

India's Number 1 Education App

MATHS

BOOKS - RD SHARMA MATHS (ENGLISH)

SCALAR TRIPLE PRODUCT

Others

1. Find
$$\left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c}\right]$$
, when (i) $\overrightarrow{a} = 2\hat{i} - 3\hat{j}$, $\overrightarrow{b} = \hat{i} + \hat{j} - \hat{k}$ and $\overrightarrow{c} = 3\hat{i} - \hat{k}$ (ii) $\overrightarrow{a} = \hat{i} - 2\hat{j} + 3\hat{k}$, $\overrightarrow{b} = 2\hat{i} + \hat{j} - \hat{k}$ and $\overrightarrow{c} = \hat{j} + \hat{k}$



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2. Find the volume of the parallelepiped whose coterminous edges are

the

represented bν

i,

vectors:

 $\overrightarrow{a}=2\hat{i}+3\hat{j}+4\hat{k}, \overrightarrow{b}=\hat{i}+2\hat{j}-\hat{k}, \overrightarrow{c}=3\hat{i}-\hat{j}+2\hat{k}$

ii,

3. Evaluate : $\left[\hat{i}\,\hat{j}\hat{k}
ight]+\left[\hat{j}\hat{k}\hat{i}
ight]+\left[\hat{k}\hat{i}\hat{j}
ight]\left[2\hat{i}\,\hat{j}\hat{k}
ight]+\left[\hat{i}\hat{k}\hat{j}
ight]+\left[\hat{k}\hat{j}2\hat{i}
ight]$

 $\stackrel{
ightarrow}{\overrightarrow{a}}=2\hat{i}-3\hat{j}+4\hat{k},\stackrel{
ightarrow}{\overrightarrow{b}}=\hat{i}+2\hat{j}-\hat{k},\stackrel{
ightarrow}{\overrightarrow{c}}=3\hat{i}-\hat{j}-2\hat{k}$

 $\overrightarrow{a} = \hat{i} + \hat{j} + \hat{k}, \overrightarrow{b} = \hat{i} - \hat{j} + \hat{k}, \overrightarrow{c} = \hat{i} + 2\hat{i} - \hat{k}$

iii,

iv,

4. Prove that:
$$\left(\overrightarrow{a}-\overrightarrow{b}\right)\cdot\left\{\left(\overrightarrow{b}-\overrightarrow{c}\right)\times\left(\overrightarrow{c}-\overrightarrow{a}\right)\right\}=0$$

 $\overrightarrow{a}=11\hat{i}, \overrightarrow{b}=2\hat{j}, \overrightarrow{c}=13\hat{k}$

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$$egin{aligned} \overrightarrow{a} &= \hat{i} + 2\hat{j} - \hat{k}, \ \overrightarrow{b} &= 3\hat{i} + 2\hat{j} + 7\hat{k}, \ \overrightarrow{c} &= 5\hat{i} + 6\hat{j} + 5\hat{k} \end{aligned} \ \overrightarrow{a} &= -4\hat{i} - 6\hat{j} - 2\hat{k}, \ \overrightarrow{b} &= -\hat{i} + 4\hat{j} + 3\hat{k}, \ \overrightarrow{c} &= -8\hat{i} - \hat{j} + 3\hat{k} \end{aligned}$$

 $\widehat{a} = \widehat{i} - 2\widehat{j} + 3\widehat{k}, \overrightarrow{b} = -2\widehat{i} + 3\widehat{j} - 4\widehat{k}, \overrightarrow{c} = \widehat{i} - 3\widehat{j} + 5\widehat{k}$

6. Find the value of λ so that the following vectors are coplanar:

$$\overrightarrow{a} = \hat{i} - \hat{j} + \hat{k}, \, \overrightarrow{b} = 2\hat{i} + \hat{j} - \hat{k}, \, \overrightarrow{c} = \lambda \hat{i} - \hat{j} + \lambda \hat{k}$$

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7. Find the value of λ for which the four points with position vectors

$$-\hat{j}-\hat{k},4\hat{i}+5\hat{j}+\lambda\hat{k},3\hat{i}+9\hat{j}+4\hat{k}$$
 and $4\hat{i}+4\hat{j}+4\hat{k}$ are coplanar.

- **8.** \overrightarrow{a} , \overrightarrow{b} and \overrightarrow{c} are the position vectors of points A,B and C respectively, prove that : $\overrightarrow{a} \times \overrightarrow{b} + \overrightarrow{b} \times \overrightarrow{c} + \overrightarrow{c} \times \overrightarrow{a}$ is vector perpendicular to the plane of triangle ABC.
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9. Let $\overrightarrow{a}=\hat{i}+\hat{j}+\hat{k}, \overrightarrow{b}=\hat{i}$ and $\hat{c}=c_1\hat{i}+c_2\hat{j}+c_3\hat{k}$. Then, (1)If $c_1=1$ and $c_2=2$, find c_3 which makes $\overrightarrow{a}, \overrightarrow{b}$ and \overrightarrow{c} coplanar. (2)If $c_2=-1$ and $c_3=1$, show that no value of c_1 can make $\overrightarrow{a}, \overrightarrow{b}$ and \overrightarrow{c}



$$\left[\overrightarrow{a},\overrightarrow{b},\overrightarrow{c}
ight], when \overrightarrow{a}=2\hat{i}-3\hat{j}+4\hat{k}, \ \overrightarrow{b}=\hat{i}+2\hat{j}-\hat{k}and \ \overrightarrow{c}=3\hat{i}-\hat{j}+$$

$$\left[\overrightarrow{a},\overrightarrow{b},\overrightarrow{c}\right], when \overrightarrow{a}=2\hat{i}-3\hat{j}+4\hat{k}, \ \overrightarrow{b}=\hat{i}+2\hat{j}-\hat{k}and \ \overrightarrow{c}=3\hat{i}-\hat{j}+$$

$$\left[\overrightarrow{b}\right]$$
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Find

 $-3\hat{i}+7\hat{j}-5\hat{k},\ -5\hat{i}+7\hat{j}-3\hat{k}$ and $7\hat{i}-5\hat{j}-3\hat{k}$

coplanar.

10.

- **12.** If $|aa^21 + a\hat{3} \cdot 21 + b^3 \cdot 21 + c^3| = 0$ and the vectors
- $\overrightarrow{A} = \hat{i} + a\hat{j} + a^2\hat{k}, \overrightarrow{B} = \hat{i} + b\hat{j} + b^2\hat{k}, \overrightarrow{C} = \hat{i} + c\hat{j} + c^2\hat{k}$ are

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14. Simplify: $\left[\overrightarrow{a} - \overrightarrow{b}\overrightarrow{b} - \overrightarrow{c}\overrightarrow{c} - \overrightarrow{a}\right]$

If

then prove that c is the geometric mean of a and b.

the

 $\overrightarrow{lpha}=a\hat{i}+a\hat{j}+c\hat{k}, \overrightarrow{eta}=\hat{i}+\hat{k} \ ext{and} \ \overrightarrow{\gamma}=c\hat{i}+c\hat{j}+b\hat{k}$ are coplanar,

vectors

- coplanar, then prove that abc = -1.
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- **13.** Evaluate $0.2^3 + 100.45^0$

15.

16. Determine α such that a vector \overrightarrow{r} is at right angles to each of the vectors $\overrightarrow{a} = \alpha \hat{i} + \hat{j} + 3\hat{k}, \overrightarrow{b} = 2\hat{i} + \hat{j} - \alpha \hat{k}, \overrightarrow{c} = -2\hat{i} + \alpha \hat{j} + 3\hat{k}$



18. If \overrightarrow{a} , \overrightarrow{b} , \overrightarrow{c} are three non-coplanar vectors, prove that

17. Find the range of $f(x) = \sin^{-1} x + \tan^{-1} x + \cos^{-1} x$.

$$\left[\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c}\overrightarrow{a} + \overrightarrow{b}\overrightarrow{a} + \overrightarrow{c}\right] = -\left[\overrightarrow{a}\overrightarrow{b}\overrightarrow{c}\right]$$



19. For any three vectors a b,c, show that

$$\overrightarrow{a} imes \left(\overrightarrow{b} + \overrightarrow{c}
ight) + \overrightarrow{b} imes \left(\overrightarrow{c} + \overrightarrow{a}
ight) + \overrightarrow{c} imes \left(\overrightarrow{a} + \overrightarrow{b}
ight) = 0$$



20. Let \overrightarrow{a} , \overrightarrow{b} , \overrightarrow{c} be three non-zero vectors such that \overrightarrow{c} is a unit vector perpendicular to both \overrightarrow{a} and \overrightarrow{b} . If the between \overrightarrow{a} and \overrightarrow{b} is $\pi/6$, prove that $\left[\overrightarrow{a} \overrightarrow{b} \overrightarrow{c}\right]^2 = \frac{1}{4} \left|\overrightarrow{a}\right|^2 \left|\overrightarrow{b}\right|^2$.



21. Let \overrightarrow{a} , \overrightarrow{b} and \overrightarrow{c} , be non-zero non-coplanar vectors. Prove that: $\overrightarrow{a} - 2\overrightarrow{b} + 3\overrightarrow{c}$, $-2\overrightarrow{a} + 3\overrightarrow{b} - 4\overrightarrow{c}$ and $\overrightarrow{c} - 3\overrightarrow{b} + 5\overrightarrow{c}$ are coplanar vectors. $2\overrightarrow{a} - \overrightarrow{b} + 3\overrightarrow{c}$, $\overrightarrow{a} + \overrightarrow{b} - 2\overrightarrow{c}$ and $\overrightarrow{a} + \overrightarrow{b} - 3\overrightarrow{c}$ are non-coplanar vectors.

22. Find the altitude of a parallelepiped determined by the vectors

 \overrightarrow{a} , \overrightarrow{b} and \overrightarrow{c} , if the base is taken as the parallelogram determined by

$$\overrightarrow{a}$$
 and \overrightarrow{b} , and

 $\overrightarrow{a} = \hat{i} + \hat{j} + \hat{k}, \ \overrightarrow{b} = 2\hat{i} + 4\hat{j} - \hat{k}$ and $\overrightarrow{c} = \hat{i} + \hat{j} + 3\hat{k}$.

- **23.** Let \overrightarrow{a} , \overrightarrow{b} , \overrightarrow{c} , be three non-zero vectors. If \overrightarrow{a} . $(\overrightarrow{b} \times \overrightarrow{c}) = 0$ and \overrightarrow{b} and \overrightarrow{c} are not parallel, then prove that $\overrightarrow{a} = \lambda \overrightarrow{b} + \mu \overrightarrow{c}$, $where \lambda$ are some scalars.
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- **24.** If the vectors $\overrightarrow{\alpha}=a\hat{i}+\hat{j}+\hat{k}, \overrightarrow{\beta}=\hat{i}+b\hat{j}+\hat{k}and \overrightarrow{\gamma}=\hat{i}+\hat{j}+c\hat{k}$ are coplanar, then prove that $\dfrac{1}{1-a}+\dfrac{1}{1+b}+\dfrac{1}{1-c}=1, wherea\neq 1, b\neq 1 and c\neq 1.$
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25. If a is a non-zero real number, then prove that the vectors $\overrightarrow{lpha}=a\hat{i}+2a\hat{j}-3a\hat{k}, \overrightarrow{eta}=(2a+1)\hat{i}+(2a+3)\hat{j}+(a+1)\hat{k}and, \overrightarrow{\gamma}=0$

$$\overrightarrow{lpha}=a\hat{i}+2a\hat{j}-3a\hat{k}, \overrightarrow{eta}=(2a+1)\hat{i}+(2a+3)\hat{j}+(a+1)\hat{k}and, \overrightarrow{\gamma}=0$$
are never coplanar.

that

vectors



26. If
$$\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c} = 0$$
, prove

that

 $\stackrel{
ightarrow}{a}=\ -2\hat{i}-2\hat{j}+4\hat{k}, \stackrel{
ightarrow}{b}=\ -2\hat{i}+4\hat{j}-2\hat{k}\ and \stackrel{
ightarrow}{c}=4\hat{i}-2\hat{j}-2\hat{k}$

the

$$\left(\overrightarrow{a} imes\overrightarrow{b}
ight)=\left(\overrightarrow{b} imes\overrightarrow{c}
ight)=\left(\overrightarrow{c} imes\overrightarrow{a}
ight)$$

Show

27.

are coplanar.

28. Find λ so that the vectors $\overrightarrow{a}=2\hat{i}-\hat{j}+\hat{k}, \ \overrightarrow{b}=\hat{i}+2\hat{j}-3\hat{k} \ and \ \overrightarrow{c}=3\hat{i}+\lambda\hat{j}+5\hat{k}$ are coplanar.



29. The four points whose position vector are $6\hat{i}-7\hat{j}, 16\hat{i}-29\hat{j}-4\hat{k}, 3\hat{j}-6\hat{k}, 2\hat{i}+5\hat{j}+10\hat{k}$ are coplanar



30. For any three vectors a, b, c prove that $\left[\overrightarrow{a} + \overrightarrow{b} \overrightarrow{b} + \overrightarrow{c} \overrightarrow{c} + \overrightarrow{a}\right] = 2 \left[\overrightarrow{a} \overrightarrow{b} \overrightarrow{c}\right].$

31. Show that vectors \overrightarrow{a} , \overrightarrow{b} , \overrightarrow{c} are coplanar if $\overrightarrow{a} + \overrightarrow{b}$, \overrightarrow{b} , \overrightarrow{c} , \overrightarrow{c} + \overrightarrow{a} are coplanar.



32. Show that the vectors $\overrightarrow{a} - \overrightarrow{b}$, $\overrightarrow{b} - \overrightarrow{c}$, $\overrightarrow{c} - \overrightarrow{a}$ are coplaner.



33. What can you conclude about four non zero vectors

$$\overrightarrow{a}\,,\,\,\overrightarrow{b}\,,\,\,\overrightarrow{c}\,\,and\,\overrightarrow{d}\,\,$$
 given that $\left|\left(\overrightarrow{a} imes\overrightarrow{b}\right)\overrightarrow{c}
ight|+\left|\left(\overrightarrow{b} imes\overrightarrow{c}\right)\overrightarrow{d}
ight|=0\,.$

- **34.** Evaluate the following: $\left[\hat{i}\;\hat{j}\;\hat{k}\right]+\left[\hat{j}\;\hat{k}\;\hat{i}\right]+\left[\hat{k}\;\hat{i}\;\hat{j}\right]$.
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35. Evaluate : $\left[\hat{i}\hat{j}\hat{k}
ight]+\left[\hat{j}\hat{k}\hat{i}
ight]+\left[\hat{k}\hat{i}\hat{j}
ight]\left[2\hat{i}\hat{j}\hat{k}
ight]+\left[\hat{i}\hat{k}\hat{j}
ight]+\left[\hat{k}\hat{j}2\hat{i}
ight]$

when

36. Find $\left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c}\right]$,

 $\overrightarrow{a} = 2\hat{i} - 3\hat{j}, \ \overrightarrow{b} = \hat{i} + \hat{j} - \hat{k} \ and \ \overrightarrow{c} = 3\hat{i} - \hat{k}.$

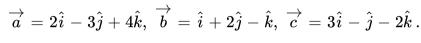
37. Find
$$\left[\overrightarrow{a}\ \overrightarrow{b}\ \overrightarrow{c}\right]$$
 , when $\overrightarrow{a}=\hat{i}-2\hat{j}+3\hat{k},\ \overrightarrow{b}=2\hat{i}+\hat{j}-\hat{k}\ and\ \overrightarrow{c}=\hat{j}+\hat{k}$.

38. Find the volume of the parallelepiped whose coterminous edges are represented by the vector:

→

$$\overrightarrow{a}=2\hat{i}+3\hat{j}+4\hat{k},\ \overrightarrow{b}=\hat{i}+2\hat{j}-\hat{k},\ \overrightarrow{c}=3\hat{i}-\hat{j}+2\hat{k}\,.$$

39. Find the volume of the parallelepiped whose coterminous edges are represented by the vector:





40. Find the volume of the parallelepiped whose coterminous edges are represented by the vector: $\overrightarrow{a}=11\hat{i},\ \overrightarrow{b}=2\hat{j},\ \overrightarrow{c}=13\hat{k}$.



41. Find the volume of the parallelepiped whose coterminous edges are represented by the vector:

$$\overrightarrow{a} = \hat{i} + \hat{j} + \hat{k}, \ \overrightarrow{b} = \hat{i} - \hat{j} + \hat{k}, \ \overrightarrow{c} = \hat{i} + 2\hat{j} - \hat{k} \,.$$

42. Show that each of the following triads of vectors are coplanar:

$$\overrightarrow{a} = \hat{i} + 2\hat{j} - \hat{k}, \ \overrightarrow{b} = 3\hat{i} + 2\hat{j} + 7\hat{k}, \ \overrightarrow{c} = 5\hat{i} + 6\hat{j} + 5\hat{k}\,.$$

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43. Show that each of the following triads of vectors are coplanar:

$$\overrightarrow{a} = \, -4\hat{i} - 6\hat{j} - 2\hat{k}, \; \overrightarrow{b} = \, -\, \hat{i} + 4\hat{j} + 3\hat{k}, \; \overrightarrow{c} = \, -\, 8\hat{i} - \hat{j} + 3\hat{k} \,.$$

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44. Show that each of the following triads of vectors are coplanar:

$$\overrightarrow{a} = \hat{i} - 2\hat{j} + 3\hat{k}, \ \overrightarrow{b} = -2\hat{i} + 3\hat{j} - 4\hat{k}, \ \overrightarrow{c} = \hat{i} - 3\hat{j} + 5\hat{k}.$$

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45. Find the value of λ so that the following vectorts are coplanar:

$$\overrightarrow{a} = \hat{i} - \hat{j} + \hat{k}, \ \overrightarrow{b} = 2\hat{i} + \hat{j} - \hat{k}, \ \overrightarrow{c} = \lambda\hat{i} - \hat{j} + \lambda\hat{k}$$

46. Find the value of
$$\lambda$$
 so that the following vectorts are coplanar:

$$\overrightarrow{a} = 2\hat{i} - \hat{j} + \hat{k}, \; \overrightarrow{b} = \hat{i} + 2\hat{j} - 3\hat{k}, \; \overrightarrow{c} = \lambda\hat{i} + \lambda\hat{j} + 5\hat{k}$$



47. Find the value of
$$\lambda$$
 so that the following vectorts are coplanar:

$$\overrightarrow{a} = \hat{i} + 2\hat{j} - 3\hat{k}, \ \overrightarrow{b} = 3\hat{i} + \lambda\hat{j} + \hat{k}, \ \overrightarrow{c} = \hat{i} + 2\hat{j} + 2\hat{k}$$



48. Find the value of λ so that the following vectorts are coplanar:

$$\overrightarrow{a} = \hat{i} + 3\hat{j}, \ \overrightarrow{b} = 5\hat{k}, \ \overrightarrow{c} = \lambda\hat{i} - \hat{j}$$



49. Show that the points having position vectors $6\hat{i}-7\hat{j},\ 16\hat{i}-19\hat{j}-4\hat{k},\ 3\hat{j}-6\hat{k},\ 2\hat{i}+5\hat{j}+10\hat{k}$ are not coplanar.

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- 50. Show that the points A(-1, 4, -3), B(3, 2, -5), C(-3, 8, -5)and D(-3, 2, 1)
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are coplanar.

- **51.** Show that four points whose position vectors are $6\hat{i}-7\hat{j},\ 16i-19\hat{j}-4\hat{k},\ 3\hat{i}-6\hat{k},\ 2\hat{i}-5\hat{j}+10\ \hat{k}$ are coplanar.
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52. Find the value of λ for which the four points with position vectors

$$\hat{j}-\hat{k},\;4\hat{i}+5\hat{j}+\lambda\hat{k},\;3\hat{i}+9\hat{j}+4\hat{k}\;and-4\hat{i}+4\hat{j}+4\hat{k}$$
 are coplanar.



53. Prove that
$$(\overrightarrow{a}-\overrightarrow{b})(\overrightarrow{b}-\overrightarrow{c}) \times (\overrightarrow{c}-\overrightarrow{a})=0$$



(a) If
$$(b)(c)(d)c_e1(f)(g)=\setminus \ 1(h)$$
 (i) and $(j)(k)(l)c_m2(n)(o)=\setminus \ 2(p)$

(q), find `(r) (s) (t) c (u)3(v) (w) (x

55. Find
$$\lambda$$
 for which the points $A(3,\ 2,\ 1),\ B(4,\ \lambda,\ 5),\ C(4,\ 2,\ -2)\ and\ D(6,\ 5,\ -1)$ are coplanar.

54. Let $\rightarrow a=\hat{i}+\hat{j}+\hat{k}$, $\rightarrow b=\hat{i}$ and $\rightarrow c=c_1\hat{i}+c_2\hat{j}+c_3\hat{k}$ Then

56. Write the value of
$$\left[2\hat{i}\,\,3\hat{j}\,\,4\hat{k}
ight]$$

57. Write the value of $\left[\hat{i}+\hat{j}\;\hat{j}+\hat{k}\;\hat{k}+\hat{i}\right]$

58. Write the value of $\left[\hat{i}-\hat{j}\;\hat{j}-\hat{k}\;\hat{k}-\hat{i}\right]$

59. Find the values of
$$a$$
 for which are vectors $\overrightarrow{\alpha} = \hat{i} + 2\hat{j} + \hat{k}, \overrightarrow{\beta} = a\hat{i} + \hat{j} + 2\hat{k}$ and $\overrightarrow{\gamma} = \hat{i} + 2\hat{j} + a\hat{k}$ are coplanar.

60. Find the volume of the parallepiped with its edges represented by the vectors $\hat{i} + \hat{j}$, $\hat{i} + 2\hat{j}$ and $\hat{i} + \hat{j} + \pi \hat{k}$.



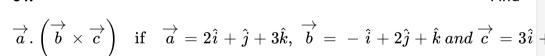
61. If
$$\overrightarrow{a}$$
, \overrightarrow{b} , are non collinear vectors, then find the value of $\left[\overrightarrow{a} \ \overrightarrow{b} \ \hat{i}\right] \hat{i} + \left[\overrightarrow{a} \ \overrightarrow{b} \ \hat{j}\right] \hat{j} + \left[\overrightarrow{a} \ \overrightarrow{b} \ \hat{k}\right] \hat{k}$.

- **62.** For any two vectors \overrightarrow{a} and \overrightarrow{b} writhe the value o $\left(\overrightarrow{a} \overset{\cdot}{b}\right) y^2 + \left|\overrightarrow{a} \times \overrightarrow{b}\right|^2$ in terms of their magnitudes.
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63. If
$$\left[\overrightarrow{3a} + \overrightarrow{7b} \overset{
ightarrow}{\overrightarrow{c}} \overset{
ightarrow}{\overrightarrow{d}} \right] = \lambda \left[\overrightarrow{a} \overset{
ightarrow}{\overrightarrow{c}} \overset{
ightarrow}{\overrightarrow{d}} \right] + \mu \left[\overrightarrow{b} \overset{
ightarrow}{\overrightarrow{c}} \overset{
ightarrow}{\overrightarrow{d}} \right]$$
 , then find the

value of
$$\lambda + \mu$$

Find







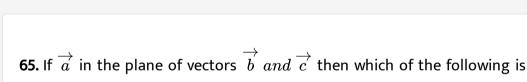
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c]=3" d. "[vec b\ vec c\ vec a]=1"

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correct? $\left|\overrightarrow{a}\overrightarrow{b}\overrightarrow{c}\right|=0$ b. "\" [vec a\ vec b\ vec c]=1' c. "[vec a\ vec b\ vec































of

$$\left[\overrightarrow{a}-\overrightarrow{b},\ \overrightarrow{b}-\overrightarrow{c},\ \overrightarrow{c}-\overrightarrow{a}
ight],\ where\ \left|\overrightarrow{a}
ight|=1,\ \left|\overrightarrow{b}
ight|=5,\ \left|\overrightarrow{c}
ight|=3,is$$

- $0\ \mathrm{b.}\ 1\ \mathrm{c.}\ 6\ \mathrm{d.}$ none of these
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- **67.** If \overrightarrow{a} , \overrightarrow{b} , \overrightarrow{c} are three non coplanar mutually perpendicular unit vectors then $\begin{bmatrix} \overrightarrow{a} & \overrightarrow{b} & \overrightarrow{c} \end{bmatrix}$ is ± 1 b. \setminus 0 \setminus c. -1 d. 2
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68. For any three vectors \overrightarrow{a} , \overrightarrow{b} , \overrightarrow{c} the expression

$$\begin{pmatrix} \overrightarrow{a} & \overrightarrow{b} \end{pmatrix} \begin{pmatrix} \overrightarrow{b} & \overrightarrow{c} \end{pmatrix} \times \begin{pmatrix} \overrightarrow{c} & \overrightarrow{a} \end{pmatrix} \qquad \text{equals} \qquad \begin{bmatrix} \overrightarrow{a} & \overrightarrow{b} & \overrightarrow{c} \end{bmatrix} \qquad \text{b}$$

$$2 \begin{bmatrix} \overrightarrow{a} & \overrightarrow{b} & \overrightarrow{c} \end{bmatrix} \setminus \text{ c. } \begin{bmatrix} \overrightarrow{a} & \overrightarrow{b} & \overrightarrow{c} \end{bmatrix}^2 \text{ d. none of these }$$

69. If a, b, c are non coplanar vectors then

$$\frac{\overrightarrow{a} \overrightarrow{b} \times \overrightarrow{c}}{\left(\overrightarrow{c} \times \overrightarrow{a}\right) \overrightarrow{b}} + \frac{\overrightarrow{b} \overrightarrow{a} \times \overrightarrow{c}}{\overrightarrow{c} \left(\overrightarrow{a} \times \overrightarrow{b}\right)} \text{ is equal to } 2 \text{ b.} \setminus 0 \setminus \text{ c. } 1 \text{ d. none of }$$



these

70. Let $\overrightarrow{a}=a_1\hat{i}+a_2\hat{j}+a_2\hat{k}, \overrightarrow{b}=b_1\hat{i}+a_2\hat{j}+b_2\hat{k},$ and $\overrightarrow{c}=c_1\hat{i}+c_2\hat{j}+c_2\hat{k},$ be three non-zero vectors such that \overrightarrow{c} is a unit vector perpendicular to both vectors \overrightarrow{a} and \overrightarrow{b} . If the angle between a and b is $\pi/6$, then $\begin{vmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{vmatrix}^2$ is equal to

71. Find $\frac{dy}{dx}$ if 3 = 2x - 3y



72. If the vectors $4\hat{i}+11\hat{j}+m\hat{k},~7\hat{i}+2\hat{j}+6\hat{k}~and~\hat{i}+5\hat{j}+4\hat{k}$ are coplanar then m=~38 b. $\backslash~~10\backslash~~$ c. -1 d. -10



73. For non-zero vectors
$$\overrightarrow{a}$$
, \overrightarrow{b} , $and\overrightarrow{c}$ $\left| \left(\overrightarrow{a} \times \overrightarrow{b} \right) \overrightarrow{c} \right| = \left| \overrightarrow{a} \right| \left| \overrightarrow{b} \right| \left| \overrightarrow{c} \right|$ holds if and only if $\overrightarrow{a} \overset{\cdot}{b} = 0$, $\overrightarrow{b} \overset{\cdot}{c} = 0$ b. $\overrightarrow{b} \overset{\cdot}{\rightarrow} = 0$, $\overrightarrow{a} = 0$ c. $\overrightarrow{a} = 0$, $\overrightarrow{a} \overset{\cdot}{b} = 0$ d. $\overrightarrow{a} \overset{\cdot}{b} = 0$, $\overrightarrow{b} \overset{\cdot}{c} = 0$ $\overrightarrow{c} = 0$



74.
$$(\overrightarrow{a} + \overrightarrow{b})\overrightarrow{b} + \overrightarrow{c} \times (\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c}) = [\overrightarrow{a} \overrightarrow{b} \overrightarrow{c}] \text{ b. } \setminus 0 \setminus c.$$

$$2[\overrightarrow{a} \overrightarrow{b} \overrightarrow{c}] \text{ d. } -[\overrightarrow{a} \overrightarrow{b} \overrightarrow{c}]$$

75. If
$$\overrightarrow{a}$$
, \overrightarrow{b} , \overrightarrow{c} are three non coplanar vectors, then

$$\left(\overrightarrow{a} + \overrightarrow{b} + \overrightarrow{c}\right) \left(\overrightarrow{a} + \overrightarrow{b}\right) \times \overrightarrow{a} + \overrightarrow{c} \right) \right] \text{ equals } \left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c}\right] \text{ b. } \setminus 0 \setminus 0 \setminus \left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c}\right] \text{ d. } - \left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c}\right]$$

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76.
$$\left(\overrightarrow{a} + 2\overrightarrow{b} - \overrightarrow{c}\right) \left(\overrightarrow{a} - \overrightarrow{b}\right) \times \left(\overrightarrow{a} - \overrightarrow{b} - \overrightarrow{c}\right)$$
 is equal to $\left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c}\right]$ b. c. $2\left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c}\right]$ d. $3\left[\overrightarrow{a} \ \overrightarrow{b} \ \overrightarrow{c}\right]$