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## MATHS

### BOOKS - RD SHARMA MATHS (ENGLISH)

#### TRIGONOMETRIC RATIOS

Others

1. In a  $\Delta ABC$  right angled at  $C$ , if  $\tan A = \frac{1}{\sqrt{3}}$ , find the value of  $\sin A \cos B + \cos A \sin B$ .



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2. The altitude  $AD$  of a  $\Delta ABC$ , in which  $\angle A$  obtuse and,  $AD = 10\text{cm}$ . If  $BD=10\text{cm}$  and  $CD=10\sqrt{3}\text{cm}$ , determine  $\angle A$ .



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3. A rhombus of side 20cm has two angles of  $60^0$  each. Find the length of the diagonals.



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4.  $ABC$  is a right triangle, right angled at  $C$ . If  $A = 30^0$  and  $AB = 40$  units, find the remaining two sides and  $\angle B$  of  $ABC$ .



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5. Evaluate the following: (i)  $\frac{\cos 37^0}{\sin 53^0}$  (ii)  $\frac{\tan 54^0}{\cot 36^0}$  (iv)  $\frac{\cos ec 34^0}{\sec 56^0}$



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6. Find acute angles  $A$  and  $B$ , if

$$\sin(A + 2B) = \frac{\sqrt{3}}{2} \text{ and } \cos(A + 4B) = 0, A > B.$$



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7. In an acute angled triangle  $ABC$ , if  $\tan(A + B - C) = 1$

and,  $\sec(B + C - A) = 2$ , find the value of  $A$ ,  $B$  and  $C$



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8. If each of  $\alpha$ ,  $\beta$  and  $\gamma$  is a positive acute angle such that  
 $\sin(\alpha + \beta - \gamma) = \frac{1}{2}$ ,  
 $\cos(\beta + \gamma - \alpha) = \frac{1}{2}$  and  $\tan(\gamma + \alpha - \beta) = 1$ , find the values of  $\alpha$ ,  $\beta$  and  $\gamma$ .



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9. In a  $ABC$ , right angled at  $A$ , if  $AB = 12$ ,  $AC = 5$  and  $BC = 13$ , find all the six trigonometric ratios of angle  $B$ .



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10. If  $\cos B = \frac{1}{3}$ , find the other five trigonometric ratios.



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11. In a  $ABC$ , right angled at  $A$ , if  $AB = 5$ ,  $AC = 12$  and  $BC = 13$ , find  $\sin B$ ,  $\cos C$  and  $\tan B$ .



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12. If  $\sin \theta = \frac{a^2 - b^2}{a^2 + b^2}$ , find the values of other five trigonometric ratios.



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13. If  $\cos ec A = \sqrt{10}$ , find other five trigonometric ratios.



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14. If  $\tan A = \sqrt{2} - 1$  show that  $\sin A \cos A = \frac{\sqrt{2}}{4}$



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15. If  $\cos ec A = 2$ , find the value of  $\frac{1}{\tan A} + \frac{\sin A}{1 + \cos A}$



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16. Evaluate the following:

(i)  $\sin 39^\circ - \cos 51^\circ$  (ii)  $\cos ec 25^\circ - \sec 65^\circ + \cot 34^\circ - \tan 56^\circ$  (iii)

$$\frac{\sin 36^\circ}{\cos 54^\circ} - \frac{\sin 54^\circ}{\cos 36^\circ} + \cos^2 13^\circ - \sin^2 77^\circ$$


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17. The value of  $\frac{\tan 55^0}{\cot 35^0} + \cot 1^0 \cot 2^0 \cot 3^0 \cot 90^0$ , is -2 (b) 2  
(c) 1 (d) 0



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18. If A + B is  $90^\circ$ , then  
 $\frac{\tan A \cdot \tan B + \tan A \cdot \cot B}{\sin A \cdot \sec B} - \frac{\sin^2 B}{\cos^2 A}$  is equal to:



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19. If  $\frac{x \cos ec^2 30^0 \sec^2 45^0}{8 \cos^2 45^0 \sin^2 60^0} = \tan^2 60^0 - \tan^2 30^0$ , than  $x =$   
(a) 1 (b) -1 (c) 2 (d) 0



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20. The value of

$$\frac{\cos(90^\circ - \theta) \sec(90^\circ - \theta) \tan \theta}{\csc(90^\circ - \theta) \sin(90^\circ - \theta) \cot(90^\circ - \theta)} + \frac{\tan(90^\circ - \theta)}{\cot \theta}$$
 is

- 1 (b) -1 (c) 2 (d) -2



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21. If  $\tan 2A = \cot(A - 18^\circ)$ , where  $2A$  is an acute angle, find the value of  $A$ .



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22. Prove the following:

$$\sin \theta \sin(90^\circ - \theta) - \cos \theta \cos(90^\circ - \theta) = 0$$


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23. Find an acute angle  $\theta$ , when  $\frac{\cos \theta - \sin \theta}{\cos \theta + \sin \theta} = \frac{1 - \sqrt{3}}{1 + \sqrt{3}}$



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24. If  $\sin(A + B) = 1$  and  $\cos(A - B) = \frac{\sqrt{3}}{2}$ , then find A and B.



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25. Evaluate each of the following:

$$\cot 12^\circ \cot 38^\circ \cot 52^\circ \cot 60^\circ \cot 78^\circ$$

$$\tan 5^\circ \tan 25^\circ \tan 30^\circ \tan 65^\circ \tan 85^\circ$$



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**26.** Prove that:  $\tan 10^\circ \tan 15^\circ \tan 75^\circ \tan 80^\circ = 1$

$$\tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \tan 89^\circ = 1$$

$$\cos 1^\circ \cos 2^\circ \cos 3^\circ \dots \cos 180^\circ = 0$$



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**27.** If  $A + B = 90^\circ$ , prove that

$$\sqrt{\frac{\tan A \tan B + \tan A \cot B}{\sin A \sec B}} - \frac{\sin^2 B}{\cos^2 A} = \tan A$$



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**28.** If  $\sin 5\theta = \cos 4\theta$ , where  $5\theta$  and  $4\theta$  are acute angles, find the value of  $\theta$ .



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**29.** If  $\tan \theta + \frac{1}{\tan \theta} = 2$ , find the value of  $\tan^2 \theta + \frac{1}{\tan^2 \theta}$

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**30.** Evaluate each of the following in the simplest form:

1).  $\cos ec 30^\circ + \cot 45^\circ$

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**31.** In a right triangle  $ABC$ , right angled at  $B$ , the ratio of  $AB \rightarrow AC$  is  $1:\sqrt{2}$ . Find the values of  $\frac{2 \tan A}{1 + \tan^2 A}$  and (ii)

$$\frac{2 \tan A}{1 - \tan^2 A}$$

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**32.** In Figure,  $AD = DB$  and  $\angle B$  is a right angle.

Determine. (a)  $\sin \theta$  (b)  $\cos \theta$  (c)  $\tan \theta$  (d)  $\sin^2 \theta + \cos^2 \theta$



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**33.** Find the value of  $x$  in each of the following:

$$\tan 3x = \sin 45^\circ \cos 45^\circ + \sin 30^\circ, \quad (\text{ii})$$

$$\cos x = \cos 60^\circ \cos 30^\circ + \sin 60^\circ \sin 30^\circ, \quad (\text{iii})$$

$$\sin 2x = \sin 60^\circ \cos 30^\circ - \cos 60^\circ \sin 30^\circ.$$



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**34.** If  $\theta$  is an acute angle and  $\tan \theta + \cot \theta = 2$ , find the value

$$\text{of } \tan^7 \theta + \cot^7 \theta.$$



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35. Prove that:  $\frac{\cos 30^0 + \sin 60^0}{1 + \cos 60^0 + \sin 30^0} = \frac{\sqrt{3}}{2}$



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36. Find the value of  $\theta$  in each of the following: (i)

$$2\sin 2\theta = \sqrt{3}$$
 (ii)  $2\cos 3\theta = 1$  (iii)  $\sqrt{3}\tan 2\theta - 3 = 0$



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37. An equilateral triangle is inscribed in a circle of radius 6cm.

Find its side.



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**38.**

If

$$\tan A = 1$$

and

$\tan B = \sqrt{3}$ , evaluate  $\cos A \cos B - \sin A \sin B$ .



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**39.** Evaluate each of the following:

$$\begin{aligned} & \cos(40^\circ - \theta) - \sin(50^\circ + \theta) + \frac{\cos^2 40^\circ + \cos^2 50^\circ}{\sin^2 40^\circ + \sin^2 50^\circ} \\ & \frac{\cos 70^\circ}{\sin 20^\circ} + \frac{\cos 55^\circ \cos ec 35^\circ}{\tan 5^\circ \tan 25^\circ \tan 45^\circ \tan 65^\circ \tan 85^\circ} \\ & 2 \left( \frac{\cos 58^\circ}{\sin 32^\circ} \right) - \sqrt{3} \left( \frac{\cos 38^\circ \cos ec 52^\circ}{\tan 15^\circ \tan 60^\circ \tan 75^\circ} \right) \end{aligned}$$



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**40.** If  $\sec 4A = \cos ec(A - 20^\circ)$ , where  $4A$  is an acute angle, find the value of  $A$ .



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**41.** Evaluate each of the following: (a)

$$\cos(40^\circ - \theta) - \sin(50^\circ + \theta) + \frac{\cos^2 40^\circ + \cos^2 50^\circ}{\sin^2 40^\circ + \sin^2 50^\circ} \quad (\text{b})$$

$$\frac{\cos 70^\circ}{\sin 20^\circ} + \frac{\cos 55^\circ \cos ec 35^\circ}{\tan 5^\circ \tan 25^\circ \tan 45^\circ \tan 65^\circ \tan 85^\circ} \quad (\text{c})$$
$$2 \left( \frac{\cos 58^\circ}{\sin 32^\circ} \right) - \sqrt{3} \left( \frac{\cos 38^\circ \cos ec 52^\circ}{\tan 15^\circ \tan 60^\circ \tan 75^\circ} \right)$$



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**42.** Evaluate :

$$4(\sin^4 30^\circ + \cos^4 60^\circ) - \frac{2}{3}(\sin^2 60^\circ - \cos^2 45^\circ) + \frac{1}{2} \tan^2 60^\circ$$



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**43.** Evaluate :  $\frac{\sin 50^\circ}{\cos 40^\circ} + \frac{\cos ec 40^\circ}{\sec 50^\circ} - 4 \cos 50^\circ \cos ec 40^\circ$



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44. Evaluate :  $\tan 35^\circ \tan 40^\circ \tan 45^\circ \tan 50^\circ \tan 55^\circ$



45. Evaluate :

$$\cos ec(65^\circ + \theta) - \sec(25^\circ - \theta) - \tan(55^\circ - \theta) + \cot(35^\circ + \theta)$$



46. Evaluate :  $\tan 7^\circ \tan 23^\circ \tan 60^\circ \tan 67^\circ \tan 83^\circ$



**47.**

Evaluate

$$\frac{2\sin 68^0}{\cos 22^0} - \frac{2\cot 15^0}{5\tan 75^0} - \frac{3\tan 45^0 \tan 20^0 \tan 40^0 \tan 50^0 \tan 70^0}{5}$$



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**48.**

Evaluate

:

$$\frac{3\cos 55^0}{7\sin 35^0} - \left(\frac{4}{7}\right) \frac{\cos 70^0 \cos ec 20^0}{\tan 5^0 \tan 25^0 \tan 45^0 \tan 65^0 \tan 85^0},$$



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**49.**

Prove

the

following:

$$\frac{\cos(90^0 - \theta) \sec(90^0 - \theta) \tan \theta}{\cos ec(90^0 - \theta) \sin(90^0 - \theta) \cot(90^0 - \theta)} + \frac{\tan(90^0 - \theta)}{\cot \theta} = 2$$



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50. Prove the following:  $\frac{\tan(90^\circ - A) \cot A}{\cos ec^2 A} - \cos^2 A = 0$



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51. Prove the following:

$$\sin \theta \sin(90^\circ - \theta) - \cos \theta \cos(90^\circ - \theta) = 0$$



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52. In a  $\triangle ABC$ , right angled at  $B$ , if  $AB = 4$  and  $BC = 3$ , find all the six trigonometric ratios of  $\angle A$ .



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**53.** In a  $\triangle ABC$ , right angled at  $B$ , if  $AB = 12$  and  $BC = 5$ , find: (i)  $\sin A$  and  $\tan A$  (ii)  $\cos C$  and  $\cot C$



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**54.** If  $\sin A = \frac{3}{5}$ , find  $\cos A$  and  $\tan A$ .



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**55.** If  $\cos \theta = \frac{8}{17}$ , find the other five trigonometric ratios.



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**56.** In a right triangle  $ABC$  right angled at  $B$ , if  $\sin A = \frac{3}{5}$ , find all the six trigonometric ratios of  $\angle C$ .



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57. If  $\sin A = \frac{1}{3}$ , evaluate  $\cos A \cos ec A + \tan A \sec A$ .



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58. In a right triangle  $ABC$ , right angled at  $C$ , if  $\tan A = 1$ , then verify that  $2 \sin A \cos A = 1$ .



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59. If  $\sec \alpha = \frac{5}{4}$ , evaluate  $\frac{1 - \tan \alpha}{1 + \tan \alpha}$ .



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**60.** If  $\sin \theta = \frac{1}{2}$ , show that  $(3 \cos \theta - 4 \cos^3 \theta) = 0$



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**61.** If  $\tan A = 2$ , evaluate  $\sec A \sin A + \tan^2 A - \csc A$ .



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**62.** Given  $\triangle ACB$  right angled at  $C$  in which  $AB = 29$  units ,  $BC = 21$  units and  $\angle ABC = \theta$ . Determine the values of (i)  $\cos^2 \theta + \sin^2 \theta$  (ii)  $\cos^2 \theta - \sin^2 \theta$



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63. If  $\cot B = \frac{12}{5}$ , prove that  
 $\tan^2 B - \sin^2 B = \sin^4 B \sec^2 B$ .



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64. If  $\sec \alpha = \frac{5}{4}$ , verify that  $\frac{\tan \alpha}{1 + \tan^2 \alpha} = \frac{\sin \alpha}{\sec \alpha}$



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65. If  $\sin \theta = \frac{4}{5}$ , find the value of  $\frac{4 \tan \theta - 5 \cos \theta}{\sec \theta + 4 \cot \theta}$



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66. In a right triangle  $ABC$  right angled at  $B$ ,  $\angle ACB = \theta$ ,  
 $AB = 2\text{cm}$  and  $BC = 1\text{ cm}$ . Find the value of  $\sin^2 \theta + \tan^2 \theta$



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**67.** From Fig. , write the values of: (i)  $\sin A$  (ii)  $\cot A$



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**68.** From Fig., write the values of: (i)  $\tan B$  (ii)  $\sin^2 B + \cos^2 B$



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**69.** In  $\triangle OPQ$  right angled at  $P$ ,  $OP = 7\text{cm}$  ,  
 $OQ - PQ = 1\text{cm}$  . Determine the values of  $\sin Q$  and  $\cos Q$  .



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70. In  $\triangle PQR$ , right angled at  $Q$ ,  $PR + QR = 25\text{cm}$  and  $PQ = 5\text{cm}$ . Determine the values of  $\sin P$ ,  $\cos P$  and  $\tan P$ .



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71. In a  $\triangle ABC$ , right angled at  $C$  and  $\angle A = \angle B$ , is  $\cos A = \cos B$ ?



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72. In a  $\triangle ABC$ , right angled at  $C$  and  $\angle A = \angle B$ , is  $\tan A = \tan B$ ?



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73. In  $\triangle ABC$ , right angled at  $B$ , if  $\tan A = \frac{1}{\sqrt{3}}$ , find the value of (i)  $\sin A \cos C + \cos A \sin C$  (ii)  $\cos A \cos C - \sin A \sin C$



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74. Given that  $16 \cot A = 12$ ; find the value of  $\frac{\sin A + \cos A}{\sin A - \cos A}$ .



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75. If  $5 \tan \alpha = 4$ , show that  $\frac{5 \sin \alpha - 3 \cos \alpha}{5 \sin \alpha + 2 \cos \alpha} = \frac{1}{6}$



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**76.** If  $\tan \theta = \frac{12}{13}$ , evaluate  $\frac{2 \sin \theta \cos \theta}{\cos^2 \theta - \sin^2 \theta}$ .



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**77.** If  $\angle B$  and  $\angle Q$  are acute angles such that  $\sin B = \sin Q$ , then prove that  $\angle B = \angle Q$ .



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**78.** If  $\sin A = \frac{2}{3}$ , find other trigonometric ratios.



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**79.** If  $\cos A = \frac{4}{5}$ , find other trigonometric ratios.



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80. If  $\tan \theta = 11$ , find other trigonometric ratios



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81. If  $\sin \theta = \frac{11}{15}$ , find other trigonometric ratios



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82. Given  $\tan \alpha = \frac{5}{12}$ , find other trigonometric ratios



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83.  $\sin \theta = \frac{\sqrt{3}}{2}$ , find other trigonometric ratios



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84. If  $\cos \theta = \frac{7}{25}$ , find other trigonometric ratios



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85. If Value of  $\tan \theta = \frac{8}{15}$ , find other trigonometric ratios



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86. If  $\cot \theta = \frac{12}{5}$ , find other trigonometric ratios



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**87.** If  $\sec \theta = \frac{13}{5}$ , find other trigonometric ratios

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**88.** If  $\cos ec A = \sqrt{10}$ , find other five trigonometric ratios.

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**89.**  $\cos \theta = \frac{12}{15}$  is given, find other trigonometric ratios

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**90.** In a  $\triangle ABC$ , right angled at  $B$ ,  $AB = 24\text{cm}$ ,  $BC = 7\text{cm}$ . Determine (i)  $\sin A, \cos A$  (ii)  $\sin C, \cos C$

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91. In Fig., find  $\tan P$  and  $\cot R$ . Is  $\tan P = \cot R$  ?



92. If  $\sin A = \frac{9}{41}$ , compute  $\cos A$  and  $\tan A$ .



93. given :  $15 \cot A = 8$  find  $\sin A$  and  $\sec A$



**94.** In  $\triangle PQR$ , right angled at  $Q$ ,  $PQ = 4\text{cm}$  and  $RQ = 3\text{cm}$ . Find the values of  $\sin P$ ,  $\sin R$ ,  $\sec P$  and  $\sec R$ .



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**95.** If  $\cot \theta = \frac{7}{8}$ , evaluate . 1.) 
$$\frac{(1 + \sin \theta)(1 - \sin \theta)}{(1 - \cos \theta)(1 + \cos \theta)}$$



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**96.** If  $3 \cot A = 4$ , check whether  $\frac{1 - \tan^2 A}{1 + \tan^2 A} = \cos^2 A - \sin^2 A$  or not.



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97. If  $\tan \theta = \frac{a}{b}$  then find the value of  $\frac{\cos \theta + \sin \theta}{\cos \theta - \sin \theta}$



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98. If  $3 \tan \theta = 4$ , find the value of  $\frac{4 \cos \theta - \sin \theta}{2 \cos \theta + \sin \theta}$



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99. If  $3 \cot \theta = 2$ , find the value of  $\frac{4 \sin \theta - 3 \cos \theta}{2 \sin \theta + 6 \cos \theta}$



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100. If  $\tan \theta = \frac{a}{b}$ , show that  $\frac{a \sin \theta - b \cos \theta}{a \sin \theta + b \cos \theta} = \frac{a^2 - b^2}{a^2 + b^2}$



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**101.** If  $\sec \theta = \frac{13}{5}$ , show that  $\frac{2 \sin \theta - 3 \cos \theta}{4 \sin \theta - 9 \cos \theta} = 3$



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**102.** If  $\cos \theta = \frac{12}{13}$ , show that  $\sin \theta(1 - \tan \theta) = \frac{35}{156}$



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**103.** If  $\cot \theta = \frac{1}{\sqrt{3}}$ , show that  $\frac{1 - \cos^2 \theta}{2 - \sin^2 \theta} = \frac{3}{5}$



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**104.** If  $\tan \theta = \frac{1}{\sqrt{7}}$ , then  $\frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta} = ?$



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105. If  $\sin \theta = \frac{12}{13}$ , find the value of  $\frac{\sin^2 \theta - \cos^2 \theta}{2 \sin \theta \cos \theta} \times \frac{1}{\tan^2 \theta}$



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106. If  $\sec \theta = \frac{5}{4}$ , find the value of  $\frac{\sin \theta - 2 \cos \theta}{\tan \theta - \cot \theta}$



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107. If  $\cos \theta = \frac{5}{13}$ , find the value of  $\frac{\sin^2 \theta - \cos^2 \theta}{2 \sin \theta \cos \theta} \times \frac{1}{\tan^2 \theta}$



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108. If  $\tan \theta = \frac{12}{13}$ , evaluate  $\frac{2 \sin \theta \cos \theta}{\cos^2 \theta - \sin^2 \theta}$ .



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109. If  $\cos \theta = \frac{3}{5}$ , find the value of  $\frac{\sin \theta - \frac{1}{\tan \theta}}{2 \tan \theta}$



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110. If  $\sin \theta = \frac{3}{5}$ , evaluate  $\frac{\cos \theta - \frac{1}{\tan \theta}}{2 \cot \theta}$



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111. If  $\sec A = \frac{5}{4}$ , verify that  
$$\frac{3 \sin A - 4 \sin^3 A}{4 \cos^3 A - 3 \cos A} = \frac{3 \tan A - \tan^3 A}{1 - 3 \tan^2 A}$$



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112. If  $\sin \theta = \frac{3}{4}$ , prove that  $\sqrt{\frac{\cos ec^2 \theta - \cot^2 \theta}{\sec^2 \theta - 1}} = \frac{\sqrt{7}}{3}$



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113. If  $\sec A = \frac{17}{8}$ , verify that  $\frac{3 - 4 \sin^2 A}{4 \cos^2 A - 3} = \frac{3 - \tan^2 A}{1 - 3 \tan^2 A}$



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114. If  $\cot \theta = \frac{3}{4}$ , prove that  $\sqrt{\frac{\sec \theta - \cos ec \theta}{\sec \theta + \cos ec \theta}} = \frac{1}{\sqrt{7}}$



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115. If  $\tan \theta = \frac{24}{7}$ , find  $\sin \theta + \cos \theta$ .



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**116.** If  $\sin \theta = \frac{a}{b}$ , find  $\sec \theta + \tan \theta$  in terms of  $a$  and  $b$ .



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**117.** If  $8 \tan A = 15$ , find  $\sin A - \cos A$



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**118.** If  $3 \cos \theta - 4 \sin \theta = 2 \cos \theta + \sin \theta$ , find  $\tan \theta$ .



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**119.** If  $\tan \theta = \frac{20}{21}$ , show that  $\frac{1 - \sin \theta + \cos \theta}{1 + \sin \theta + \cos \theta} = \frac{3}{7}$



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120. If  $\csc A = 2$ , find the value of  $\frac{1}{\tan A} + \frac{\sin A}{1 + \cos A}$



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121. If  $\angle A$  and  $\angle B$  are acute angles such that  $\cos A = \cos B$ .  
then show that  $\angle A = \angle B$ .



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122. If  $\angle A$  and  $\angle P$  are acute angle such that  $\tan A = \tan P$ ,  
then show that  $\angle A = \angle P$ .



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**123.** In a  $\triangle ABC$ , right angled at  $A$ , if  $\tan C = \sqrt{3}$ , find the value of  $\sin B \cos C + \cos B \sin C$ .



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**124.** State whether the following are true or false. Justify your answer.

(i) The value of  $\tan A$  always less than 1. (ii)  $\sec A = \frac{12}{5}$  for some value of angle  $A$  (iii)  $\cos A$  is the abbreviation used for the cosecant of angle  $A$ . (iv)  $\cot A$  is the product of  $\cot$  and  $A$  (v)  $\sin \theta = \frac{4}{3}$  for some angle  $\theta$



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**125.** State whether the following are true or false. Justify your answer.

(i) The value of  $\tan A$  always less than 1. (ii)

$\sec A = \frac{12}{5}$  for some value of angle A (iii)  $\cos A$  is the abbreviation used for the cosecant of angle A. (iv)  $\cot A$  is the product of  $\cot$  and A (v)  $\sin \theta = \frac{4}{3}$  for some angle  $\theta$



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**126.** Evaluate each of the following in the simplest form:

$$\sin 60^\circ \cos 30^\circ + \cos 60^\circ \sin 30^\circ \quad (\text{ii})$$

$$\sin 60^\circ \cos 45^\circ + \cos 60^\circ \sin 45^\circ$$



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**127.** Evaluate the following expressions:

$$(i) 2 \sin^2 30^\circ \tan 60^\circ - 3 \cos^2 60^\circ \sec^2 30^\circ \quad (\text{ii})$$

$$\csc^2 30^\circ \sin^2 45^\circ - \sec^2 60^\circ \quad (\text{iii})$$

$$\tan 60^\circ \cos ec^2 45^\circ + \sec^2 60^\circ \tan 45^\circ$$



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128. Evaluate the following expressions:

$$(i) 4 \cot^2 45^\circ - \sec^2 60^\circ + \sin^2 60^\circ + \cos^2 90^\circ \quad . \quad (ii)$$

$$3 \cos^2 30^\circ + \sec^2 30^\circ + 2\cos 0^\circ + 3\sin 90^\circ - \tan^2 60^\circ$$



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129. Evaluate each of the following:  $\frac{\sin^2 45^\circ + \cos^2 45^\circ}{\tan^2 60^\circ} \quad (ii)$

$$\frac{\sin 30^\circ - \sin 90^\circ + 2\cos 0^\circ}{\tan 30^\circ \tan 60^\circ}$$



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130. Evaluate each of the following:

$$\frac{\sin 60^\circ}{\cos^2 45^\circ} - \cot 30^\circ + 15\cos 90^\circ \quad (ii)$$

$$\frac{5 \sin^2 30^\circ + \cos^2 45^\circ - 4 \tan^2 30^\circ}{2 \sin 30^\circ \cos 30^\circ + \tan 45^\circ}$$



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131.

Show

that:

$$2(\cos^2 45^\circ + \tan^2 60^\circ) - 6(\sin^2 45^\circ - \tan^2 30^\circ) = 6 \quad (\text{ii})$$

$$2(\cos^4 60^\circ + \sin^4 30^\circ) - (\tan^2 60^\circ + \cot^2 45^\circ) + 3 \sec^2 30^\circ = \frac{1}{4}$$



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132. Solve each of the following equations when  $0^\circ < \theta < 90^\circ$

$$(i) 2 \cos \theta = 1 \quad (ii) 2 \cos^2 \theta = \frac{1}{2}$$



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**133.** Solve each of the following equations when  $0 < \theta < 90$

$$(i) 2 \sin^2 \theta = \frac{1}{2} \quad (ii) 3 \tan^2 \theta - 1 = 0$$



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**134.** Find the value of  $\theta$  in each of the following: (i)

$$2 \sin 2\theta = \sqrt{3}$$
 (ii)  $2 \cos 3\theta = 1$



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**135.** If  $A = 30^\circ$  verify that  $\cos 3A = 4 \cos^3 A - 3 \cos A$



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**136.** If  $x = 30^\circ$ , verify that : (i)  $\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$  (ii)  
 $\sin x = \sqrt{\frac{1 - \cos 2x}{2}}$



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**137.** Verify that:  $\sin 60o = \frac{2 \tan 30o}{1 + \tan^2 30o} = \frac{\sqrt{3}}{2}$  (ii)  
 $\cos 60o = \frac{1 - \tan^2 30o}{1 + \tan^2 30o} = \frac{1}{2}$



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**138.** Verify that: (i)  $\cos 60^\circ = \cos^2 30^\circ - \sin^2 30^\circ = \frac{1}{2}$



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**139.** If  $\theta$  is an acute angle and  $\sin \theta = \cos \theta$ , find the value of  $2\tan^2 \theta + \sin^2 \theta - 1$



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**140.** Given that  $\sin(A + B) = \sin A \cos B + \cos A \sin B$ , find the value of  $\sin 75^\circ$ .



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**141.** In a rectangle  $ABCD$ ,  $AB = 20\text{cm}$ ,  $\angle BAC = 60^\circ$ . Calculate side  $BC$ .



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**142.** Evaluate the following: (i)  $\sin 45^\circ \sin 30^\circ + \cos 45^\circ \cos 30^\circ$

(ii)  $\sin 60^\circ \cos 30^\circ + \cos 60^\circ \sin 30^\circ$



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**143.** Evaluate the following: (i)  $\cos 60^\circ \cos 45^\circ - \sin 60^\circ \sin 45^\circ$

(ii)  $\sin^2 30^\circ + \sin^2 45^\circ + \sin^2 60^\circ + \sin^2 90^\circ$



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**144.** Evaluate the following:

$\cos^2 30^\circ + \cos^2 45^\circ + \cos^2 60^\circ + \cos^2 90^\circ$  (ii)

$\tan^2 30^\circ + \tan^2 60^\circ + \tan^2 45^\circ$



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**145.** Evaluate the following: (i)

$$2 \sin^2 30o - 3 \cos^2 45 \oplus \tan^2 60o \quad (\text{ii})$$

$$\sin^2 30o \cos^2 45 \oplus 4 \tan^2 30 \oplus \frac{1}{2} \sin^2 90o - 2 \cos^2 90 \oplus \frac{1}{24} \cos^2 0o$$

.



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**146.** Evaluate the following:

$$4(\sin^4 60 \oplus \cos^4 30o) - 3(\tan^2 60o - \tan^2 45o) + 5 \cos^2 45o$$

$$(\text{ii}) (\cos ec^2 45o \sec^2 30o) (\sin^2 30 \oplus 4 \cot^2 45o - \sec^2 60o)$$



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**147.** Evaluate the following:

$$\cos ec^3 30o \cos 60o \tan^3 45o \sin^2 90o \sec^2 45o \cot 30o \quad (\text{ii})$$

$$\cot^2 30o - 2 \cos^2 60o - \frac{3}{4} \sec^2 45o - 4 \sec^2 30o$$



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148. Evaluate the following:

$$(\cos 0 \oplus \sin 45 \oplus \sin 30o)(\sin 90o - \cos 45 \oplus \cos 60o) \quad (ii)$$

$$\frac{\sin 30o - \sin 90 \oplus 2 \cos 0o}{\tan 30o \tan 60o}$$



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149. Evaluate the following: (i)

$$\frac{4}{\cot^2 30o} + \frac{1}{\sin^2 60o} - \cos^2 45o \quad (ii)$$

$$4(\sin^4 30 \oplus \cos^2 60o) - 3(\cos^2 45o - \sin^2 90o) - \sin^2 60o$$



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**150.** Evaluate the following:

$$\frac{\tan^2 60^\circ + 4 \cos^2 45^\circ + 3 \sec^2 30^\circ + 5 \cos^2 90^\circ}{\csc 30^\circ + \sec 60^\circ - \cot^2 30^\circ}$$



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**151.** Evaluate the following:

$$\frac{\tan 45^\circ}{\csc 30^\circ} + \frac{\sec 60^\circ}{\cot 45^\circ} - \frac{5 \sin 90^\circ}{2 \cos 0^\circ}$$



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**152.** Find the value of  $x$  in each of the following: (i)

$$2 \sin 3x = \sqrt{3}$$
 (ii)  $2 \sin\left(\frac{x}{2}\right) = 1$  (iii)  $\sqrt{3} \sin x = \cos x$



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**153.** Find the value of  $x$  in each of the following:

$$\tan x = \sin 45^\circ \cos 45^\circ + \sin 30^\circ \quad (\text{ii})$$

$$\sqrt{3} \tan 2x = \cos 60^\circ + \sin 45^\circ \cos 45^\circ \quad (\text{iii})$$

$$\cos 2x = \cos 60^\circ \cos 30^\circ + \sin 60^\circ \sin 30^\circ$$



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**154.** If  $\theta = 30^\circ$ , verify that: (i)  $\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$  (ii)

$$\sin 2\theta = \frac{2 \tan \theta}{1 + \tan^2 \theta}$$



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**155.** If  $\theta = 30^\circ$ , verify that: (i)  $\cos 2\theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$  (ii)

$$\cos 3\theta = 4 \cos^3 \theta - 3 \cos \theta$$



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**156.** If  $A = B = 60^\circ$ , verify that (i)

$$\cos(A - B) = \cos A \cos B + \sin A \sin B \quad (\text{ii})$$

$$\sin(A - B) = \sin A \cos B - \cos A \sin B \quad (\text{iii})$$

$$\tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$



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**157.** If  $A = 30^\circ$  and  $B = 60^\circ$ , verify that (i)

$$\sin(A + B) = \sin A \cos B + \cos A \sin B \quad (\text{ii})$$

$$\cos(A + B) = \cos A \cos B - \sin A \sin B$$



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**158.** Using the formula of  $\sin(A - B) = \sin A \cos B - \cos A \sin B$  find the value of  $\sin 15^\circ$

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**159.** In a right triangle  $ABC$ , right angled at  $C$ , if  $\angle B = 60^\circ$  and  $AB = 15$  units. Find the remaining angles and sides.

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**160.** If  $\triangle ABC$  is a right triangle such that  $\angle C = 90^\circ$ ,  $\angle A = 45^\circ$  and  $BC = 7$  units. Find  $\angle B$ ,  $AB$  and  $AC$ .

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**161.** In a rectangle  $ABCD$ ,  $AB = 20\text{cm}$ ,  $\angle BAC = 60^\circ$  , calculate side  $BC$  and diagonals  $AC$  and  $BD$  .



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**162.** If  $\sin(A + B) = 1$  and  $\cos(A - B) = 1$ ,  $0^\circ < A + B \leq 90^\circ$  ,  $A \geq B$  find  $A$  and  $B$  .



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**163.** If  $\tan(A - B) = \frac{1}{\sqrt{3}}$  and  $\tan(A + B) = \sqrt{3}$  ,  $0^\circ < A + B \leq 90^\circ$  ,  $A > B$  find  $A$  and  $B$  .



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**164.** If  $\sin(A-B) = \frac{1}{2}$  and  $\cos(A+B) = \frac{1}{2}$ ,  $0^\circ < A+B < 90^\circ$  and  $A>B$ , then find A and B.



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**165.** In a  $\triangle ABC$  right angled at  $B$ ,  $\angle A = \angle C$ . Find the values of (i)  $\sin A \cos C + \cos A \sin C$  (ii)  $\sin A \sin B + \cos A \cos B$



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**166.** If  $A$  and  $B$  are acute angles such that  $\tan A = \frac{1}{2}$ ,  $\tan B = \frac{1}{3}$  and  $\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$ , find  $A + B$ .



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**167.** In  $\triangle PQR$ , right-angled at  $Q$ ,  $PQ = 3\text{cm}$  and  $PR = 6\text{cm}$ . Determine  $\angle P$  and  $\angle R$ .



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**168.** Evaluate the following: (i)  $\frac{\cos 80^\circ}{\sin 10^\circ} + \cos 59^\circ \cos ec 31^\circ$  (ii)  $\frac{\cot 54^\circ}{\tan 36^\circ} + \frac{\tan 20^\circ}{\cot 70^\circ} - 2$  (iii)  $\frac{2\tan 53^\circ}{\cot 37^\circ} - \frac{\cot 80^\circ}{\tan 10^\circ}$



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**169.** Evaluate the following: (i)

$$\sec 50^\circ \sin 40^\circ + \cos 40^\circ \cos ec 50^\circ \quad (\text{ii})$$

$$\sec 70^\circ \sin 20^\circ - \cos 20^\circ \cos ec 70^\circ$$



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**170.** Prove that: (i)  $\sin 35 \sin 55 - \cos 35 \cos 55 = 0$

(ii)  $\frac{\cos 70}{\sin 20} + \frac{\cos 59}{\sin 31} - 8 \sin^2 30 = 0$



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**171.** Express each of the following in terms of trigonometric

ratios of angles between 0 and 45 : (i)  $\sin 85 + \cos ec 85$

(ii)  $\tan 68 + \sec 68$  (iii)  $\cos ec 69 + \cot 69$



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**172.** Express each of the following in terms of trigonometric

ratios of angles between 0 and 45 : (i)  $\sin 81 + \tan 81$

(ii)  $\sin 72 + \cot 72$



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173. Evaluate the following: (i)

$$\left(\frac{\sin 35}{\cos 55}\right)^2 + \left(\frac{\cos 55}{\sin 35}\right)^2 - 2 \cos 60$$

$$(ii) \frac{2 \cos 67}{\sin 23} - \frac{\tan 40}{\cot 50} - \cos 0$$



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174. Evaluate:  $\left(\frac{\sin 47^\circ}{\cos 43^\circ}\right)^2 + \left(\frac{\cos 43^\circ}{\sin 47^\circ}\right)^2 - 4 \cos^2 45^\circ$



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175. If  $A, B, C$  are the interior angles of a triangle  $ABC$ ,

prove that  $\frac{\tan(B+C)}{2} = \frac{\cot A}{2}$



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**176.** Find  $\theta$ ; if  $\sin(\theta + 36^\circ) = \cos \theta$ ; where  $\theta + 36^\circ$  is an acute angle.



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**177.** If  $\tan 2\theta = \cot(\theta + 6^\circ)$ , where  $2\theta$  and  $\theta + 6^\circ$  are acute angles, find the value of  $\theta$ .



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**178.** If  $\tan A = \cot B$ , prove that  $A + B = 90^\circ$



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**179.** If  $\sec 5A = \cos ec(A + 36^\circ)$ , where  $5A$  is an acute angle, find the value of  $A$



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**180.** If  $\sec 4A = \cos ec(A - 20^\circ)$ , where  $4A$  is an acute angle, find the value of  $A$ .



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**181.** Evaluate the following: (i)  $\frac{\sin 20^\circ}{\cos 70^\circ}$  (ii)  $\frac{\cos 19^\circ}{\sin 71^\circ}$



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**182.** Evaluate the following: (i)  $\frac{\sin 21^\circ}{\cos 69^\circ}$  (ii)  $\frac{\tan 10^\circ}{\cot 80^\circ}$  (iii)  
$$\frac{\sec 11^\circ}{\csc 79^\circ}$$

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**183.** Evaluate the following: (i)  $\left(\frac{\sin 49^\circ}{\cos 41^\circ}\right)^2 + \left(\frac{\cos 41^\circ}{\sin 49^\circ}\right)^2$  (ii)  
 $\cos 48^\circ - \sin 42^\circ$

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**184.** Evaluate the following: (i)  $\frac{\cot 40^\circ}{\tan 50^\circ} - \frac{1}{2} \left( \frac{\cos 35^\circ}{\sin 55^\circ} \right)$  (ii)  
 $\left( \frac{\sin 27^\circ}{\cos 63^\circ} \right)^2 - \left( \frac{\cos 63^\circ}{\sin 27^\circ} \right)^2$

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**185.** Evaluate the following: (i)  $\frac{\tan 35^\circ}{\cot 55^\circ} + \frac{\cot 78^\circ}{\tan 12^\circ} - 1$  (ii)  
$$\frac{\sec 70^\circ}{\cos ec 20^\circ} + \frac{\sin 59^\circ}{\cos 31^\circ}$$

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**186.** Evaluate the following: (i)  $\cos ec 31^\circ - \sec 59^\circ$  (ii)  
 $(\sin 72^\circ + \cos 18^\circ)(\sin 72^\circ - \cos 18^\circ)$

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**187.** Evaluate the following: (i)  $\sin 35^\circ \sin 55^\circ - \cos 35^\circ \cos 55^\circ$   
(ii)  $\tan 48^\circ \tan 23^\circ \tan 42^\circ \tan 67^\circ$  (iii)  
 $\sec 50^\circ \sin 40^\circ \oplus \cos 40^\circ \cos ec 50^\circ$

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**188.** Express each one of the following in terms of trigonometric ratios of angles lying between  $0^\circ$  and  $45^\circ$

$$(i) \sin 59^\circ + \cos 56^\circ$$

$$(ii) \tan 65^\circ + \cot 49^\circ$$

$$(iii) \sec 76^\circ + \csc 52^\circ$$



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**189.** Express each one of the following in terms of trigonometric ratios of angles lying between  $0^\circ$  and  $45^\circ$

$$\cos 78^\circ + \sec 78^\circ$$

$$(ii) \csc 54^\circ + \sin 72^\circ$$

$$(iii) \cot 85^\circ + \cos 75^\circ$$

$$(iv) \sin 67^\circ + \cos 75^\circ$$



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**190.** Express  $\cos 75^\circ + \cot 75^\circ$  in terms of angles between  $0^\circ$  and  $30^\circ$ .



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**191.** If  $\sin 3A = \cos(A - 26^\circ)$ , where  $3A$  is an acute angle, find the value of  $A$ .



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**192.** If  $A, B, C$  are the interior angles of a triangle  $ABC$ , prove that  $\tan\left(\frac{C+A}{2}\right) = \frac{\cot B}{2}$  (ii)  
 $\sin\left(\frac{B+C}{2}\right) = \frac{\cos A}{2}$



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**193.** Prove that:  $\tan 20^\circ \tan 35^\circ \tan 45^\circ \tan 55^\circ \tan 70^\circ = 1$



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**194.** Prove that:  $\sin 48^\circ \sec 42^\circ + \cos 48^\circ \cos ec 42^\circ = 2$



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**195.** Prove that:

$$\frac{\sin 70^\circ}{\cos 20^\circ} + \frac{\cos ec 20^\circ}{\sec 70^\circ} - 2\cos 70^\circ \cos ec 20^\circ = 0$$



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**196.** Prove that:  $\frac{\cos 80^\circ}{\sin 10^\circ} + \cos 59^\circ \cos ec 31^\circ = 2$



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197. If  $\sin \theta = \cos(\theta - 45^\circ)$ , where  $\theta$  and  $\theta - 45^\circ$  are acute angles, find the degree measure of  $\theta$ .



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198. If A, B and C are interior angles of a triangle ABC, then show that  $\sin\left(\frac{B+C}{2}\right) = \frac{\cos A}{2}$ .



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199. If  $2\theta + 45^\circ$  and  $30^\circ - \theta$  are acute angles, find the degree measures of  $\theta$  satisfying  $\sin(2\theta + 45^\circ) = \cos(30^\circ - \theta)$



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**200.** If  $\theta$  is a positive acute angle such that  $\sec \theta = \cos ec 60^\circ$ , find the value of  $2\cos^2 \theta - 1$ .

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**201.** If  $\cos 2\theta = \sin 4\theta$ , where  $2\theta$  and  $4\theta$  are acute angles, find the value of  $\theta$ .

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**202.** If  $\sin 3\theta = \cos(\theta - 6^\circ)$ , where  $(3\theta)$  and  $(\theta - 6^\circ)$  are both acute angles, then the value of  $\theta$  is (a)  $18^\circ$  (b)  $24^\circ$  (c)  $36^\circ$  (d)  $30^\circ$

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**203.** If  $\sec 4A = \cos ec(A - 20^\circ)$ , where  $4A$  is an acute angle, find the value of  $A$ .



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**204.** Write the maximum and minimum values of  $\sin \theta$ .



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**205.** Write the maximum and minimum values of  $\cos \theta$ .



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**206.** What is the maximum value of  $\frac{1}{\sec \theta}$ ?



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207. What is the maximum value of  $\frac{1}{\csc \theta}$ ?



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208. If  $\tan \theta = \frac{4}{5}$ , find the value of  $\frac{\cos \theta - \sin \theta}{\cos \theta + \sin \theta}$ .



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209. If  $\cos \theta = \frac{2}{3}$ , find the value of  $\frac{\sec \theta - 1}{\sec \theta + 1}$ .



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**210.** If  $3 \cot \theta = 4$ , find the value of  $\frac{4 \cos \theta - \sin \theta}{2 \cos \theta + \sin \theta}$ .



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**211.** Given  $\tan \theta = \frac{1}{\sqrt{5}}$ , what is the value of  $\frac{\cos ec^2 \theta - \sec^2 \theta}{\cos ec^2 \theta + \sec^2 \theta}$ ?



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**212.** If  $\cot \theta = \frac{1}{\sqrt{3}}$ , show that  $\frac{1 - \cos^2 \theta}{2 - \sin^2 \theta} = \frac{3}{5}$



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**213.** If  $\tan A = \frac{3}{4}$  and  $A + B = 90^\circ$ , then what is the value of  $\cot B$  ?



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**214.** If  $A + B = 90^\circ$  and  $\cos B = \frac{3}{5}$ , what is the value of  $\sin A$  ?



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**215.** Write the acute angle  $\theta$  satisfying  $\sqrt{3} \sin \theta = \cos \theta$ .



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**216.** Write the value of  $\tan 10^\circ \tan 15^\circ \tan 75^\circ \tan 80^\circ$ .



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**217.** If  $\tan A = \frac{3}{4}$  and  $A + B = 90^\circ$ , then what is the value of  $\cot B$  ?



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**218.** If  $\tan A = \frac{5}{12}$ , find the value of  $(\sin A + \cos A)\sec A$  .



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**219.** If  $\theta$  is an acute angle such that  $\cos \theta = \frac{3}{5}$  , then  
$$\frac{\sin \theta \tan \theta - 1}{2 \tan^2 \theta} =$$
 (a)  $\frac{16}{625}$  (b)  $\frac{1}{36}$  (c)  $\frac{3}{160}$  (d)  $\frac{160}{3}$



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**220.** If  $\tan \theta = \frac{a}{b}$ , then  $\frac{a \sin \theta + b \cos \theta}{a \sin \theta - b \cos \theta}$  is equal to (a)  $\frac{a^2 + b^2}{a^2 - b^2}$  (b)  $\frac{a^2 - b^2}{a^2 + b^2}$  (c)  $\frac{a + b}{a - b}$  (d)  $\frac{a - b}{a + b}$



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**221.** If  $5 \tan \theta - 4 = 0$ , then the value of  $\frac{5 \sin \theta - 4 \cos \theta}{5 \sin \theta + 4 \cos \theta}$  is

A.  $\frac{5}{3}$

B.  $\frac{5}{6}$

C. 0

D.  $\frac{1}{6}$

**Answer: c**



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**222.** If  $16 \cot x = 12$ , then  $\frac{\sin x - \cos x}{\sin x + \cos x}$  equals (a)  $\frac{1}{7}$  (b)  $\frac{3}{7}$  (c)  $\frac{2}{7}$  (d) 0

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**223.** If  $8 \tan x = 15$ , then  $\sin x - \cos x$  is equal to

A.  $\frac{8}{17}$

B.  $\frac{17}{7}$

C.  $\frac{1}{17}$

D.  $\frac{7}{17}$

**Answer:** D

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**224.** If  $\tan \theta = \frac{1}{\sqrt{7}}$ , find the value of  $\frac{\cos ec^2 \theta - \sec^2 \theta}{\cos ec^2 \theta + \sec^2 \theta}$ .



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**225.** If  $\tan \theta = \frac{3}{4}$ , then  $\cos^2 \theta - \sin^2 \theta =$  (a)  $\frac{7}{25}$  (b) 1 (c)  $-\frac{7}{25}$  (d)  $\frac{4}{25}$



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**226.** If  $\theta$  is an acute angle such that  $\tan^2 \theta = \frac{8}{7}$ , then the value of  $\frac{(1 + \sin \theta)(1 - \sin \theta)}{(1 + \cos \theta)(1 - \cos \theta)}$  is (a)  $\frac{7}{8}$  (b)  $\frac{8}{7}$  (c)  $\frac{7}{4}$  (d)  $\frac{64}{49}$



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**227.** If  $3 \cos \theta = 5 \sin \theta$ , then the value of  $\frac{5 \sin \theta - 2 \sec^3 \theta + 2 \cos \theta}{5 \sin \theta + 2 \sec^3 \theta - 2 \cos \theta}$  is (a)  $\frac{271}{979}$  (b)  $\frac{316}{2937}$  (c)  $\frac{542}{2937}$  (d)

None of these



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**228.** If  $\tan^2 45^\circ - \cos^2 30^\circ = x \sin 45^\circ \cos 45^\circ$ , then  $x$  is (a) 2  
(b) -2 (c)  $-\frac{1}{2}$  (d)  $\frac{1}{2}$



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**229.** The value of  $\cos^2 17^\circ - \sin^2 73^\circ$  is (a) 1 (b)  $\frac{1}{3}$  (c) 0 (d) -1



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**230.** The value of  $\frac{\cos^3 20^\circ - \cos^3 70^\circ}{\sin^3 70^\circ - \sin^3 20^\circ}$  is (a)  $\frac{1}{2}$  (b)  $\frac{1}{\sqrt{2}}$  (c) 1 (d) 2



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**231.** If  $A$  and  $B$  are complementary angles, then  
(a)  $\sin A = \cos B$  (b)  $\cos A = \sin B$  (c)  $\tan A = \cot B$  (d)  
 $\sec A = \csc B$



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**232.** If  $x \sin(90^\circ - \theta) \cot(90^\circ - \theta) = \cos(90^\circ - \theta)$ , then  
 $x =$

A. (a) 0

B. (b) 1

C. (c) -1

D. (d) 2

**Answer:** null



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**233.** If  $x \tan 45^\circ \cos 60^\circ = \sin 60^\circ \cot 60^\circ$ , then  $x$  is equal to

A. (a) 1

B. (b)  $\sqrt{3}$

C. (c)  $\frac{1}{2}$

D. (d)  $\frac{1}{\sqrt{2}}$

**Answer:** null



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234. If angles  $A, B, C$  of a  $\triangle ABC$  form an increasing AP ,

then  $\sin B =$  (a)  $\frac{1}{2}$  (b)  $\frac{\sqrt{3}}{2}$  (c) 1 (d)  $\frac{1}{\sqrt{2}}$



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235. If  $\theta$  is an acute angle such that  $\sec^2 \theta = 3$  , then the value

of  $\frac{\tan^2 \theta - \cos ec^2 \theta}{\tan^2 \theta + \cos ec^2 \theta}$  is (a)  $\frac{4}{7}$  (b)  $\frac{3}{7}$  (c)  $\frac{2}{7}$  (d)  $\frac{1}{7}$



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236. The value of  $\tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \tan 89^\circ$  is (a) 1 (b)  $-1$  (c)

0 (d) None of these



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237. The value of  $\cos 1^\circ \cos 2^\circ \cos 3^\circ \dots \cos 180^\circ$  is (a) 1 (b) 0 (c) -1 (d) None of these



238. The value of  $\tan 10^\circ \tan 15^\circ \tan 75^\circ \tan 80^\circ$  is (a) -1 (b) 0 (c) 1 (d) None of these



239. If  $\theta$  and  $2\theta - 45^\circ$  are acute angles such that  $\sin \theta = \cos(2\theta - 45^\circ)$ , then  $\tan \theta$  is equal to (a) 1 (b) -1 (c)  $\sqrt{3}$  (d)  $\frac{1}{\sqrt{3}}$



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**240.** If  $5\theta$  and  $4\theta$  are acute angles satisfying  $\sin 5\theta = \cos 4\theta$  ,  
then  $2 \sin 3\theta - \sqrt{3} \tan 3\theta$  is equal to

A. (a) 1

B. (b) 0

C. (c) -1

D. (d)  $1 + \sqrt{3}$

**Answer:** null



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241.  $\frac{2 \tan 30^\circ}{1 - \tan^2 30^\circ}$  is equal to (a)  $\sin 60^\circ$  (b)  $\cos 60^\circ$  (c)  $\tan 60^\circ$   
(d)  $\sin 30^\circ$



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242.  $\frac{1 - \tan^2 45^\circ}{1 + \tan^2 45^\circ}$  is equal to

A. (a)  $\tan 90^\circ$

B. (b) 1

C. (c)  $\sin 45^\circ$

D. (d)  $\sin 0^\circ$

**Answer:** null



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- 243.**  $\sin 2A = 2 \sin A$  is true when  $A =$  (a)  $0^\circ$  (b)  $30^\circ$  (c)  $45^\circ$  (d)  $60^\circ$



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- 244.**  $\frac{2\tan 30^\circ}{1 - \tan^2 30^\circ}$  is equal to (a)  $\cos 60^\circ$  (b)  $\sin 60^\circ$  (c)  $\tan 60^\circ$  (d)  $\sin 30^\circ$



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- 245.** If A, B and C are interior angles of a triangle ABC, then show that  $\sin\left(\frac{B+C}{2}\right) = \cos\left(\frac{A}{2}\right)$ .



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- 246.** If  $\cos \theta = \frac{2}{3}$ , then  $2\sec^2 \theta + 2\tan^2 \theta - 7$  is equal to (a) 1  
(b) 0 (c) 3 (d) 4



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- 247.**  $\tan 5^\circ \times \tan 30^\circ \times \tan 45^\circ \times \tan 85^\circ$  is equal to  $\frac{4}{\sqrt{3}}$  (b)  $4\sqrt{3}$  (c)  
1 (d) 4



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- 248.** In Fig. 5.47, the value of  $\cos \varphi$  is (FIGURE) (a)  $\frac{5}{4}$  (b)  $\frac{5}{3}$  (c)  $\frac{3}{5}$   
(d)  $\frac{4}{5}$



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**249.** In Figure,  $AD = 4\text{cm}$ ,  $BD = 3\text{cm}$  and  $CB = 12\text{cm}$ , find

$$\cot \theta . (a) \frac{12}{5} (b) \frac{5}{12} (c) \frac{13}{12} (d) \frac{12}{13}$$



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