



# MATHS

# **BOOKS - RD SHARMA MATHS (ENGLISH)**

# **APPLICATION OF INTEGRALS**

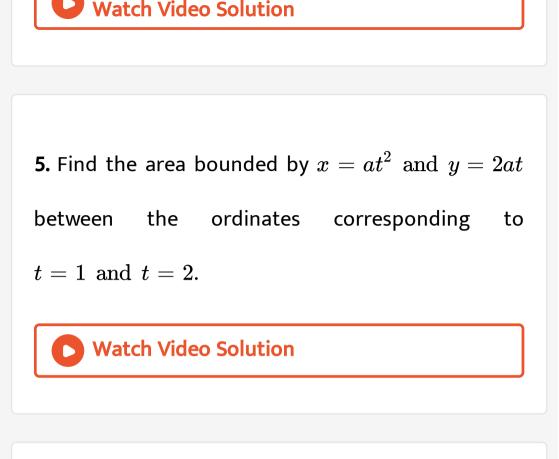


**1.** Find the area enclosed by the curve  $y = -x^2$ 

and straight line x + y + 2 = 0.

2. Find the area of the region bounded by the curve  $y=x^2$  and the line y=4 . Watch Video Solution 3. Find the area bounded by the curve  $y^2 = 4a^2(x-1)$  and the lines x = 1andy = 4a. Watch Video Solution

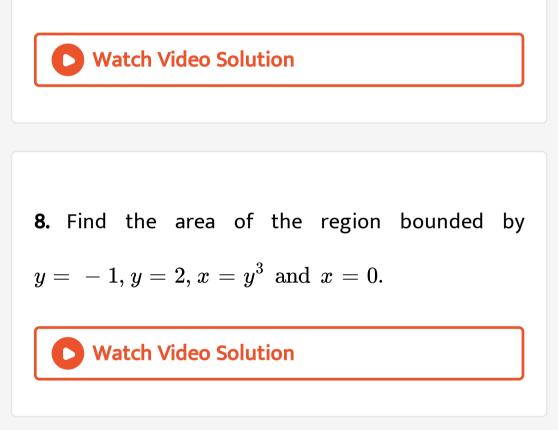
**4.** Find the area of the smaller part of the circle  $x^2 + y^2 = a^2$  cut off by the line  $x = \frac{a}{\sqrt{2}}$ 



- 6. Find the area enclosed by the curve
- $x = 3\cos t, y = 2\sin t$

7. Sketch the region lying in the first quadrant and bounded by  $y = 9x^2, x = 0, y = 1$ andy = 4. Find

the area of the region using integration.



**9.** Find the area of region bounded by  $x^2 + 16y = 0$ 

and its latusrectum.



10. Find the area of region bounded by the curve

 $ay^2=x^3,$  the y-axis and the lines  $y=a ext{ and } y=2a.$ 

11. Find the area of the region included between the

parabolas  $y^2 = 4axandx^2 = 4ay, wherea > 0.$ 

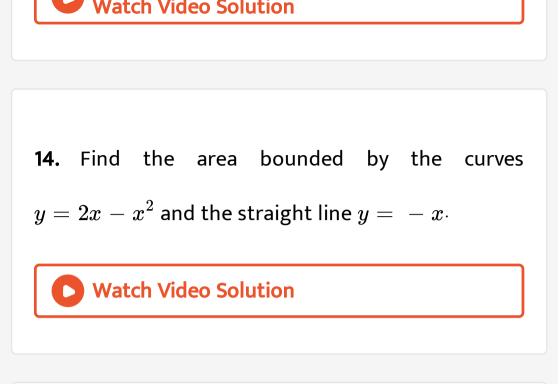
## Watch Video Solution

12. Find the area of the region bounded by the curve

 $y = x^3$  and the lines y = x + 6 and y =0.

### Watch Video Solution

13. Find the area bounded by the curves  $y = xandy = x^3$ .



15. Find the area of the region between the parabola

$$x=y^2-6y$$
 and the line  $x=\,-y$ 

16. Find the area of the region bounded by the parabola  $y = x^2$  and y = |x|.

## Watch Video Solution

17. Determine the area under the curve $y = \sqrt{a^2 - x^2}$  included between the lines

$$x = 0$$
and $x = a$ .

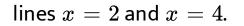
18. Find the area of the region bounded by the parabola  $y^2 = 2x$  and straight line x - y = 4.

## Watch Video Solution

**19.** Find the area of the region bounded by the curves  $y = x^3$  and the lines y = x + 6 and y = 0.

### Watch Video Solution

20. Using integration, find the area of the region bounded by the line 2y = -x + 8,x-axis is and the





21. If the area above x-axis bounded by the curves  $y=2^{kx}andx=0 ext{ and } x=2israc{3}{(\log)_e2}, ext{ then find}$ 

the value of  $k \cdot$ 

Watch Video Solution

**22.** Sketch the region bounded by  $y = 2x - x^2$  and

x-axis and find its area using integration.

**23.** Using integration, find the area of the region bounded by the line y - 1 = x, thex-a xi s and the ordinates x=-2 and x=3.

Watch Video Solution

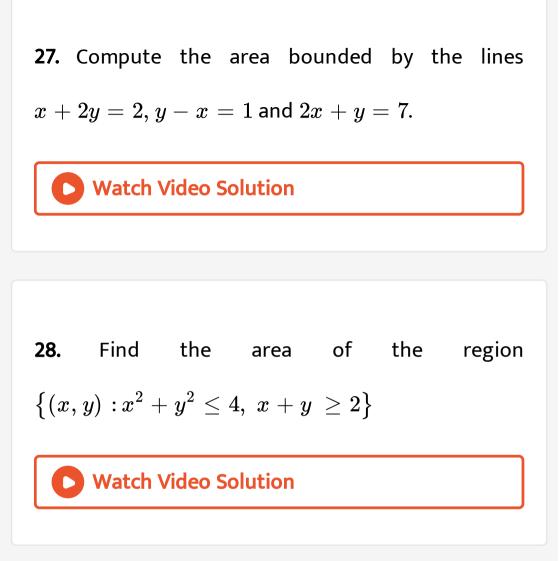
24. Find the area bounded by the curve y = (x - 1)(x - 2)(x - 3) lying between the

ordinates x = 0 and x = 3.

25. Find the area bounded by the curve  $y = \sin x between x = 0 and x = 2\pi dx$ Watch Video Solution **26.** Sketh the graph y = |x + 1|. Evaluate  $\int_{-3}^{1} |x+1| dx.$  What does this value represent on

the graph?





**29.** Using integration, find the area of the region bounded by the following curves after making a

rough

sketch:

$$y=1+|x+1|, x=-2, x=3, y=0.$$

### Watch Video Solution

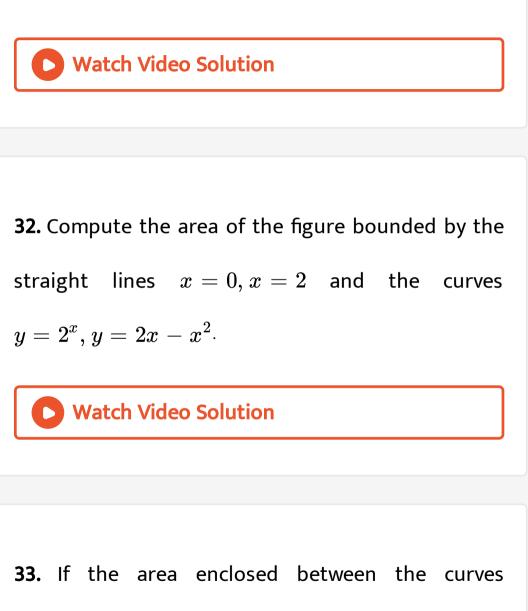
**30.** Draw a rough sketch of the curves  $y = \sin x$  varies from 0 to  $\frac{\pi}{2}$  and find the area of the region enclosed by them and x-axis

# Watch Video Solution

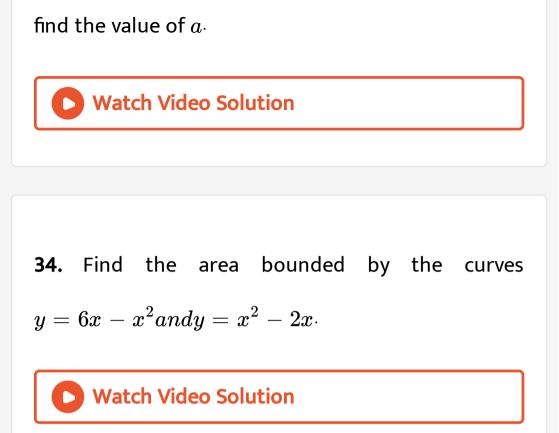
**31.** Sketch the curves and identify the region bounded by the curves

$$x=rac{1}{2}, x=2, y=\log xany=2^x$$
 . Find the area of

this region.

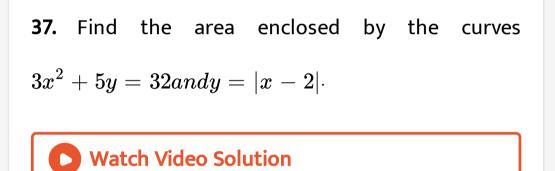


 $y = ax^2 andx = ay^2(a>0)$  is 1 square unit, then



**35.** Find the area of the region bounded by  $y = \sqrt{x} andy = x$ .

**36.** Calculate the area of the region bounded by the parabolas  $y^2 = 6xandx^2 = 6y$ .



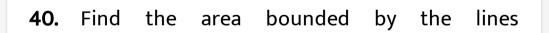
**38.** If the area bounded by the parabola  $y^2 = 4ax$ and the line y=mx is  $\frac{a^2}{12}$  sq. units, by using integration find the value of m.



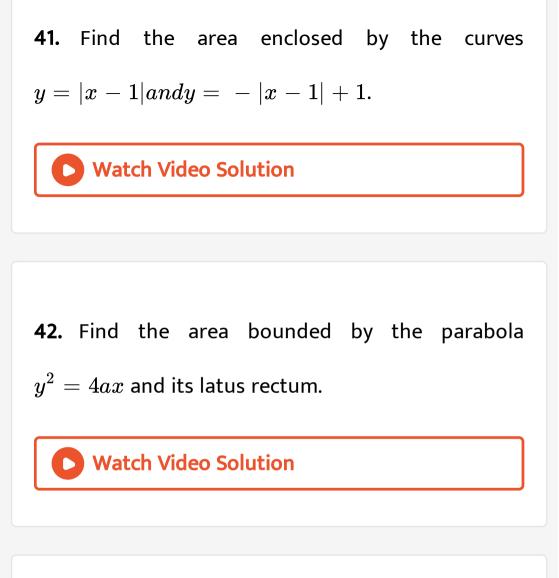
**39.** If the area enclosed by the parabolas  $y^2 = 16axandx^2 = 16ay, a > 0israc{1024}{3}sq$  units,

find the value of a.





$$y = 4x + 5, y = 5 - xand4y = x + 5.$$



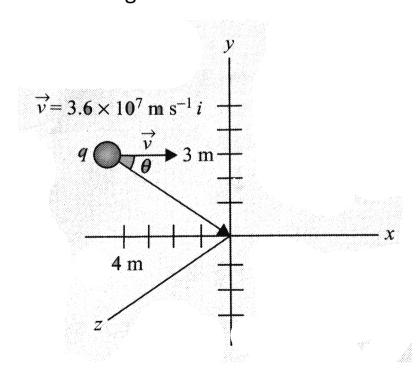
**43.** Find the area of the region bounded by the parabola  $y^2 = 2x$  and straight line x - y = 4.

44. Find the area of the region bounded by the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ 



**45.** Draw a rough sketch of the curve  $y = \cos^2 x$  in [0, 1] and find the area enclosed by the curve,the lines  $x = 0, x = \pi$  and the x-axis.

**46.** A point change of magnitude q = 4.5nC is moving with speed  $v = 3.6 \times 10^7 m s^{-1}$  parallel to the x-axis along the line y = 3m. Find the magnetic field at the origin produced by this charge when the charge is at the point x = -4m, y = 3m, as shown in Fig.





**47.** Using the integration, find the area of he region bounded by the following curves, after making a rough sketch:

 $y=1+|x+1|,\;x=\;-3,\;x=3,\;y=0.$ 

Watch Video Solution

**48.** Using integration, find the area of the triangle formed by positive x-axis and tangent and normal to the circle  $x^2 + y^2 = 4$  at  $(1, \sqrt{3})$ .

**49.** Using the method of integration find the area

bounded by the curve |x| + |y| = 1.

Watch Video Solution

50. Find the integration, find the area of the region bounded between the line x=2 and the parabola  $y^2=8x$ .

51. Find the area of the region bounded parabola

$$y^2=4ax$$
 and the line  $x=a_{\cdot}$ 

## Watch Video Solution

52. Find the area lying above the x-axis and under

the parabola  $y=4x-x^2$ 

#### Watch Video Solution

53. Draw a rough sketch to indicate the region bounded between the curve  $y^2 = 4ax$  and the line

x = 3. also, find the area of this region.

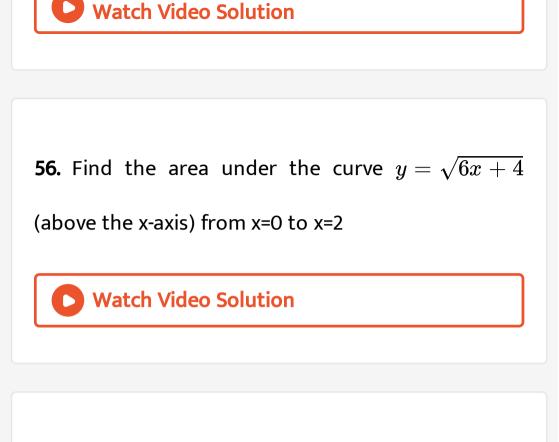
## Watch Video Solution

54. Make a rough sketch of the graph of the function  $y = 4 - x^2$ ,  $0 \le x \le 2$  and determine the area enclosed by the curve, the x-axis and the lines x = 0 and x = 2.

Watch Video Solution

55. Using integration, find the area bounded by the

lines x+2y=2, y-x=1 and 2x+y=7



57. Draw the rough sketch of  $y^2+1=x, \ x\leq 2.$ 

Find the area enclosed by the curve and the line

x = 2.

**58.** Draw a rough sketch of the graph of the curve  $\frac{x^2}{4} + \frac{y^2}{9} = 1$  and evaluate the area of the region

under the curve and above the x-axis.



**59.** Sketch the region  $|(x, y): 9x^2 + 4y^2 = 36|$  and find the area of the region enclosed by it using integration.



60. Draw rough sketch of the graph of the function  $y=2\,\sqrt{1-x^2}\,,\;x\in[0,1]$  and evaluate the area enclosed between the curve and the x-axis.

Watch Video Solution

**61.** Using integration, find the area of the region bounded by the line 2y = 5x + 7, x-axis and the lines x = 2 and x = 8.

62. Sketch the graph of y = |x - 5|. Evaluate  $\int_0^1 |x - 5| dx$ . What does this value of the integral

represent on the graph.

Watch Video Solution

**63.** Sketch the graph of y=|x+3|. Evaluate  $\int_{-6}^{0} |x+3| dx$ . What does the value of this integral

represent?

64. Sketch the graph y = |x+1|. Evaluate $\int_{-4}^{2} |x+1| dx$ . What does the value of this integral

represent on the graph?



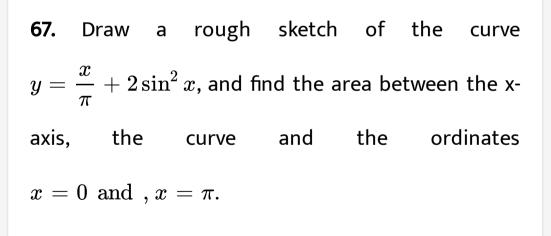
65. The area of the region bounded by the curve y =

x + 1 and the lines x = 2, x = 3, is



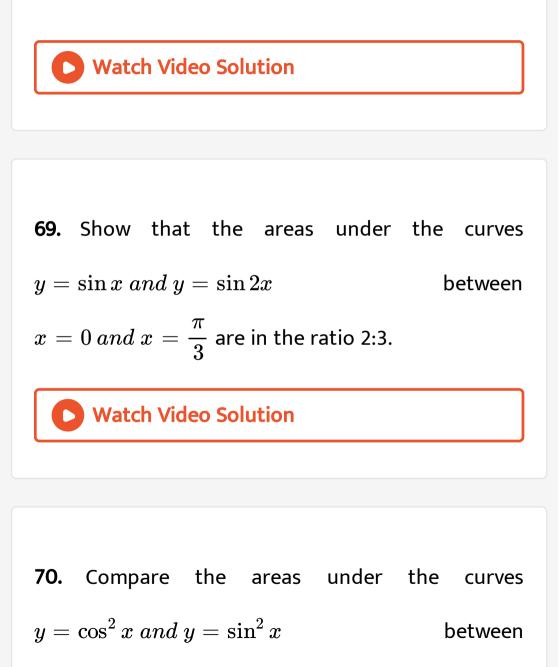
**66.** Draw a rough sketch of the curve  $y = \frac{x}{\pi} + 2\sin^2 x$  and find the area between the x-axis, the curve and the ordinates x = 0 and  $x = \pi$ .

Watch Video Solution



**68.** Find the area bounded by the curve  $y = \cos x$ ,

x-axis and the ordinates x=0 and  $x=2\pi$ .



$$x=0$$
 and  $x=\pi\cdot$ 



71. Find the area bounded by the ellipse  $rac{x^2}{a^2}+rac{y^2}{b^2}=1$  and the ordinates x=0 and x=ae, where,  $b^2=a^2ig(1-e^2ig)$  and e<1.

#### Watch Video Solution

72. Examples: Find the area of the region bounded

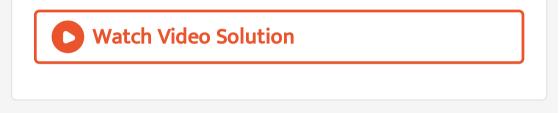
by the curve  $y^2 = 2y - x$  and the y-axis.

73. Find the area bounded by the curve  $y^2 = 4ax$ and the lines y = 2 and y-axis.

Watch Video Solution

74. Find the area of the region lying in the first quadrant and bounded by  $y = 4x^2$ , x = 0, y = 1 and y = 4.

75. Find the area of the region bounded by  $x^2 = 16y, \ y = 1, \ y = 4$  and the y-axis in the first quadrant.



**76.** Find the area of the region bounded by  $x^2 = 4ay$  and its latus rectum.



77. Find the area enclosed between the parabola  $4y = 3x^2$  and the straight line 3x - 2y + 12 = 0Watch Video Solution

**78.** Find the area bounded by the curve  $x^2 = 4y$  and

the straight line x = 4y - 2.

## Watch Video Solution

79. Find the area enclosed between the parabola

$$y^2=4ax$$
and the line  $y=mx_{
m e}$ 



80. Find the area of the region bounded by the

curves 
$$y=x^2+2, y=x, x=0, and x=3.$$

Watch Video Solution

**81.** Find the area of the region bounded by 
$$y = \sqrt{x} andy = x$$
.

82. Find the area of the region  $ig\{(x,y)\!:\!x^2\leq y\leq |x|ig\}$  . Watch Video Solution **83.** Evaluate  $\int \cos 2x + e^x dx$ Watch Video Solution

84. Find the area of the smaller region bounded by

the ellipse 
$$\displaystyle rac{x^2}{a^2} + \displaystyle rac{y^2}{b^2} = 1$$
and the line  $\displaystyle rac{x}{a} + \displaystyle rac{y}{b} = 1$ 

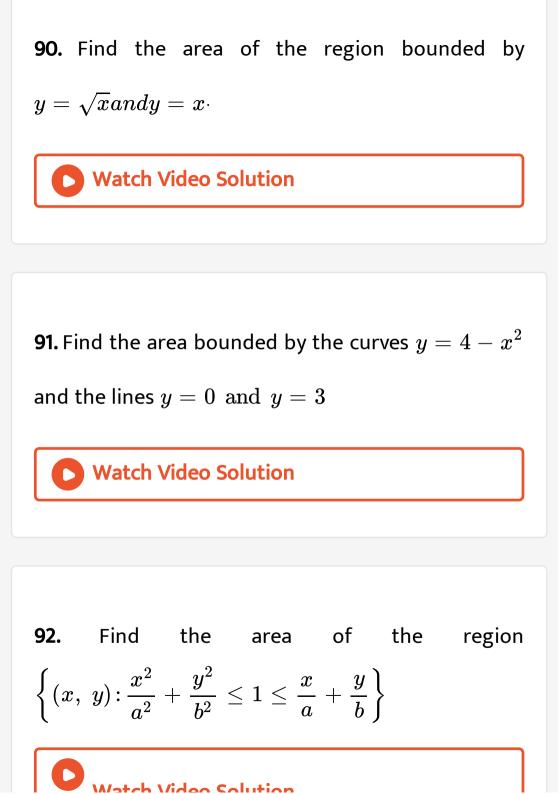
# 85. Find the area of the region $\{(x,y): x^2+y^2 \le 1 \le x+y\}$ . Watch Video Solution **86.** Find $\frac{dy}{dx}$ if $y = \sin^2 x$ Watch Video Solution

**87.** Find the area of the region enclosed between the two circles  $x^2 + y^2 = 1$  and  $\left(x - 1
ight)^2 + y^2 = 1$ 

**88.** Prove that the curves  $y^2 = 4x$  and  $x^2 = 4y$  divide the area of square bounded by x = 0, x = 4, y = 4 and y = 0 into three equal parts.

Watch Video Solution

89. Find the area bounded by the curve $4y^2=9x ext{ and } 3x^2=16y$ 



**93.** Using integration, find the area of the region bounded by the triangle whose vertices are (2,1), (3, 4) and (5,2).



**94.** Using integration, find the area of the triangle ABC whose vertices are A(-1, 1), B(0, 5) and C(3, 2).



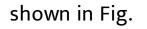
95. Using integration find the area of the triangular

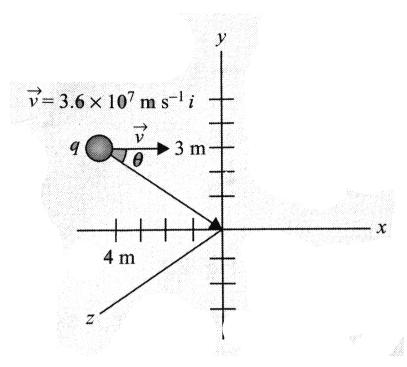
region whose sides have equations

 $y = 2x + 1, \ y = 3x + 1$  and x = 4

# Watch Video Solution

**96.** A point change of magnitude q = 4.5nC is moving with speed  $v = 3.6 \times 10^7 m s^{-1}$  parallel to the x-axis along the line y = 3m. Find the magnetic field at the origin produced by this charge when the charge is at the point x = -4m, y = 3m, as





# Watch Video Solution

97. Find 
$$rac{dy}{dx}$$
 if  $y = \log x + \sin x$ 

**98.** Find 
$$\displaystyle rac{dy}{dx}$$
 if  $x^2+y^2=16$ 

# Watch Video Solution

**99.** Find the area of the region included between the parabola  $y^2 = x$  and the line x + y = 2 .

# Watch Video Solution

100. Draw a rough sketch of the region  $ig\{(x,y)\!:\!y^2\leq 3x,\,3x^2+3y^2\leq 16ig\}$  and find the

area enclosed by the region using the method of

integration



101. Draw a rough sketch of the region  $\{(x,y): y^2 \le 5x, \ 5x^2 + 5y^2 \le 36\}$  and find the area enclosed by the region using method of integration



**102.** Draw a rough sketch and find the area of the region bounded by the parabolas  $y^2 = 4x$  and  $x^2 = 4y$ , using the method of integration.



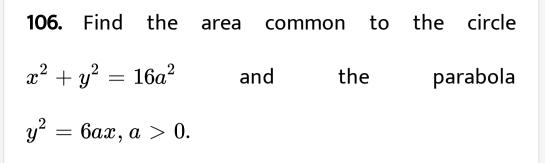
103. Find the area included between the parabolas

$$y^2=4ax \ and \ x^2=4by$$
.

104. Find the area of the region in the first quadrant enclosed by x-axis, line  $x = \sqrt{3}y$ and the circle $x^2 + y^2 = 4$ .

Watch Video Solution

105. Find the area of the region bounded by  $y=\sqrt{x},\;x=2y+3$  in the first quadrant and x-axis.



Watch Video Solution

107. Find the area, lying above the x=axis and included between the circle  $x^2 + y^2 = 8x$  and the parabola  $y^2 = 4x$ .

**108.** Find the area enclosed by the parabolas  $y = 5x^2 and \ y = 2x^2 + 9.$ 

# Watch Video Solution

109. The area common to the parabolas  $y = 2x^2$ and  $y = x^2 + 4$  (in square units) is (A)  $\frac{2}{3}$  (B)  $\frac{3}{2}$  (C)  $\frac{32}{3}$  (D)  $\frac{3}{32}$ 



**110.** Using integration, find the area of the region bounded by the triangle whose vertices are (-1, 2), (1, 5) and (3, 4).

Watch Video Solution

111. Find the area of the region in the first quadrant enclosed by x-axis, the line  $y = \sqrt{3} x$  and the circle  $x^2 + y^2 = 16$ 

**112.** Find the area of the region bounded by parabola  $y^2 = 2x + 1$  and the line x - y - 1 = 0.

# Watch Video Solution

113. Find the area of the region bounded by the

curves 
$$y = x - 1$$
 &  $\left(y - 1
ight)^2 = 4(x + 1).$ 

#### Watch Video Solution

114. Find the area bounded by the parabola  $y = 2 - x^2$  and the straight line y + x = 0.



115. Using the method of integration, find the area of the region bounded by the following lines 3x - y - 3 = 0, 2x + y - 12 = 0, x - 2y - 1 = 0.



**116.** Sketch the region bounded by the curves  $y = x^2 + 2, \ y = x, \ x = 0 \ and \ x = 1.$  also, find

the area of this region.



117. Find the area bounded by the curves  $x = y^2$ and  $x = 3 - 2y^2$ .

**118.** Using integration, find the area of the triangle ABC, coordinates of whose vertices are A(4,1), B(6,6)

and C(8,4)



119. Find the area of the region in the first quadrant

enclosed by the y-axis, the line y = x and the circle

 $x^2 + y^2 = 32$ , using integration.



**120.** Find the area of the circle  $x^2 + y^2 = 16$  exterior to the parabola  $y^2 = 6x$ .

Watch Video Solution

**121.** Find the area of the region enclosed by the parabola  $x^2 = y$ , the line y = x + 2 and the X-axis.

122. Make a rough sketch of the region given below and find its area using integration  $ig\{(x,y)\!:\!0\leq y\leq x^2+3, 0\leq y\leq 2x+3, 0\leq x\leq 3ig\}$ Watch Video Solution 123. Find the area of the region  $ig\{(x,y): x^2+y^2\leq 4, \; x+y \; \geq 2ig\}$ 

**124.** Using integration, find the area of the following region:  $\left\{ (x, y) : \frac{x^2}{9} + \frac{y^2}{4} \le 1 \le \frac{x}{3} + \frac{y}{2} \right\}$ . Watch Video Solution

125. In what ratio does the x-axis divide the area of the region bounded by the parabolas  $y = 4x - x^2 andy = x^2 - x$ ?



126. In what ratio does the x-axis divide the area of the region bounded by the parabolas  $y = 4x - x^2 andy = x^2 - x$ ?

Watch Video Solution

127. Using integration, find the area bounded by the

curves 
$$y=|x-1|$$
 and  $y=3-|x|.$ 

128. Sketch the region common to the circle  $x^2 + y^2 = 16$  and the parabols  $x^2 = 6y$ . Also find the area of the region using integration.



**129.** Find the area of the region between the parabola  $x = 4y - y^2$  and the line x = 2y - 3.



130. Find the area bounded by the parabola $x=8+2y-y^2;$  the y-axis and the lines y=-1and y=3.

Watch Video Solution

**131.** The area bounded by the parabolay  $y^2 = 4x$ and the line y = 2x - 4 on the *Y*-axis.



132. If the area above x-axis bounded by the curves  $y=2^{kx}andx=0 ext{ and } x=2israc{3}{(\log)_e2}, ext{ then find}$ 

the value of k.



**133.** Find the area included between the curves  $x^2 = 4y$  and  $y^2 = 4x$ .

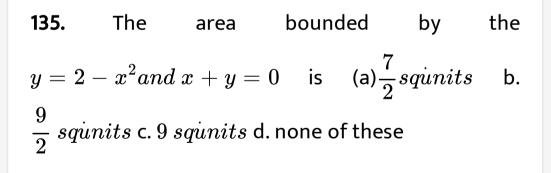


**134.** The area bounded by the curve  $y = \log_e x$ , the

x-axis and the line x = e is (A) e sq. units (B) 1 sq.

unit (C) 
$$\left(1-rac{1}{e}
ight)$$
 sq. units (D)  $\left(1+rac{1}{e}
ight)$  sq. units

Watch Video Solution



**136.** The area bounded by the parabola  $x = 4 - y^2$ and y-axis, in square units, is  $\frac{3}{32}$  b.  $\frac{32}{3}$  c.  $\frac{33}{2}$  d.  $\frac{16}{3}$ 

# Watch Video Solution

137. If  $A_n$  be the area bounded by the curve  $y=(\tan x)^n$  and the lines  $x=0,\;y=0,\;x=\pi/4$  , then for n>2.



**138.** The area enclosed between the curves 
$$y = (\log)_e(x+e), x = (\log)_e\left(rac{1}{y}
ight)$$
, and the x-axis

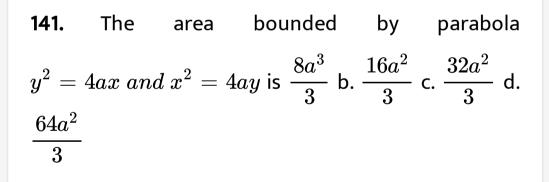
is 2squalts (b) 1squalts 4squalts (d) none of these

Watch Video Solution

**139.** The area of the figure bounded by the parabola  $(y-2)^2 = x - 1$ , the tangent to it at the point with the ordinate x = 3, and the  $x - a\xi s$  is 7squnites (b) 6squnites 9squnites (d) None of these

**140.** The area bounded by the curves  $y = \sin x$ between the ordinates x = 0,  $x = \pi$  and the x-axis is 2 squares b. 4 squares c. 3 squares d. 1 squares





142. The area bounded by the curve  $y = x^4 - 2x^3 + x^2 + 3$  with x-axis and ordinates corresponding to the minima of y, is

Watch Video Solution

**143.** The area bounded by the parabola  $y^2 = 4ax$ , the latusrectum and x-axis is 0 b.  $\frac{4}{3}a^2$  c.  $\frac{2}{3}a^2$  d.  $\frac{a^2}{3}$ 

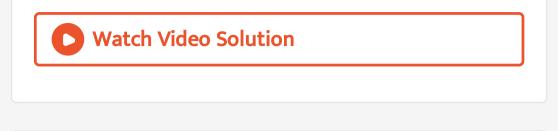
144. Find the area of the region  $\{(x, y): x^2 + y^2 \le 1 \le x + y\}$ .

Watch Video Solution

**145.** The area common to the parabola  $y=2x^2$  and

$$y = x^2 + 4$$
 is:

A. (a)  $\frac{2}{3}u^2$ B. (b)  $\frac{3}{2}u^2$ C. (c)  $\frac{32}{3}u^2$ D. (d)  $\frac{3}{32}u^2$ 



146. Find the area bounded by the parabola  $y = x^2 + 1$  and the straight line x + y = 3.



147. Find the angle between the curves  $2y^2=x^3$  and  $y^2=32x.$ 

A. (A) 1:3

B. (B) 2:1

C. (C)  $\sqrt{3}$  : 1

D. (D) none of these

#### Answer: null



**148.** Area between the x-axis and the curve  $y = \cos x$ , when  $0 \le x \le 2\pi$  is:

A. (A) 0

B. (B) 2

C. (C) 3

D. (D) 4

Answer: null



**149.** Area bounded by the parabola  $y^2 = x$  and the

line 2y = x is:

A. (A) 
$$\frac{4}{3}$$
  
B. (B) 1  
C. (C)  $\frac{2}{3}$ 

D. (D) 
$$\frac{1}{3}$$

# Watch Video Solution

**150.** The area bounded by the curve  $y = 4x - x^2$ and the *x*-axis is:

A. (a) 
$$\frac{30}{7}u^2$$
  
B. (b)  $\frac{31}{7}u^2$   
C. (c)  $\frac{32}{3}u^2$   
D. (d)  $\frac{34}{3}u^2$ 



151. The area enclosed between the curve  $y^2(2a-x)=x^3$  and the line x=2a above the x-axis is

A. (a) 
$$\pi a^2 u^2$$
  
B. (b)  $\frac{3\pi a^2}{2} u^2$   
C. (c)  $2\pi a^2 u^2$   
D. (d)  $3\pi a^2 u^2$ 



**152.** The area of the region (in square units) bounded by the curve  $x^2 = 4y$  and the line x = 2 and x-axis is:

A. (a) 1 B. (b)  $\frac{2}{3}$ C. (c)  $\frac{4}{3}$ D. (d)  $\frac{8}{3}$ 



**153.** If the area bounded by the curve y=f(x), x-axis and the ordinates x=1 and x=b is (b-1) sin(3b+4), then find f(x).

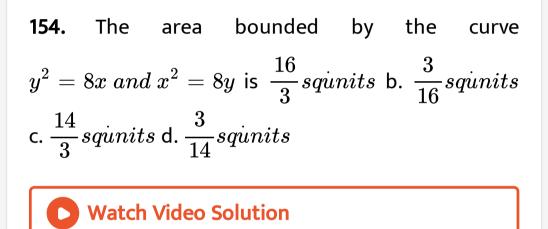
A. (a) 
$$(x-1)\cos(3x+4)$$

B. (b)  $\sin(3x + 4)$ 

C. (c)  $\sin(3x+4) + 3(x-1)\cos(3x+4)$ 

## D. (d) None of these





**155.** The area bounded by the parabola  $y^2 = 8x$ , the x-axis and the latus rectum is a. $\frac{16}{3}$  b. $\frac{23}{3}$  c. $\frac{32}{3}$  d. $\frac{16\sqrt{2}}{3}$ 



**156.** Area bounded by the curve  $y = x^3$ , the *x*-axis and the ordinates x = -2 and x = 1 is:

A. (a) 
$$-9$$
  
B. (b)  $\frac{-15}{4}$   
C. (c)  $\frac{15}{4}$   
D. (d)  $\frac{17}{4}$ 

## Answer: null

**157.** The area bounded by the curve y = x|x|, x-axis

and the ordinates x = -1 & x = 1 is:

A. (A) 
$$\frac{5}{3}$$
  
B. (B)  $\frac{4}{3}$   
C. (C)  $\frac{2}{3}$   
D. (D)  $\frac{1}{3}$ 



158. Find the area bounded by the y-axis,  $y = \cos x$  ,and  $y = \sin x$  when  $0 \le x \le rac{\pi}{2}$ .

A. (A) 
$$2ig(\sqrt{2-1}ig)$$

B. (B) 
$$\sqrt{2}-1$$

C. (C) 
$$\sqrt{2}+1$$

D. (D) 
$$\sqrt{2}$$



**159.** The area of the circle  $x^2 + y^2 = 16$  exterior to the parabola  $y^2 = 6x$  is :

A. (A) 
$$\frac{4}{3} (4\pi - \sqrt{3})$$
  
B. (B)  $\frac{4}{3} (4\pi + \sqrt{3})$   
C. (C)  $\frac{4}{3} (8\pi - \sqrt{3})$   
D. (D)  $\frac{4}{3} (8\pi + \sqrt{3})$ 



160. Smaller area enclosed by the circle  $x^2+y^2=4$ 

and the line x + y = 2 is:

A. (A) 
$$2(\pi-2)$$

- B. (B)  $\pi-2$
- C. (C)  $2\pi 1$
- D. (D)  $2(\pi + 2)$



161. Area lying between the curves  $y^2 = 4x$  and y = 2x is: A. (A)  $\frac{2}{3}$ B. (B)  $\frac{1}{3}$ C. (C)  $\frac{1}{4}$ 

Answer: null

D. (D)  $\frac{3}{4}$ 



**162.** Area lying in the first quadrant and bounded by the circle  $x^2 + y^2 = 4$  and the lines x = 0 and x = 2 is:

A. (A)  $\pi$ B. (B)  $\frac{\pi}{2}$ C. (C)  $\frac{\pi}{3}$ D. (D)  $\frac{\pi}{4}$ 

#### Answer: null

163. Area of the region bounded by the curve 
$$y^2 = 4x$$
, y-axis and the line  $y = 3$  is (A) 2  
(B)  $\frac{9}{4}$  (C)  $\frac{9}{3}$  (D)  $\frac{9}{2}$