



# MATHS

## BOOKS - CBSE COMPLEMENTARY

### MATERIAL MATHS (HINGLISH)

## APPLICATIONS OF INTEGRALS

### Four Six Mark Questions

1. Calculate the area bounded by the parabola

$$y^2 = 4ax \text{ and its latus rectum}$$



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2. Find the area of the region

$$\{(x, y) : x^2 \leq y \leq x\}$$



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3. Find the area of the region in the first quadrant enclosed by the x-axis, the line  $y = x$ , and the circle  $x^2 + y^2 = 32$ .



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4. Find the area of the region

$$\{(x, y) : y^2 \leq 4x, 4x^2 + 4y^2 \leq 9\}$$



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5. Prove that the curve  $y = x^2$  and,  $x = y^2$  divide the square bounded by  $x = 0, y = 0, x = 1, y = 1$  into three equal parts.



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6. Find the area of the smaller region bounded

by the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  and the line

$$\frac{x}{a} + \frac{y}{b} = 1$$



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7. Find the area of the region bounded by the

curves  $x^2 + y^2 = 4$  and  $(x - 2)^2 + y^2 = 4$ .



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8. Using the method of integration find the area of the region bounded by lines:

$$2x + y = 4, 3x - 2y = 6 \text{ and } x - 3y + 5 = 0$$



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9. Using integration, find the area of the triangle whose vertices are  $(-1, 0)$ ,  $(1, 3)$  and  $(3, 2)$ .



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10. The area of the region

$\{(x, y) : x^2 + y^2 \leq 1 \leq x + y\}$ , is



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11. Find the area of the region bounded by the parabola  $x^2 = 4y$  and the line  $x = 4y - 2$



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**12.** Find the area lying above x-axis and included between the circle  $x^2 + y^2 = 8x$  and the parabola  $y^2 = 4x$ .



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**13.** Using integration, find the area enclosed by the curve  $y = \cos x$ ,  $y = \sin x$  and x - axis in the interval  $[0, \pi/2]$ .



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14. Using integration find area of the region bounded by the curves  $y = \sqrt{5 - x^2}$  and  $y = |x - 1|$



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15. Show that the area of the triangle formed by the positive x-axis and the normal and tangent to the circle  $x^2 + y^2 = 4$  at  $(1, \sqrt{3})$  is  $2\sqrt{3}$



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**16.** Using integration, find the area of the region bounded by the line  $xy + 2 = 0$ , the curve  $x = \sqrt{y}$  and  $y = a$ .



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**17.** The area of the region bounded by the curve  $ay^2 = x^3$ , the Y-axis and the lines  $y = a$  and  $y = 2a$ , is



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**18.** Find the area bounded by  $x$  - axis, the curve  $y = 2x^2$  and tangent to the curve at the point whose abscissa is 2.



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**19.** Using integration, find the area of the region bounded by the curve  $y = 1 + |x + 1|$  and lines  $x = -3$ ,  $x = 3$ ,  $y = 0$ .



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20. Draw a rough sketch of the region

$$\{(x, y) : y^2 \leq 6ax \text{ and } x^2 + y^2 \leq 16a^2\}.$$

Also, find the area of the region sketched using method of integration.



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21. Find the area of the region enclosed

between curves  $y = |x - 1|$  and  $y = 3 - |x|$ .



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22. If the area bounded by the parabola  $y^2 = 16ax$  and the line  $y = 4mx$  is  $\frac{a^2}{12}$  sq unit then using integration find the value of  $m$ .



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23. Given  $\frac{dy}{dx}$  is directly proportional to the square of  $x$  and  $\frac{dy}{dx} = 6$  at  $x = 2$ . Then find the equation of the curve, when  $x = 2$  and  $y = 4$ . Also find the area of the region bounded by curve between lines  $y = 1$  and  $y = 3$ .



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**24.** Find the area between  $x$  - axis, curve  $x = y^2$  and its normal at the point  $(1, 1)$ .



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**25.** Find the area of the region bounded by the curve  $x = at^2$  and  $y = 2at$  between the ordinates corresponding to  $t = 1$  and  $t = 2$ .



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**26.** Using integration find the area bounded by the tangent to the curve  $y = 3x^2$  at the point  $(1, 3)$ , and the Lines whose equations are  $y = \frac{x}{3}$  and  $x + y = 4$ .



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