



MATHS

BOOKS - RD SHARMA MATHS (ENGLISH)

THE CIRCLE

Others

1. Find the equation of the circle whose centre is at the point (4, 5)and which passes through the centre of the circle $x^2 + y^2 - 6x + 4y - 12 = 0.$

2. Find the equation of the circle passing through (1, 0) and (0, 1) and having the smallest possible radius.



3. If (-3,2) lie on the circle $x^2 + y^2 + 2gx + 2fy + c = 0$ which is concentric with the circle $x^2 + y^2 + 6x + 8fy - 5 = 0$, then c =(a)11 (b) - 11 (c)24 (d)32

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4. Find the equation of the circle drawn on the intercept made by the

line 2x + 3y = 6 between the coordinate axes as diameter.

5. The straight line $\frac{x}{a} + \frac{y}{b} = 1$ cuts the coordinate axes at A and B. Find the equation of the circle passing through O(0,0), AandB.



8. If the lines 3x - 4y + 4 = 0 and 6x - 8y - 7 = 0 are tangents to

a circle, then find the radius of the circle.

9. Show that the point
$$(x, y)$$
 given by $x = \frac{2at}{1+t^2}andy = \left(\frac{1-t^2}{1+t^2}\right)$ lies on a circle for all real values of t

such that $-1 \leq t \leq 1$, where a is any given real number.

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10. If the line lx+my-1=0 touches the circle $x^2+y^2=a^2$,

then prove that (l, m) lies on a circle.



11. Find the radius of the circle $(x \cos \alpha + y \sin \alpha - a)^2 + (x \sin \alpha - y \cos \alpha - b)^2 = k^2$, if α varies, the locus of its centre is again a circle. Also, find its centre and radius.

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12. Find the equation to the circle which passes through the origin and cut off equal chords of length 'a' from the straight lines y = xandy = -x.

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13. On the joining (1, 0)and(3, 0) be and equilateral triangle is drawn, having its vertex in the first quadrant. Find the equation to the circles described on its sides as diameter.

14. If the point (k+1,k) lies inside the region bound by the curve $x=\sqrt{25-y^2}$ and the y-axis, then the integral value of k is/are

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15. If the point
$$(2, k)$$
 lies outside the circles
 $x^2 + y^2 + x - 2y - 14 = 0$ and $x^2 + y^2 = 13$ then k lies in the
interval (a) $(-3, -2) \cup (3, 4)$ (b) $(-3, 4)$ (c)
 $(-\infty, -3) \cup (4, \infty)$ (d) $(-\infty - 2) \cup (3, \infty)$

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16. A circle has radius 3units and its centre lies on the line y = x - 1. Find the equation of the circle, if it passes through (7, 3).

17. Find the equation of the circle which touches both the axes and

the line 3x - 4y + 8 = 0 and lies in the third quadrant.

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18. A circle of radius 2 lies in the first quadrant and touches both the axes. Find the equation of the circle with centre at (6, 5) and touching the above circle externally.

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19. Find the equation of a circle of radius 5 which lies within the circle $x^2 + y^2 + 14x + 10y - 26 = 0$ and which touches the given circle at the point (-1, 3).



20. Find the equation of the circle whose radius is 5 and which touches the circle $x^2 + y^2 - 2x - 4y - 20 = 0$ externally at the point (5, 5).

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21. The circle $(x - a)^2 + (y - a)^2 = a^2$ is rolled on the $y - a\xi s$ in the positive direction through one complete revolution. Find the equation of the circle in its new-position.

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22. Find the equation of the image of the circle $x^2 + y^2 + 8x - 16y + 64 = 0$ in the line mirror x = 0.

23. A circle of radius *5units* touches the coordinate axes in the first quadrant. If the circle makes one complete roll on x-axis along the positive direction of x-axis , find its equation in new position.

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24. Find the equation of a circle which passes through the point (2, 0) and whose centre is the limit of the point of intersection of the lines 3x + 5y = 1 and $(2 + c)x + 5c^2y = 1$ as c tends to 1.

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25. Find the equation of a circle which touches y - axis at a distance of 4units from the origin and cuts an intercept of 6units along the positive direction of x - axis.



26. If the circle $x^2+y^2+2ax+8y+16=0$ touch x-axis , $then, the value of 'a\,'is(a)$ +-16(b)+-4(c)+-8(d)+-1'

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27. If the abscissae and the ordinates of two point AandB be the roots of $ax^2 + bx + c = 0$ and $a'y^2 + b'y = c' = 0$ respectively, show that the equation of the circle described on AB as diameter is $aa'(x^2 + y^2) + a'bx + ab'y + (ca' + ca) = 0.$

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28. Find the equation of the circle which passes through the points

 $(2,\ -2)$, and (3,4) and whose centre lies on the line x+y=2 .

29. If $2x^2 + \lambda xy^+ 2y^2 + (\lambda - 4)x + 6y - 5 = 0$, is the equation of a circle, then its radius is :



31. If the line lx+my+n=0 touches the circle $x^2+y^2=a^2$, then prove that $ig(l^2+m^2ig)a^2=n^2ig\cdot$

32. Find the equation of the circle which passes through the origin and cut off equal chords of $\sqrt{2}$ units from the lines y = xandy = -x.



33. Prove that the locus of a point which moves such that the sum of the square of its distances from the vertices of a triangle is constant is a circle having centre at the centroid of the triangle.



35. A dip circle is at right angles to the magnetic meridian. What will be

the apparent dip ?

Watch Video Solution 36. Find the equation to the circle which passes through the points (1, 2)(2, 2) and whose radius is 1. Watch Video Solution 37. Find the equation of the circle, the coordinates of the end points of whose diameter are (-1,2) and (4, -3). Watch Video Solution

38. If the circles $x^2 + y^2 + 2ax + c = 0$ and $x^2 + y^2 + 2by + c = 0$ touch each other, then $(a)\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{c}$ (b) $\frac{1}{a^2} + \frac{1}{b^2} = \frac{1}{c^2}$ (c) a + b = 2c (d) $\frac{1}{a} + \frac{1}{b} = \frac{2}{c}$

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39. Find the equation of the circle which passes through the points (1, -2), (4, -3) and whose center lies on the line 3x + 4y = 7.

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40. The equation of the circle which touches the axes of coordinates and the line $\frac{x}{3} + \frac{y}{4} + = 1$ and whose centres lie in the first quadrant is $x^2 + y^2 - 2cx - 2cy + c^2 = 0$, where *c* is equal to 4 (b) 2 (c) 3 (d) 6

41. Find the equation of the circle which passes through the points (2, 3)(4, 2) and the centre lies on the straight line y - 4x + 3 = 0.



42. The number of integral values of λ for which the equation $x^2 + y^2 + \lambda x + (1 - \lambda)y + 5 = 0$ is the equation fo a circle whose radius cannot exceed 5, is (a) 14 (b) 18 (c) 16 (d) none of these

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43. Find the equation of the circle which touches the lines 4x - 3y + 10 = 0 and 4x - 3y - 30 = 0 and whose centre lies on the line 2x + y = 0.



44. If the line $y = \sqrt{3}x + k$ touches the circle $x^2 + y^2 = 16$, then find

the value of k.



$$3x + y = 14$$
 and $2x + 5y = 18$.

46. Find the locus of the centre of the circle touching the line x + 2y = 0 and x = 2y



47. Let C be any circle with centre $(0, \sqrt{2})$. Prove that at most two rational points can be there on C. (A rational point is a point both of whose coordinates are rational numbers)

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48. Find the equation of the circle which touches x-axis and whose centre is (1,2).



49. Find the equation of the circle which passes through the origin and cuts off intercepts 3and4 from the positive parts of the axes respectively.



50. Find the equation of the circle whose centre is at (3, -1) and which cuts off a chord of length 6units on the line 2x - 5y + 18 = 0.

51. A rectangle ABCD is inscribed in a circle with a diameter lying along the line 3y = x + 10. If A and B are the points (-6,7)and(4,7) respectively, find the area of the rectangle and equation of the circle.

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52. Find the equation of a circle with origin as centre and which circumscribes an equilateral triangle whose median is of length 3a



53. Find the equation of a circle whose diameters are 2x - 3y + 12andx + 4y - 5 = 0 and area is 154squareunits.



56. Find the equation of the circle is (2, -3) and radius is 8.



57. Find the equation of the circle which passes through the point of intersection of the lines 3x - 2y - 1 = 0 and 4x + y - 27 = 0 and whose centre (2, -3).

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58. Find the equation of the circle having centre at (3, -4) and touching the line 5x + 12y - 12 = 0.

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59. Find the center and radius of the circle given by the equation

$$2x^2+2y^2+3x+4y+rac{9}{8}=0.$$

60. If the line 2x - y + 1 = 0 touches the circle at the point (2, 5) and the centre of the circle lies in the line x + y - 9 = 0. Find the equation of the circle.



63. If the equations of the two diameters of a circle are x - y = 5 and 2x + y = 4 and the radius of the circle is 5, find the equation of the circle.

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64. Find the equation of the circle which passes through two points on

the x-axis which are at distances 4 from the origin and whose radius is

5.



65. A circle of radius 6 units touches the coordinates axes in the first quadrant. Find the equation of its image in the line mirror y = 0.





69. Find the equation of the circle with: centre (a, b) and radius

$$\sqrt{a^2+b^2}$$
 .



72. Find the equation of the circle with: Centre (a,a) and radius $\sqrt{2}a$.



73. Find the centre and radius of each of the following circle: $(x-1)^2 + y^2 = 4$

74. Find the centre and radius of each of the following circle: $(x+5)^2 + (y+1)^2 = 9$

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75. Find the centre and radius of each of the following circle:

$$x^2 + y^2 - 4x + 6y = 5$$



77. Find the equation of the circle whose centre is (1,2) and which passes through the point (4,6).

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78. Find the equation of the circle passing through the point of intersection of the lines x + 3y = 0 and 2x - 7y = 0 and whose centre is the point of intersection of the lines x + y + 1 = 0 and x - 2y + 4 = 0.

79. Find the equation of the circle whose centre lies on the positive direction of y-axis at as distance 6 from the origin and whose radius is 4.



80. Find the equation of a circle: 1)Which touches both the axes at a distance of 6 units from the origin. 2)Which touches x-axis at a distance 5 from the origin and radius 6 units 3)Which touches both the origin, radius 17 and ordinate of the centre is -15.

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81. If the equations of two diameters of a circles are x + y = 6 and x + 2y = 4 and the radius is 10, find the equation of the circle.

82. Find the equation of the circle which has its centre at the point (3,4)

and touches the straight line 5x + 12y - 1 = 0.

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83. Find the equation of the circle which touches the coordinate axes

and whose centre lies on the line x-2y = 3.

84. A circle whose centre is the point of intersection of the lines 2x - 3y + 4 = 0 and 3x + 4y - 5 = 0 passes through the origin. Find its equation.

85. A circle of radius 4 units touches the coordinate axes in the first quadrant. Find the equation of its images with respect to the line mirrors x = 0 and y = 0.



87. Find the equations of the circles passing through two points on y-

axis at distance 3 from the origin and having radius 5.



88. If the lines 3x - 4y - 7 = 0 and 2x - 3y - 5 = 0 are two diameters of a circle of area 49π square units, the equation of the circle is:

89. The circle $x^2 + y^2 - 2x - 2y + 1 = 0$ is rolled along the positive direction of x-axis and makes one complete roll. Find its equation in new position.

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90. One of the diameters of the circle circumscribing the rectangle ABCD is 4y = x + y. If A and B are the points (-3, 4) and (5, 4) respectively, find the area of the rectangle and equation of the circle.

91. Find the centre of a circle passing through (5,-8), (2,-9) and (2,1)



93. Find the coordinates of the centre and radius of each of the following circle: $x^2 + y^2 + 6x - 8y - 24 = 0$

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94. Find the coordinates of the centre and radius of each of the following circle: $2x^2 + 2y^2 - 3x + 5y = 7$

95. Find the coordinates of the centre and radius of each of the following circle: $\frac{1}{2}(x^2+y^2)+x\cos\theta+y\sin\theta-4=0$

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96. Find the coordinates of the centre and radius of each of the

following circle: $x^2 + y^2 - ax - by = 0$

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97. Find the equation of the circle passing through the point: (5,1), (8, 1)

and (1,3)



98. Find the equation of the circle passing through the point: (1, 2),

$$(3, -4)$$
 and $(5, -6)$.



99. Find the equation of the circle passing through the point: (5, -8), (-2, 9) and (2, 1)

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101. Find the equation of the circle which passes through the points (3,

-2), (-2, 0) and has its centre on the line 2x - y = 3.



102. Find the equation of the circle which passes through the points

(3,7), (5,5) and has its centre on the line x - 4y = 1.

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103. Show that the points (3,-2), (1,0), (-1, -2) and (1,-4) are con-cyclic.

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104. Show that the points A(5,5), B(6,4), C(-2,4) and D(7,1) all

lies on the circle. Find the centre, radius and equation of circle.

105. Find the equation of the circle which circumscribes the triangle formed by the line: x + y + 3 = 0, x - y + 1 = 0 and x = 3



106. Find the equation of the circle which circumscribes the triangleformedbytheline:

 $2x+y-3=0,\;x+y-1=0\;and\;3x+2y-5=0$

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107. Prove that the centres of the three circles
$$(x^2+y^2-4x-6y-12=0)$$
 , $(x^2+y^2+2x+4y-5=0)$ and $(x^2+y^2-10x-16y+7=0)$ are collinear.

108. Find the equation of the circle which circumscribes the triangle formed by the line: x + y = 2, 3x - 4y = 6 and x - y = 0.



109. Find the equation of the circle which circumscribes the triangle formed by the line: y = x + 2, 3y = 4x and 2y = 3x

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110. Find the equation of the circle which passes through the origin and cuts off chords of lengths 4 and 6 on the positive side of the x-axis and y-axis respectively.







112. If a circle passes through the point (0, 0), (a, 0)and(0, b), then find its center.

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113. Find the equations of the circles drawn on the diagonals of the

rectangle as its diameter whose sides are x = 5, x = -2, y = 3 and y = -1.



114. Find the equation of the circle, the end points of whose diameter are (2,-3) and (-2,4). Find the centre and radius.



115. Find the equation of the circle the end points of whose diameters are the centres of the circles $x^2 + y^2 + 16x - 14y = 1$ and $x^2 + y^2 - 4x + 10y = 2$

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116. The sides of a square are x = 6, x = 9, y = 3 and y = 6. Find the equation of a circle drawn on the diagonal of the square as its diameter.



117. Find the equation of the circle circumscribing the rectangle whose sides are x - 3y = 4, 3x + y = 32, x - 3y = 14 and 3x + y = 62.



118. Find the equation of the circle passing through the origin and the

points where the line 3x + 4y = 12 meets the axes of coordinates.

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119. Find the equation of the circle which passes through the origin and

cuts off intercepts a and b respectively from x and y - axes.



120. Find the equation of the circle whose diameter is the line segment

joining (-4,3) and (12,-1). Find also the intercept made by it on y-axis.

121. The abscissa of the two points A and B are the roots of the equation $x^2 + 2ax - b^2 = 0$ and their ordinates are the roots of the equation $x^2 + 2px - q^2 = 0$. Find the equation of the circle with AB as diameter. Also, find its radius.

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122. ABCD is a square in first quadrant whose side is a, taking AB and AD as axes, prove that the equation to the circle circumscribing the square is $x^2 + y^2 = a(x + y)$.

123. The line 2x - y + 6 = 0 meets the circle $x^2 + y^2 - 2y - 9 = 0$ at

A and B. Find the equation of the circle on AB as diameter.



126. Write the coordinates of the centre of the circle passing through

(0,0), (4,0) and (0,-6).



129. Write the equation of the unit circle concentric with $x^2+y^2-8x+4y-8=0.$



130. Find the number of integral values of λ for which $x^2+y^2+\lambda x+(1-\lambda)y+5=0$ is the equation of a circle whose

radius does not exceed 5.



131. Write the equation of the circle passing through (3,4) and touching

y-axis at the origin.



132. If the line y=mx does not intersect the circle $(x+10)^2+(y+10)^2=180$ then write the set of values of taken by $m\cdot$

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133. Write the coordinates of the center of the circle inscribed in the

square formed by the lines x = 2, x = 6, y = 5 and y = 9.

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134. The equation $x^2 + y^2 + 2x - 4y + 5 = 0$ represents a. a point b.

a pair of straight lines c. a circle of non zero radius d. none of these

135. If the equation $(4a - 3)x^2 + ay^2 + 6x - 2y + 2 = 0$ represents a circle, then its centre is a. (3,-1) b. (3,1) c. (-3,1) d. none of these

136. The equation of the circle passing through the point (1, 1) and having two diameters along the pair of lines $x^2 - y^2 - 2x + 4y - 3 = 0$ is $a \cdot x^2 + y^2 - 2x - 4y + 4 = 0$ b. $x^2 + y^2 + 2x + 4y - 4 = 0$ c. $x^2 + y^2 - 2x + 4y + 4 = 0$ d. none of these

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137. If the centroid of an equilateral triangle is (1,1) and its one vertex is (-1, 2), then the equation of its circumcircle is: is $x^2 + y^2 - 2x - 2y - 3 = 0$ b. $x^2 + y^2 + 2x - 2y - 3 = 0$ c. $x^2 + y^2 + 2x + 2y - 3 = 0$ d. none of these



the line 4x+3y=6 is

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139. The equation of a circle with radius 5 and touching both the

coordinateaxesis $x^2 + y^2 \pm 10x \pm 10y + 5 = 0$ $x^2 + y^2 \pm 10x \pm 10y = 0$ $x^2 + y^2 \pm 10x \pm 10y + 25 = 0$

$$x^2 + y^2 \pm 10x \pm 10y + 51 = 0$$

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140. The equation of the circle passing through the origin which cuts of intercept of length 6 and 8 from the axes is a.



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141. The area of an equilateral triangle inscribed in the circle $x^2 + y^2 - 6x - 8y - 25 = 0$ is a. $\frac{225\sqrt{3}}{6}$ b. 25π c. $50\pi - 100$ d. none

of these

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142. If the circles $x^2 + y^2 = a \ and \ x^2 + y^2 - 6x - 8y + 9 = 0$ touch

externally then $a=\,$ a. 1 b. -1 c. 21 d. 16

143. If (x, 3) and (3, 5) are the extremities of a diameter of a circle with centre at (2, y) then the values of x and y are a. (3,1) b. x = 4, y = 1 c. x = 8, y = 2 d. none of these

144. Equation of the diameter of the circle $x^2 + y^2 - 2x + 4y = 0$ which passes through the origin is a.x+2y=0 b.x-2y=0 c. 2x + y = 0d. 2x-y=0.

145. Equation of the circle through origin which cuts intercepts of
length
$$a$$
 and b on axes is a. $x^2 + y^2 = ax + by = 0$ b.
 $x^2 + y^2 - ax - by = 0$ c. $x^2 + y^2 + bx + ay = 0$ d. none of these

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