The area bounded by the line $y=x$, the x-axis, the ordinates $x=1, x=2$ is

A. $\frac{3}{2}$

B. $\frac{5}{2}$

C. $\frac{1}{2}$

D. $\frac{7}{2}$

Answer: a



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25. The area of the region bounded by the graph of $y = \sin x$ and $y = \cos x$ between $x = 0$ and $x = \frac{\pi}{4}$ is

A. $\sqrt{2}$

B. $\sqrt{2} - 1$

C. $\sqrt[2]{2} - 2$

D. $\sqrt[2]{2} + 2$

Answer: b



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26. Find the area of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$.

A. $\pi b(a - b)$

B. $2\pi a(a - b)$

C. $\pi a(a - b)$

D. $2\pi b(a - b)$

Answer: c



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27. The area bounded by the parabola $y^2 = x$ and its latus rectum is

A. $\frac{4}{3}$

B. $\frac{1}{6}$

C. $\frac{2}{3}$

D. $\frac{8}{3}$

Answer: B



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28. The volume of solid obtained by revolving

$$\frac{x^2}{9} + \frac{y^2}{16} = 1 \text{ about the minor axis :}$$

A. 48π

B. 64π

C. 32π

D. 128π

Answer: b



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29. The volume when $y = \sqrt{3 + x^2}$ from $x = 0$ to $x = 4$ is rotated about x-axis is

A. 100π

B. $\frac{100}{9}\pi$

C. $\frac{100}{3}\pi$

D. $\frac{100}{9}$

Answer: c



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30. the volume generated when the region bounded by $y=x$, $y=1$, $x=0$, is rotated about y -axis is

A. $\frac{\pi}{4}$

B. $\frac{\pi}{2}$

C. $\frac{\pi}{3}$

D. $\frac{2\pi}{3}$

Answer: c



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31. Volume of solid obtained by revolving the area of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ about major and minor axes are in the ratio.....

A. $b^2 : a^2$

B. $a^2 : b^2$

C. $a : b$

D. $b : a$

Answer: d



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32. The volume generated by rotating the triangle with vertices at $(0,0)$, $(3,0)$ and $(3,3)$ about x-axis is

A. 18π

B. 2π

C. 36π

D. 9π

Answer: d



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33. The length of the arc of the curve

$$x^{2/3} + y^{2/3} = 4 \text{ is.....}$$

A. 48

B. 24

C. 12

D. 96

Answer: a



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34. The surface area of the solid of revolution of the region bounded by $y = 2x$, $x = 0$ and $x = 2$ about x-axis is....

A. $8\sqrt{5}\pi$

B. $2\sqrt{5}\pi$

C. $\sqrt{5}\pi$

D. $4\sqrt{5}\pi$

Answer: a



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35. The curved surface area of a sphere of radius 5, intercepted between two parallel planes of distance 2 and 4 from the centre is

A. 20π

B. 40π

C. 10π

D. 30π

Answer: a



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