



MATHS

BOOKS - RD SHARMA MATHS (ENGLISH)

RELATIONS

Others

1. Let R be the relation on Z defined by $R=\{(a,b)\!:\!a,b ext{ belongs to Z}$

, a-b is an integer}. Find the domain and range of R.

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2. If $A = \{1, 2, 4\}, B = \{2, 4, 5\}, C = \{2, 5\}, then(A - B) \times (B - C)$

is (a){(1, 2), (1, 5), (2, 5)} (b) {(1, 4)} (c) (1, 4) (d) none of these.

3. If AandB are two sets having 3 elements in common. If n(A) = 5, n(B) = 4, find $n(A imes B)andn[(A imes B) \cap (B imes A)]$.



4. If $A = \{1,3,5\}, B = \{x,y\}$ represent the following products: A imes B

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5. If
$$A = \{-1,2\}$$
 , find $A imes A$

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6. Let AandB be two sets. Show that the sets $A \times BandB \times A$ have an element in common iff the sets AadnB have an element in common.

7. If
$$A=\{1,5\}$$
 , $B=\{3\}$, find $A imes B$

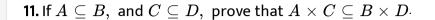


8. For any three sets
$$A, B, C$$
 prove that:
 $A \times (B' \cup C')' = (A \times B) \cap (A \times C)$ and
 $A \times (B' \cap C')' = (A \times B) \cup (A \times C)$

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9. If $A\subseteq B, ext{ show that } A imes A\subseteq (A imes B)\cap (B imes A).$

10. If A and B are any two non-empty sets, then prove that: $A \times B = B \times A' \Rightarrow A = B$





12. If $A \subseteq B$, prove that $A \times C \subseteq B \times C$ for any set C.



13. If R is a relation on the set $A = \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$ given by $xRy \Leftrightarrow y = 3x$, then R = (a) $\{(3, 1), (6, 2), (8, 2), (9, 3)\}$ (b) $\{(3, 1), (6, 2), (9, 3)\}$ (c) $\{(3, 1), (2, 6), (3, 9)\}$ (d) none of these.

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14. If $A = \{1, 2, 3\}, B = \{4, 5, 6\}$, which of the following are relations from $A \rightarrow B$? Give reasons in support of your answer. $\{(1,6), (3,4), (5,2)\}$ (ii) $\{(1,5), (2,6), (3,4), (3,6)\}$ (iii)

 $\{(4,2),(4,3),(5,1)\}$ (iv) $A imes B_{\cdot}$

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15. $A = \{1, 2, 3, 5\}$ and $B = \{4, 6, 9\}$. Define a relation R from A to B by R = {(x, y): the difference between x and y is odd: $x \in A$, $y \in B$ }. Write R in roster form.

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16. Let R be the relation on the Z of all integers defined by $(x, y) \in Rx - y$ is divisible by n. Prove that: $(x, x) \in R$ for all $x \in Z$ $(x, y) \in R(y, x) \in R$ for all $x, y \in Z$ $(x, y) \in Rand(y, z) \in R(x, z) \in R$ for all $x, y, z \in R$

17. A relation R is defined from $\{2, 3, 4, 5\}$ to $\{3, 6, 7, 10\}$ by :xRy:x is relatively prime to y. Then, domain of R is (a) $\{2, 3, 5\}$ (b) $\{3, 5\}$ (c) $\{2, 3, 4\}$ (d) $\{2, 3, 4, 5\}$.



18. Let R be a relation in N defined by $(x,y)\in Rx+2y=8$. Express R

and R^{-1} as sets of ordered pairs.

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19. The Cartesian product A imes A has 9 elements among which are found

 $(\ -1, \ \ 0)$ and $(\ 0, \ \ 1)$. Find the set A and the remaining elements of A imes A .

20. Let $A=\{-1,3,5\}$ and $B=\{2,3\}$ find A imes B



21. Express $A = \{(a, b) : 2a + b = 5, a, b \in W\}$ as the set ordered pairs.

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22. If $A imes B = \{(a,1)(b,3), (a,3), (b,1), (a,2), (b,2)\}$, find $AandB_{\cdot}$

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23. Let $A=\{1,2,3\}$ and $B=\{x\colon x\in N,x ext{ is prime less than 5}\}.$ Find

A imes B

24. If $A imes B = \{(a,1)(a,5), (a,2), (b,2), (b,5), (b,1)\}$, find B imes A.



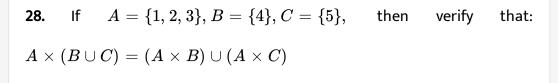
25. If
$$A = \{1, 2\}, B = \{3, 4\}$$
 find $A imes B$

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26. Find x and y, if (x+3,5) = (6, 2x+y).

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27. If $A=\{a,b\}$ and $B=\{1,2,3\}, ext{ find } A imes B, B imes A$





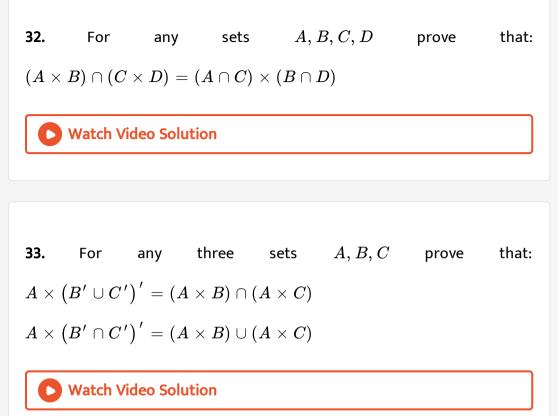
29. If
$$A = \{a, b\}$$
 and $B = \{3\}$, find $A \times B$

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30. If $A \times B \subseteq C \times DandA \times B \neq \varphi$, prove that $A \subseteq C$ and $B \subseteq D$.

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31. Express $A = \{(a, b) : a + b = 4, a, b \in W\}$ as the set ordered pairs.



34. A and B are two non empty set having n element in common ; then

prove that A imes B and B imes A have n^2 element in common.



35. Let A be a non-empty set such that A imes B = A imes C . Show that B = C .



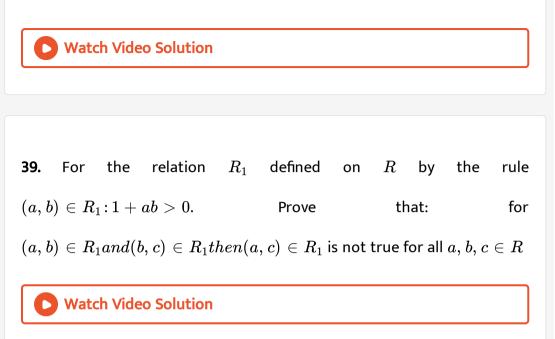
36. Let R be the relation on the set N of natural numbers defined by $R=\{(a,b):a+3b=12,a\in N,b\in N\}$. Find : (i) R (ii) $Doma\in of$ R(iii)RangeofR

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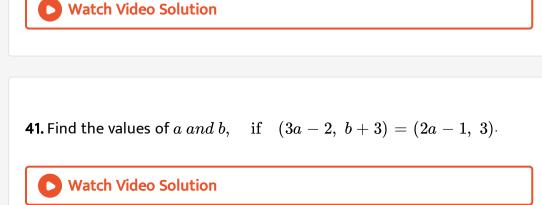
37. If $A=\{a,b\}$ and $B=\{-4,6\}, ext{ find } A imes B$



38. A relation R is defined on the set Z of integers as: $(x,y)\in Rx^2+y^2=25$. Express $RandR^{-1}$ as the sets of ordered pairs and hence find their respective domains.



40. The position of a point in a two dimensional plane in Cartesian coordinates is represented by an ordered pair. Accordingly the ordered pairs (1,3), (2,4), (2,3) and (3,2) represents different points in a plane.



42. If $A=\{1,3,5,6\}$ and $B=\{2,4\}, f\in dA imes B$ and B imes A.



43. If $A=\{1,2,3\},\ B=\{3,4\}$ and $C=\{1,3,5\}$, find $A imes (B\cup C)$

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44. If $A = \{1, 2, 3\}, \; B = \{3, 4\} and \; C = \{1, 3, 5\}$, find $A imes (B \cap C)$

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45. If
$$A = \{1, 2, 3\}, \ B = \{3, 4\} and \ C = \{1, 3, 5\}$$
, find $(A \times B) \cap (A \times C)$

46. If $A = \{1, 2\}$, from the set A imes A imes A

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47. If R is the set of all real numbers, what do the cartesian products

R imes R and R imes R imes R represent?

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48. Let A and B be two sets such that $A \times B$ consists of 6 elements. If three elements of $A \times B$ are: (1, 4), (2, 6), (3, 6). Find other elements of $A \times B$ and $B \times A$.

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49. Let A and B be two sets such that n(A) = 5 and n(B) = 2, if a, b, c, d, e are distinct and (a, 2), (b, 3), (c, 2), (d, 3), (e, 2) are in $A \times B$, find A and B.

50. If
$$\left(rac{a}{3}-1,\ b-rac{2}{3}
ight)=\left(rac{5}{3},rac{1}{3}
ight)$$
 , find the values of a and b .

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51. If the ordered pairs
$$(x, -1)$$
 and $(5, y)$ belong to the set $\{(a, b): b = 2a - 3\}$, find the values of x and y .

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52. If (x + 1, 1) = (3, y - 2), find the value of x and y.

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53. If $a \in \{2,4,6,9\} and \, b \in \{4,6,18,27\}$, then from the set of al

ordered pairs (a, b) such that a divides `b and a

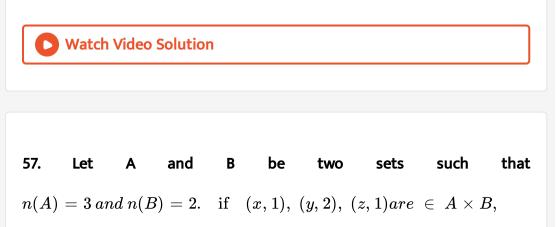
54. if $A = \{1, 2\}$ and $B = \{1, 3\}$, find $A \times B$ and $B \times A$.

55. If $A=\{1,2,3\}$ and $B=\{3,4\}$. Find A imes B and show it graphically.

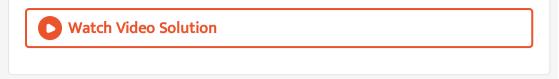
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56. If
$$A = \{1, 2, 3\}$$
 and $B = \{2, 4\}$, what are

 $A \times B, \ B \times A, \ A \times A, \ B \times B, \ and \ (A \times B) \cap (B \times A)?$



find A and B, where x, y, z are distinct elements.



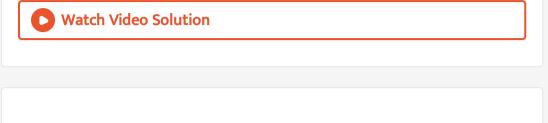
58. Let $A = \{1, 2, 3, 4\}$ and $R = \{(a, b) : a \in A, b \in A, a \text{ divides } b\}$.

Write R explicity.

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59. State whether each of the following statements are true or false. If the statement is false re-write the given statement correctly: (i) If $p = \{m, n\}$ and $Q = \{n, m\}$, then $P \times Q = \{(m, n), (n, m)\}$ (ii) If A and B are non empty sets then $A \times B$ is a non empty set of ordered pairs (x, y) such that $x \in B$ and $y \in A$. (iii) If $A = \{1, 2\}, B = \{3, 4\}, then A \times (B \cap \varphi) = \varphi$.

60. If $A=\{1,2\}, \,\,$ form the set A imes A imes A .



61. If $A = \{1, 2, 4\} and B = \{1, 2, 3\}$, represent following sets graphically- $A \times B$

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62. If $A = \{1, 2, 4\}$ and $B = \{1, 2, 3\}$, represent following sets graphically- $B \times A$

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63. If $A = \{1, 2, 4\}$ and $B = \{1, 2, 3\}$, represent following sets graphically- $A \times A$

64. If $A = \{1, 2, 4\}$ and $B = \{1, 2, 3\}$, represent following sets graphically- $B \times B$ Watch Video Solution $A = \{2, 3\}, B = \{4, 5\}, C = \{5, 6\},$ find 65. lf $A \times (B \cup C), \ A \times (B \cap C), \ (A \times B) \cup (A \times C).$ Watch Video Solution **66.** Let $A = \{1, 2\}, B = \{1, 2, 3, 4\}, C = \{5, 6\}$ and $D = \{5, 6, 7, 8\}$. Verity that: $A \times C \subset B \times D$

67. Let $A = \{1,2\}, \ B = \{1,2,3,4\}, \ C = \{5,6\} and \ D = \{5,6,7,8\}$. Verity that: $A \times (B \cap C) = (A \times B) \cap (A \times C)$



68. If $A = \{1, 2, 3\}, \; B = \{1, 2, 3, 4\}, \; C = \{4, 5, 6\},$ find $: A imes (B \cap C)$

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69.

 $A=\{1,2,3\},\;B=\{1,2,3,4\},\;C=\{4,5,6\},\;f\in d:(A imes B)\cap (A imes C)$

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70.

lf

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 $A=\{1,2,3\},\;B=\{1,2,3,4\},\;C=\{4,5,6\},\;find:A imes(B\cap C)$

 $A=\{1,2,3\},\;B=\{1,2,3,4\},\;C=\{4,5,6\},\;f\in d\!:\!(A imes B)\cap(A imes C)$

72. Let
$$A = \{1, 2, 3\}, B = \{a, b, c, d\}$$
 be two sets and let
 $R = \{(1, a), (1, c), (2, d), (2, c)\}$ be a relation from A to B. Then
 $R^{-1} = \{(a, 1), (c, 1), (d, 2), (c, 2)\}$ is a relation from B to A.

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73. If $A = \{a, b, c, d\}$, $B = \{p, q, r, s\}$ than is the following relation from $A \rightarrow B$? Give reasons for your answer: $R_1 = \{(a, p), (b, r), (c, s)\}$

74. If $A = \{a, b, c, d\}$, $B = \{p, q, r, s\}$ than is the following relation from $A \rightarrow B$? Give reasons for your answer.: $R_2 = \{(q, b), (c, s), (d, r)\}$

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75. If $A = \{a, b, c, d\}$, $B = \{p, q, r, s\}$ than Is the following relation from $A \rightarrow B$? Give reasons for your answer.: $R_3 = \{(a, p), (a, q), (d, p), (c, r), (b, r)\}$

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76. If $A = \{a, b, c, d\}$, $B = \{p, q, r, s\}$ than is the following relation from $A \rightarrow B$? Give reasons for your answer.: $R_4 = \{(a, p), (q, a), (b, s), (s, b)\}$

77. If $A = \{1, 3, 5, 7\}, B = \{2, 4, 6, 8, 10\}$ and let $R = \{(1, 8), (3, 6), (5, 2), (1, 4)\}$ be a relation form A to B. Then, find Dom(R) and Ran(R)



78. If R is a relation from set $A = \{2, 4, 5\}$ to set $B = \{1, 2, 3, 4, 6, 8\}$ defined by $xRy \Leftrightarrow x$ divides y. Write R as a set of ordered pairs Find the domain and the range of R.

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79. Let $A = \{1, 2, 3\}, B = \{a, b, c, d\}$ be two sets and let $R = \{(1, a), (1, c), (2, d), (2, c)\}$ be a relation from A to B. Then $R^{-1} = \{(a, 1), (c, 1), (d, 2), (c, 2)\}$ is a relation from B to A.

80. If $A = \{1, 2, 3\}, B = \{4, 5, 6\}$ Is the following ralation from $A \to B$? Give reason in support of your answer: $R_1 = \{(1, 4), (1, 5), (1, 6)\}$

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81. If $A = \{1, 2, 3\}, B = \{4, 5, 6\}$ Is the following relation from $A \rightarrow B$? Give reason in support of your answer: $R_2 = \{(1, 5), (2, 4), (3, 6)\}$

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82. If $A = \{1, 2, 3\}, B = \{4, 5, 6\}$ Is the following relatios from $A \rightarrow B$? Give reason in support of your answer: $R_3 = \{(1, 4), (1, 5), (3, 6), (2, 6), (3, 4)\}$

83. If $A = \{1, 2, 3\}, B = \{4, 5, 6\}$ then, is the following relation from $A \rightarrow B$? Give reason in support of your answer: $R_4 = \{(4, 2), (2, 6), (5, 1), (2, 4)\}$

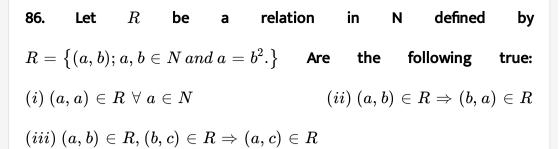


84. Let $A = \{1, 2, 3, 4, 5, 6\}$. Define a relation R on set A by $R = \{(x, y) : y = x + 1\}$ Depict this relation using an arrow diagram Write down the domain, co domain and range of R.

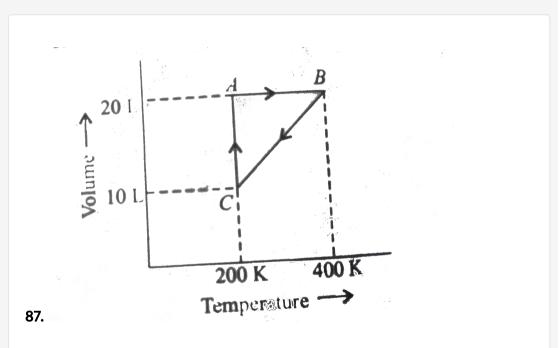
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85. Figure 2.14 shows a relation R between the sets P and Q. Write this relation R in i. Roster form ii. Set builder form. What is it's domain and range?









The pressures at A and B in the atmosphere are, respectively,



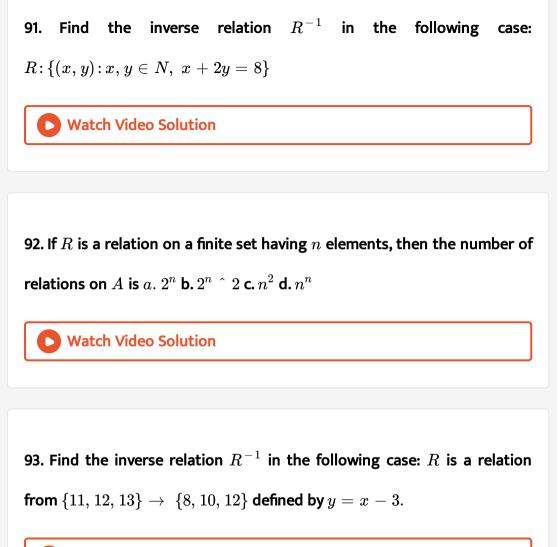
88. A relation R is defined from a set $A = \{2, 3, 4, 5\} \rightarrow a \ set \ B = \{3, 6, 7, 10\}$ as follows: $(x, y) \in R \Leftrightarrow x$ is relatively prime to y. Express R as a set of ordered pairs and determine its domain and range.

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89. Let A be the set of first five natural numbers and let R be a relation on A defined as follows $(x, y) \in R \Leftrightarrow x \leq y$. Express R and R^{-1} as sets of ordered pairs. Determine also The domain of R^{-1} The range of R.

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90. Find the inverse relation R^{-1} in the following case: $R: \{(1, 2), (1, 3), (2, 3), (3, 2), (5, 6)\}$



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94. Write the following relation as the sets of ordered pair: A relation \boldsymbol{R}

from the set $\{2,3,4,5,6\}$ to the set $\{1,2,3\}$ defined by x=2y .

95. Write the following relation as the set of ordered pair: A relation R on the set $\{1,2,3,4,5,6,7\}$ defined by $(x,y)\in R\Leftrightarrow x$ is relatively prime to y.

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96. Write the following relation as the set of ordered pair: A relation ${\cal R}$ on

the set $\{0, 1, 2, ; 10\}$ defined by 2x + 3y = 12.



97. Write the following relation as the set of ordered pair: A relation Rfrom a set $A = \{5, 6, 7, 8\}$ to the set $B = \{10, 12, 15, 16, 18\}$ defined by $(x, y) \in R \Leftrightarrow x$ divides y.

98. Let
$$A = \{3, 5\} and B = \{7, 11\}$$
. Let

 $R = \{(a,b) : a \in A, \; b \in b, \; a-b \; ext{is odd} \}$. Show that R is an empty

relation from A and B.

99. Let $A = \{1,2] and B = \{3,4\}$. Find the total number of relations

from A into B.

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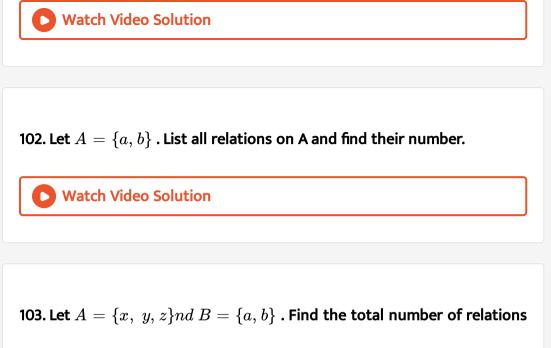
100. Determine the domain and range of the relation R defined by:

$$R=\{(x,x+5)\!:\!x\in\{0,1,2,3,4,5\}$$



101. Determine the domain and range of the relation R defined by:

$$R = \{(a,b) : b = |a-1|, \; a \in Z \, and \; |a| \leq 3\}$$



from A into B.

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104. Let R be a relation from N to N defined by $R = \{(a, b) : a\dot{b} \in N \text{ and } a = b^2\}$. Are the following true?(i) $(a, a) \in R, \forall a \in N \text{ (ii)}$ $(a, b) \in R, implies(b, a) \in R \text{ (iii)} (a, b) \in R, \text{ (b, c)} \in R \text{ implies (a, c)} \in R$.

105. Let $A=\{1,2,3,...,14\}$. Define a relation on a set A by $R=\{(x,y)\colon 3x-y=0.\ where\ x,y\in A\}.$ Depict this relationship

using an arrow diagram. Write down its domain, co-domain and range.



106. Define a relation R on the set N of natural numbers by $R = \{(x, y) : y = x + 5, x \text{ is a natural number less than } 4, x, y \in N\}$. Depict this relationship using i. roster form ii. an arrow diagram. Write down the domain and range or R.

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107. Let $A = \{1, 2, 3, 5\}B = \{2, 4, 9\}$.Define a relation. from A to B by $R = \{(x, y):$ the difference between x and y is odd, $x \in A, y \in B\}$. Write it in Roster from

108. Write the relation $R = ig\{ ig(x,x^3ig) : x ext{ is a prime number less than 10} ig\}$

in roster form.



109. Let $A = \{1, 2, 3, 4, 5, 6\}$. Let R be a relation on A defined by $R = \{(a, b) : a, b \in A, b \text{ is exactly divisible by a}\}$ Write R is roster form Find the domain of R Find the range of R.

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110. Figure 2.15 shows a relationship between the sets P and Q. Write this relation in Set builder form ii. Roster form What is its domain and range?

111. Let R be the relation on Z defined by $R = \{(a, b) : a, b \in Z, a - b \text{ is }$

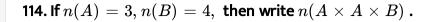
an integer}. Find the domain and range of R_{\cdot}



112. Let
$$R$$
 be a relation on $N \times N$ defined by
 $(a, b) R(c, d) \Leftrightarrow a + d = b + c$ if $(a, b), (c, d) \in N \times N$ then show
that:
 $(i) (a, b) R (a, b) f$ or $all (a, b) \in N \times N$
 $(ii) (a, b) R(c, d) \Rightarrow (c, d) R(a, b) f$ or $all (a, b), (c, d) \in N \times N$
 $(iii) (a, b) R (c, d) and (c, d) R(e, f) \Rightarrow (a, b) R(e, f)$ for all
 $(a, b), (c, d), (e, f) \in N \times N$

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113. If $A = \{1, 2, 4\}, B = \{2, 4, 5\}$ and $C = \{2, 5\},$ write $(A - B) \times (B - C)$.





115. If R is a relation defined on the set Z of integers by the rule $(x,y)\in R\Leftrightarrow x^2+y^2=9,$ then write domain of R.

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116. If $R=ig\{(x,\ y)\!:\!x^2+y^2\leq 4;x,\ y\in Zig\}$ is a relation on Z , write the domain of R .

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117. If R is a relation from set $A = \{11, 12, 13\}$ to set $B = \{8, 10, 12\}$ defined by y = x - 3, then write R^{-1} .

 $\mathbf{A}\{(8,11),(10,13)\}$

 $\mathbf{B.}\left\{(8,11),\,(10,12)\right\}$

 $C. \{(10, 13), (10, 11)\}$

D. none of these

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118.

Let

 $R = \{(x,y)\!:\! x,y\in Z,\; y=2x-4\} If\,(a,\;-2) \; and \; igl(4,b^2igr)\in R, \; \; { t then }$

write the values of a and b.

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119. If $R=\{(2,1),\;(4,7),\;(1,\;-2)...\}$, then writhe the linear relation

between the components of the ordered pairs of the relation R.

120. If $A = \{1, 3, 5\}$ and $B = \{2, 4\}$ list the elements of R, if $R = \{(x, y) : x, y \in A \times B \text{ and } x > y\}$.

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121. If $R = \{(x,y) : x, y \in W, 2x + y = 8\}$, then write the domain and

range of R.

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122. Let A and B be two sets such that n(A) = 3 and n(B) = 2. If

(x, 1), (y, 2), (z, 1) are in A imes B, write A and B.

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123. Let $A = \{1, 2, 3\}, \ B = \{1, 3, 5\}$. If relation R from A to B is given by $R = \{(1, 3), \ (2, 5), \ (3, 3)\}$. Then R^{-1} is

 $A. \{ (3,3), (3,1), (5,2) \}$

 $\mathbf{B.}\left\{(1,3),(2,5),(3,3)\right\}$

 $C. \{(1, 3), (5, 2)\}$

D. none of these

Answer: A

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124. If $A = \{1, 2, 3\}, B = \{1, 4, 6, 9| and R$ is a relation from A to B

defined by x is greater than y. The range of R is

 $\mathbf{A}\{1, 4, 6, 9\}$

B. $\{4, 6, 9\}$

C. $\{1\}$

D. none of these

125. If $R = \{(x, y): x, y \in Z, x^2 + y^2 \le 4\}$ is a relation on Z, then domain of R is $\{0, 1, 2\}$ b. $\{0, -1, -2\}$ c. $\{-2, -1, 0, 1, 2\}$ d. none of these

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126. A relation arphi from $C \ o \ R$ is defined by $x arphi y \Leftrightarrow |x| = y$. Which one

is correct? a.(2+3i)arphi 13 b. 3arphi(-3) c. (1+i)arphi 2 d. iarphi 1

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127. Let R be a relation n N defined by x + 2y = 8. The domain of R is

(a) $\{2, 4, 8\}$ b. $\{2, 4, 6, 8\}$ c. $\{2, 4, 6\}$ d. (1, 2, 3, 4)

128. R is a relation from {11,12,13} to {8,10,12} defined by y=x-3 Then

 R^{-1} is



129. Let R be a relation from a set A to a set B, then

A. A. $R = A \cup B$

B. B. $R = A \cap B$

C.C. $R \subseteq A imes B$

D. D. $R \subseteq B imes A$

Answer: C

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130. If R is a relation from a finite set A having m elements to a finite set

B having n elements then the number of relations from A to B is

A. A. 2^{mn}

B. B. $2^{mn} - 1$

 $\mathbf{C.}\,\mathbf{C.}\,n^m$

D. D. m^n

Answer: A