MATHS

BOOKS - RD SHARMA MATHS (ENGLISH)

MAXIMA AND MINIMA

Others

1. Find the coordinates of a point on the parabola $y = x^2 + 7x + 2$ which is closest to

the straight line $y = 3x - 3$.

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2. Find the points of local maxima or local minima, if any, of the following function, using the first derivative test. Also, find the local maximum or local minimum values, as the case may be: $f(x) = \frac{x}{2} + \frac{2}{x}, x > 0$

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3. An open tank is to be constructed with square base and vertical sides so as to contain a given quantity of water. Show that the expenses of lining with lead will be least, if depth is made half of width.

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4. Find the points of local maxima or local minima, if any, of the following function, using the first derivative test. Also, find the local

maximum or local minimum values, as the case may be: $f(x) = \sin 2x - x, \ -\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$

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5. Find the maximum slope of the curve $y = -x^3 + 3x^2 + 2x - 27$.

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6. The total cost of producing x radio sets per day is $Rs\frac{x^2}{4}35x + 25$ and the price per set at

which they may be sold is $Rs50 - \frac{x}{2}$. Find the daily output to maximize the total profit.

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7. A box of constant volume c is to be twice as long as it is wide. The material on the top and four sides cost three times as much per square metre as that in the bottom. What are the most economic dimensions?

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8. The sum of the surface areas of a sphere and a cube is given. Show that when the sum of their volumes is least, the diameter of the sphere is equal to the edge of the cube.

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9. Find the maximum and the minimum values, if any, without using derivatives of the following functions: $f(x) = |x + 2|$ on R

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10. Find the maximum and the minimum values, if any, without using derivatives of the following functions: $f(x) = 4x^2 - 4x + 4$ on R

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11. Show that the maximum volume of the cylinder which can be inscribed in a sphere of radius $5\sqrt{3}cm$ is $500\pi cm^3$.

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12. Find the maximum and the minimum values, if any, without using derivatives of the following functions: $f(x) = 2x^3 + 5$ on R

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13. Find the points of local maxima or local minima and corresponding local maximum and local minimum values of each of the given function. Also, find the points of inflection, if any : $f(x) = xe^x$

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14. Find the points of local maxima or local minima and corresponding local maximum and local minimum values of each of the following functions. Also, find the points of inflection, if any :

$f(x) = x^4 - 62x^2 + 120x + 9$

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15. The function $y = a\log x + bx^2 + x$ has extreme values at x=1,2.Find a and b

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16. Find the absolute maximum and the absolute minimum values of the following function in the given intervals:

$f(x) = (x-2)\sqrt{x-1}$ in $[1, 9]$

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17. A rectangle is inscribed in a semi-circle of radius r with one of its sides on diameter of semi-circle. Find the dimensions of the rectangle so that its area is maximum. Find also the area.

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18. A large window has the shape of a rectangle surmounted by an equilateral triangle. If the perimeter of the window is 12 metres find the dimensions of the rectangle

that will produce the largest area of the window.

19. Find the largest possible area of a right angled triangle whose hypotenuse is 5cm long.

20. A closed cylinder has volume $2156cm^3$. What will be the radius of its base so that its total surface area is minimum?

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21. Find the points of local maxima or local minima, if any, of the following function, using the first derivative test. Also, find the local maximum or local minimum values, as the case may be: $f(x) = x^3(x-1)^2$

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22. Show that among all positive numbers x and y with $x^2 + y^2 = r^2$, the sum $x + y$ is largest when $x = y = \dfrac{r}{\sqrt{2}}$.

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23. Find the points of local maxima or local minima, if any, of the following function, using the first derivative test. Also, find the local

maximum or local minimum values, as the case may be: $f(x) = (x-5)^4$

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24. Prove that the semi-vertical angle of the right circular cone of given volume and least curved surface is $\cot^{-1}(\sqrt{2})$.

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25. Show that the cone of the greatest volume which can be inscribed in a given sphere has an altitude equal to 2/3 of the diameter of the sphere.

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26. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = (x-1)(x+2)^2$

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27. Find the points of local maxima or local minima, if any, of the following function, using the first derivative test. Also, find the local maximum or local minimum values, as the case may be: `f(x)=cosx ,0

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28. Determine the points on the curve $x^2 = 4y$ which are nearest to the point (0,5).

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29. The total area of a page is $150cm^2$. The combined width of the margin at the top and bottom is $3cm$ and the side 2cm. What must be the dimensions of the page in order that the area of the printed matter may be maximum?

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30. A straight line is drawn through a given point $P(1, 4)$. Determine the least value of the sum of the intercepts on the coordinate axes.

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31. The strength of a beam varies as the product of its breadth and square of its depth. Find the dimensions of the strongest beam which can be cut from a circular log of radius a.

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32. The given quantity of metal is to be cost into a half cylinder with a rectangular base and semicircular ends. Show that in order that the total surface area may be minimum, the ratio of the length of the cylinder to the diameter of its semi-circular ends is $\pi : (\pi + 2)$.

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33. A particle is moving in a straight line such that its distance s at any time t is given by $s = \frac{t^4}{4} - 2t^3 + 4t^2 - 7$. Find when its velocity is maximum and acceleration minimum.

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34. A wire of length 20m is to be cut into two pieces. One of the places will be bent into shape of a square and the other shape of an

equilateral triangle. Where the wire should be cut so that the sum of the areas of the square and triangle is minimum?

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35. A beam is supported at the two ends and is uniformly loaded. The bending moment M at a distance x from one end is given by $M = \frac{WL}{2}x - \frac{W}{2}x^2$ $M = \frac{Wx}{3} - \frac{W}{3}\frac{x^3}{L^2}$ Find the point at which M is maximum in each case.

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36. Determine two positive numbers whose sum is 15 and the sum of whose squares is minimum.

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37. Show that the right circular cylinder, open at the top, and of given surface area and maximum volume is such that its height is equal to the radius of the base.

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38. Find the volume of the largest cylinder that can be inscribed in a sphere of radius rcm.

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39. A rectangular sheet of fixed perimeter with sides having their lengths in the ratio $8:15$ is converted into anopen rectangular box by folding after removing squares of equal area

from all four corners. If the total area of removed squares is 100, the resulting box has maximum volume. Then the length of the sides of the rectangular sheet are 24 (b) 32 (c) 45 (d) 60

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40. A square piece of tin of side 18 cm is to be made into a box without top, by cutting a square from each corner and folding up the flaps to form the box. What should be the side

of the square to be cut off so that the volume of the box is the maximum possible?

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41. Find both the maximum and the minimum value of $3x^4 - 8x^3 + 12x^2 - 48x + 1$ on the interval $[1, 4]$.

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42. Show that $f(x) = \sin x(1 + \cos x)$ is maximum at $x = \frac{\pi}{3}$ in the interval $[0, \pi]$.

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43. Show that the triangle of maximum area that can be inscribed in a given circle is an equilateral triangle.

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44. The sum of the surface areas of a cuboid with sides x, $2x$ and $\frac{x}{3}$ and a sphere is given to be constant. Prove that the sum of their volumes is minimum, if x is equal to three times the radius of sphere. Also find the minimum value of the sum of their volumes.

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45. Find the maximum and minimum value of $f(x) = \sin x + \frac{1}{2}\cos 2\xi n\left[0, \frac{\pi}{2}\right]$.

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46. Prove that $f(x) = \sin x + \sqrt{3}\cos x$ has maximum value at $x = \frac{\pi}{6}$.

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47. Find the difference between the greatest and least values of the function $f(x) = \sin 2x - x on\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$.

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48. Find the maximum and minimum values of $f(x) = x^{50} - x^{20}$ in the interval $[0, 1]$.

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49. If $f(x) = a\log|x| + bx^2 + x$ has extreme values at $x = -1 \, and \, at \, x = 2,$ then find a and b .

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50. At what points, the slope of the curve $y = -x^3 + 3x^2 + 9x - 27$ is maximum? Also, find the maximum slope.

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51. Show that the maximum value of $\left(\frac{1}{x}\right)^x$ is $e^{\frac{1}{e}}$.

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52. If $y = \frac{ax - b}{(x-1)(x-4)}$ has a turning point $P(2, -1)$, find the value of a and b.

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53. A metal box with a square base and vertical sides is to contain 1024 cm3 of water, the material for the top and bottom costs Rs 5 per cm2 and the material for the sides costs Rs 2.50 per cm2. Find the least cost of the box.

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54. OR An open box with a square base is to be made out of a given quantity of cardboard of area c^2 square units. Show that the maximum volume of the box is $\frac{c^3}{6\sqrt{3}}$ cubic units.

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55. Find the point on the curve $y^2 = 4x$ which is nearest to the point (2, 1).

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56. A telephone company in a town has 500 subscribers on its list and collects fixed charges of Rs. 300 per subscriber. The company proposes to increase the annual subscription and it is believed that every increase of Rs. 1 one subscriber will discontinue the services. Find what increase will bring maximum revenue?

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57. The maximum value of $f(x) = \frac{x}{4 - x + x^2}$ on $[-1, 1]$ is (a) $\frac{1}{4}$ (b) $-\frac{1}{3}$ (c) $\frac{1}{6}$ (d) $\frac{1}{5}$

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58. The function $f(x) = \sum_{r=1}^{5} (x - r)^2$ assuming minimum value at $x =$ (a)5 (b) $\frac{5}{2}$ (c)3 (d)2

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59. The least value of the function $f(x) = x^3 - 18x^2 + 96x$ in the interval $[0, 9]$ is 126 (b) 135 (c) 160 (d) 0

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60. The maximum value of $x^{\frac{1}{x}}, x > 0$ is (a)$e^{\frac{1}{e}}$ (b) $\left(\frac{1}{e}\right)^e$ (c) 1 (d) none of these

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61. Let

$f(x) = (x-a)^2 + (x-b)^2 + (x-c)^2.$

Then, $f(x)$ has a minimum at $x = \dfrac{a+b+c}{3}$

(b) $\dfrac{1}{2}$ (c) $\dfrac{1}{8}$ (d) none of these

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62. Show that of all the rectangles inscribed in a given fixed circle, the square has the maximum area.

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63. AB is a diameter of a circle and C is any point on the circumference of the circle. Then a) the area of ABC is maximum when it is isosceles b) the area of ABC is minimum when it is isosceles c) the perimeter of ABC is minimum when it is isosceles d) none of these

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64. Find the points of local maxima and local minima, if any, $y = 3x^3 + 12x^2 + 7$. Find also

the local maximum and local minimum values, as the case may be:

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65. Find the local maximum and local minimum value of $f(x) = \sec x + \log \cos^2 x, 0 < x < 2\pi$

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66. Amongst all pairs of positive numbers with product 256, find those whose sum is the least.

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67. Find two positive numbers whose sum is 14 and the sum of whose squares in minimum.

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68. A beam is supported at the two ends and is uniformly loaded. The bending moment M at a distance x from one end is given by (i) $M = \frac{WL}{2}x - \frac{W}{2}x^2$ (ii) $M = \frac{Wx}{3} - \frac{W}{3}\frac{x^3}{L^2}$ Find the point at which M is maximum in each case.

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69. Show that all the rectangles with a given perimeter, the square has the largest area.

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70. Find all the points of local maxima and local minima of the function $f(x) = x^3 - 6x^2 + 12x - 8.$

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71. Show that the function $f(x) = 4x^3 - 18x^2 + 27x - 7$ has neither maxima nor minima.

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72. Find all the points of local maxima and minima and the corresponding maximum and minimum values of the function $f(x) = -\frac{3}{4}x^4 - 8x^3 - \frac{45}{2}x^2 + 105$.

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73. Find all the points of local maxima and minima and the corresponding maximum and

minimum values of the function $f(x) = 2x^3 - 21x^2 + 36x - 20.$

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74. Find the points of local maxima, local minima and the points of inflection of the function $f(x) = x^5 - 5x^4 + 5x^3 - 1.$ Also, find the corresponding local maximum and local minimum values.

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75. Find the point of local maxima or local minima of the function

$$f(x) = \left(\sin^4 x + \cos^4 x\right) \quad \text{in} \quad 0 < x < \frac{\pi}{2}$$

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76. Prove that the area of right-angled triangle of given hypotenuse is maximum when the triangle is isosceles.

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77. Show that the total surface area of a closed cuboid with square base and given volume is minimum, when it is a cube.

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78. Find the maximum and the minimum values, if any, of the following functions $f(x) = 3x^2 + 6x + 8, x \in R$

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79. Find the maximum and the minimum values, if any, of the following functions $f(x) = -|x-1| + 5f \text{ or } allx \in R$

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80. Find the maximum and the minimum values, if any, of the following functions $f(x) = \sin 3x + 4, x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$

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81. Find the maximum and the minimum values, if any, of the following functions f(x)=|x+3| for all $x \in R$.

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82. A rectangle is inscribed in a semi-circle of radius r with one of its sides on diameter of semi-circle. Find the dimensions of the rectangle so that its area is maximum. Find also the area.

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83. A wire of length 36m is to be cut into two pieces. One of the pieces is to be made into a square and the other into a circle. What should be the lengths of the two pieces, so that the combined area of the square and the circle is minimum?

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84. Find the maximum and the minimum values of $f(x) = 3x^2 + 6x + 8, \quad x \in R$, if any.

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85. Find the maximum and the minimum values of $f(x) = -|x - 1| + 5$ for all $x \in R$, if any.

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86. Find the maximum and the minimum values of $f(x) = \sin 3x + 4, \quad x \in (-\pi/2, \pi/2)$, if any.

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87. Find the maximum and the minimum values of $f(x) = x^3 + 1$ for all $x \in R$, if any.

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88. Find the maximum and the minimum values of $f(x) = \sin(\sin x)$ for all $x \in R$, if any.

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89. Find the maximum and the minimum values of $f(x) = |x + 3|$ for all $x \in R$, if any.

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90. Find the maximum and minimum values of $f(x) = 4x^2 - 4x + 4$ on R, if any, without using derivatives.

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91. Find the maximum and minimum values of $f(x) = -(x-1)^2 + 2$ on R, if any, without using derivatives.

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92. Find the maximum and minimum values of $f(x) = |x + 2|$ on R, if any, without using derivatives.

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93. Find the maximum and minimum values of $f(x) = \sin 2x + 5$ on R, if any, without using derivatives.

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94. Find the maximum and minimum values of $f(x) = |\sin 4x + 3|$ on R, if any, without using derivatives.

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95. Find the maximum and minimum values of $f(x) = 2x^3 + 5$ on R, if any, without using derivatives.

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96. Find the maximum and minimum values of $f(x) = -|x+1|+3$ on R, if any, without using derivatives.

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97. Find the maximum and minimum values of $f(x) = 16x^2 - 16x + 28$ on R, if any, without using derivatives.

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98. Find the maximum and minimum values of $f(x) = x^3 - 1$ on R, if any, without using derivatives.

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99. Find all the points of local maxima and minima of the function $f(x) = x^3 - 6x^2 + 9x - 8$.

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100. Find all the points of local maxima and local minima as well as the corresponding local maximum and local minimum values for the function $f(x) = (x-1)^3(x+1)^2$.

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101. Find all the points of local maxima and local minima of the function $f(x) = x^3 - 6x^2 + 12x - 8$.

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102. Show that the function $f(x) = 4x^3 - 18x^2 + 27x - 7$ has neither maxima nor minima.

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103. Find the points of local maxima, local minima and the points of inflection of the function $f(x) = x^5 - 5x^4 + 5x^3 - 1$. Also, find the corresponding local maximum and local minimum values

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104. Find the local maxima or local minima, if any, of the function `f(x)=sinx+cosx ,\ \ 0

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105. Find the local maximum or local minimum, if any, of the function f(x)=$\sin^4 x + \cos^4 x$, where x belongs to $\left[0, \quad \frac{\pi}{2}\right]$

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106. Find the points at which the function f given by $f(x) = (x-2)^4(x+1)^3$has(i) local maxima (ii) local minima (iii) point of inflexion

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107. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = (x-5)^4$

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108. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = x^3 - 3x$

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109. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = x^3(x-1)^2$

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110. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = (x-1)(x+2)^2$

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111. Find the points of local maxima or local minima, if any, using first derivative test, and

local maximum or local minimum of $f(x) = \frac{1}{x^2 + 2}$

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112. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = x^3 - 6x^2 + 9x + 15$

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113. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = \sin 2x, 0 < x < \pi$

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114. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = \sin x - \cos x\ , x \in (0, 2\pi)$

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115. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = \cos x$, x belongs to $(0, \pi)$

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116. Find the points of local maxima or local minima, if any, using first derivative test, and

local maximum or local minimum of $f(x) = \sin 2x - x, \quad -\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$

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117. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = \sin 2x, \ 0 < x < \pi$

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118. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = x\sqrt{1-x}, \quad x > 0$

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119. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = x^3(2x-1)^3$

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120. Find the points of local maxima or local minima, if any, using first derivative test, and local maximum or local minimum of $f(x) = \frac{x}{2} + \frac{2}{x}, \quad x > 0$

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121. Find all the points of local maxima and minima and the corresponding maximum and

minimum values of the function $f(x) = -\frac{3}{4}x^4 - 8x^3 - \frac{45}{2}x^2 + 105$.

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122. Find all the points of local maxima and minima and the corresponding maximum and minimum values of the function $f(x) = 2x^3 - 21x^2 + 36x - 20$.

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123. Find the points of local maxima and local minima, if any, and local maximum and local minimum values of $f(x) = \sin 2x - x$, where `-pi/2

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124. Find maximum and minimum values of $f(x) = \sin x + \frac{1}{2}\cos 2x$, where `0

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125. Find the points of local maxima and local minima, if any, and local maximum and local minimum values of $f(x) = \sin^4 x + \cos^4 x$, `0

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126. Find the points of local maxima or local minima, if any, and local maximum or local minimum values of $f(x) = \sin x + \cos x$, where `0

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127. Find the points of local maxima and local minima, if any, and local maximum and local minimum values of $f(x) = \sin x - \cos x$,where $0 < x < 2\pi$

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128. Find the points of local maxima and local minima, if any, and local maximum and local minimum values of $f(x) = \sin 2x$, where $0 < x < \pi$

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129. Find the second order derivative of $f(x) = 2\cos x + x$ with respect to x

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130. Find the points of local maxima and local minima, if any, and local maximum and local minimum values of $f(x) = 2\sin x - x$, $-\frac{\pi}{2} < x < \frac{\pi}{2}$

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131. Find the local maximum and local minimum values of $f(x) = \sec x + \log \cos^2 x, \quad 0 < x < 2\pi$

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132. Show that none of the following functions has a local maximum or a local minimum: $x^3 + x^2 + x + 1$ (ii) e^x

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133. Show that none of the following functions has a local maximum or a local minimum: $\log x$

(ii) $\cos x, \quad 0 < x < \pi$

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134. Find the maximum profit that a company can make, if the profit function is given $P(x) = 41 + 24x - 18x^2$.

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135. At what points, the slope of the curve $y = -x^3 + 3x^2 + 9x - 27$ is maximum.

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136. If $f(x) = a\log|x| + bx^2 + x$ has extreme values at $x = -1$ and at $x = 2$, then find a and b.

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137. It is given that at $x = 1$, the function $x^4 - 62x^2 + ax + 9$ attains its maximum value on the interval $[0,\ 2]$. Find the value of a .

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138. If $y = \frac{ax - b}{(x-1)(x-4)}$ has a turning point $P(2,\ -1)$, find the values of a and b and show that y is maximum at P .

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139. Show that the maximum value of $\left(\frac{1}{x}\right)^x$ is $e^{1/e}$.

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140. Show that $\sin^p\theta\cos^q\theta$ attains a maximum, when $\theta = \tan^{-1}\sqrt{\frac{p}{q}}$.

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141. Find the points of local maxima or minima and corresponding local maximum and minimum values of $f(x) = x^4 - 62x^2 + 120x + 9$. Also, find the points of inflection, if any:

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142. Find the points of local maxima or minima and corresponding local maximum and minimum values of

$f(x) = x^3 - 6x^2 + 9x + 15$. Also, find the points of inflection, if any:

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143. Find the points of local maxima or minima and corresponding local maximum and minimum values of $f(x) = (x-1)(x+2)^2$. Also, find the points of inflection, if any:

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144. Find the points of local maxima or minima and corresponding local maximum and minimum values of $f(x) = x^5 - 5x^4 + 5x^3 - 1$

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145. Find the points of local maxima or minima and corresponding local maximum and minimum values of $f(x) = x\, e^x$. Also, find the points of inflection, if any:

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146. Find the points of local maxima or minima and corresponding local maximum and minimum values of $f(x) = x/2 + 2/x, \quad x > 0$. Also, find the points of inflection, if any:

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147. Find the points of local maxima or minima and corresponding local maximum and

minimum values of $f(x) = (x+1)(x+2)^{1/3}, \ x \geq -2$. Also, find the points of inflection, if any:

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148. Find the points of local maxima or minima and corresponding local maximum and minimum values of $f(x) = x\sqrt{32 - x^2}, \ -5 \leq x \leq 5$. Also, find the points of inflection, if any:

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149. Find the points of local maxima or minima and corresponding local maximum and minimum values of $f(x) = x\sqrt{1-x}, \quad x \leq 1$, $x > 0, \quad x \in R$. Also, find the points of inflection, if any:

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150. Find the points of local maxima or minima and corresponding local maximum and minimum values of

$f(x) = x + \frac{a^2}{x}, \quad a > 0, \quad x \neq 0$. Also, find the points of inflection, if any:

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151. Find the points of local maxima or minima and corresponding local maximum and minimum values of $f(x) = x\sqrt{2 - x^2} - \sqrt{2} \leq x \leq \sqrt{2}$. Also, find the points of inflection, if any:

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152. Find the points of local maxima or minima and corresponding local maximum and minimum values of $f(x) = x + \sqrt{1-x}, \quad x \leq 1$

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153. Find the local extremum values of the following functions: $f(x) = (x-1)(x-2)^2$

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154. The function $y = a\log x + bx^2 + x$ has extreme values at $x = 1$ and $x = 2$. Find a and b.

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155. Show that $\frac{\log x}{x}$ has a maximum value at $x = e$.

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156. Find the maximum and minimum values of the function $f(x) = \dfrac{4}{x+2} + x$.

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157. Find the maximum and minimum values of the function $f(x) = \tan x - 2x$.

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158. If $f(x) = x^3 + ax^2 + bx + c$ has a maximum at $x = -1$ and minimum at $x = 3$. Determine a, b and c.

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159. Prove that $f(x) = \sin x + \sqrt{3}\cos x$ has maximum value at $x = \frac{\pi}{6}$.

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160. Find the maximum and minimum values of $f(x) = 2x^3 - 24x + 107$ in the interval $[1,\ 3]$.

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161. Find the second order derivative of $f(x) = \sin x$ with respect to x .

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162. Find the maximum and minimum values of $f(x) = \sin x + \frac{1}{2}\cos 2x$ in $\left[0, \frac{\pi}{2}\right]$.

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163. Find the maximum and minimum values of $f(x) = x^{50} - x^{20}$ in the interval $[0, 1]$.

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164. Find the maximum and minimum values of $f(x) = x + \sin 2x$ in the interval $[0,\ 2\pi]$

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165. Find the difference between the greatest and least values of the function $f(x) = \sin 2x - x$ on $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$.

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166. Show that $f(x) = \sin x(1 + \cos x)$ is maximum at $x = \frac{\pi}{3}$ in the interval $[0,\ \pi]$.

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167. Find the absolute maximum value and the absolute minimum value of $f(x) = (1/2 - x)^2 + x^3$ in $[-2,\ 2.5]$

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168. Find the absolute maximum value and the absolute minimum value of $f(x) = \sin x + \cos x$ in $[0,\ \pi]$

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169. Find both the maximum and the minimum value of $3x^4 - 8x^3 + 12x^2 - 48x + 1$ on the interval $[1, 4]$.

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170. Find the absolute maximum and absolute minimum values of $f(x) = 4x - \frac{x^2}{2}$ in $[-2,\ 4.5]$

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171. Find the absolute maximum and absolute minimum values of $f(x) = (x-1)^2 + 3$ in $[-3,\ 1]$

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172. Find the absolute maximum and absolute minimum values of $f(x) = 3x^4 - 8x^3 + 12x^2 - 48x + 25$ in $[0,\ 3]$

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173. Find the absolute maximum and the absolute minimum values of the following function in the given intervals: $f(x) = (x-2)\sqrt{x-1}$ in $[1, 9]$

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174. Find the maximum value of $2x^3 - 24x + 107$ in the interval $[1,\ 3]$.

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175. Find the absolute maximum and minimum values of the function f given by $f(x) = \cos^2 x + \sin x\ , x \in [0,\ \pi]$.

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176. Find absolute maximum and minimum values of a function f given by $f(x) = 12x^{4/3} - 6x^{1/3}, \quad x \in [-1, 1]$.

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177. Find the absolute maximum and minimum values of a function f given by $f(x) = 2x^3 - 15x^2 + 36x + 1$ on the interval $[1, 5]$.

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178. Find two numbers whose sum is 24 and whose product is as large as possible.

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179. Find two positive numbers x and y such that $x + y = 60$ and xy^3 is maximum.

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180. Find two positive numbers x and y such that their sum is 35 and the product x^2y^5 is a maximum.

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181. Amongst all pairs of positive numbers with product 64, find those whose sum is the least.

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182. Find two positive numbers whose sum is 14 and the sum of whose squares is minimum.

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183. Find the second order derivative of $x^{19} + \cos x$ with respect to x

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184. Find the second order derivative of $f(x) = x^7 + \tan x$ with respect to x

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185. Find the minimum value of $ax + by$, where $xy = c^2$ and $a,\ b,\ c$ are positive.

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186. Show that all the rectangles with a given perimeter, the square has the largest area.

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187. Show that of all the rectangles of given area, the square has the smallest perimeter.

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188. Show that of all the rectangles inscribed in a given circle, the square has the maximum area.

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189. Find the second order derivative of $f(x) = (\tan x)^2$ with respect to x

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190. Find the second order derivative of x^{100} with respect to x

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191. Find the derivative of $x^2 + y^2 = a^2$ with respect to x .

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192. Find the derivative of $x^3 + y^3 = \sin x$ with respect to x .

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193. Find the derivative of $x^4 + y^4 = \cos x$ with respect to x

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194. Show that the surface area of a closed cuboid with square base and given volume is minimum, when it is a cube.

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195. Find the derivative of $x + y^6 = \tan x$ with respect to x

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196. Find the derivative of $\tan(x+y) = y^3$ with respect to x

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197. Find the derivative of $x^2 + y^3 = \sin 2x$ with respect to x

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198. Find the derivative of $xy + y^2 = \sin x$ with respect to x

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199. Find the second order derivative of $x^2 y$ with respect to x

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200. Find the second order derivative of x^{10} with respect to x

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201. Find the second order derivative of $x^3 y = 8$ with respect to x

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202. Find the second order of $x + 2y^2$ with respect to x

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203. Find the derivative of $e^x \tan x$ with respect to x

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204. Find the derivative of $e^x \log x$ with respect to x

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205. Find the derivative of $e^x . x$ with respect to x

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206. Show that the height of a closed right circular cylinder of given surface and maximum volume, is equal to the diameter of its base.

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207. Find $\frac{dy}{dx}$ if $x^3 + xy + y^3 = 40$

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208. Find the derivative of $e^x . \tan x$ with respect to x .

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209. Find the derivative of $\tan^{-1} \sqrt{x}$ with respect to x .

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210. Find the derivative of $\sin^{-1}(x)$ with respect to x

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211. Find the derivative of $e^{\sin x}.\cos x$ with respect to x

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212. Find the derivative of $\log x . e^x$ with respect to x

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213. Find the derivative of $e^{\log x}$ with respect to x

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214. Find the derivative of $xy = x + \sin y$ with respect to x

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215. Find the derivative of $xy = \sin x + y$ with respect to x

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216. Find the derivative of x^{1000} with respect to x

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217. Find the point on the curve $y^2 = 4x$ which is nearest to the point $(2,\ 1)$.

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218. A jet of enemy is along the curve $y = x^2 + 2$ and a soldier is placed at (3,2).Find the minimum distance between the jet and soldier.

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219. The shortest distance between line $y - x = 1$ and curve $x = y^2$ is (a) $\frac{3\sqrt{2}}{8}$ (b) $\frac{8}{3\sqrt{2}}$ (c) $\frac{4}{\sqrt{3}}$ (d) $\frac{\sqrt{3}}{4}$

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220. Find the shortest distance of the point (0, c) from the parabola $y = x^2$, where $0 \leq c \leq 5$.

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221. Find the derivative of the function $\left(\frac{x^2}{a^2}\right) + \left(\frac{y^2}{b^2}\right) = 1$ with respect to x

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222. Find the derivative of the function $\frac{x}{a^2} + \frac{y}{b^2} = 1$ with respect to x

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223. Find the differentiation of $x = \sin y + y$ with respect to x

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224. Find the second order derivative of $x^{1000} + 5x$ with respect to x

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225. Divide 64 into two parts such that the sum of the cubes of two parts is minimum.

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226. Find the second order derivative of $e^{\sin x}$ with respect to x

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227. Divide 15 into two parts such that product of square of one part and cube of other is maximum

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228. Find the derivative of $x^{\tan x}$ with respect to x

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229. A beam is supported at the two ends and is uniformly loaded. The bending moment M at a distance x from one end is given by $M = \frac{WL}{2}x - \frac{W}{2}x^2$. Find the point at which M is maximum.

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230. A beam is supported at the two ends and is uniformly loaded. The bending moment M at a distance x from one end is given by $M = \frac{Wx}{3} - \frac{W}{3}\frac{x^3}{L^2}$. Find the point at which M is maximum.

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231. Find $\frac{dy}{dx}$ if $x^2y = e^y$

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232. Find the derivative of $xy = e^x$ with respect to x

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233. Find the derivative of $xy = e^y$ with respect x

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234. Find the largest possible area of a right angled triangle whose hypotenuse is 5 cm long.

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235. Find the derivative of $e^y + y = \sin x$ with respect to x

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236. Find the derivative of $\sin x . e^x$ with respect to x

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237. Find $\frac{dy}{dx}$ if $y = \sin 2x . e^x$

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238. Find $\frac{dy}{dx}$ if $y = \log x . e^x$

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239. Find $\frac{dy}{dx}$ if $y = \frac{\sin x}{\cos x}$

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240. Find $\frac{dy}{dx}$ if $y = \frac{\cos x}{x}$

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241. Show that the height of the cylinder of maximum volume that can be inscribed in a

sphere of radius R is $\frac{2R}{\sqrt{3}}$.

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242. Find $\frac{dy}{dx}$ if $y = \frac{\tan x}{\sin x}$

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243. Prove that a conical tent of given capacity will require the least amount of canvas when the height is $\sqrt{2}$ times the radius of the base.

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244. Find $\frac{dy}{dx}$ if $y = \frac{x + \sin x}{\cos x}$

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245. Prove that the semi-vertical angle of the right circular cone of given volume and least curved surface is $\cot^{-1}\left(\sqrt{2}\right)$.

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246. An isosceles triangle of vertical angle 2θ is inscribed in a circle of radius a . Show that the area of the triangle is maximum when $\theta = \frac{\pi}{6}$.

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247. Prove that the least perimeter of an isosceles triangle in which a circle of radius r can be inscribed is $6\sqrt{3}r$

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248. Find the dimensions of the rectangle of perimeter 36cm which will sweep out a volume as large as possible when revolved about one of its sides.

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249. Find $\frac{dy}{dx}$ if $y = \frac{\tan x}{\sec x}$

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250. Find $\frac{dy}{dx}$ if $y = \frac{\log x}{e^x}$

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251. Find $\frac{dy}{dx}$ if $y = \frac{e^x}{x}$

Watch Video Solution

252. Find $\frac{dy}{dx}$ if $x^2 + y^2 = r^2$.

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253. Find $\frac{dy}{dx}$ if $x^2 = 4y$

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254. Find $\frac{dy}{dx}$ if $y^2 = 4x$.

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255. Find the point on the curve $x^2 = 8y$ which is nearest to the point $(2,\ 4)$.

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256. Find the point on the parabolas $x^2 = 2y$ which is closest to the point $(0,\ 5)$.

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257. Find the coordinates of a point on the parabola $y = x^2 + 7x + 2$ which is closest to the straight line $y = 3x - 3$.

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258. Find the point on the curve $y^2 = 2x$ which is at a minimum distance from the point $(1,\ 4)$.

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259. Find $\frac{dy}{dx}$ if $y = -x^3 + 3x^2 + 2x - 27$.

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260. Find $\frac{dy}{dx}$ if $y = \frac{e^x}{\sin x}$

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261. A manufacturer can sell x items at a price of Rs. $\left(5-\frac{x}{100}\right)$ each. The cost price of x items is Rs. $\left(\frac{x}{5}+500\right)$. Find the number of items he should sell to earn maximum profit.

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262. An open tank is to be constructed with square base and vertical sides so as to contain a given quantity of water. Show that the

expenses of lining with lead will be least, if depth is made half of width.

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263. Find $\frac{dy}{dx}$ if $x + y = e^y + \sin x$

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264. The sum of the surface areas of a sphere and a cube is given. Show that when the sum

of their volumes is least, the diameter of the sphere is equal to the edge of the cube.

265. The given quantity of metal is to be cost into a half cylinder with a rectangular base and semicircular ends. Show that in order that the total surface area may be minimum, the ratio of the length of the cylinder to the diameter of its semi-circular ends is $\pi : (\pi + 2)$.

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266. Find $\frac{dy}{dx}$ if $y = x.\sin y$

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267. A straight line is drawn through a given point $P(1, 4)$. Determine the least value of the sum of the intercepts on the coordinate axes.

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268. The total area of a page is $150cm^2$. The combined width of the margin at the top and bottom is $3cm$ and the side 2cm. What must be the dimensions of the page in order that the area of the printed matter may be maximum?

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269. The space s described in time t by a particle moving in a straight line is given by

$s = t^5 - 40t^3 + 30t^2 + 80t - 250$. Find the minimum value of acceleration.

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270. A particle is moving in a straight line such that its distance s at any time t is given by $s = \frac{t^4}{4} - 2t^3 + 4t^2 - 7.$ Find when its velocity is maximum

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271. Write necessary condition for a point $x = c$ to be an extreme point of the function $f(x)$.

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272. Write sufficient conditions for a point $x = c$ to be a point of local maximum.

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273. If $f(x)$ attains a local minimum at $x = c$, then write the values of $f'(c)$ and $f''(c)$.

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274. Write the minimum value of $f(x) = x + \frac{1}{x}, \quad x > 0$

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275. Write the maximum value of $f(x) = x + \frac{1}{x}, \quad x < 0$.

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276. Write the point where $f(x) = x\,(\log)_e x$ attains minimum value.

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277. Find the least value of $f(x) = ax + \frac{b}{x}$, where $a > 0, \quad b > 0$ and $x > 0$.

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278. Write the minimum value of $f(x) = x^x$.

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279. Write the maximum value of $f(x) = x^{1/x}$.

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280. Write the maximum value of $f(x) = \frac{\log x}{x}$, if it exists.

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281. The maximum value of $x^{\frac{1}{x}}, x > 0$ is (a)$e^{\frac{1}{e}}$ (b) $\left(\frac{1}{e}\right)^e$ (c) 1 (d) none of these

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282. If $ax + \frac{b}{x} \geq c$ for all positive x where $a, b, > 0$, then $ab < \frac{c^2}{4}$ (b) $\geq \frac{c^2}{4}$ (c) $ab \geq \frac{c}{4}$ (d) none of these

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283. The minimum value of $\frac{x}{(\log)_e x}$ is e (b) $1/e$ (c) 1 (d) none of these

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284. For the function $f(x) = x + \frac{1}{x}$ $x = 1$ is a point of maximum (b) $x = -1$ is a point of minimum (c) maximum value > minimum value (d) maximum value < minimum value

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285. Let $f(x) = x^3 + 3x^2 - 9x + 2$. Then, $f(x)$ has a maximum at $x = 1$ (b) a minimum at $x = 1$ (c) neither a maximum nor a minimum at $x = -3$ (d) none of these

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286. The minimum value of $f(x) = x^4 - x^2 - 2x + 6$ is (a) 6 (b) 4 (c) 8 (d) none of these

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287. The number which exceeds its square by the greatest possible quantity is $\frac{1}{2}$ (b) $\frac{1}{4}$ (c) $\frac{3}{4}$ (d) none of these

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288. Let $f(x) = (x-a)^2 + (x-b)^2 + (x-c)^2$.

Then, $f(x)$ has a minimum at $x = \frac{a+b+c}{3}$

(b) $3\sqrt{abc}$ (c) $\frac{3}{\frac{1}{a}+\frac{1}{b}+\frac{1}{c}}$ (d) none of these

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289. The sum of two non-zero numbers is 8, the minimum value of the sum of their reciprocals is $\frac{1}{4}$ (b) $\frac{1}{2}$ (c) $\frac{1}{8}$ (d) none of these

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290. The function $f(x) = \sum_{r=1}^{5} (x - r)^2$ assuming minimum value at $x =$ (a)5 (b) $\frac{5}{2}$ (c)3 (d)2

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291. At $x = \frac{5\pi}{6}$, $f(x) = 2\sin 3x + 3\cos 3x$ is (a) 0 (b) maximum (c) minimum (d) none of these

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292. If x lies in the interval $[0,\ 1]$, then the least value of $x^2 + x + 1$ is (a) 3 (b) $3/4$ (c) 1 (d) none of these

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293. The least value of the function $f(x) = x^3 - 18x^2 + 96x$ in the interval $[0, 9]$ is 126 (b) 135 (c) 160 (d) 0

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294. The maximum value of $f(x) = \frac{x}{4 + x + x^2}$ on $[-1, 1]$ is (a) $\frac{1}{4}$ (b) $-\frac{1}{3}$ (c) $\frac{1}{6}$ (d) $\frac{1}{5}$

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295. Find the point on the curve $y^2 = 4x$ which is nearest to the point (2, 1).

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296. If $x + y = 8$, then the maximum value of xy is (a) 8 (b) 16 (c) 20 (d) 24

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297. The least and greatest values of $f(x) = x^3 - 6x^2 + 9x$ in $[0,\ 6]$, are $3,\ 4$ (b) $0,\ 6$ (c) $0,\ 3$ (d) $3,\ 6$

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298. $f(x) = \sin + \sqrt{3}\cos x$ is maximum when $x =$ $\frac{\pi}{3}$ (b) $\frac{\pi}{4}$ (c) $\frac{\pi}{6}$ (d) 0

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299. If a cone of maximum volume is inscribed in a given sphere, then the ratio of the height of the cone to the diameter of the sphere is $3/4$ (b) $1/3$ (c) $1/4$ (d) $2/3$

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300. The minimum value of $\left(x^2+\frac{250}{x}\right)$ is (a) 75 (b) 50 (c) 25 (d) 55

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301. If $f(x)=x+\frac{1}{x}, \quad x>0$, then its greatest value is -2 (b) 0 (c) 3 (d) none of these

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302. If $f(x) = \dfrac{1}{4x^2 + 2x + 1}$, then its maximum value is $\dfrac{4}{3}$ (b) $\dfrac{2}{3}$ (c) 1 (d) $\dfrac{3}{4}$

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303. Let x, y be two variables and $x > 0, \quad xy = 1$, then minimum value of $x + y$ is (a) 1 (b) 2 (c) $2\dfrac{1}{2}$ (d) $3\dfrac{1}{3}$

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304.

$f(x) = 1 + 2\sin x + 3\cos^2 x,\ 0 \leq x \leq \frac{2\pi}{3}$

is (a)Minimum at $x = \pi/2$ (b) Maximum at $x = \sin^{-1}\left(1/\sqrt{3}\right)$ (c) Minimum at $x = \pi/6$ (d) Maximum at $\sin^{-1}(1/6)$

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305. The function $f(x) = 2x^3 - 15x^2 + 36x + 4$ is maximum at $x =$ (a) 3 (b) 0 (c) 4 (d) 2

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306. The maximum value of $f(x) = \frac{x}{4 - x + x^2}$ on $[-1, 1]$ is (a) $\frac{1}{4}$ (b) $-\frac{1}{3}$ (c) $\frac{1}{6}$ (d) $\frac{1}{5}$

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307. Let $f(x) = 2x^3 - 3x^2 - 12x + 5$ on $[-2, 4]$. The relative maximum occurs at $x = -2$ (b) -1 (c) 2 (d) 4

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308. The minimum value of $x\ (\log)_e x$ is equal to e (b) $1/e$ (c) $-1/e$ (d) $2e$ (e) e

309. The minimum value of the function $f(x) = 2x^3 - 21x^2 + 36x - 20$ is -128 (b) -126 (c) -120 (d) none of these