

MATHS

BOOKS - RD SHARMA MATHS (ENGLISH)

DEFINITE INTEGRALS

Others

1. Evaluate : $\int_0^{\frac{\pi}{6}} \cos x \cos 2x dx$



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2. Evaluate : $\int_0^{\frac{\pi}{2}} \cos^3 x dx$



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3. Evaluate : $\int_0^{\frac{\pi}{4}} \sec x dx$

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4. $\int_{\pi/4}^{\pi/2} \cot x dx = ?$

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5. Evaluate : $\int_0^{\frac{\pi}{2}} (\sin x + \cos x) dx$

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6. Evaluate : $\int_{-2}^3 \frac{1}{x+7} dx$

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7. Evaluate : $\int_0^{\pi} \frac{1}{1 + \sin x} dx$

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8. Evaluate : $\int_1^4 \frac{x^2 + x}{\sqrt{2x + 1}} dx$

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9. Evaluate : $\int_0^1 x(1 - x)^5 dx$

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10. Evaluate : $\int_1^2 \left(\frac{x - 1}{x^2} \right) e^x dx$

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11. Evaluate : $\int_0^1 \sqrt{x(1-x)} dx$

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12. Evaluate : $\int_0^2 \frac{1}{\sqrt{3+2x-x^2}} dx$

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13. Evaluate : $\int_0^{\frac{\pi}{4}} (\tan x + \cot x)^{-2} dx$

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14. Evaluate : $\int_0^1 \left(xe^{2x} + \sin\left(\frac{\pi x}{2}\right) \right) dx$

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15. Evaluate : $\int_0^1 \frac{1}{1 + 2x + 2x^2 + 2x^3 + x^4} dx$

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16. Evaluate : $\int_0^1 x \log(1 + 2x) dx$

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17. Evaluate : $\int_2^3 \frac{x}{x^2 + 1} dx$

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18. Evaluate : $\int_0^\infty e^{-x} dx$

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19. Evaluate : $\int_0^{\frac{\pi}{2}} x^2 \sin x dx$

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20. Evaluate : $\int_4^9 \frac{1}{\sqrt{x}} dx$

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21. Evaluate : $\int_0^{\frac{\pi}{2}} \sqrt{1 + \sin x} dx$

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22. Evaluate : $\int_0^{\frac{1}{2}} \frac{1}{\sqrt{1-x^2}} dx$

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23. Evaluate : $\int_0^1 \frac{1}{1+x^2} dx$

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24. Evaluate : $\int_0^{\pi/2} (a^2 \cos^2 x + b^2 \sin^2 x) dx$

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25. Evaluate : $\int_0^{\infty} \frac{1}{a^2 + b^2 x^2} dx$

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26. Evaluate : $\int_{\frac{\pi}{3}}^{\frac{\pi}{4}} (\tan x + \cot x)^2 dx$

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27. Evaluate : $\int_1^e \frac{\log x}{x} dx$

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28. Evaluate : $\int_0^{2\pi} e^x \cos\left(\frac{\pi}{4} + \frac{x}{2}\right) dx$

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29. Evaluate : $\int_1^2 \frac{x+3}{x(x+2)} dx$

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30. Evaluate : $\int_e^{e^2} \left\{ \frac{1}{\log x} - \frac{1}{(\log x)^2} \right\} dx$

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31. If $\int_0^k \frac{1}{2 + 8x^2} dx = \frac{\pi}{16}$, find the value of k.

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32. Evaluate: $\int_{-\pi}^{\pi} \left((2x) \frac{1 + \sin x}{1 + \cos^2 x} \right) dx$

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33. Evaluate: $\int_{-1}^1 \frac{x^3 + |x| + 1}{x^2 + 2|x| + 1} dx$

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34. $\int_0^1 \log\left(\frac{1}{x} - 1\right) dx$ is equal to

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35. Evaluate: $\int_0^{\frac{\pi}{2}} \frac{\sin^2 x}{1 + \sin x \cos x} dx$

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36. Prove that: $\int_0^{\pi/2} \frac{\sin x}{\sin x - \cos x} dx = \frac{\pi}{4}$

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37. Prove that: $\int_0^{2a} f(x) dx = \int_0^{2a} f(2a - x) dx$.

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38. Evaluate: $\int_{-\pi/4}^{\pi/4} x^3 \sin^4 x dx$ (ii) $\int_a^a \sqrt{\frac{a-x}{a+x}} dx$

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39. Evaluate: $\int_{\pi/4}^{\pi/4} \frac{x + \pi/4}{2 - \cos 2x} dx$

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40. Evaluate: $\int_0^{\pi/2} \frac{\cos x}{1 + \cos x + \sin x} dx$

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41. Prove that: $\int_0^{\pi} \frac{x}{1 - \cos \alpha \sin x} dx = \frac{\pi(\pi - \alpha)}{\sin \alpha}$

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42. Evaluate the following integrals: (1-35) $\int_{-a}^a \log \left(\frac{a - \sin \theta}{a + \sin \theta} \right) d\theta, a > 0$

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43. Evaluate the following integrals: $\int_{-1}^1 |x \cos \pi x| dx$

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44. Evaluate the following integrals: (1-35) $\int_0^\pi \left(\frac{x}{1 + \sin^2 x} + \cos^7 x \right) dx$

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45. Evaluate : $\int_0^\pi \frac{x}{1 + \sin \alpha \sin x} dx$

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46. Evaluate the following integrals: (1-35) $\int_0^{\pi/2} \frac{a \sin x + b \cos x}{\sin x + \cos x} dx$

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47. Evaluate the following integrals as limit of sums: $\int_0^2 (x + 4) dx$ (ii)

$$\int_0^2 (2x + 1) dx$$

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48. Evaluate $\int_1^4 (x^2 - x) dx$ as a limit of sums.

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49. Evaluate: $\int_a^b \sin x dx$ using limit of sum

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50. Mark the correct alternative in each of the following:

$$\int_0^1 \sqrt{x(1-x)} dx \text{ equals } \pi/2 \text{ (b) } \pi/4 \text{ (c) } \pi/6 \text{ (d) } \pi/8$$

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51. Evaluate : $\int_0^{\pi} \frac{1}{1 + \sin x} dx$

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52. If $\int_0^a \sqrt{x} dx = 2a \int_0^{\pi/2} \sin^3 x dx$ find the value of integral $\int_a^{a+1} x dx$.

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53. Evaluate: (i) $\int_0^4 \frac{1}{\sqrt{x^2 + 2x + 3}} dx$ (ii) $\int_0^a \frac{1}{\sqrt{ax - x^2}} dx$

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54. If $\int_0^1 (3x^2 + 2x + k) dx = 0$, find the value of k .

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55. If $\int_1^a (3x^2 + 2x + 1)dx = 11$ then the value of a is

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56. If $\int_a^b x^3 dx = 0$, and If $\int_a^b x^2 dx = \frac{2}{3}$, find a and b .

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57. Evaluate: $\int_0^{\pi/2} \sqrt{1 - \cos 2x} dx$.

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58. Evaluate: $\int_0^{\pi/2} \sin^4 x dx$

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59. Evaluate: $\int_0^{\pi/4} \sqrt{1 + \sin 2x} dx$ (ii) $\int_0^{\pi/4} \sqrt{1 - \sin 2x} dx$

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60. Evaluate: $\int_{\pi/4}^{\pi/2} \sqrt{1 - \sin 2x} dx$

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61. Evaluate the following integrals: (1-35) $\int_{-2}^2 \frac{3x^3 + 2|x| + 1}{x^2 + |x| + 1} dx$

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62. Evaluate the following integrals: (1-35) $\int_0^{\pi} x \sin x \cos^2 x dx$

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63. Show that: $\int_0^{\pi/2} f(\sin 2x) \sin x dx = \sqrt{2} \int_0^{\pi/4} f(\cos 2x) \cos x dx$.

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64. For $x > 0$, let $f(x) = \int_1^x \frac{(\log)_e t}{1+t} dt$. Find the function $f(x) + f\left(\frac{1}{x}\right)$ and show that $f(e) + f\left(\frac{1}{e}\right) = \frac{1}{2}$.

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65. Evaluate the following integrals: (1-35) $\int_0^{\pi/2} \frac{\sin^n x}{\sin^n x + \cos^n x} dx$

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66. Prove that: $\int_0^{2\pi} \frac{x \sin^{2n} x}{\sin^{2n} x + \cos^{2n} x} dx = \pi^2$

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67. Prove that: $\int_0^{\pi/2} \log|\tan x + \cot x| dx = \pi(\log)_e 2$

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68. Evaluate: $\int_{-2}^2 |x \cos \pi x| dx$

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69. Evaluate: $\int_{-\pi/2}^{\pi/2} \log(\sin x + \cos x) dx$

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70. Evaluate: $\int_0^{\pi} x \log \sin x dx$

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71. If $\int_0^{\pi} \frac{1}{a + b \cos x} dx = \frac{\pi}{\sqrt{a^2 - b^2}}$, then $\int_0^{\pi} \frac{1}{(a + b \cos x)^2} dx$ is



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72. $\int_0^1 \sqrt{\frac{1-x}{1+x}} dx =$ (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{2} - 1$ (c) $\frac{\pi}{2} + 1$ (d) $\pi + 1$



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73. $\int_0^{\pi/2} \frac{\cos x}{(2 + \sin x)(1 + \sin x)} dx$ equals (a) $\log\left(\frac{2}{3}\right)$ (b) $\log\left(\frac{3}{2}\right)$ (c) $\log\left(\frac{3}{4}\right)$ (d) $\log\left(\frac{4}{3}\right)$



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74. $\int_0^{\pi} \frac{x \tan x}{\sec x + \cos x} dx$ is (a) $\frac{\pi^2}{4}$ (b) $\frac{\pi^2}{2}$ (c) $\frac{3\pi^2}{2}$ (d) $\frac{\pi^2}{3}$



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75. $\int_0^{21} \frac{dx}{1 + \tan x}$ is equal to (a) $\frac{\pi}{4}$ (b) $\frac{\pi}{3}$ (c) $\frac{\pi}{2}$ (d) π



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76. $\int_{-\pi/2}^{\pi/2} \sin|x| dx$ is equal to (a) 1 (b) 2 (c) -1 (d) -2

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77. The value of the integral $\int_0^{\infty} \frac{x}{(1+x)(1+x^2)} dx$ is $\frac{\pi}{2}$ (b) $\frac{\pi}{4}$ (c) $\frac{\pi}{6}$ (d) $\frac{\pi}{3}$

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78. $\int_0^3 \frac{3x+1}{x^2+9} dx = \frac{\pi}{12} + \log(2\sqrt{2})$ (b) $\frac{\pi}{2} + \log(2\sqrt{2})$ (c) $\frac{\pi}{6} + \log(2\sqrt{2})$ (d) $\frac{\pi}{3} + \log(2\sqrt{2})$

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79. $I_{10} = \int_0^{\frac{\pi}{2}} x^{10} \sin x dx$ then $I_{10} + 90I_8$ is (A) $10\left(\frac{\pi}{2}\right)^6$ (B) $10\left(\frac{\pi}{2}\right)^9$ (C) $10\left(\frac{\pi}{2}\right)^8$ (D) $10\left(\frac{\pi}{2}\right)^7$

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80. The derivative of $f(x) = \int_{x^2}^{x^3} \frac{1}{(\log)_e t} dt$, ($x > 0$), is $\frac{1}{3 \ln x}$ (b) $\frac{1}{3 \ln x} - \frac{1}{2 \ln x}$ (c) $(\ln x)^{-1} x(x-1)$ (d) $\frac{3x^2}{\ln x}$

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81. Evaluate: $\int_0^{\pi/2} \frac{\cos x}{1 + \cos x + \sin x} dx$

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82. Evaluate: $\int_0^{\pi/2} \frac{1}{3 + 2 \cos x} dx$

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83. Evaluate: $\int_{\pi/4}^{\pi/2} \cos 2x \log \sin x dx$

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84. integrate $\int_0^{2\pi} \sin\left(\frac{\pi}{4} + \frac{x}{2}\right) dx$

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85. Evaluate: $\int_1^2 \frac{1}{(x+1)(x+2)} dx$ (ii) $\int_1^2 \frac{1}{x(1+x^2)} dx$

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86. Evaluate: (i) $\int_0^{\pi/6} (2 + 3x^2) dx$

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87. Evaluate: $\int_0^4 \frac{1}{x + \sqrt{x}} dx$ (ii) $\int_0^1 \frac{2x}{5x^2 + 1} dx$

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88. Evaluate the following definite integrals (1-58):

$$\int_1^2 \frac{1}{\sqrt{(x-1)(2-x)}} dx$$

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89. If (x) is of the form $f(x) = a + bx + cx^2$, show that

$$\int_0^1 f(x) dx = \frac{1}{6} \left\{ f(0) + 4f\left(\frac{1}{2}\right) + f(1) \right\}$$

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90. Evaluate: $\int_0^{\infty} \frac{1}{(x^2 + a^2)(x^2 + b^2)} dx$.

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91. Evaluate the following integrals: $\int_0^{\pi/6} \cos^{-3} 2\theta \sin 2\theta d\theta$

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92. Evaluate the following integrals: $\int_0^{(\pi)^{2/3}} \sqrt{x} \cos^2 x^{3/2} dx$

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93. Evaluate the following integrals: $\int_0^1 \frac{24x^3}{(1+x^2)^4} dx$

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94. Evaluate the following integrals: $\int_0^1 \sqrt{\frac{1-x}{1+x}} dx$

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95. If $I_n = \int_0^{\pi/4} \tan^n x dx$, prove that $I_n + I_{n-2} = \frac{1}{n-1}$.

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96. If $I_n = \int_0^{\pi/4} \tan^n x dx$, show that $\frac{1}{I_2 + I_4}, \frac{1}{I_3 + I_5}, \frac{1}{I_4 + I_6}, \frac{1}{I_5 + I_7}$, form an A.P. Find the common difference of this progression.

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97. Evaluate: $\int_0^{\pi/2} \frac{1}{(a^2 \cos^2 x + b^2 \sin^2 x)^2} dx$

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98. Find $\frac{dy}{dx}$ if $x^2 = \cos y$

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99. Evaluate: $\int_0^a \frac{1}{(x^2 + a^2)} dx$ (ii) $\int_0^\infty \frac{x^2}{(a^2 + x^2)^{5/2}} dx$

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100. Evaluate: $\int_0^1 x \sqrt{\frac{1-x^2}{1+x^2}} dx$

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101. Evaluate the following integrals: $\int (\sin)^{-1} \sqrt{\frac{x}{a+x}} dx$

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102. Evaluate the following integrals: $\int_1^2 \frac{1}{x(1 + \log x)^2} dx$

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103. Evaluate the following integrals: $\int_0^{\pi/4} \frac{\sin^2 x \cos^2 x}{(\sin^3 x + \cos^3 x)^2} dx$

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104. Evaluate the following integrals: $\int_0^{\pi/2} \frac{\tan x}{1 + m^2 \tan^2 x} dx$

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105. Evaluate: $\int_0^1 |5x - 3| dx$ (ii) $\int_0^{\pi} |\cos x| dx$ (iii) $\int_{-5}^5 |x - 2| dx$ (iv)
 $\int_{-1}^1 e^{|x|} dx$ (v) $\int_0^2 |x^2 + 2x - 3| dx$ (v)
 $\int_1^4 (|x - 1| + |x - 2| + |x - 3|) dx$ (vi) $\int_{-1}^2 |x^3 - x| dx$

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106. Evaluate:

(i) $\int_{-1}^1 f(x) dx$, where, $f(x) = \{1 - 2x, x \leq 0; 1 + 2x, x \geq 0\}$,

(ii) $\int_{-1}^4 f(x) dx$, where, $f(x) = \{2x + 8, -1 \leq x \leq 2; 6x, 2 \leq x \leq 4\}$



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107. $\int_1^x \frac{1}{x} dx =$



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108. If $a > 0$, find $\int_0^{3a} |x^2 - a^2| dx$.



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109. If $[\cdot]$ denotes the greatest integer function, then find the value of

$$\int_1^2 [3x] dx$$



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110. Evaluate: $\int_0^3 [x] dx$



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111. $\int_0^1 \frac{d}{dx} \left\{ \sin^{-1} \left(\frac{2x}{1+x^2} \right) \right\} dx$ is equal to 0 (b) π (c) $\pi/2$ (d) $\pi/4$

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112. Evaluate the following integrals: $\int_{-a}^a \frac{xe^{x^2}}{1+x^2} dx$

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113. Evaluate the following integrals: $\int_0^{\pi/4} |\cos 2x| dx$

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114. Evaluate the following integrals:

$\int_{-5}^0 f(x) dx$, where $f(x) = |x| + |x+2| + |x+5|$

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115. Evaluate the following definite integrals (1-58):

$$\int_1^2 \frac{1}{\sqrt{(x-1)(2-x)}} dx$$

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116. Evaluate the following integrals: $\int_0^\pi \cos x |\cos x| dx$

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117. Let $f(x) = x - [x]$, for every real number x , where $[x]$ is the greatest integer less than or equal to x . Then, evaluate $\int_{-1}^1 f(x) dx$.

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118. Evaluate: $\int_0^{\sqrt{3}} \frac{1}{1+x^2} \sin^{-1} \left(\frac{2x}{1+x^2} \right) dx$

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119. Evaluate the following integrals:

$$\int_0^9 f(x) dx, \text{ where } f(x) = \begin{cases} \sin x, & 0 \leq x \leq \pi/2 \\ e^{x-3}, & 3 \leq x \leq 9 \end{cases} \quad 1, \frac{\pi}{2} \leq x \leq 3$$

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120. Evaluate the following integrals: $\int_0^2 |x^2 - 3x + 2| dx$

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121. Evaluate the following integrals: $\int_0^1 \sqrt{\frac{1-x}{1+x}} dx$

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122. Prove that: $\int_a^b \frac{f(x)}{f(x) + f(a+b-x)} dx = \frac{b-a}{2}$

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123. Evaluate each of the following integrals (1-15):

$$\int_0^5 \frac{\sqrt[3]{x+4} dx}{\sqrt[3]{x+4} + \sqrt[3]{9-x}}$$

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124. Evaluate each of the following integrals (1-15):

$$\int_{-\pi/4}^{\pi/4} \frac{x^{11} - 3x^9 + 5x^7 - x^5 + 1}{\cos^2 x} dx$$

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125. Evaluate each of the following integrals (1-15):

$$\int_{-a}^a \frac{1}{1+a^x} dx, a > 0$$

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126. Evaluate $\int_{\pi/6}^{\pi/3} \frac{\sqrt{(\sin x)} dx}{\sqrt{(\sin x)} + \sqrt{(\cos x)}}$

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127. Evaluate of each of the following integrals (1-15):

$$\int_0^{2\pi} \log(\sec x + \tan x) dx$$

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128. Evaluate: $\int_{-\pi/4}^{\pi/4} \frac{\sec^2 x}{1 + e^x} dx$

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129. Evaluate: $\int_{-\pi/4}^{\pi/4} \frac{\sec^2 x}{1 + e^x} dx$

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130. Evaluate: $\int_{-\pi/2}^{\pi/2} \frac{x \sin x}{e^x + 1} dx$

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131. If $f(a + b - x) = f(x)$, then prove that

$$\int_a^b x f(x) dx = \frac{a + b}{2} \int_a^b f(x) dx.$$

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132. Evaluate of each of the following integrals (1-15):

$$\int_0^7 \left(\frac{x^{\frac{1}{3}}}{x^{\frac{1}{3}} + (7 - x)^{\frac{1}{3}}} \right) dx$$

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133. Evaluate: $\int_1^2 x^2 dx$

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134. Evaluate: $\int_4^1 \frac{1}{x} dx$

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135. Evaluate: $\int_0^1 \frac{1}{\sqrt{1+x} + \sqrt{x}} dx$

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136. Evaluate: $\int_0^1 \frac{1}{2x-3} dx$

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137. Evaluate: $\int_0^{\pi/4} \tan^2 x dx$

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138. Evaluate $\int_0^{\frac{\pi}{2}} \sin^2 x dx$

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139. Evaluate: $\int_0^{\pi/4} \sin 3x \sin 2x dx$

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140. Evaluate: $\int_{1/4}^{1/2} \frac{1}{\sqrt{x-x^2}} dx$

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141. Evaluate: $\int_2^4 \frac{x}{x^2+1} dx$

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142. Evaluate: $\int_0^1 \frac{2x}{5x^2 + 1} dx$

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143. Evaluate: $\int_0^2 \frac{5x + 1}{x^2 + 4} dx$

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144. Evaluate: $\int_0^1 x e^x dx$

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145. Evaluate: $\int_1^2 \frac{\log x}{x^2} dx$

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146. Evaluate: $\int_0^{\pi/2} \cos x \, dx$

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147. Evaluate: $\int_1^2 \frac{\log x}{x} \, dx$

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148. Evaluate: $\int_0^{\pi/2} \sin x \, dx$

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149. Evaluate the definite integrals $\int_0^1 \left(xe^x + \frac{\sin(\pi x)}{4} \right) dx$

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150. Evaluate : $\int_1^2 \frac{5x^2}{x^2 + 4x + 3} dx$

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151. Evaluate: $\int_1^3 \frac{1}{x^2(x+1)} dx$

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152. Evaluate: $\int_1^3 \frac{1}{x^2(x+1)} dx$

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153. Evaluate : $\int_4^9 \frac{1}{\sqrt{x}} dx$

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154. Evaluate the following definite integral: $\int_2^3 \frac{1}{x+7} dx$

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155. Evaluate the following definite integral: $\int_0^{1/2} \frac{1}{\sqrt{1-x^2}} dx$

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156. Evaluate the following definite integral: $\int_0^1 \frac{1}{1+x^2} dx$

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157. Evaluate the following definite integral: $\int_2^3 \frac{x}{x^2+1} dx$

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158. Evaluate : $\int_0^{\infty} \frac{1}{a^2 + b^2 x^2} dx$

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159. Evaluate the following definite integral: $\int_{-1}^1 \frac{1}{1 + x^2} dx$

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160. Evaluate the following definite integrals: $\int_0^{\infty} e^{-x} dx$

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161. Evaluate the following definite integral: $\int_0^1 \frac{x}{x + 1} dx$

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162. Evaluate the following definite integral: $\int_0^{\pi/2} (\sin x + \cos x) dx$

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163. Evaluate the following definite integral: $\int_{\pi/4}^{\pi/2} \cot x dx$

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164. Evaluate the following definite integral: $\int_0^{\pi/4} \sec x dx$

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165. Evaluate the following definite integral: $\int_{\pi/6}^{\pi/4} \operatorname{cosec} x dx$

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166. Evaluate : $\int_0^{\pi} \frac{1}{1 + \sin x} dx$

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167. Evaluate the definite integrals $\int_0^{\frac{\pi}{2}} \cos^2 x dx$

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168. Evaluate the following definite integral: $\int_0^{\pi/6} \cos x \cos 2x dx$

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169. Evaluate : $\int_{\frac{\pi}{3}}^{\frac{\pi}{4}} (\tan x + \cot x)^2 dx$

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170. Evaluate the following definite integral $\int_0^{\frac{\pi}{2}} \cos^4 x dx$

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171. Evaluate the following definite integral:

$$\int_0^{\pi/2} (a^2 \cos^2 x + b^2 \sin^2 x) dx$$

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172. Evaluate the following definite integral: $\int_0^{\pi/2} \sqrt{1 + \cos x} dx$

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173. Evaluate the following definite integral: $\int_0^1 \frac{1-x}{1+x} dx$

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174. Evaluate the following definite integral: $\int_{-\pi/4}^{\pi/4} \frac{1}{1 + \sin x} dx$

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175. Evaluate the following definite integral: $\int_0^{\pi/2} \cos^3 x dx$

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176. Evaluate the following definite integral $\int_0^{\pi/2} \cos^4 x dx$

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177. Evaluate the following definite integral: $\int_0^{\pi/2} x^2 \sin x dx$

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178. Evaluate the following definite integral: $\int_0^{\pi/2} x \cos x dx$



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179. Evaluate the following definite integral: $\int_0^{\pi/4} x^2 \sin x \, dx$



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180. Evaluate the following definite integral: $\int_0^{\pi/2} x^2 \cos^2 x \, dx$



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181. Evaluate the following definite integral: $\int_1^3 \frac{\log x}{(x+1)^2} dx$



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182. Evaluate the following definite integral: $\int_1^e \frac{\log x}{x} dx$



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183. Evaluate the following definite integral: $\int_1^2 \frac{x + 3}{x(x + 2)} dx$

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184. Evaluate the following definite integral: $\int_0^2 \frac{1}{4 + x - x^2} dx$

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185. Evaluate the following definite integral: $\int_0^1 \sqrt{x(1 - x)} dx$

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186. Evaluate the following definite integral: $\int_0^4 \frac{1}{\sqrt{4x - x^2}} dx$

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187. Evaluate the following definite integral: $\int_1^4 \frac{x^2 + x}{\sqrt{2x + 1}} dx$

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188. Evaluate the following definite integral: $\int_1^2 \left(\frac{x - 1}{x^2} \right) e^x dx$

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189. Evaluate the following definite integral: $\int_0^1 \left(x e^x + \frac{\cos(\pi x)}{4} \right) dx$

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190. Evaluate the following definite integral: $\int_0^{2\pi} e^{x/2} \sin\left(\frac{x}{2} + \frac{\pi}{4}\right) dx$

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191. Evaluate the definite integrals $\int_0^1 \frac{dx}{\sqrt{1+x} - \sqrt{x}}$

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192. Evaluate the following definite integral: $\int_1^2 e^{2x} \left(\frac{1}{x} - \frac{1}{2x^2} \right) dx$

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193. Evaluate the following definite integral: $\int_0^{\pi/2} \cos x^2 dx$

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194. Evaluate the following definite integral: $\int_0^{\pi/2} x^2 \cos 2x dx$

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195. Evaluate the following definite integral: $\int_1^2 \log x \, dx$

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196. Evaluate the following definite integral: $\int_1^e \frac{e^x}{x} (1 + x \log x) dx$

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197. Evaluate : $\int_e^{e^2} \left\{ \frac{1}{\log x} - \frac{1}{(\log x)^2} \right\} dx$

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198. Evaluate the definite integrals $\int_0^1 \frac{2x + 3}{5x^2 + 1} dx$

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199. Evaluate the following definite integral: $\int_0^1 \frac{1}{2x^2 + x + 1} dx$

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200. Evaluate the following definite integral: $\int_0^2 \frac{1}{\sqrt{3 + 2x - x^2}} dx$

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201. Evaluate : $\int_0^1 x(1 - x)^5 dx$

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202. Evaluate the following definite integral: $\int_0^1 \left(xe^{2x} + \sin \pi \frac{x}{2} \right) dx$

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203. Evaluate the following definite integral: $\int_{\pi/2}^{\pi} e^x \left(\frac{1 + \sin x}{1 + \cos x} \right) dx$

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204. Evaluate : $\int_0^{2\pi} e^x \cos\left(\frac{\pi}{4} + \frac{x}{2}\right) dx$

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205. Evaluate the following definite integral: $\int_0^{\pi} \left(\frac{\sin^2 x}{2} - \frac{\cos^2 x}{2} \right) dx$

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206. If $\int_0^a 3x^2 dx = 8$, find the value of a .

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207. Evaluate the following integral : $\int_{\pi}^{3\pi/2} \sqrt{1 - \cos 2x} \, dx$

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208. Evaluate the following integral : $\int_0^{2\pi} \sqrt{1 + \sin\left(\frac{x}{2}\right)} \, dx$

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209. Evaluate : $\int_0^{\pi/4} (\tan x + \cot x)^{-2} \, dx$

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210. Evaluate the following integral : $\int_{\pi/6}^{\pi/3} (\tan x + \cot x)^2 \, dx$

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211. Evaluate: $\int_0^1 \frac{1}{1 + 2x + 2x^2 + 2x^3 + x^4} dx$

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212. Evaluate: $\int_0^1 x \log(1 + 2x) dx$

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213. Evaluate: $\int_0^{\pi/2} \frac{1}{(a^2 \cos^2 x + b^2 \sin^2 x)^2} dx$

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214. Evaluate: $\int_0^1 \sin^{-1} x dx$

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215. Evaluate: $\int_0^{\pi/2} \sqrt{\cos \theta} \sin^3 \theta d\theta$

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216. Evaluate: $\int_0^{\pi/2} \frac{1}{\cos^3 x \sqrt{2 \sin 2x}} dx$

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217. Evaluate: $\int_0^{\pi/2} \frac{\cos \theta}{(1 + \sin \theta)(2 + \sin \theta)} d\theta$

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218. Evaluate the following integral: $\int_0^{1/2} \frac{1}{\sqrt{1-x^2}} dx$

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219. Evaluate: $\int_0^a \frac{x^4}{\sqrt{a^2 - x^2}} dx$

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220. Evaluate: $\int_0^{\frac{1}{\sqrt{2}}} \frac{\sin^{-1} x}{(1 - x^2)\sqrt{1 - x^2}} dx$

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221. Evaluate: $\int_0^{\pi/4} \tan^2 x dx$

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222. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{2 \cos x + 4 \sin x} dx$

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223. Evaluate: $\int_0^{\pi/2} \frac{\sin x}{1 + \cos^2 x} dx$

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224. Evaluate: $\int_0^{\pi/2} \frac{1}{4 \sin^2 x + 5 \cos^2 x} dx$

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225. Evaluate: $\int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$

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226. Evaluate: $\int_0^{\pi/4} \frac{\sin 2x}{\cos^4 x + \sin^4 x} dx$

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227. Evaluate: $\int_0^{\pi/2} \frac{\cos^2 x}{\cos^2 x + 4 \sin^2 x} dx$

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228. Evaluate the following integral: $\int_2^4 \frac{x}{x^2 + 1} dx$

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229. Evaluate the following integral: $\int_1^2 \frac{1}{x(1 + \log x)^2} dx$

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230. Evaluate the following integral: $\int_1^2 \frac{3x}{9x^2 - 1} dx$

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231. Evaluate the following integral: $\int_0^a \frac{x}{\sqrt{a^2 + x^2}} dx$

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232. Evaluate the following integral: $\int_0^1 x e^{x^2} dx$

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233. Evaluate the following integral: $\int_0^1 \frac{2x}{1 + x^4} dx$

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234. Evaluate the following integral: $\int_1^2 \frac{1}{x(1 + \log x)^2} dx$

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235. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{5 \cos x + 3 \sin x} dx$

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236. Evaluate the following integral: $\int_0^1 \frac{e^x}{1 + e^{2x}} dx$

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237. Evaluate the following integral: $\int_1^3 \frac{\cos(\log x)}{x} dx$

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238. Evaluate the following integral: $\int_0^a \sqrt{a^2 - x^2} dx$

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239. Evaluate the following integral: $\int_0^{\pi/2} \sqrt{\sin \varphi} \cos^5 \varphi d\varphi$

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240. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin \theta}{\sqrt{1 + \cos \theta}} d\theta$

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241. Evaluate the following integral: $\int_0^1 \frac{\sqrt{\tan^{-1} x}}{1 + x^2} dx$

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242. Evaluate the following integral: $\int_0^1 \tan^{-1} \left(\frac{2x}{1 - x^2} \right) dx$

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243. Evaluate the following integral: $\int_0^{\pi/2} \frac{dx}{a \cos x + b \sin x} a, b > 0$

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244. Evaluate the following integral: $\int_0^{\pi} \frac{\sin x}{\sin x + \cos x} dx$

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245. Evaluate the following integral: $\int_0^1 \tan^{-1} x dx$

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246. Evaluate the following integral: $\int_0^{\pi/4} (\sqrt{\tan x} + \sqrt{\cot x}) dx$

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247. Evaluate the following integral: $\int_0^{\pi} \frac{1}{5 + 3 \cos x} dx$

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248. Evaluate the following integral: $\int_0^{\pi/2} \frac{x + \sin x}{1 + \cos x} dx$

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249. Evaluate the following integral: $\int_0^{\pi/4} \frac{\sin x + \cos x}{3 + \sin 2x} dx$

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250. Evaluate the following integral: $\int_0^1 \frac{1 - x^2}{x^4 + x^2 + 1} dx$

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251. Evaluate the following integral: $\int_4^{12} x(x-4)^{1/3} dx$

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252. Evaluate the following integral: $\int_{-1}^1 5x^4 \sqrt{x^5 + 1} dx$

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253. Evaluate the following integral: $\int_0^{\pi/4} \sin^3 2t \cos 2t dt$

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254. Evaluate the following integral: $\int_0^{\pi/2} \frac{\cos x}{1 + \sin^2 x} dx$

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255. Evaluate the following integral: $\int_0^{\pi/3} \frac{\cos x}{3 + 4 \sin x} dx$

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256. Evaluate the following integral: $\int_0^2 x \sqrt{x+2} dx$

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257. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin x \cos x}{1 + \sin^4 x} dx$

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258. Evaluate the following integral: $\int_0^{\pi} \frac{1}{5 + 4 \sin x} dx$

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259. Evaluate the following integral: $\int_0^{\pi} \frac{1}{3 + 2 \sin x + \cos x} dx$

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260. Evaluate: $\int_0^{\frac{1}{2}} \frac{x \sin^{-1} x}{\sqrt{1 - x^2}} dx$

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261. Evaluate the following integral: $\int_0^{\pi/4} \frac{\tan^3 x}{1 + \cos 2x} dx$

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262. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{a^2 \sin^2 x + b^2 \cos^2 x} dx$

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263. Evaluate the following integral: $\int_0^1 \frac{\tan^{-1} x}{1+x^2} dx$

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264. Evaluate the following integral: $\int_0^1 x \tan^{-1} x dx$

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265. Evaluate the following integral: $\int_0^{\pi/2} \sin^2 x dx$

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266. Evaluate the following integral: $\int_0^1 \frac{1-x^2}{(1+x^2)^2} dx$

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267. Evaluate the following integral: $\int_0^{\pi/2} \frac{\cos^2 x}{1 + 3 \sin^2 x} dx$



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268. Evaluate the following integral: $\int_0^{\pi} 5(5 - 4 \cos \theta)^{1/4} \sin \theta d\theta$



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269. Evaluate the following integral: $\int_4^9 \frac{\sqrt{x}}{(30 - x^{3/2})^2} dx$



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270. Evaluate the following integral: $\int_0^{\pi/2} 2 \sin x \cos x \tan^{-1}(\sin x) dx$



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271. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin x \cos x}{\cos^2 x + 3 \cos x + 2} dx$

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272. Evaluate the following integral: $\int_0^{1/2} \frac{1}{(1+x^2)\sqrt{1-x^2}} dx$

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273. Evaluate the following integral: $\int_0^1 (\cos^{-1} x)^2 dx$

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274. Evaluate the following integral: $\int_{\pi/3}^{\pi/2} \frac{\sqrt{1+\cos x}}{(1-\cos x)^{3/2}} dx$

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275. Evaluate the following integral: $\int_{-a}^a \sqrt{\frac{a-x}{a+x}} dx$

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276. Evaluate the following integral: $\int_{1/3}^1 \frac{(x-x^3)^{1/3}}{x^4} dx$

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277. Evaluate: $\int_{-\pi/4}^{\pi/4} \frac{\sec^2 x}{1+e^x} dx$

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278. Evaluate the following integral:

$$\int_0^9 f(x) dx, \text{ where } f(x) = \sin x, 0 \leq x \leq \pi/2$$

$$\text{where } f(x) = 1, \frac{\pi}{2} \leq x \leq 3$$

$$\text{where } f(x) = e^{x-3}, 3 \leq x \leq 9$$

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279. Evaluate the following integral:

$$\int_2^4 f(x)dx, \text{ where } f(x) = \begin{cases} 7x + 3, & \text{if } 1 \leq x \leq 3 \\ 8x & \text{if } 3 \leq x \leq 4 \end{cases},$$

where $f(x) = 8x$ if $3 \leq x \leq 4$

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280. Evaluate the following integral: $\int_{-4}^4 |x + 2|dx$

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281. Evaluate the following integral: $\int_{-1}^1 |2x + 1|dx$

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282. Evaluate the following integral: $\int_{-6}^6 |x + 2|dx$

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283. Evaluate the following integral: $\int_1^2 |x - 3| dx$

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284. Evaluate the following integral: $\int_0^{2\pi} |\sin x| dx$

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285. Evaluate the following integral: $\int_2^8 |x - 5| dx$

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286. Evaluate the following integral: $\int_0^4 |x - 1| dx$

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287. Evaluate the following integral: $\int_0^4 (|x| + |x - 2| + |x - 4|) dx$

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288. Evaluate the following integral: $\int_{-2}^2 e^{|x|} dx$

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289. Evaluate the following integral: $\int_{-\pi/2}^{\pi} \sin^{-1}(\sin x) dx$

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290. Evaluate the following integral: $\int_{-3}^3 |x + 1| dx$

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291. Evaluate the following integral: $\int_{-1}^2 |2x + 3| dx$

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292. Evaluate the following integral: $\int_0^3 |3x - 1| dx$

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293. Evaluate the following integral: $\int_{-2}^2 |x + 1| dx$

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294. Evaluate the following integral: $\int_{-\pi/4}^{\pi/4} |\sin x| dx$

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295. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} (\sin|x| + \cos|x|) dx$

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296. Evaluate the following integral: $\int_1^4 \{|x - 1| + |x - 2| + |x - 4|\} dx$

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297. Evaluate the following integral: $\int_{-\pi/4}^{\pi/2} \sin x dx$

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298. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} (2 \sin|x| + \cos x) dx$

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299. Evaluate of each of the following integral: $\int_0^{2\pi} \frac{e^{\sin x}}{e^{\sin x} + e^{-\sin x}} dx$

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300. Evaluate of each of the following integral: $\int_{-\pi/4}^{\pi/4} (\tan^2 x) dx$

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301. Evaluate of each of the following integral: $\int_{-\pi/3}^{\pi/3} \frac{1}{1 + e^x} dx$

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302. Evaluate of each of the following integral:

$$\int_0^{\pi/2} (2 \log \cos x - \log \sin 2x) dx$$

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303. Evaluate of each of the following integral: $\int_{\pi/6}^{\pi/3} \frac{1}{1 + \sqrt{\tan x}} dx$

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304. Evaluate of each of the following integral: $\int_{-\pi/2}^{\pi/2} \frac{\cos^2 x}{1 + e^x} dx$

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305. Evaluate of each of the following integral:

$$\int_a^b \frac{x^{1/n}}{x^{1/n} + (a + b - x)^{\frac{1}{n}}} dx, n \geq 2$$

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306. Evaluate of each of the following integral: $\int_0^a \frac{\sqrt{x}}{\sqrt{x} + \sqrt{a-x}} dx$

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307. If $f(a + b - x) = f(x)$, then prove that

$$\int_a^b x f(x) dx = \frac{a + b}{2} \int_a^b f(x) dx$$

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308. Evaluate: $\int_0^{\pi/2} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$

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309. Evaluate: $\int_0^{\pi/2} \log \tan x dx$

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310. Evaluate: $\int_0^{\pi/4} \log(1 + \tan x) dx$

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311. Evaluate: $\int_0^{\pi/2} \frac{\sin x - \cos x}{1 + \sin x \cos x} dx$

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312. Evaluate: $\int_0^{\pi/2} (2 \log \sin x - \log \sin 2x) dx$

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313. Evaluate: $\int_0^{\pi} \frac{e^{\cos x}}{e^{\cos x} + e^{-\cos x}} dx$

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314. Evaluate: $\int_0^1 x(1-x)^n dx$

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315. Evaluate: $\int_0^1 \cot^{-1}(1 - x + x^2) dx$

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316. If f and g are continuous on $[0, a]$ and satisfy $f(x) = f(a - x)$ and $g(x) + g(a - x) = 2$. show that

$$\int_0^a f(x)g(x)dx = \int_0^a f(x)dx$$

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317. Evaluate: $\int_0^{2\pi} \frac{1}{1 + e^{\sin x}} dx$

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318. Evaluate: $\int_0^{\pi} \frac{1}{1 + e^{\cos x}} dx$

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319. Evaluate: $\int_0^{\pi} \frac{x}{a^2 \cos^2 x + b^2 \sin^2 x} dx$

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320. Evaluate: $\int_0^{\pi} \frac{x \sin x}{1 + \cos^2 x} dx$

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321. Evaluate: $\int_0^{\pi} \frac{x}{1 + \sin x} dx$

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322. Evaluate: $\int_0^{\pi} \frac{x \tan x}{\sec x + \tan x} dx$

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323. Evaluate: $\int_0^{\pi/2} \frac{x}{\sin x + \cos x} dx$



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324. Evaluate: $\int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$



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325. Evaluate: $\int_{-\pi/2}^{\pi/2} \frac{1}{1 + e^{\sin x}} dx$



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326. Evaluate: $\int_{-\pi/2}^{\pi/2} \frac{1}{1 + e^{\sin x}} dx$



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327. Evaluate: $\int_{-\pi/2}^{\pi/2} \frac{\cos x}{1 + e^x} dx$



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328. Evaluate: $\int_{-\pi/2}^{\pi/2} \sin^7 x dx$

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329. Evaluate: $\int_{-\pi/2}^{\pi/2} \sin^2 x dx$

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330. Evaluate: $\int_{-\pi/2}^{\pi/2} |\sin x| dx$

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331. Evaluate: $\int_{-\pi}^{\pi} (\cos ax + \sin bx)^2 dx$

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332. Find the value of $\int_{-1}^{\frac{3}{2}} |x \sin \pi x| dx$

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333. Evaluate: $\int_0^{2\pi} \cos^5 x dx$

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334. Prove that: $\int_0^{\pi/2} \log \sin x dx = \int_0^{\pi/2} \log \cos x dx = -\frac{\pi}{2} \log 2$

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335. Evaluate: $\int_0^{\pi} \log(1 + \cos x) dx$

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336. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \tan x} dx$



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337. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sqrt{\cot x}}{\sqrt{\cot x} + \sqrt{\tan x}} dx$



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338. Evaluate the following integral: $\int_0^a \frac{1}{x + \sqrt{a^2 - x^2}} dx$



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339. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \cot x} dx$



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340. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin^{3/2} x}{\sin^{3/2} x + \cos^{3/2} x} dx$



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341. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \tan x} dx$

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342. Evaluate the following integral: $\int_0^{\infty} \frac{\log x}{1 + x^2} dx$

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343. Evaluate the following integral: $\int_0^1 \frac{\log(1 + x)}{1 + x^2} dx$

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344. Evaluate the following integral: $\int_0^{\pi} \frac{x \tan x}{\sec x \cos ec x} dx$

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345. Evaluate the following integral: $\int_0^{\pi} x \sin^3 x \, dx$

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346. Evaluate the following integral: $\int_0^{\pi} \frac{x \sin x}{1 + \sin x} dx$

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347. Evaluate the following integral: $\int_0^{\pi/2} \frac{\tan^7 x}{\tan^7 x + \cot^7 x} dx$

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348. Evaluate the following integral: $\int_0^{\pi/2} x \sin x \cos^2 x \, dx$

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349. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \sin^3 x \, dx$

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350. Evaluate the following integral: $\int_{-1}^1 \log\left(\frac{2-x}{2+x}\right) dx$

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351. Evaluate the following integral: $\int_0^{\pi} \log(1 - \cos x) dx$

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352. Evaluate the following integral: $\int_{-\pi}^{\pi} \frac{2x(1 + \sin x)}{1 + \cos^2 x} dx$

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353. Evaluate the following integral: $\int_0^2 x \sqrt{2-x} dx$

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354. Evaluate the following integral: $\int_0^{\infty} \frac{x}{(1+x)(1+x^2)} dx$

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355. Evaluate the following integral: $\int_0^{\pi} x \sin x \cos^4 x dx$

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356. Evaluate the following integral: $\int_0^{\pi} x \log \sin x dx$

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357. Evaluate the following integral: $\int_0^{\pi} x \log \sin x dx$



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358. Evaluate the following integral: $\int_{\pi/6}^{\pi/3} \frac{1}{1 + \cot^{3/2} x} dx$,



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359. Evaluate the following integral: $\int_{\pi/6}^{\pi/3} \frac{1}{1 + \cot^{3/2} x} dx$



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360. Evaluate the following integral: $\int_2^8 \frac{\sqrt{10-x}}{\sqrt{x} + \sqrt{10-x}} dx$



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361. Evaluate the following integral: $\int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$



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362. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \sin^2 x \, dx$

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363. Evaluate the following integral: $\int_{-\pi/4}^{\pi/4} \sin^2 x \, dx$

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364. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \log\left(\frac{2 - \sin x}{2 + \sin x}\right) dx$

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365. Evaluate the following integral:

$$\int_{-3\pi/2}^{-\pi/2} \left\{ \sin^2(3\pi + x) + (\pi + x)^3 \right\} dx$$

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366. Evaluate the following integral: $\int_0^1 \log\left(\frac{1}{x} - 1\right) dx$

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367. Evaluate the following integral: $\int_0^{2\pi} \sin^{100} x \cos^{101} x dx$

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368. If f is an integrable function such that $f(2a - x) = f(x)$, then

prove that $\int_0^{2a} f(x) dx = 2 \int_0^a f(x) dx$

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369. If $f(2a - x) = -f(x)$, prove that $\int_0^{2a} f(x) dx = 0$

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370. If f is an integrable function, show that

$$\int_{-a}^a f(x^2) dx = 2 \int_0^a f(x^2) dx$$

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371. If f is an integrable function, show that $\int_{-a}^a x f(x^2) dx = 0$

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372. If $f(x)$ is a continuous function defined on $[0, 2a]$. Then prove that

$$\int_0^{2a} f(x) dx = \int_0^a \{f(x) + (2a - x)\} dx$$

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373. If $f(a + b - x) = f(x)$, then prove that

$$\int_a^b x f(x) dx = \frac{a + b}{2} \int_a^b f(x) dx.$$

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374. If $f(a + b - x) = f(x)$, then prove that

$$\int_a^b x f(x) dx = \left(\frac{a + b}{2} \right) \int_a^b f(x) dx.$$

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375. Property 8: If $f(x)$ is a continuous function defined on $[-a; a]$ then

$$\int_{-a}^a f(x) dx = \int_0^a \{f(x) + f(-x)\} dx$$

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376. If $\int_0^\pi x f(\sin x) dx = A \int_0^{\frac{\pi}{2}} f(\sin x) dx$, then A is

(A) $\frac{\pi}{2}$

(B) π

(C) 0

(D) 2π



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377. Evaluate the following integrals as limit of sum: $\int_0^2 (x + 4)dx$

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378. Evaluate: $\int (2x + 1)dx$

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379. Evaluate the following integrals as limit of sum: $\int_0^3 (x + 4)dx$

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380. Evaluate the following integrals as limit of sum: $\int_1^3 (3x - 2)dx$

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381. Evaluate the following integrals as limit of sum: $\int_1^3 (3x - 2) dx$

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382. Evaluate $\int (x + 1) dx$

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383. Evaluate: $\int_3^5 (2 - x) dx$

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384. Evaluate the definite integrals as limit of sums $\int_z^1 x^2 dx$

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385. Evaluate the following integrals as limit of sum: $\int_1^2 (x^2 - 1) dx$



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386. Evaluate the following integrals : $\int_0^2 (x + 3)dx$



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387. Evaluate the following integrals : $\int_{-1}^1 (x + 3)dx$



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388. Evaluate the following integrals as limit of sum: $\int_1^3 (2x + 3)dx$



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389. Evaluate the following integrals $\int_1^3 (2x + 3)dx$



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390. Evaluate the following integrals as limit of sum: $\int_0^2 (x^2 + 1) dx$

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391. Evaluate the following integrals : $\int_2^3 (2x^2 + 1) dx$

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392. Evaluate the following integrals as limit of sum: $\int_0^2 (x^2 + 4) dx$

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393. Evaluate the following integrals as limit of sum: $\int_1^4 (x^2 - x) dx$

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394. Evaluate the following integrals as limit of sum: $\int_0^2 e^x dx$

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395. Evaluate.

$$\int_a^b \cos x dx$$

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396. Evaluate the following integrals as limit of sum: $\int_0^{\pi/2} \cos x dx$

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397. Evaluate the following integrals as limit of sum: $\int_0^2 (3x^2 - 2) dx$

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398. Evaluate $\int (x + e^{2x}) dx$

A. $\int_0^4 (x + e^{2x}) dx$

B. null

C. null

D. null

Answer: null

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399. Evaluate $\int (x^2 + 2x + 1) dx$

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400. Evaluate $\int abx dx$

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401. Evaluate the following integrals as limit of sum: $\int_2^3 x^2 dx$

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402. Evaluate $\int x^2 dx$

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403. Evaluate: $\int(x^2 - x) dx$

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404. Evaluate : $\int(3x^2 + 1) dx$

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405. Evaluate: $\int_0^1 (3x^2 + 5x) dx$



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406. Evaluate the following integrals as limit of sum: $\int_a^b e^x dx$



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407. Evaluate : $\int_0^{\pi/2} \sin x dx$



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408. Evaluate : $\int_0^2 (x^2 + 2) dx$



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409. Evaluate the following integrals : $\int_1^4 (3x^2 + 2x) dx$



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410. Evaluate the following integrals : $\int_0^2 (x^2 + x) dx$

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411. Evaluate the following integrals : $\int_0^3 (2x^2 + 3x + 5) dx$

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412. Evaluate the following definite integrals as limit of sums.

$$\int_0^5 (x + 1) dx$$

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413. Evaluate the following definite integrals $\int (x^2 - x) dx$

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414. Evaluate: $\int_1^3 (2x^2 + 5x) dx$

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415. Evaluate each of the following integral: $\int_0^{\pi/2} \sin^2 x dx$

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416. Evaluate : $\int_{-\pi/2}^{\pi/2} \sin^2 x dx$

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417. Evaluate each of the following integral: $\int_{-\pi/2}^{\pi/2} \sin^2 x dx$

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418. Evaluate each of the following integral: $\int_0^{\pi/4} \tan^2 x \, dx$

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419. Evaluate each of the following integral: $\int_{-2}^1 \frac{|x|}{x} dx$

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420. Evaluate each of the following integral: $\int_0^4 \frac{1}{\sqrt{16-x^2}} dx$

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421. Evaluate: $\int_0^{\pi/2} \sqrt{1 - \cos 2x} \, dx$.

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422. Evaluate each of the following integral: $\int_0^{\pi/2} \log\left(\frac{3 + 5 \cos x}{3 + 5 \sin x}\right) dx$

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423. Evaluate each of the following integral: $\int_0^{\pi} \cos^5 x dx$

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424. Evaluate each of the following integral: $\int_{-1}^1 x|x| dx$

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425. Evaluate the following definite integral: $\int_0^1 \frac{1}{1+x^2} dx$

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426. Evaluate each of the following integral: $\int_2^3 \frac{1}{x} dx$

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427. Evaluate each of the following integral: $\int_0^1 \frac{2x}{1+x^2} dx$

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428. Evaluate each of the following integral: $\int_0^{\pi/4} \sin 2x dx$

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429. Evaluate each of the following integral: $\int_0^{\pi/2} \cos^2 x dx$

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430. Evaluate each of the following integral: $\int_{-\pi/2}^{\pi/2} \cos^2 x \, dx$

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431. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} x \cos^2 x \, dx$

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432. Evaluate the following definite integral: $\int_{-1}^1 \frac{1}{1+x^2} \, dx$

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433. Evaluate each of the following integral: $\int_0^{\infty} e^{-x} \, dx$

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434. Evaluate each of the following integral: $\int_{-1}^1 \frac{1}{x^2 + 1} dx$

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435. Evaluate each of the following integral: $\int_0^{\pi/2} \log \tan x dx$

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436. Evaluate the following integrals: $\int_0^{\pi/2} \frac{\sin^n x}{\sin^n x + \cos^n x} dx$

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437. Evaluate each of the following integral: $\int_{-\pi/2}^{\pi/2} \log \left(\frac{a - \sin \theta}{a + \sin \theta} \right) d\theta$

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438. Evaluate each of the following integral: $\int_a^b \frac{f(x)}{f(x) + f(a + b - x)} dx$

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439. Evaluate each of the following integral: $\int_0^2 \sqrt{4 - x^2} dx$

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440. Evaluate each of the following integral: $\int_0^1 x e^{x^2} dx$

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441. Evaluate each of the following integral: $\int_e^{e^2} \frac{1}{x \log x} dx$

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442. Evaluate each of the following integral: $\int_0^{\pi/2} e^x(\sin x - \cos x)dx$

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443. Evaluate each of the following integral: $\int_2^4 \frac{x}{x^2 + 1} dx$

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444. If $\int_0^1 (3x^2 + 2x + k)dx = 0$, find the value of k .

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445. If $\int_0^a 3x^2 dx = 8$, write the value of ' a '.

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446. If $f(x) = \int_0^x t \sin t \, dt$, then write the value of $f'(x)$

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447. If $\int_0^a \frac{1}{4+x^2} dx = \frac{\pi}{8}$, find the value of a .

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448. The value of $\int_{-2}^2 (ax^3 + bx + c) dx$ depends on (A) the value of b
(B) the value of c (C) the value of a (D) the value of a and b

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449. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^2 [x] dx$

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450. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^1 \{x\} dx$

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451. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^2 x[x] dx$

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452. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral:

$$\int_1^2 (\log)_e [x] dx$$

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453. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^{15} [x] dx$

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454. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^1 e^{[x]} dx$

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455. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^1 2^{x - [x]} dx$

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456. If $[.]$ and $\{.\}$ denote respectively the greatest integer and fractional part functional respectively, evaluate the following integral: $\int_0^{\sqrt{2}} [x^2] dx$



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457. The value of $\int_0^{\pi/2} \frac{\sqrt{\cos x}}{\sqrt{\cos x} + \sqrt{\sin x}} dx$ is $\pi/2$ b. $\pi/4$ c. 0 d. none of these



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458. $\int_0^{\pi} \frac{1}{1 + \sin x} dx$ equals a. 0 b. $1/2$ c. 2 d. $3/2$



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459. $\int_0^{\infty} \frac{1}{1 + e^x} dx$ equals a. $\log 2 - 1$ b. $\log 2$ c. $\log 4 - 1$ d. $\log 2$



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460. The value of $\int_0^{2\pi} \sqrt{1 + \sin\left(\frac{x}{2}\right)} dx$ is a. 0 b. 4 c. 2 d. 8



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461. $\int_0^{\pi^2/4} \frac{\sin \sqrt{x}}{\sqrt{x}} dx$ equals a. $\pi^2/8$ b. $\pi/4$ c. 2 d. 1

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462. $\int_0^{\pi/2} \frac{1}{2 + \cos x} dx$ equals a. $\frac{1}{3} \tan^{-1} \left(\frac{1}{\sqrt{3}} \right)$ b. $\frac{2}{\sqrt{3}} \tan^{-1} \left(\frac{1}{\sqrt{3}} \right)$
 c. $\sqrt{3} \tan^{-1}(\sqrt{3})$ d. $2\sqrt{3} \tan^{-1} \sqrt{3}$

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463. $\frac{36}{\pi} \int_{\pi/6}^{\pi/3} \frac{dx}{1 + \sqrt{\cot x}}$ equals to

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464. Given that

$$\int_0^{\infty} \frac{x^2}{(x^2 + a^2)(x^2 + b^2)(x^2 + c^2)} dx = \frac{\pi}{2(a + b)(b + c)(c + a)}$$

the

value of $\int_0^{\infty} \frac{dx}{(x^2 + 4)(x^2 + 9)}$, is

- a. $\frac{\pi}{60}$
- b. $\frac{\pi}{40}$
- c. $\frac{\pi}{20}$
- d. $\frac{\pi}{80}$



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465. $\int_1^e \log x \, dx =$ a. 1 b. $e - 1$ c. $e + 1$ d. 0



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466. $\int_1^{\sqrt{3}} \frac{1}{1+x^2} dx$ is equal to a. $\frac{\pi}{12}$ b. $\frac{\pi}{4}$ c. $\frac{\pi}{6}$ d. $\frac{\pi}{3}$



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467. The value of $\int_0^{\pi/2} \cos x e^{\sin x} dx$ is a. 1 b. $e - 1$ c. 0 d. -1



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468. If $\int_0^a \frac{1}{1+4x^2} dx = \frac{\pi}{8}$, then a equals a. $\frac{\pi}{2}$ b. $\frac{\pi}{4}$ c. $\frac{1}{2}$ d. 1



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469.

$\int_0^1 f(x) dx = 1$, $\int_0^1 x f(x) dx = a$, $\int_0^1 x^2 f(x) dx = a^2$, then $\int_0^1 (a-x)^2$ equals a. $4a^2$ b. 0 c. $2a^2$ d. none of these



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470. The value of $\int_{-\pi}^{\pi} \sin^3 x \cos^2 x dx$ is a. $\frac{\pi^4}{2}$ b. $\frac{\pi^4}{4}$ c. 0 d. none of these



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471. $\int_{\pi/6}^{\pi/3} \frac{1}{\sin 2x} dx$ is equal to a. $(\log)_e 3$ b. $(\log)_e \sqrt{3}$ c. $\frac{1}{2} \log(-1)$ d. $\log(-1)$



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472. $\int_{-1}^1 |1 - x| dx$ is equal to a. -2 b. 2 c. 0 d. 4



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473. $\int_0^1 \frac{x}{(1-x)^{54}} dx =$

a. $9 \left(\frac{\pi}{2}\right)^9$

b. $10 \left(\frac{\pi}{2}\right)^9$

c. $\left(\frac{\pi}{2}\right)^9$

d. $9 \left(\frac{\pi}{2}\right)^8$



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474. $(\lim)_{n \rightarrow \infty} \left\{ \frac{1}{2n+1} + \frac{1}{2n+2} + \dots + \frac{1}{2n+n} \right\}$ a. $\ln\left(\frac{1}{3}\right)$ b. $\ln\left(\frac{2}{3}\right)$ c. $\ln\left(\frac{3}{2}\right)$ d. $\ln\left(\frac{4}{3}\right)$



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475. The value of the integral $\int_{-2}^2 |1 - x^2| dx$ is a. 4 b. 2 c. -2 d. 0



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476. $\int_0^{\pi/2} \frac{1}{1 + \cot^3 x} dx$ is equal to a. 0 b. 1 c. $\pi/2$ d. $\pi/4$



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477. $\int_0^{\pi/2} \frac{\sin x}{\sin x + \cos x} dx$ equals to a. $\pi/2$ b. $\pi/4$ c. $\pi/3$ d. π



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478. $\int_0^{\pi/2} x \sin x \, dx$ is equal to a. $\pi/2$ b. $\pi/4$ c. π d. 1



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479. $\int_0^{\pi/2} \sin 2x \log \tan x \, dx$ is equal to a. $\pi/2$ b. π c. 0 d. 2π



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480. The value of $\int_0^{\pi} \frac{1}{5 + 3 \cos x} \, dx$ is

a. $\pi/2$

b. $\pi/4$

c. 0

d. $\pi/8$



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481. Evaluate: $\int_0^{\infty} \log\left(x + \frac{1}{x}\right) \frac{dx}{1+x^2}$



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482. $\int_0^{2a} f(x) dx$ is equal to

a. $2 \int_0^a f(x) dx$

b. 0

c. $\int_0^a f(x) dx + \int_0^a f(2a - x) dx$

d. $\int_0^a f(x) dx + \int_0^{2a} f(2a - x) dx$

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483. If $f(a + b - x) = f(x)$, then $\int_a^b x f(x) dx$ is equal to

a. $\frac{a + b}{2} \int_a^b f(b - x) dx$

b. $\frac{a + b}{2} \int_a^b f(b + x) dx$

c. $\frac{b - 1}{2} \int_a^b f(x) dx$

d. $\frac{a + b}{2} \int_a^b f(x) dx$

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484. The value of $\int_0^1 \tan^{-1}\left(\frac{2x-1}{1+x-x^2}\right) dx$, is

- a. 1
- b. -1
- c. 0
- d. $\pi/4$

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485. Choose the correct answer The value of $\int_0^{\frac{\pi}{2}} \log\left(\frac{4-3\sin x}{4+3\cos x}\right) dx$

- (A) 2 (B) $\frac{3}{4}$ (C) 0 (D) -2

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486. The value of $\int_{-\pi/2}^{\pi/2} (x^3 + x \cos x + \tan^5 x + 1) dx$, is a. 2 b. π c. 0 d.

1

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487. Evaluate the following integral: $\int_0^4 x \sqrt{4-x} dx$

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488. Evaluate the following integral: $\int_1^5 \frac{x}{\sqrt{2x-1}} dx$

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489. Evaluate the following integral: $\int_0^1 \tan^{-1} x dx$

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490. Evaluate the following integral: $\int_0^1 \tan^{-1} \left(\frac{2x}{1-x^2} \right) dx$

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491. Evaluate the following integral: $\int_0^1 \frac{1-x}{1+x} dx$

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492. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin^2 x}{(1 + \cos x)^2} dx$

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493. Evaluate the following integral: $\int_0^{\pi/2} \frac{\cos x}{1 + \sin^2 x} dx$

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494. Evaluate the following integrals: $\int_0^1 \sqrt{\frac{1-x}{1+x}} dx$

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495. Evaluate the following integral: $\int_0^{\pi/4} \cos^4 x \sin^3 x \, dx$

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496. Evaluate the following integral: $\int_0^{\pi/2} x^2 \cos 2x \, dx$

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497. Evaluate the following integral: $\int_2^4 \frac{x^2 + x}{\sqrt{2x + 1}} \, dx$

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498. $\int_0^1 (\cos^{-1} x)^2 \, dx$

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499. Evaluate the following integral: $\int_1^2 x \sqrt{3x-2} dx$

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500. Evaluate the following integral: $\int_0^1 \cos^{-1} x dx$

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501. Evaluate the following integral: $\int_0^1 \cos^{-1} \left(\frac{1-x^2}{1+x^2} \right) dx$

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502. Evaluate the following integral: $\int_0^{1/\sqrt{3}} \tan^{-1} \left(\frac{3x-x^3}{1-3x^2} \right) dx$

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503. If $\int_0^{\frac{\pi}{3}} \frac{\cos x}{3 + 4 \sin x} dx = k \log \left(\frac{3 + 2\sqrt{3}}{3} \right)$, then k is equal to

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504. Evaluate the following integral: $\int_0^{\pi/2} \frac{\sin x}{\sqrt{1 + \cos x}} dx$

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505. $\int_0^{\pi} \sin^3 x (1 + 2 \cos x)(1 + \cos x)^2 dx$

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506. Evaluate the following integral: $\int_0^{\pi/4} \sin 2x \sin 3x dx$

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507. Evaluate the following integral: $\int_1^2 \frac{1}{x^2} e^{-1/x} dx$

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508. Evaluate the following integral: $\int_0^1 \log(1+x) dx$

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509. Evaluate: $\int_0^1 x \tan^{-1} x dx$

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510. Evaluate the following integral: $\int_1^2 \frac{x+3}{x(x+2)} dx$

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511. Evaluate the following integral: $\int_0^{\pi/4} e^x \sin x \, dx$

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512. Evaluate the following integral: $\int_0^1 |2x - 1| \, dx$

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513. Evaluate the following integral: $\int_0^{\pi/2} |\sin x - \cos x| \, dx$

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514. Evaluate the following integral: $\int_1^3 |x^2 - 4| \, dx$

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515. Evaluate: $\int_{-\frac{1}{2}}^{\frac{1}{2}} \cos x \log\left(\frac{1-x}{1+x}\right) dx$

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516. By using the properties of definite integrals, evaluate the integrals

$$\int_0^a \frac{\sqrt{x}}{\sqrt{x} + \sqrt{a-x}} dx$$

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517. Evaluate $\int_0^{\pi} \frac{x \sin x}{1 + \cos^2 x} dx$

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518. $\int_0^{\pi} \frac{x}{a^2 \cos^2 x + b^2 \sin^2 x} dx$

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519. Evaluate the following integral: $\int_0^{15} [x^2] dx$

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520. Evaluate: $\int_0^{\frac{\pi}{2}} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$

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521. Evaluate: $\int_0^{\pi} \frac{x \tan x}{\sec x + \tan x} dx$

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522. Evaluate the following integral: $\int_0^{\pi} \cos 2x \log \sin x dx$

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523. Evaluate the following integral: $\int_{-\pi}^{\pi} x^{10} \sin^7 x dx$



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524. Evaluate the following integral: $\int_0^{\pi} \frac{dx}{6 - \cos x}$



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525. Evaluate the following integral: $\int_0^{\pi/4} \tan^2 x \, dx$



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526. Evaluate the following integral: $\int_1^3 |x^2 - 2x| \, dx$



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527. Evaluate the following integral: $\int_0^1 |\sin 2\pi x| \, dx$



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528. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \sin^9 x \, dx$

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529. Evaluate the following integral: $\int_0^{2\pi} \cos^7 x \, dx$

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530. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \tan^3 x} \, dx$

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531. Evaluate the following integral: $\int_0^{\pi} x \sin x \cos^4 x \, dx$

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532. Evaluate the following integral: $\int_{-\pi/4}^{\pi/4} |\tan x| dx$

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533. Evaluate the following integral: $\int_0^{\pi} \frac{x}{1 + \cos \alpha \sin x} dx$

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534. Evaluate the following integral: $\int_0^{\pi/2} (\cos^2 x) dx$

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535. Evaluate the following integral: $\int_{-\pi}^{\pi} x^{10} \sin^7 x dx$

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536. Evaluate the following integral: $\int_0^{\pi} \frac{dx}{6 - \cos x}$

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537. Evaluate the following integral: $\int_0^{\pi/4} \tan^2 x \, dx$

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538. Evaluate the following integral: $\int_1^3 |x^2 - 2x| \, dx$

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539. Evaluate the following integral: $\int_0^1 |\sin 2\pi x| \, dx$

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540. Evaluate the following integral: $\int_{-\pi/2}^{\pi/2} \sin^9 x \, dx$

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541. Evaluate the following integrals: $\int_0^{\pi} \left(\frac{x}{1 + \sin^2 x} + \cos^7 x \right) dx$

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542. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{1 + \tan^3 x} dx$

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543. Evaluate the following integral: $\int_0^{\pi} x \sin x \cos^4 x \, dx$

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544. Evaluate the following integral: $\int_{-\pi/4}^{\pi/4} |\tan x| dx$

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545. Evaluate the following integral: $\int_0^{\pi} \frac{x}{1 + \cos \alpha \sin x} dx$

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546. Evaluate the following integral: $\int_0^{\pi/2} \frac{\cos^2 x}{\sin x + \cos x} dx$

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547. Evaluate $\int_0^{\pi} \frac{x}{a^2 - \cos^2 x} dx$

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548. The value of $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x} + \sqrt{x}} dx$ is $-\frac{1}{2}$.

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549. Evaluate the following integral: $\int_0^{\pi/2} \frac{x}{\sin^2 x + \cos^2 x} dx$

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550. $\int_0^1 \cot^{-1}(1 - x + x^2) dx$

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551. Evaluate the following integral: $\int_0^{\pi/2} \frac{1}{2 \cos x + 4 \sin x} dx$

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552. Evaluate the following integral: $\int_{\pi/6}^{\pi/2} \frac{\cos ec x \cot x}{1 + \cos ec^2 x} dx$

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553. Evaluate the following integral: $\int_0^{\pi/2} \frac{dx}{4 \cos x + 2 \sin x}$

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554. Evaluate the following definite integrals : $\int_0^4 x dx$

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555. Evaluate the following definite integrals : $\int_1^4 (x^2 + x) dx$

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556. Evaluate $\int 1 + e^x dx$

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557. Evaluate the following definite integrals: $\int_1^3 (x^2 + 3x) dx$

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558. Evaluate the following definite integrals : $\int_0^2 (2x^2 + 3) dx$

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559. Evaluate the following definite integrals: $\int_{-1}^1 (e^{2x} dx)$

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560. Evaluate: $\int_1^3 (2x^2 + 5x) dx$

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561. Evaluate the following definite integrals: $\int_0^2 (x^2 + 2) dx$

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562. Evaluate the following definite integrals: $\int_0^3 (x^2 + 1) dx$

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