



## MATHS

### BOOKS - FULL MARKS MATHS (TAMIL ENGLISH)

#### SAMPLE PAPER - 17

#### Part I

1. If  $A = \begin{bmatrix} 1 & \tan \frac{\theta}{2} \\ -\tan \frac{\theta}{2} & 1 \end{bmatrix}$  and  $AB = I_2$ , then  $B =$

A.  $\left( \cos^2 \cdot \frac{\theta}{2} \right) A$

B.  $\left( \cos^2 \cdot \frac{\theta}{2} \right) A^T$

C.  $(\cos^2 \theta) I$

D.  $\left( \sin^2 \cdot \frac{\theta}{2} \right) A$

**Answer: B**



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2. If  $\alpha$  and  $\beta$  are the roots of  $x^2 + x + 1 = 0$ , then  $\alpha^{2020} + \beta^{2020}$  is

A.  $-2$

B.  $-1$

C.  $1$

D.  $2$

Answer: B



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3. The value of  $e^{i\theta} - e^{-i\theta}$  is .....

A.  $\sin \theta$

B.  $2 \sin \theta$

C.  $i \sin \theta$

D.  $2i \sin \theta$

**Answer: D**



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4. The area of the triangle formed by the complex number  $z$ ,  $iz$  in the Argand's diagram is .....

A.  $\frac{1}{2}|z^2|$

B.  $|z^2|$

C.  $\frac{3}{2}|z|^2$

D.  $2|z|^2$

**Answer: A**



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5. If  $\cot^{-1} 2$  and  $\cot^{-1} 3$  are two angles of a triangle, then the third angle is

A.  $\frac{\pi}{4}$

B.  $\frac{3\pi}{4}$

C.  $\frac{\pi}{6}$

D.  $\frac{\pi}{3}$

**Answer: B**



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6.  $\sec^{-1}\left(\frac{2}{3}\right) + \operatorname{cosec}^{-1}\left(\frac{2}{3}\right) = \dots\dots\dots$

A.  $\frac{-\pi}{2}$

B.  $\frac{\pi}{2}$

C.  $\pi$

D.  $-\pi$

**Answer: A**



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7. If the normals of the parabola  $y^2=4x$  drawn at the end points of its latus rectum are tangents to the circle  $(x-3)^2 + (y+2)^2 = r^2$  then the value of  $r^2$  is

A. 2

B. 3

C. 1

D. 4

**Answer: B**



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8. The vertices of the ellipse  $16x^2 + 25y^2 = 400$  are .....

- A.  $(0, \pm 4)$
- B.  $(\pm 5, 0)$
- C.  $(\pm 4, 0)$
- D.  $(0, - \pm 5)$

**Answer: B**



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9. If  $\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \times \vec{b}) \times \vec{c}$ , where  $\vec{a}, \vec{b}, \vec{c}$  are any three vectors such that  $\vec{b} \cdot \vec{c} \neq 0$  and  $\vec{a} \cdot \vec{b} \neq 0$ , then  $\vec{a}$  and  $\vec{c}$  are

- A. perpendicular
- B. parallel
- C. inclined at an angle  $\frac{\pi}{3}$

D. inclined at an angle  $\frac{\pi}{6}$

**Answer: D**



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10. The number given by the Rolle's theorem for the function  $x^3 - 3x^2, x \in [0, 3]$  is

A. 1

B.  $\sqrt{2}$

C.  $\frac{3}{2}$

D. 2

**Answer: D**



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11. The function  $f(x) = x^3$  has..... .

- A. absolute maximum
- B. absolute minimum
- C. local maximum
- D. no extrema

**Answer: B**



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12. Linear approximation for  $g(x) = \cos x$  at  $x = \frac{\pi}{2}$  is

- A.  $x + \frac{\pi}{2}$
- B.  $-x + \frac{\pi}{2}$
- C.  $x - \frac{\pi}{2}$
- D.  $-x - \frac{\pi}{2}$



**Answer: B**



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**13.** The differential of  $y$  if  $y = \sin 2x$  is .....

A.  $2 \cos 2x$

B.  $2 \cos 2x \cdot dx$

C.  $-2 \cos 2x dx$

D.  $\cos 2x \cdot dx$

**Answer: B**



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**14.** The value of  $\int_{-1}^2 |x| dx$

A.  $\frac{1}{2}$

B.  $\frac{3}{2}$

C.  $\frac{5}{2}$

D.  $\frac{7}{2}$

**Answer: B**



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15.  $\int_0^{2a} f(x) dx = 0$  if .....

A.  $f(2a - x) = f(x)$

B.  $f(2a - x) = -f(x)$

C.  $f(x) = -f(x)$

D.  $f(x) = f(x)$

**Answer: A**



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16. The population  $P$  in any year  $t$  is such that the rate of increase in the population is proportional to the population. Then

A.  $P = ce^{kt}$

B.  $P = ce^{-kt}$

C.  $P = cKt$

D.  $P = c$

**Answer: A**



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17. On a multiple-choice exam with 3 possible destructive for each of the 5 questions, the probability that a student will get 4 or more correct answers just by guessing is

A.  $\frac{11}{243}$

B.  $\frac{3}{8}$

C.  $\frac{1}{243}$

D.  $\frac{5}{243}$

**Answer: A**



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**18.** Consider a game where the player tosses a six sided fair die. If the face that comes up is 6, the player wins Rs. 36, otherwise he loses Rs.  $k^2$ , where  $k$  is the face that comes up  $k = \{1, 2, 3, 4, 5\}$ .

The expected amount to win at this game in Rs. is

A.  $\frac{19}{6}$

B.  $-\frac{19}{6}$

C.  $\frac{3}{2}$

D.  $-\frac{3}{2}$

**Answer: B**



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19. A binary operation on a set  $S$  is a function from

A.  $S \rightarrow S$

B.  $(S \times S) \rightarrow S$

C.  $S \rightarrow (S \times S)$

D.  $(S \times S) \rightarrow (S \times S)$

**Answer: B**



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20. If  $X$  is a continuous random variable then  $p(a < x < b) = \underline{\hspace{2cm}}$ .

A.  $P(a \leq X \leq b)$

B.  $P(a \leq X \leq b)$

C.  $P(a \leq X < b)$

D. all the three above

**Answer: D**

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## Part II

1. Discuss the maximum possible number of positive and negative zeros of the polynomials  $x^2 - 5x + 6$  and  $x^2 - 5x + 16$ . Also draw rough sketches of the graphs.

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2. Show that  $\cot(\sin^{-1} x) = \frac{\sqrt{1-x^2}}{x}$ ,  $-1 \leq x \leq 1$  and  $x \neq 0$

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3. Find the distance between the parallel planes  $\vec{r} \cdot (2\hat{i} - \hat{j} - 2\hat{k}) = 6$  and  $\vec{r} \cdot (6\hat{i} - 3\hat{j} - 6\hat{k}) = 27$

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4. If the mass  $m(x)$  (in kilograms) of a thin rod of length  $x$  (in metres) is given by,  $m(x) = \sqrt{3x}$  then what is the rate of change of mass with respect to the length when it is  $x = 27$  meters.

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5. In each of the following cases, determine whether the following function is homogeneous or not. If it is so, find the degree. (i)

$$f(x, y) = x^2y + 6x^3 + 7 \quad \text{(ii) } h(x, y) = \frac{6x^2y^3 - \pi y^5 + 9x^4y}{2020x^2 + 2019y^2}$$

$$\text{(iii) } g(x, y, z) = \frac{\sqrt{3x^2 + 5y^2 + z^2}}{4x + 7y} \quad \text{(iv)}$$

$$U(x, y, z) = xy + \sin\left(\frac{y^2 - 2z^2}{xy}\right)$$

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6. Evaluate  $\int_0^{\frac{\pi}{3}} \frac{\sec x \tan x}{1 + \sec^2} x \, dx$

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7.  $y = e^{2x}(a + bx)$

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8. For the probability density function  $f(x) \begin{cases} cx(1-x)^3 & 0 < x < 1 \\ 0 & \text{elsewhere} \end{cases}$

find the constant  $c$ .

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9. Verify the

Associative property

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10. If  $y = 2\sqrt{2}x + c$  is a tangent to the circle  $x^2 + y^2 = 16$ , find the value of  $c$ .

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### Part Iii

1. Verify  $(AB)^{-1} = B^{-1}A^{-1}$  with  $A = \begin{bmatrix} 0 & -3 \\ 1 & 4 \end{bmatrix}$ ,  $B = \begin{bmatrix} -2 & -3 \\ 0 & -1 \end{bmatrix}$

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2. Simplify:  $\left(\sin\frac{\pi}{6} + i\cos\frac{\pi}{6}\right)^{08}$ .

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3. Solve the equation  $9x^3 - 36x^2 + 44x - 16 = 0$  if the roots form an arithmetic progression.

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4. Prove that  $\tan^{-1} x + \tan^{-1} \frac{2x}{1-x^2} = \tan^{-1} \left( \frac{3x-x^3}{1-3x^2} \right) |x| < \frac{1}{\sqrt{3}}$ .

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5. Find the equation of the tangent at  $t = 2$  to the parabola  $y^2 = 8x$ .  
(Hint use parametric form)

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6. If a plane meets the coordinate axes at A, B, C such that the centroid of the triangle ABC is the point  $(u, v, w)$ , find the equation of the plane.

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7. Compute the value of 'c' satisfied by the Rolle's theorem for the function  $f(x) = \log\left(\frac{x^2 + 6}{5x}\right)$  in the interval [2,3].

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8. If  $w(x, y, z) = \log\left(\frac{5x^3y^4 + 7y^2xz^4 - 75y^3z^4}{x^2 + y^2}\right)$ , find  $x \frac{\partial w}{\partial x} + y \frac{\partial w}{\partial y} + z \frac{\partial w}{\partial z}$ ,

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9. Find the area of the region bounded by the curve  $y = x^2$  and the line  $y = 4$ .

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10. A random variable  $X$  has a probability density function

$$f(x) = \begin{cases} k & 0 < x < 2\pi \\ 0 & \text{elsewhere} \end{cases} \quad \text{find (i) } k, \text{ (ii) } P(0 < X < \pi/2) \text{ (iii)}$$

$$P(\pi/2 < X < 3\pi/2)$$



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## Part Iv

1. Investigate for what values of  $\lambda$  and  $\mu$  the system of linear equations.

$$x + 2y + z = 7, x + y + \lambda z = \mu, x + 3y - 5z = 5. \text{ Has (i) no solution}$$

(ii) a unique solution (iii) an infinite number of solutions.

(b)  $P$  represents the variable complex number  $z$ . Find the locus of  $P$ , if

$$\operatorname{Re}\left(\frac{z+1}{z+i}\right) = 1.$$



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2. Assume that water issuing from the end of a horizontal pipe. 7.5 m above the ground describes a parabolic path. The vertex of the parabolic path is at the end of the pipe. At a position 2.5 m below the line of the pipe, the flow of water has curved outward 3m beyond the vertical line through the end of the pipe. How far beyond this vertical line will the water strike the ground ?



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3. If  $V(x, y) = e^x(x \cos y - y \sin y)$ , then prove that  $\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} = 0$



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4. If the curve  $y^2 = x$  and  $xy = k$  are orthogonal then prove that  $8k^2 = 1$



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5.

If

$$\vec{a} = \hat{i} + 2\hat{j} + 3\hat{k}, \vec{b} = 2\hat{i} - \hat{j} + \hat{k}, \vec{c} = 3\hat{i} + 2\hat{j} + \hat{k} \text{ and } \vec{a} \times (\vec{b} \times \vec{c})$$

find the values for l,m,n.



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6. Find the probability mass function and cumulative distribution function of number of girl child in families with 4 children, assuming equal probabilities for boys and girls.



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7. A steel plant is capable of producing  $x$  tonnes per day of a low-grade steel and  $y$  tonnes per day of a high-grade steel, where  $y = \frac{40 - 5x}{10 - x}$ . If the fixed market price of low-grade steel is half that of high-grade steel, then what should be optimal productions in low-grade steel and high-grade steel in order to have maximum receipts.



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