



MATHS

BOOKS - CENGAGE MATHS (ENGLISH)

DIFFERENT PRODUCTS OF VECTORS AND THEIR GEOMETRICAL APPLICATIONS

Exercises

1. If $\begin{vmatrix} (a-x)^2 & (a-y)^2 & (a-z)^2 \\ (b-x)^2 & (b-y)^2 & (b-z)^2 \\ (c-x)^2 & (c-y)^2 & (c-a)^2 \end{vmatrix} = 0$ and vectors \vec{A}, \vec{B} and \vec{C} , where

$\vec{A} = a^2\hat{i} = a\hat{j} + \hat{k}$ etc. are non-coplanar, then prove that vectors

\vec{X}, \vec{Y} and \vec{Z} where $\vec{X} = x^2\hat{i} + x\hat{j} + \hat{k}$. etc. may be coplanar.



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2. OABC is a tetrahedron where O is the origin and A,B,C have position vectors \vec{a} , \vec{b} , \vec{c} respectively prove that circumcentre of tetrahedron OABC

is
$$\frac{a^2(\vec{b} \times \vec{c}) + b^2(\vec{c} \times \vec{a}) + c^2(\vec{a} \times \vec{b})}{2[\vec{a}\vec{b}\vec{c}]}$$

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3. Let k be the length of any edge of a regular tetrahedron (a tetrahedron whose edges are equal in length is called a regular tetrahedron). Show that the angle between any edge and a face not containing the edge is $\cos^{-1}(1/\sqrt{3})$.

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4. In ABC , a point P is taken on AB such that $AP/BP = 1/3$ and point Q is taken on BC such that $CQ/BQ = 3/1$. If R is the point of intersection of the lines AQ and CP , using vector method, find the area of ABC if the area of BRC is 1 unit

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5. Let O be an interior point of ΔABC such that $OA + 2OB + 3OC = 0$.

Then the ratio of area of ΔABC to area of ΔAOC is

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6. The lengths of two opposite edges of a tetrahedron are a and b ; the shortest distance between these edges is d , and the angle between them is θ . Prove using vectors that the volume of the tetrahedron is $\frac{abd \sin \theta}{6}$.

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7. Find the volume of a parallelepiped having three coterminal vectors of equal magnitude $|a|$ and equal inclination θ with each other.

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8. Let \vec{p} and \vec{q} any two orthogonal vectors of equal magnitude 4 each. Let \vec{a}, \vec{b} and \vec{c} be any three vectors of lengths $7\sqrt{15}$ and $2\sqrt{33}$, mutually perpendicular to each other. Then find the distance of the vector $(\vec{a} \cdot \vec{p})\vec{p} + (\vec{a} \cdot \vec{q})\vec{q} + (\vec{a} \cdot (\vec{p} \times \vec{q}))(\vec{p} \times \vec{q}) + (\vec{b} \cdot \vec{p})\vec{p} + (\vec{b} \cdot \vec{q})\vec{q} + (\vec{b} \cdot (\vec{p} \times \vec{q}))(\vec{p} \times \vec{q}) + (\vec{c} \cdot \vec{p})\vec{p} + (\vec{c} \cdot \vec{q})\vec{q} + (\vec{c} \cdot (\vec{p} \times \vec{q}))(\vec{p} \times \vec{q})$ from the origin.



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9. Given that $\vec{A}, \vec{B}, \vec{C}$ form triangle such that $\vec{A} = \vec{B} + \vec{C}$. Find a,b,c,d such that area of the triangle is $5\sqrt{6}$ where $\vec{A} = a\vec{i} + b\vec{j} + c\vec{k}, \vec{B} = d\vec{i} + 3\vec{j} + 4\vec{k}$ and $\vec{C} = 3\vec{i} + \vec{j} - 2\vec{k}$.



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10. A line l is passing through the point \vec{b} and is parallel to vector \vec{c} . Determine the distance of point $A(\vec{a})$ from the line l in from

$$\left| \vec{b} - \vec{a} + \frac{(\vec{a} - \vec{b})\vec{c}}{|\vec{c}|^2} \vec{c} \right| \text{ or } \frac{|(\vec{b} - \vec{a}) \times \vec{c}|}{|\vec{c}|}$$

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11. If $\vec{e}_1, \vec{e}_2, \vec{e}_3$ and $\vec{E}_1, \vec{E}_2, \vec{E}_3$ are two sets of vectors such that $\vec{e}_i \cdot \vec{E}_j = 1$, if $i = j$ and $\vec{e}_i \cdot \vec{E}_j = 0$ and if $i \neq j$, then prove that

$$[\vec{e}_1 \vec{e}_2 \vec{e}_3][\vec{E}_1 \vec{E}_2 \vec{E}_3] = 1.$$

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12. In a quadrilateral ABCD, it is given that $AB \parallel CD$ and the diagonals AC and BD are perpendicular to each other. Show that $AD \cdot BC \geq AB \cdot CD$.

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13. $OABC$ is regular tetrahedron in which D is the circumcentre of OAB and E is the midpoint of edge AC . Prove that DE is equal to half the edge of tetrahedron.

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14. If $A(\vec{a}), B(\vec{b})$ and $C(\vec{c})$ are three non-collinear points and origin does not lie in the plane of the points A, B and C , then point $P(\vec{p})$ in the plane of the ABC such that vector \vec{OP} is \perp to plane of ABC , show that

$$\vec{OP} = \frac{[\vec{a}\vec{b}\vec{c}](\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a})}{4^2}, \text{ where } \Delta \text{ is the area of the } ABC$$

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15. If $\vec{a}, \vec{b}, \vec{c}$ are three given non-coplanar vectors and any arbitrary vector

$$\vec{r} \text{ in space, where } \Delta_1 = \begin{vmatrix} \vec{r} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{r} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{r} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{c} \cdot \vec{c} \end{vmatrix}, \Delta_2 = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{r} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{r} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{r} \cdot \vec{c} & \vec{c} \cdot \vec{c} \end{vmatrix}$$

$$\Delta_3 = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{r} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{r} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{r} \cdot \vec{c} \end{vmatrix}, \Delta = \begin{vmatrix} \vec{a} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{c} \cdot \vec{c} \end{vmatrix},$$

then prove that $\vec{r} = \frac{\Delta_1}{\Delta} \vec{a} + \frac{\Delta_2}{\Delta} \vec{b} + \frac{\Delta_3}{\Delta} \vec{c}$



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Exercises Mcq

1. Two vectors in space are equal only if they have equal component in a. a given direction b. two given directions c. three given directions d. in any arbitrary direction

- A. a given direction
- B. two given directions
- C. three given direction
- D. in any arbitrary direaction

Answer: c



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2. Let \vec{a} , \vec{b} and \vec{c} be the three vectors having magnitudes, 1, 5 and 3, respectively, such that the angle between \vec{a} and \vec{b} is θ and $\vec{a} \times (\vec{a} \times \vec{b}) = \vec{c}$. Then $\tan \theta$ is equal to

A. 0

B. $\frac{2}{3}$

C. $\frac{3}{5}$

D. $\frac{3}{4}$

Answer: d



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3. Let \vec{a} , \vec{b} , \vec{c} be three vectors of equal magnitude such that the angle between each pair is $\frac{\pi}{3}$. If $|\vec{a} + \vec{b} + \vec{c}| = \sqrt{6}$, then $|\vec{a}| =$

A. 2

B. -1

C. 1

D. $\sqrt{6}/3$

Answer: c

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4. If $\vec{a}, \vec{b}, \vec{c}$ are three mutually perpendicular vectors, then the vector which is equally inclined to these vectors is (A) $\vec{a} + \vec{b} + \vec{c}$ (B)

$\frac{\vec{a}}{|\vec{a}|} + \frac{\vec{b}}{|\vec{b}|} + \vec{c}$ (C) $\frac{\vec{a}}{|\vec{a}|^2} + \frac{\vec{b}}{|\vec{b}|^2} + \frac{\vec{c}}{|\vec{c}|^2}$ (D) $|\vec{a}|\vec{a} - |\vec{b}|\vec{b} + |\vec{c}|\vec{c}$

A. $\vec{a} + \vec{b} + \vec{c}$

B. $\frac{\vec{a}}{|\vec{a}|} + \frac{\vec{b}}{|\vec{b}|} + \frac{\vec{c}}{|\vec{c}|}$

C. $\frac{\vec{a}}{|\vec{a}|^2} + \frac{\vec{b}}{|\vec{b}|^2} + \frac{\vec{c}}{|\vec{c}|^2}$

$$D. |\vec{a}| |\vec{a} - \vec{b}| + |\vec{c}| |\vec{c}|$$

Answer: b



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5. Let $\vec{a} = \hat{i} + \hat{j}$ and $\vec{b} = 2\hat{i} - \hat{k}$. Then the point of intersection of the lines $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}$ and $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$ is (A) (3, -1, 10) (B) (3, 1, -1) (C) (-3, 1, 1) (D) (-3, -1, -1)

A. $\hat{i} - \hat{j} + \hat{k}$

B. $3\hat{i} - \hat{j} + \hat{k}$

C. $3\hat{i} + \hat{j} - \hat{k}$

D. $\hat{i} - \hat{j} - \hat{k}$

Answer: c



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6. If \vec{a} and \vec{b} are two vectors, such that $\vec{a} \cdot \vec{b} < 0$ and $|\vec{a} \cdot \vec{b}| = |\vec{a} \times \vec{b}|$ then the angle between the vectors \vec{a} and \vec{b} is (a) π (b) $\frac{7\pi}{4}$ (c) $\frac{\pi}{4}$ (d) $\frac{3\pi}{4}$

A. π

B. $7\pi/4$

C. $\pi/4$

D. $3\pi/4$

Answer: d



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7. If \hat{a} , \hat{b} and \hat{c} are three unit vectors such that $\hat{a} + \hat{b} + \hat{c}$ is also a unit vector and θ_1 , θ_2 and θ_3 are angles between the vectors \hat{a} , \hat{b} , \hat{c} and \hat{c} , \hat{a} , respectively then among θ_1 , θ_2 and θ_3

A. all are acute angles

B. all are right angles

C. at least one is obtuse angle

D. none of these

Answer: c



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8. If $\vec{a}, \vec{b}, \vec{c}$ are unit vectors such that $\vec{a} \cdot \vec{b} = 0 = \vec{a} \cdot \vec{c}$ and the angle between \vec{b} and \vec{c} is $\frac{\pi}{3}$, then find the value of $|\vec{a} \times \vec{b} - \vec{a} \times \vec{c}|$

A. $1/2$

B. 1

C. 2

D. none of these

Answer: b



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9. P (\vec{p}) and Q (\vec{q}) are the position vectors of two fixed points and R (\vec{r}) is the position vector of a variable point. If R moves such that $(\vec{r} - \vec{p}) \times (\vec{r} - \vec{q}) = \vec{0}$ then the locus of R is

A. a plane containing the origin O and parallel to two non-collinear

vectors \vec{OP} and \vec{OQ}

B. the surface of a sphere described on PQ as its diameter

C. a line passing through points P and Q

D. a set of lines parallel to line PQ

Answer: c



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10. Two adjacent sides of a parallelogram ABCD are

$2\hat{i} + 4\hat{j} - 5\hat{k}$ and $\hat{i} + 2\hat{j} + 3\hat{k}$. Then the value of $\left| \vec{AC} \times \vec{BD} \right|$ is

A. $20\sqrt{5}$

B. $22\sqrt{5}$

C. $24\sqrt{5}$

D. $26\sqrt{5}$

Answer: b



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11. If \hat{a} , \hat{b} , and \hat{c} are three unit vectors inclined to each other at angle θ ,

then the maximum value of θ is $\frac{\pi}{3}$ b. $\frac{\pi}{4}$ c. $\frac{2\pi}{3}$ d. $\frac{5\pi}{6}$

A. $\frac{\pi}{3}$

B. $\frac{\pi}{2}$

C. $\frac{2\pi}{3}$

D. $\frac{5\pi}{5}$

Answer: c



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12. Let the pair of vector \vec{a}, \vec{b} and \vec{c}, \vec{d} each determine a plane. Then the planes are parallel if

A. $(\vec{a} \times \vec{c}) \times (\vec{b} \times \vec{d}) = \vec{0}$

B. $(\vec{a} \times \vec{c}) \cdot (\vec{b} \times \vec{d}) = \vec{0}$

C. $(\vec{a} \times \vec{c}) \times (\vec{c} \times \vec{d}) = \vec{0}$

D. $(\vec{a} \times \vec{c}) \cdot (\vec{c} \times \vec{d}) = \vec{0}$

Answer: c



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13. If $\vec{r} \cdot \vec{a} = \vec{r} \cdot \vec{b} = \vec{r} \cdot \vec{c} = 0$ where \vec{a}, \vec{b} and \vec{c} are non-coplanar, then

A. $\vec{r} \perp (\vec{c} \times \vec{a})$

B. $\vec{r} \perp (\vec{a} \times \vec{b})$

C. $\vec{r} \perp (\vec{b} \times \vec{c})$

D. $\vec{r} = \vec{0}$

Answer: d

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14. If \vec{a} satisfies $\vec{a} \times (\hat{i} + 2\hat{j} + \hat{k}) = \hat{i} - \hat{k}$ then \vec{a} is equal to

A. a) $\lambda\hat{i} + (2\lambda - 1)\hat{j} + \lambda\hat{k}, \lambda \in R$

B. b) $\lambda\hat{i} + (1 - 2\lambda)\hat{j} + \lambda\hat{k}, \lambda \in R$

C. c) $\lambda\hat{i} + (2\lambda + 1)\hat{j} + \lambda\hat{k}, \lambda \in R$

D. d) $\lambda\hat{i} + (1 + 2\lambda)\hat{j} + \lambda\hat{k}, \lambda \in R$

Answer: c

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15. Vectors $3\vec{a} - 5\vec{b}$ and $2\vec{a} + \vec{b}$ are mutually perpendicular. If $\vec{a} + 4\vec{b}$ and $\vec{b} - \vec{a}$ are also mutually perpendicular, then the cosine of the angle between \vec{a} and \vec{b} is (a) $\frac{19}{5\sqrt{43}}$ (b) $\frac{19}{3\sqrt{43}}$ (c) $\frac{19}{\sqrt{45}}$ (d) $\frac{19}{6\sqrt{43}}$

A. $\frac{19}{5\sqrt{43}}$

B. $\frac{19}{3\sqrt{43}}$

C. $\frac{19}{\sqrt{45}}$

D. $\frac{19}{6\sqrt{43}}$

Answer: a



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16. The units vectors orthogonal to the vector $-\hat{i} + 2\hat{j} + 2\hat{k}$ and making equal angles with the X and Y axes is/are :

A. $\pm \frac{1}{3}(2\hat{i} + 2\hat{j} - \hat{k})$

B. $\frac{19}{5\sqrt{43}}$

C. $\pm \frac{1}{3}(\hat{i} + \hat{j} - \hat{k})$

D. none of these

Answer: a

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17. The value of x for which the angle between $\vec{a} = 2x^2\hat{i} + 4x\hat{j} = \hat{k} + \hat{k}$ and $\vec{b} = 7\hat{i} - 2\hat{j} = x\hat{k}$, is obtuse and the angle between \vec{b} and the z-axis is acute and less than $\pi/6$, are

A. $a < x < 1/2$

B. $1/2 < x < 15$

C. $x < 1/2$ or $x < 0$

D. none of these

Answer: d



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18. If vectors \vec{a} and \vec{b} are two adjacent sides of parallelogram then the vector representing the altitude of the parallelogram which is

perpendicular to \vec{a} is (A) $\vec{b} + \frac{\vec{b} \times \vec{a}}{|\vec{a}|^2}$ (B) $\frac{\vec{a} \cdot \vec{b}}{|\vec{b}|^2}$ (C) $\vec{b} - \frac{\vec{b} \cdot \vec{a}}{(|\vec{a}|)^2}$ (D)

$$\frac{\vec{a} \times (\vec{b} \times \vec{a})}{|\vec{b}|^{20}}$$

A. $\vec{b} + \frac{\vec{b} \times \vec{a}}{|\vec{a}|^2}$

B. $\frac{\vec{a} \cdot \vec{b}}{|\vec{b}|^2}$

C. $\vec{b} - \frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^2} \vec{a}$

D. $\frac{\vec{a} \times (\vec{b} \times \vec{a})}{|\vec{b}|^2}$

Answer: c



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19. A parallelogram is constructed on $3\vec{a} + \vec{b}$ and $\vec{a} - 4\vec{b}$, where $|\vec{a}| = 6$ and $|\vec{b}| = 8$ and \vec{a} and \vec{b} are anti parallel then the length of the longer diagonal is (A) 40 (B) 64 (C) 32 (D) 48

A. 40

B. 64

C. 32

D. 48

Answer: c



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20. Let $\vec{a} \cdot \vec{b} = 0$ where \vec{a} and \vec{b} are unit vectors and the vector \vec{c} is inclined at an angle θ to both \vec{a} and \vec{b} . If $\vec{c} = m\vec{a} + n\vec{b} + p(\vec{a} \times \vec{b})$, ($m, n, p \in R$) then

A. $\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$

B. $\frac{\pi}{4} \leq \theta \leq \frac{3\pi}{4}$

C. $0 \leq \theta \leq \frac{\pi}{4}$

D. $0 \leq \theta \leq \frac{3\pi}{4}$

Answer: a



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21. \vec{a} and \vec{c} are unit vectors and $|\vec{b}| = 4$ the angle between \vec{a} and \vec{c} is $\cos^{-1}(1/4)$ and $\vec{b} - 2\vec{c} = \lambda\vec{a}$ the value of λ is

A. 3,-4

B. 1/4,3/4

C. -3, 4

D. -1/4, $\frac{3}{4}$

Answer: a



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22. Let the position vectors of the points P and Q be $4\hat{i} + \hat{j} + \lambda\hat{k}$ and $2\hat{i} - \hat{j} + \lambda\hat{k}$, respectively. Vector $\hat{i} - \hat{j} + 6\hat{k}$ is perpendicular to the plane containing the origin and the points P and Q . Then λ equals a $-1/2$ b. $1/2$ c. 1 d. none of these

A. $-1/2$

B. $1/2$

C. 1

D. none of these

Answer: a



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23. A vector of magnitude $\sqrt{2}$ coplanar with the vectors $\vec{a} = \hat{i} + \hat{j} + 2\hat{k}$ and $\vec{b} = \hat{i} + \hat{j} + \hat{k}$, and perpendicular to the vector

$\vec{c} = \hat{i} + \hat{j} + \hat{k}$ is

A. $-\hat{j} + \hat{k}$

B. \hat{i} and \hat{k}

C. $\hat{i} - \hat{k}$

D. $\hat{i} - \hat{j} + \hat{k}$

Answer: a



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24. Let P be a point interior to the acute triangle ABC . If $\vec{PA} + \vec{PB} + \vec{PC}$ is a null vector, then w.r.t triangle ABC , point P is its a. centroid b. orthocentre c. incentre d. circumcentre

A. centroid

B. orthocentre

C. incentre

D. circumcentre

Answer: a



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25. G is the centroid of triangle ABC and A_1 and B_1 are the midpoints of sides AB and AC, respectively. If Δ_1 is the area of quadrilateral GA_1AB_1 and Δ is the area of triangle ABC, then $\frac{\Delta}{\Delta_1}$ is equal to

A. $\frac{3}{2}$

B. 3

C. $\frac{1}{3}$

D. none of these

Answer: b



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26. Points \vec{a} , \vec{b} , \vec{c} and \vec{d} are coplanar and $(\sin\alpha)\vec{a} + (2\sin2\beta)\vec{b} + (3\sin3\gamma)\vec{c} - \vec{d} = \vec{0}$. Then the least value of $\sin^2\alpha + \sin^22\beta + \sin^23\gamma$ is

A. $1/14$

B. 14

C. 6

D. $1/\sqrt{6}$

Answer: a



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27. If \vec{a} and \vec{b} are any two vectors of magnitudes 1 and 2, respectively, and $(1 - 3\vec{a} \cdot \vec{b})^2 + |2\vec{a} + \vec{b} + 3(\vec{a} \times \vec{b})|^2 = 47$ then the angle between \vec{a} and \vec{b} is

A. $\pi/3$

B. $\pi - \cos^{-1}(1/4)$

C. $\frac{2\pi}{3}$

D. $\cos^{-1}(1/4)$

Answer: c



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28. If \vec{a} and \vec{b} are any two vectors of magnitude 2 and 3 respectively such that $|2(\vec{a} \times \vec{b})| + |3(\vec{a} \cdot \vec{b})| = k$ then the maximum value of k is (a) $\sqrt{13}$ (b) $2\sqrt{13}$ (c) $6\sqrt{13}$ (d) $10\sqrt{13}$

A. $\sqrt{13}$

B. $2\sqrt{13}$

C. $6\sqrt{13}$

D. $10\sqrt{13}$

Answer: c



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29. \vec{a} , \vec{b} and \vec{c} are unit vectors such that $|\vec{a} + \vec{b} + 3\vec{c}| = 4$ Angle between \vec{a} and \vec{b} is θ_1 , between \vec{b} and \vec{c} is θ_2 and between \vec{a} and \vec{b} varies $[\pi/6, 2\pi/3]$. Then the maximum value of $\cos\theta_1 + 3\cos\theta_2$ is

A. 3

B. 4

C. $2\sqrt{2}$

D. 6

Answer: b



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30. If the vector product of a constant vector \vec{OA} with a variable vector \vec{OB} in a fixed plane OAB be a constant vector, then the locus of B is (a).a

straight line perpendicular to \vec{OA} (b). a circle with centre O and radius equal to $|\vec{OA}|$ (c). a straight line parallel to \vec{OA} (d). none of these

A. a straight line perpendicular to \vec{OA}

B. a circle with centre O and radius equal to $|\vec{OA}|$

C. a straight line parallel to \vec{OA}

D. none of these

Answer: c

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31. Let \vec{u} , \vec{v} and \vec{w} be such that $|\vec{u}| = 1$, $|\vec{v}| = 2$ and $|\vec{w}| = 3$ if the projection of \vec{v} along \vec{u} is equal to that of \vec{w} along \vec{u} and vectors \vec{v} and \vec{w} are perpendicular to each other then $|\vec{u} - \vec{v} + \vec{w}|$ equals

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32. If the two adjacent sides of two rectangles are represented by

vectors

$$\vec{p} = 5\vec{a} - 3\vec{b}, \vec{q} = -\vec{a} - 2\vec{b} \text{ and } \vec{r} = -4\vec{a} - \vec{b}, \vec{s} = -\vec{a} + \vec{b},$$

respectively, then the angle between the vectors

$$\vec{x} = \frac{1}{3}(\vec{p} + \vec{r} + \vec{s}) \text{ and } \vec{y} = \frac{1}{5}(\vec{r} + \vec{s}) \text{ is}$$

A. $-\cos^{-1}\left(\frac{19}{5\sqrt{43}}\right)$

B. $\cos^{-1}\left(\frac{19}{5\sqrt{43}}\right)$

C. $\pi\cos^{-1}\left(\frac{19}{5\sqrt{43}}\right)$

D. cannot of these

Answer: b



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33. If $\vec{\alpha} \perp (\vec{b} \times \vec{y})$, then $(\vec{\alpha} \times \vec{\beta}) \cdot (\vec{\alpha} \times \vec{y}) =$ (A) $|\vec{\alpha}|^2(\vec{\beta} \cdot \vec{y})$ (B)

$|\vec{\beta}|^2(\vec{y} \cdot \vec{\alpha})$ (C) $|\vec{y}|^2(\vec{\alpha} \cdot \vec{\beta})$ (D) $|\vec{\alpha}||\vec{\beta}||\vec{y}|$

A. $|\vec{\alpha}|^2(\vec{\beta} \cdot \vec{y})$

B. $|\vec{\beta}|^2(\vec{\gamma} \cdot \vec{\alpha})$

C. $|\vec{\gamma}|^2(\vec{\alpha} \cdot \vec{\beta})$

D. $|\vec{\alpha}||\vec{\beta}||\vec{\gamma}|$

Answer: a



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34. The position vectors of points A, B and C are $\hat{i} + \hat{j}$, $\hat{i} + 5\hat{j} - \hat{k}$ and $2\hat{i} + 3\hat{j} + 5\hat{k}$, respectively the greatest angle of triangle ABC is

A. 120°

B. 90°

C. $\cos^{-1}(3/4)$

D. none of these

Answer: b



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35. Given three vectors \vec{a} , \vec{b} , and \vec{c} two of which are non-collinear. Further if $(\vec{a} + \vec{b})$ is collinear with \vec{c} , $(\vec{b} + \vec{c})$ is collinear with \vec{a} , $|\vec{a}| = |\vec{b}| = |\vec{c}| = \sqrt{2}$. Find the value of $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$ a. 3 b. -3 c. 0 d. cannot be evaluated

A. 3

B. -3

C. 0

D. cannot of these

Answer: b



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36. If \vec{a} and \vec{b} are unit vectors such that $(\vec{a} + \vec{b}) \cdot (2\vec{a} + 3\vec{b}) \times (3\vec{a} - 2\vec{b}) = 0$ then angle between \vec{a} and \vec{b} is

A. 0

B. $\pi/2$

C. π

D. indeterminate

Answer: d



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37. If in a right-angled triangle ABC, the hypotenuse $AB = p$, then

$\vec{AB} \cdot \vec{AC} + \vec{BC} \cdot \vec{BA} + \vec{CA} \cdot \vec{CB}$ is equal to

A. $2p^2$

B. $\frac{p^2}{2}$

C. p^2

D. none of these

Answer: c



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38. Resolved part of vector \vec{a} and along vector \vec{b} is \vec{a}_1 and that perpendicular to \vec{b} is \vec{a}_2 then $\vec{a}_1 \times \vec{a}_2$ is equal to

A.
$$\frac{(\vec{a} \times \vec{b}) \cdot \vec{b}}{|\vec{b}|^2}$$

B.
$$\frac{(\vec{a} \cdot \vec{b})\vec{a}}{|\vec{a}|^2}$$

C.
$$\frac{(\vec{a} \cdot \vec{b})(\vec{b} \times \vec{a})}{|\vec{b}|^2}$$

D.
$$\frac{(\vec{a} \cdot \vec{b})(\vec{b} \times \vec{a})}{|\vec{b} \times \vec{a}|}$$

Answer: c



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39. Let $\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$, $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$ and $\vec{c} = \hat{i} + \hat{j} - 2\hat{k}$ be three vectors. A vector in the plane of \vec{b} and \vec{c} whose projection on \vec{a} is of magnitude $\sqrt{\left(\frac{2}{3}\right)}$ is (A) $2\hat{i} + 3\hat{j} + 3\hat{k}$ (B) $2\hat{i} + 3\hat{j} - 3\hat{k}$ (C) $-2\hat{i} - \hat{j} + 5\hat{k}$ (D) $2\hat{i} + \hat{j} + 5\hat{k}$

A. $2\hat{i} + 3\hat{j} - 3\hat{k}$

B. $-2\hat{i} - \hat{j} + 5\hat{k}$

C. $2\hat{i} + 3\hat{j} + 3\hat{k}$

D. $2\hat{i} + \hat{j} + 5\hat{k}$

Answer: b

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40. If P is any arbitrary point on the circumcircle of the equilateral triangle of side length l units, then $|\vec{PA}|^2 + |\vec{PB}|^2 + |\vec{PC}|^2$ is always equal to $2l^2$ b. $2\sqrt{3}l^2$ c. l^2 d. $3l^2$

A. $2l^2$

B. $2\sqrt{3}l^2$

C. l^2

D. $3l^2$

Answer: a



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41. If \vec{r} and \vec{s} are non-zero constant vectors and the scalar b is chosen such that $|\vec{r} + b\vec{s}|$ is minimum, then the value of $|b\vec{s}|^2 + |\vec{r} + b\vec{s}|^2$ is equal to

A. $2|\vec{r}|^2$

B. $|\vec{r}|^2/2$

C. $3|\vec{r}|^2$

D. $|\vec{r}|^2$

Answer: b

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42. \vec{a} and \vec{b} are two unit vectors that are mutually perpendicular. A unit vector that is equally inclined to \vec{a} , \vec{b} and $\vec{a} \times \vec{b}$ is equal to

A. $\frac{1}{\sqrt{2}}(\vec{a} + \vec{b} + \vec{a} \times \vec{b})$

B. $\frac{1}{2}(\vec{a} \times \vec{b} + \vec{a} + \vec{b})$

C. $\frac{1}{\sqrt{3}}(\vec{a} + \vec{b} + \vec{a} \times \vec{b})$

D. $\frac{1}{3}(\vec{a} + \vec{b} + \vec{a} \times \vec{b})$

Answer: a

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43. Given that $\vec{a}, \vec{b}, \vec{p}, \vec{q}$ are four vectors such that

$\vec{a} + \vec{b} = \mu\vec{p}$, $\vec{b} \cdot \vec{q} = 0$ and $|\vec{b}|^2 = 1$ where μ is a scalar. Then

$|(\vec{a} \cdot \vec{q})\vec{p} - (\vec{p} \cdot \vec{q})\vec{a}|$ is equal to

(a) $2|\vec{p}\vec{q}|$ (b) $(1/2)|\vec{p} \cdot \vec{q}|$ (c) $|\vec{p} \times \vec{q}|$ (d) $|\vec{p} \cdot \vec{q}|$

A. $2|\vec{p}\vec{q}|$

B. $(1/2)|\vec{p} \cdot \vec{q}|$

C. $|\vec{p} \times \vec{q}|$

D. $|\vec{p} \cdot \vec{q}|$

Answer: d



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44. The position vectors of the vertices A, B and C of a triangle are three unit vectors \vec{a} , \vec{b} and \vec{c} respectively. A vector \vec{d} is such that $\vec{d} \cdot \hat{a} = \vec{d} \cdot \hat{b} = \vec{d} \cdot \hat{c}$ and $\vec{d} = \lambda(\hat{b} + \hat{c})$. Then triangle ABC is

A. acute angled

B. obtuse angled

C. right angled

D. none of these

Answer: a



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45. If a is real constant A, B and C are variable angles and $\sqrt{a^2 - 4}\tan A + a\tan B + \sqrt{a^2 + 4}\tan C = 6a$, then the least value of $\tan^2 A + \tan^2 B + \tan^2 C$ is 6 b. 10 c. 12 d. 3

A. 6

B. 10

C. 12

D. 3

Answer: d



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46. The vertex A triangle ABC is on the line $\vec{r} = \hat{i} + \hat{j} + \lambda\hat{k}$ and the vertices B and C have respective position vectors \hat{i} and \hat{j} . Let Δ be the area of the triangle and $\Delta \in \left[\frac{3}{2}, \frac{\sqrt{33}}{2} \right]$. Then the range of values of λ corresponding to A is

a. $[-4, 4]$ b. $[-2, 2]$ c. $[-4, -2] \cup [2, 4]$

A. $[-8, -4] \cup [4, 8]$

B. $[-4, 4]$

C. $[-2, 2]$

D. $[-4, -2] \cup [2, 4]$

Answer: c

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47. A non-zero vector \vec{a} is such that its projections along vectors $\frac{\hat{i} + \hat{j}}{\sqrt{2}}$, $\frac{-\hat{i} + \hat{j}}{\sqrt{2}}$ and \hat{k} are equal, then unit vector along \vec{a} is

$$\text{A. } \frac{\sqrt{2}\hat{j} - \hat{k}}{\sqrt{3}}$$

$$\text{B. } \frac{\hat{j} - \sqrt{2}\hat{k}}{\sqrt{3}}$$

$$\text{C. } \frac{\sqrt{2}}{\sqrt{3}}\hat{j} + \frac{\hat{k}}{\sqrt{3}}$$

$$\text{D. } \frac{\hat{j} - \hat{k}}{\sqrt{2}}$$

Answer: a



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48. Position vector \hat{k} is rotated about the origin by angle 135° in such a way that the plane made by it bisects the angle between \hat{i} and \hat{j} . Then its

new position is $\pm \frac{\hat{i}}{\sqrt{2}} \pm \frac{\hat{j}}{\sqrt{2}}$ b. $\pm \frac{\hat{i}}{2} \pm \frac{\hat{j}}{2} - \frac{\hat{k}}{\sqrt{2}}$ c. $\frac{\hat{i}}{\sqrt{2}} - \frac{\hat{k}}{\sqrt{2}}$ d. none of these

$$\text{A. } \pm \frac{\hat{i}}{\sqrt{2}} \pm \frac{\hat{j}}{\sqrt{2}}$$

$$\text{B. } \pm \frac{\hat{i}}{2} \pm \frac{\hat{j}}{2} - \frac{\hat{k}}{\sqrt{2}}$$

$$\text{C. } \frac{\hat{i}}{\sqrt{2}} - \frac{\hat{k}}{\sqrt{2}}$$

D. none of these

Answer: d



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49. In a quadrilateral $ABCD$, \vec{AC} is the bisector of \vec{AB} and \vec{AD} , angle between \vec{AB} and \vec{AD} is $2\pi/3$, $15|\vec{AC}| = 3|\vec{AB}| = 5|\vec{AD}|$. Then the angle

between \vec{BA} and \vec{CD} is $\frac{\cos^{-1}(\sqrt{14})}{7\sqrt{2}}$ b. $\frac{\cos^{-1}(\sqrt{21})}{7\sqrt{3}}$ c. $\frac{\cos^{-1}2}{\sqrt{7}}$ d.

$$\frac{\cos^{-1}(2\sqrt{7})}{14}$$

A. $\cos^{-1} \frac{\sqrt{14}}{7\sqrt{2}}$

B. $\cos^{-1} \frac{\sqrt{21}}{7\sqrt{3}}$

C. $\cos^{-1} \frac{2}{\sqrt{7}}$

D. $\cos^{-1} \frac{2\sqrt{7}}{14}$

Answer: c



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50. In $\triangle ABC$, DE and GF are parallel to each other and AD , BG and EF are parallel to each other. If $CD:CE = CG:CB = 2:1$ then the value of $\text{area}(\triangle AEG):\text{area}(\triangle ABD)$ is equal to (a) $7/2$ (b) 3 (c) 4 (d) $9/2$

A. $7/2$

B. 3

C. 4

D. $9/2$

Answer: b



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51. Vectors \hat{a} in the plane of $\vec{b} = 2\hat{i} + \hat{j}$ and $\vec{c} = \hat{i} - \hat{j} + \hat{k}$ is such that it is equally inclined to \vec{b} and \vec{d} where $\vec{d} = \hat{j} + 2\hat{k}$ the value of \hat{a} is (a) $\frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$

(b) $\frac{\hat{i} - \hat{j} + \hat{k}}{\sqrt{3}}$ (c) $\frac{2\hat{i} + \hat{j}}{\sqrt{5}}$ (d) $\frac{2\hat{i} + \hat{j}}{\sqrt{5}}$

A. $\frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$

B. $\frac{\hat{i} - \hat{j} + \hat{k}}{\sqrt{3}}$

C. $\frac{2\hat{i} + \hat{j}}{\sqrt{5}}$

D. $\frac{2\hat{i} + \hat{j}}{\sqrt{5}}$

Answer: b



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52. Let $ABCD$ be a tetrahedron such that the edges AB, AC and AD are mutually perpendicular. Let the area of triangles ABC, ACD and ADB be 3, 4 and 5 sq. units, respectively. Then the area of triangle BCD is a. $5\sqrt{2}$ b. 5

c. $\frac{\sqrt{5}}{2}$ d. $\frac{5}{2}$

A. $5\sqrt{2}$

B. 5

C. $\frac{\sqrt{5}}{2}$

D. $\frac{5}{2}$

Answer: a

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53. Let $\vec{f}(t) = [t]\hat{i} + (t - [t])\hat{j} + [t + 1]\hat{k}$, where $[.]$ denotes the greatest integer

function. Then the vectors $f\left(\frac{5}{4}\right)$ and $\vec{f}(t)$, $0 < t < 1$ are (a) parallel to each

other (b) perpendicular to each other (c) inclined at $\cos^{-1}\left(\frac{2}{\sqrt{7(1-t^2)}}\right)$

(d) inclined at $\cos^{-1}\left(\frac{8+t}{9 \cdot \sqrt{1+t^2}}\right)$

A. parallel to each other

B. perpendicular to each other

C. inclined at $\frac{\cos^{-1}2}{\sqrt{7}(1-t^2)}$

D. inclined at $\frac{\cos^{-1}(8+t)}{9\sqrt{1+t^2}}$

Answer: d

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54. If \vec{a} is parallel to $\vec{b} \times \vec{c}$, then $(\vec{a} \times \vec{b}) \cdot (\vec{a} \times \vec{c})$ is equal to (a) $|\vec{a}|^2(\vec{b} \cdot \vec{c})$

(b) $|\vec{b}|^2(\vec{a} \cdot \vec{c})$ (c) $|\vec{c}|^2(\vec{a} \cdot \vec{b})$ (d) none of these

A. $|\vec{a}|^2(\vec{b} \cdot \vec{c})$

B. $|\vec{b}|^2(\vec{a} \cdot \vec{c})$

C. $|\vec{c}|^2(\vec{a} \cdot \vec{b})$

D. none of these

Answer: a

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55. The three vectors $\hat{i} + \hat{j}, \hat{j} + \hat{k}, \hat{k} + \hat{i}$ taken two at a time form three planes, The three unit vectors drawn perpendicular to these planes form a parallelepiped of volume: _____

A. $1/3$

B. 4

C. $(3\sqrt{3})/4$

D. $4\sqrt{3}$

Answer: d



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56. If $\vec{d} = \vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}$ is a non zero vector and

$$\left| (\vec{d} \cdot \vec{c})(\vec{a} \times \vec{b}) + (\vec{d} \cdot \vec{a})(\vec{b} \times \vec{c}) + (\vec{d} \cdot \vec{b})(\vec{c} \times \vec{a}) \right| = 0 \quad \text{then (A)}$$

$$|\vec{a}| + |\vec{b}| + |\vec{c}| = |\vec{d}| \quad \text{(B)} \quad |\vec{a}| = |\vec{b}| = |\vec{c}| \quad \text{(C)} \quad \vec{a}, \vec{b}, \vec{c} \text{ are coplanar (D)}$$

$$\vec{a} + \vec{c} = 2\vec{b}$$

A. $|\vec{a}| = |\vec{b}| = |\vec{c}|$

B. $|\vec{a}| + |\vec{b}| + |\vec{c}| = |\vec{d}|$

C. \vec{a} , \vec{b} and \vec{c} are coplanar

D. none of these

Answer: c



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57. If $|\vec{a}| = 2$ and $|\vec{b}| = 3$ and $\vec{a} \cdot \vec{b} = 0$, then $(\vec{a} \times (\vec{a} \times (\vec{a} \times (\vec{a} \times \vec{b}))))$ is equal to the given diagonal is $\vec{c} = 4\hat{k} = 8\hat{k}$ then , the volume of a parallelepiped is

A. $48\hat{b}$

B. $-48\hat{b}$

C. $48\hat{a}$

D. $-48\hat{a}$

Answer: a



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58. If two diagonals of one of its faces are $6\hat{i} + 6\hat{k}$ and $4\hat{j} + 2\hat{k}$ and of the edges not containing the given diagonals is $\vec{c} = 4\hat{j} - 8\hat{k}$, then the volume of a parallelepiped is

A. 60

B. 80

C. 100

D. 120

Answer: d



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59. The volume of a tetrahedron formed by the coterminus edges \vec{a} , \vec{b} and \vec{c} is 3. Then the volume of the parallelepiped formed by the coterminus edges $\vec{a} + \vec{b}$, $\vec{b} + \vec{c}$ and $\vec{c} + \vec{a}$ is

- A. 6
- B. 18
- C. 36
- D. 9

Answer: c



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60. If \vec{a} , \vec{b} and \vec{c} are three mutually orthogonal unit vectors, then the triple product $[\vec{a} + \vec{b} + \vec{c} \quad \vec{a} + \vec{b} \quad \vec{b} + \vec{c}]$ equals

- A. 0
- B. 1 or -1

C. 1

D. 3

Answer: b



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61. vector \vec{c} are perpendicular to vectors $\vec{a} = (2, -3, 1)$ and $\vec{b} = (1, -2, 3)$

and satisfies the condition $\vec{c} \cdot (\hat{i} + 2\hat{j} - 7\hat{k}) = 10$ then vector \vec{c} is equal to

(a)(7, 5, 1) (b)(-7, -5, -1) (c)(1, 1, -1) (d) none of these

A. 7,5,1

B. (-7, -5, -1)

C. 1,1,-1

D. none of these

Answer: a



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62. Given $\vec{a} = x\hat{i} + y\hat{j} + 2\hat{k}$, $\vec{b} = \hat{i} - \hat{j} + \hat{k}$, $\vec{c} = \hat{i} + 2\hat{j}$, $\vec{a} \perp \vec{b}$, $\vec{a} \cdot \vec{c} = 4$ then find the value of $[\vec{a} \ \vec{b} \ \vec{c}]$.

A. $[\vec{a}\vec{b}\vec{c}]^2 = |\vec{a}|$

B. $[\vec{a}\vec{b}\vec{c}] = |\vec{a}|$

C. $[\vec{a}\vec{b}\vec{c}] = 0$

D. $[\vec{a}\vec{b}\vec{c}] = 0$

Answer: d



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63. Let $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$, $\vec{b} = b_2\hat{j} + b_3\hat{k}$ and $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$ give three non-zero vectors such that \vec{c} is a unit vector perpendicular to both

\vec{a} and \vec{b} . If the angle between \vec{a} and \vec{b} is $\frac{\pi}{6}$, then prove that

$$\begin{vmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{vmatrix} p = \frac{1}{4} (a_1^2 + a_2^2 + a_3^2) (b_1^2 + b_2^2 + b_3^2)$$

A. 0

B. 1

C. $\frac{1}{4} (a_1^2 + a_2^2 + a_3^2) (b_1^2 + b_2^2 + b_3^2)$

D. $\frac{3}{4} (a_1^2 + a_2^2 + a_3^2) (b_1^2 + b_2^2 + b_3^2)$

Answer: c



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64. Let $\vec{r}, \vec{a}, \vec{b}$ and \vec{c} be four non-zero vectors such that

$\vec{r} \cdot \vec{a} = 0$, $|\vec{r} \times \vec{b}| = |\vec{r}| |\vec{b}|$ and $|\vec{r} \times \vec{c}| = |\vec{r}| |\vec{c}|$ then $[a b c]$ is equal to

A. $|a||b||c|$

B. $-|a||b||c|$

C. 0

D. none of these

Answer: c



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65. If \vec{a} , \vec{b} and \vec{c} are such that $[\vec{a} \vec{b} \vec{c}] = 1$, $\vec{c} = \lambda(\vec{a} \times \vec{b})$, angle between \vec{c} and \vec{b} is $2\pi/3$, $|\vec{a}| = \sqrt{2}$, $|\vec{b}| = \sqrt{3}$ and $|\vec{c}| = \frac{1}{\sqrt{3}}$ then the angle between \vec{a} and \vec{b} is

A. $\frac{\pi}{6}$

B. $\frac{\pi}{4}$

C. $\frac{\pi}{3}$

D. $\frac{\pi}{2}$

Answer: b



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66. If $4\vec{a} + 5\vec{b} + 9\vec{c} = 0$ then $(\vec{a} \times \vec{b}) \times [(\vec{b} \times \vec{c}) \times (\vec{c} \times \vec{a})]$ is equal to

A. a vector perpendicular to the plane of \vec{a} , \vec{b} and \vec{c}

B. a scalar quantity

C. $\vec{0}$

D. none of these

Answer: c



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67. value of $[\vec{a} \times \vec{b} \vec{a} \times \vec{c} \vec{d}]$ is always equal to

A. $(\vec{a} \cdot \vec{d})[\vec{a} \vec{b} \vec{c}]$

B. $(\vec{a} \cdot \vec{c})[\vec{a} \vec{b} \vec{d}]$

C. $(\vec{a} \cdot \vec{b})[\vec{a} \vec{b} \vec{d}]$

D. none of these

Answer: a



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68. Let \hat{a} and \hat{b} be mutually perpendicular unit vectors. Then for an arbitrary \vec{r} .

A. $\vec{r} = (\vec{r} \cdot \hat{a})\hat{a} + (\vec{r} \cdot \hat{b})\hat{b} + (\vec{r} \cdot (\hat{a} \times \hat{b}))(\hat{a} \times \hat{b})$

B. $\vec{r} = (\vec{r} \cdot \hat{a}) - (\vec{r} \cdot \hat{b})\hat{b} - (\vec{r} \cdot (\hat{a} \times \hat{b}))(\hat{a} \times \hat{b})$

C. $\vec{r} = (\vec{r} \cdot \hat{a})\hat{a} - (\vec{r} \cdot \hat{b})\hat{b} - (\vec{r} \cdot (\hat{a} \times \hat{b}))(\hat{a} \times \hat{b})$

D. none of these

Answer: a



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69. Let \vec{a} and \vec{b} be unit vectors that are perpendicular to each other, then

$[\vec{a} + (\vec{a} \times \vec{b}) + (\vec{a} \times \vec{b})]$ is equal to

A. 1

B. 0

C. -1

D. none of these

Answer: a



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70. \vec{a} and \vec{b} are two vectors such that $|\vec{a}| = 1$, $|\vec{b}| = 4$ and $\vec{a} \cdot \text{Vecb} = 2$. If $\text{vecc} = (2\vec{a} \times \vec{b}) - 3\vec{b}$ then find angle between \vec{b} and \vec{c} .

A. $\frac{\pi}{3}$

B. $\frac{\pi}{6}$

C. $C \frac{3\pi}{4}$

D. $D \frac{5\pi}{6}$

Answer: d

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71. If \vec{b} and \vec{c} are unit vectors, then for any arbitrary vector \vec{a} , $\left(\left((\vec{a} \times \vec{b}) + (\vec{a} \times \vec{c}) \right) \times (\vec{b} \times \vec{c}) \right) \cdot (\vec{b} - \vec{c})$ is always equal to

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72. If $\vec{a} \cdot \vec{b} = \beta$ and $\vec{a} \times \vec{b} = \vec{c}$, then \vec{b} is

A. $\frac{(\beta \vec{a} - \vec{a} \times \vec{c})}{|\vec{a}|^2}$

B. $\frac{(\beta \vec{a} + \vec{a} \times \vec{c})}{|\vec{a}|^2}$

C. $\frac{(\beta \vec{c} + \vec{a} \times \vec{c})}{|\vec{a}|^2}$

$$D. \frac{(\beta \vec{c} + \vec{a} \times \vec{c})}{|\vec{a}|^2}$$

Answer: a



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73. If $a(\vec{\alpha} \times \vec{\beta}) = b(\vec{\beta} \times \vec{\gamma}) + c(\vec{\gamma} \times \vec{\alpha}) = \vec{0}$ and at least one of a, b and c is non zero then vectors $\vec{\alpha}, \vec{\beta}, \vec{\gamma}$ are (A) parallel (B) coplanar (C) mutually perpendicular (D) none of these

A. parallel

B. coplanar

C. mutually perpendicular

D. none of these

Answer: b



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74. if $(\vec{a} \times \vec{b}) \times (\vec{b} \times \vec{c}) = \vec{b}$, where \vec{a} , \vec{b} and \vec{c} are non-zero vectors, then

- A. \vec{a} , \vec{b} and \vec{c} can be coplanar
- B. \vec{a} , \vec{b} and \vec{c} must be coplanar
- C. \vec{a} , \vec{b} and \vec{c} cannot be coplanar
- D. none of these

Answer: c



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75. If $\vec{r} \cdot \vec{a} = \vec{r} \cdot \vec{b} = \vec{r} \cdot \vec{c} = \frac{1}{2}$ for some non zero vector \vec{r} and \vec{a} , \vec{b} , \vec{c} are non coplanar, then the area of the triangle whose vertices are $A(\vec{a})$, $B(\vec{b})$ and $C(\vec{c})$ is

A. $\left| [\vec{a}\vec{b}\vec{c}] \right|$

B. $|\vec{r}|$

C. $\left| \left[\vec{a} \vec{b} \vec{c} \right] \vec{r} \right|$

D. none of these

Answer: c



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76. A vector of magnitude 10 along the normal to the curve $3x^2 + 8xy + 2y^2 - 3 = 0$ at its point $P(1, 0)$ can be $6\hat{i} + 8\hat{j}$ b. $-8\hat{i} + 3\hat{j}$ c. $6\hat{i} - 8\hat{j}$
d. $8\hat{i} + 6\hat{j}$

A. $6\hat{i} + 8\hat{j}$

B. $-8\hat{i} + 3\hat{j}$

C. $6\hat{i} - 8\hat{j}$

D. $8\hat{i} + 6\hat{j}$

Answer: a



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77. If \vec{a} and \vec{b} are two unit vectors inclined at an angle $\frac{\pi}{3}$ then

$\{\vec{a} \times (\vec{b} + \vec{a} \times \vec{b})\} \cdot \vec{b}$ is equal to (a) $-\frac{3}{4}$ (b) $\frac{1}{4}$ (c) $\frac{3}{4}$ (d) $\frac{1}{2}$

A. $\frac{-3}{4}$

B. $\frac{1}{4}$

C. $\frac{3}{4}$

D. $\frac{1}{2}$

Answer: a



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78. If \vec{a} and \vec{b} are orthogonal unit vectors, then for a vector \vec{r} non-coplanar with \vec{a} and \vec{b} vector $\vec{r} \times \vec{a}$ is equal to

A. $[\vec{r} \vec{a} \vec{b}] \vec{b} - (\vec{r} \cdot \vec{b})(\vec{b} \times \vec{a})$

B. $[\vec{r} \vec{a} \vec{b}](\vec{a} + \vec{b})$

C. $[\vec{r} \vec{a} \vec{b}] \vec{a} + (\vec{r} \cdot \vec{a}) \vec{a} \times \vec{b}$

D. none of these

Answer: a

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79. If $\vec{a} + \vec{b}, \vec{c}$ are any three non- coplanar vectors then the equation

$$[\vec{b} \times \vec{c} \vec{c} \times \vec{a} \vec{a} \times \vec{b}] x^2 + [\vec{a} + \vec{b} \vec{b} + \vec{c} \vec{c} + \vec{a}] x + 1 + [\vec{b} - \vec{c} \vec{c} - \vec{c} - \vec{a} \vec{a} - \vec{b}] = 0$$

has roots

A. real and distinct

B. real

C. equal

D. imaginary

Answer: c

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80. Solve the simultaneous vector equations for

$$\vec{x} \text{ and } \vec{y}: \vec{x} + \vec{c} \times \vec{y} = \vec{a} \text{ and } \vec{y} + \vec{c} \times \vec{x} = \vec{b}, \vec{c} \neq 0$$

$$\text{A. } \vec{x} = \frac{\vec{b} \times \vec{c} + \vec{a} + (\vec{c} \cdot \vec{a})\vec{c}}{1 + \vec{c} \cdot \vec{c}}$$

$$\text{B. } \vec{x} = \frac{\vec{c} \times \vec{b} + \vec{b} + (\vec{c} \cdot \vec{a})\vec{c}}{1 + \vec{c} \cdot \vec{c}}$$

$$\text{C. } \vec{y} = \frac{\vec{a} \times \vec{c} + \vec{b} + (\vec{c} \cdot \vec{b})\vec{c}}{1 + \vec{c} \cdot \vec{c}}$$

D. none of these

Answer: b



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81. The condition for equations $\vec{r} \times \vec{a} = \vec{b}$ and $\vec{r} \times \vec{c} = \vec{d}$ to be consistent is

$$\text{A. } \vec{b} \cdot \vec{c} = \vec{a} \cdot \vec{d}$$

B. $\vec{a} \cdot \vec{b} = \vec{c} \cdot \vec{d}$

C. $\vec{b} \cdot \vec{c} + \vec{a} \cdot \vec{d} = 0$

D. $\vec{a} \cdot \vec{b} + \vec{c} \cdot \vec{d} = 0$

Answer: c



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82. If $\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$, $\vec{b} = \hat{i} + 2\hat{j} + 2\hat{k}$ then $[\vec{a}\vec{b}\hat{i}]\hat{i} + [\vec{a}\vec{b}\hat{j}]\hat{j} + [\vec{a}\vec{b}\hat{k}]\hat{k}$ is equal to



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83.

If

$\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$, $\vec{b} = \hat{i} + 2\hat{j} + 2\hat{k}$, $\vec{c} = \hat{i} + \hat{j} + 2\hat{k}$ and $(1 + \alpha)\hat{i} + \beta(1 + \alpha)\hat{j} + \gamma(1 + \alpha)\hat{k}$

A. $-2, -4, -\frac{2}{3}$

B. $2, -4, \frac{2}{3}$

C. $-2, 4, \frac{2}{3}$

D. $2, 4, -\frac{2}{3}$

Answer: a



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84. Let $(\vec{a}(x) = (\sin x)\hat{i} + (\cos x)\hat{j})$ and $(\vec{b}(x) = (\cos 2x)\hat{i} + (\sin 2x)\hat{j})$ be two variable vectors ($x \in R$). Then $\vec{a}(x)$ and $\vec{b}(x)$ are

- A. collinear for unique value of x
- B. perpendicular for infinite values of x.
- C. zero vectors for unique value of x
- D. none of these

Answer: b



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85. For any vectors

\vec{a} and \vec{b} , $(\vec{a} \times \hat{i}) + (\vec{b} \times \hat{i}) + (\vec{a} \times \hat{j}) + (\vec{b} \times \hat{j}) + (\vec{a} \times \hat{k}) + (\vec{b} \times \hat{k})$ is always equal to

A. $\vec{a} \cdot \vec{b}$

B. $2\vec{a} \cdot \text{Vecb}$

C. zero

D. none of these

Answer: b



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86. If \vec{a} , \vec{b} and \vec{c} are three non coplanar vectors and \vec{r} is any vector in space, then

$$(\vec{a} \times \vec{b}) \times (\vec{r} \times \vec{c}) + (\vec{b} \times \vec{c}) \times (\vec{r} \times \vec{a}) + (\vec{c} \times \vec{a}) \times (\vec{r} \times \vec{b}) =$$

A. $[\vec{a}\vec{b}\vec{c}]\vec{r}$

B. $2[\vec{a}\vec{b}\vec{c}]\vec{r}$

C. $3[\vec{a}\vec{b}\vec{c}]\vec{r}$

D. none of these

Answer: b



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87. If $\vec{p} = \frac{\vec{b} \times \vec{c}}{[\vec{a}\vec{b}\vec{c}]}$, $\vec{q} = \frac{\vec{c} \times \vec{a}}{[\vec{a}\vec{b}\vec{c}]}$ and $\vec{r} = \frac{\vec{a} \times \vec{b}}{[\vec{a}\vec{b}\vec{c}]}$, where \vec{a} , \vec{b} and \vec{c} are

three non-coplanar vectors then the value of the expression

$(\vec{a} + \vec{b} + \vec{c}) \cdot (\vec{p} + \vec{q} + \vec{r})$ is (a)3 (b)2 (c)1 (d)0

A. 3

B. 2

C. 1

D. 0

Answer: a



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88. $A(\vec{a})$, $B(\vec{b})$ and $C(\vec{c})$ are the vertices of triangle ABC and $R(\vec{r})$ is any point in the plane of triangle ABC , then $r\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a}$ is always equal to a. zero b. $[\vec{a}\vec{b}\vec{c}]$ c. $-[\vec{a}\vec{b}\vec{c}]$ d. none of these

A. zero

B. $[\vec{a}\vec{b}\vec{c}]$

C. $-[\vec{a}\vec{b}\vec{c}]$

D. none of these

Answer: b



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89. If \vec{a} , \vec{b} and \vec{c} are non-coplanar vectors and $\vec{a} \times \vec{c}$ is perpendicular to $\vec{a} \times (\vec{b} \times \vec{c})$, then the value of $[\vec{a} \times (\vec{b} \times \vec{c})] \times \vec{c}$ is equal to

A. $[\vec{a}\vec{b}\vec{c}]\vec{c}$

B. $[\vec{a}\vec{b}\vec{c}]\vec{b}$

C. $\vec{0}$

D. $[\vec{a}\vec{b}\vec{c}]\vec{a}$

Answer: c



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90. If V be the volume of a tetrahedron and V' be the volume of another tetrahedron formed by the centroids of faces of the previous tetrahedron and $V = KV'$, then K is equal to a. 9 b. 12 c. 27 d. 81

A. 9

B. 12

C. 27

D. 81

Answer: c



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91. $\left[(\vec{a} \times \vec{b}) \times (\vec{b} \times \vec{c}) (\vec{b} \times \vec{c}) \times (\vec{c} \times \vec{a}) (\vec{c} \times \vec{a}) \times (\vec{a} \times \vec{b}) \right]$ is equal to

(where \vec{a}, \vec{b} and \vec{c} are non - zero non- colanar vectors). (a) $[\vec{a}\vec{b}\vec{c}]^2$

(b) $[\vec{a}\vec{b}\vec{c}]^3$ (c) $[\vec{a}\vec{b}\vec{c}]^4$ (d) $[\vec{a}\vec{b}\vec{c}]$

A. $[\vec{a}\vec{b}\vec{c}]^2$

B. $[\vec{a}\vec{b}\vec{c}]^3$

C. $[\vec{a}\vec{b}\vec{c}]^4$

D. $[\vec{a}\vec{b}\vec{c}]$

Answer: c



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92.

If

$\vec{r} = x_1(\vec{a} \times \vec{b}) + x_2(\vec{b} \times \vec{a}) + x_3(\vec{c} \times \vec{d})$ and $4[\vec{a}\vec{b}\vec{c}] = 1$ then $x_1 + x_2 + x_3$

is equal to

A. $\frac{1}{2}\vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$

B. $\frac{1}{4}\vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$

C. $2\vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$

D. $4\vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$

Answer: d



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93. If the vectors \vec{a} and \vec{b} are perpendicular to each other then a vector \vec{v}

in terms of \vec{a} and \vec{b} satisfying the equations $\vec{v} \cdot \vec{a} = 0$, $\vec{v} \cdot \vec{b} = 1$ and

$[\vec{v} \ \vec{a} \ \vec{b}] = 1$ is

A. $\frac{\vec{b}}{|\vec{b}|^2} + \frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|^2}$

B. $\frac{\vec{b}}{|\vec{b}|} + \frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|^2}$

C. $\frac{\vec{b}}{|\vec{b}|} + \frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|}$

D. none of these

Answer: a



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94. If $\vec{a}' = \hat{i} + \hat{j}$, $\vec{b}' = \hat{i} - \hat{j} + 2\hat{k}$ and $\vec{c}' = 2\hat{i} - \hat{j} - \hat{k}$ then the altitude of the parallelepiped formed by the vectors, \vec{a} , \vec{b} and \vec{c} having base formed by \vec{b} and \vec{c} is (where \vec{a}' is reciprocal vector \vec{a}) (a)1 (b) $3\sqrt{2}/2$ (c) $1/\sqrt{6}$ (d) $1/\sqrt{2}$

A. 1

B. $3\sqrt{2}/2$

C. $1/\sqrt{6}$

D. $1/\sqrt{2}$

Answer: d



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95. If $\vec{a} = \hat{i} + \hat{j}$, $\vec{b} = \hat{j} + \hat{k}$, $\vec{c} = \hat{k} + \hat{i}$ then in the reciprocal system of vectors $\vec{a}, \vec{b}, \vec{c}$ reciprocal \vec{a} of vector \vec{a} is

A. $\frac{\hat{i} + \hat{j} + \hat{k}}{2}$

B. $\frac{\hat{i} - \hat{j} + \hat{k}}{2}$

C. $\frac{-\hat{i} - \hat{j} + \hat{k}}{2}$

D. $\frac{\hat{i} + \hat{j} - \hat{k}}{2}$

Answer: d



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96. If the unit vectors \vec{a} and \vec{b} are inclined of an angle 2θ such that

$$|\vec{a} - \vec{b}| < 1 \text{ and } 0 \leq \theta \leq \pi \text{ then } \theta \text{ in the interval}$$

- A. $[0, \pi/6)$
- B. $(5\pi/6, \pi]$
- C. $[\pi/6, \pi/2]$
- D. $(\pi/2, 5\pi/6]$

Answer: a,b

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97. \vec{b} and \vec{c} are non-collinear if

$$\vec{a} \times (\vec{b} \times \vec{c}) + (\vec{a} \cdot \vec{b})\vec{b} = (4 - 2x - \sin y)\vec{b} + (x^2 - 1)\vec{c} \text{ and } d(\vec{c})\vec{a} = \vec{a} \text{ then}$$

- A. $x = 1$
- B. $x = -1$

$$C. y = (4n + 1)\frac{\pi}{2}, n \in I$$

$$D. y(2n + 1)\frac{\pi}{2}, n \in I$$

Answer: a,c



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98. Let $\vec{a} \cdot \vec{b} = 0$ where \vec{a} and \vec{b} are unit vectors and the vector \vec{c} is inclined at an angle θ to both \vec{a} and \vec{b} . If $\vec{c} = m\vec{a} + n\vec{b} + p(\vec{a} \times \vec{b})$, ($m, n, p \in R$) then

A. $\alpha = \beta$

B. $\gamma^2 = 1 - 2\alpha^2$

C. $\gamma^2 = -\cos 2\theta$

D. $\beta^2 = \frac{1 + \cos 2\theta}{2}$

Answer: a,b,c,d



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99. \vec{a} and \vec{b} are two given vectors. On these vectors as adjacent sides a parallelogram is constructed. The vector which is the altitude of the parallelogram and which is perpendicular to \vec{a} is not equal to

A. $\frac{(\vec{a} \cdot \vec{b})}{|\vec{a}|^2} \vec{a} - \vec{b}$

B. $\frac{1}{|\vec{a}|^2} \{ |\vec{a}|^2 \vec{b} - (\vec{a} \cdot \vec{b}) \vec{a} \}$

C. $\frac{\vec{a} \times (\vec{a} \times \vec{b})}{|\vec{a}|^2}$

D. $\frac{\vec{a} \times (\vec{b} \times \vec{a})}{|\vec{b}|^2}$

Answer: a,b,c



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100. If $\vec{a} \times (\vec{b} \times \vec{c})$ is perpendicular to $(\vec{a} \times \vec{b}) \times \vec{c}$, we may have

A. $(\vec{a} \cdot \vec{c})|\vec{b}|^2 = (\vec{a} \cdot \vec{b})(\vec{b} \cdot \vec{c})$

B. $\vec{a} \cdot \vec{b} = 0$

C. $\vec{a} \cdot \vec{c} = 0$

D. $\vec{b} \cdot \vec{c} = 0$

Answer: a,c

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101. If $\vec{p} = \frac{\vec{b} \times \vec{c}}{[\vec{a} \ \vec{b} \ \vec{c}]}$, $\vec{q} = \frac{\vec{c} \times \vec{a}}{[\vec{a} \ \vec{b} \ \vec{c}]}$, $\vec{r} = \frac{\vec{a} \times \vec{b}}{[\vec{a} \ \vec{b} \ \vec{c}]}$ where $\vec{a}, \vec{b}, \vec{c}$ are

three non-coplanar vectors, then the value of the expression

$(\vec{a} + \vec{b} + \vec{c}) \cdot (\vec{p} + \vec{q} + \vec{r})$ is

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102. $a_1, a_2, a_3 \in R - \{0\}$ and $a_1 + a_2 \cos 2x + a_3 \sin^2 x = 0$ " for all " x in R

then (a) vectors $\vec{a} = a_1 \hat{i} + a_2 \hat{j} + a_3 \hat{k}$ and $\vec{b} = 4\hat{i} + 2\hat{j} + \hat{k}$ are perpendicular

to each other (b) vectors $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ and $\vec{b} = \hat{i} + \hat{j} + 2\hat{k}$ are parallel to each other (c) if vector $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ is of length $\sqrt{6}$ units, then one of the ordered tripplet $(a_1, a_2, a_3) = (1, -1, -2)$ (d) if $2a_1 + 3a_2 + 6a_3 = 26$, then $|\vec{a}\hat{i} + a_2\hat{j} + a_3\hat{k}|$ is $2\sqrt{6}$

A. vectors $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ and $\vec{b} = 4\hat{i} + 2\hat{j} + \hat{k}$ are perpendicular to each other

B. vectors $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ and $\vec{b} = \hat{i} + \hat{j} + 2\hat{k}$ are parallel to each other

C. if vector $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$ is of length $\sqrt{6}$ units, then one of the ordered tripplet $(a_1, a_2, a_3) = (1, -1, -2)$

D. if $2a_1 + 3a_2 + 6a_3 = 26$, then $|\vec{a}\hat{i} + a_2\hat{j} + a_3\hat{k}|$ is $2\sqrt{6}$

Answer: a,b,c,d

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103. If \vec{a} and \vec{b} are two vectors and angle between them is θ , then

A. $|\vec{a} \times \vec{b}|^2 + (\vec{a} \cdot \vec{b})^2 = |\vec{a}|^2 |\vec{b}|^2$

B. $|\vec{a} \times \vec{b}|^2 + (\vec{a} \cdot \vec{b})^2$, if $\theta = \pi/4$

C. $\vec{a} \times \vec{b} = (\vec{a} \cdot \text{Vec}b)\hat{n}$ (where \hat{n} is a normal unit vector) if $\theta = \pi/4$

D. $(\vec{a} \times \vec{b}) \cdot (\vec{a} + \vec{b}) = 0$

Answer: a,b,c,d

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104. Let \vec{a} and \vec{b} be two non- zero perpendicular vectors. A vector \vec{r} satisfying the equation $\vec{r} \times \vec{b} = \vec{a}$ can be

A. $\vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$

B. $2\vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$

C. $|\vec{a}| \vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$

$$D. |\vec{b}| \vec{b} - \frac{\vec{a} \times \vec{b}}{|\vec{b}|^2}$$

Answer: a,b,cd,

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105. If vector $\vec{b} = (\tan\alpha, -1, 2\sqrt{\sin\alpha/2})$ and $\vec{c} = (\tan\alpha, \tan\alpha, -\frac{3}{\sqrt{\sin\alpha/2}})$ are

orthogonal and vector $\vec{a} = (1, 3, \sin 2\alpha)$ makes an obtuse angle with the z-axis, then the value of α is

a. $\alpha = (4n + 1)\pi + \tan^{-1}2$

b. $\alpha = (4n + 1)\pi - \tan^{-1}2$ c. $\alpha = (4n + 2)\pi + \tan^{-1}2$ d. $\alpha = (4n + 2)\pi - \tan^{-1}2$

A. $\alpha = (4n + 1)\pi + \tan^{-1}2$

B. $\alpha = (4n + 1)\pi - \tan^{-1}2$

C. $\alpha = (4n + 2)\pi + \tan^{-1}2$

D. $\alpha = (4n + 2)\pi - \tan^{-1}2$

Answer: b,d

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106. Let \vec{r} be a unit vector satisfying $\vec{r} \times \vec{a} = \vec{b}$, where $|\vec{a}| = \sqrt{3}$ and $|\vec{b}| = \sqrt{2}$, then (a) $\vec{r} = \frac{2}{3}(\vec{a} + \vec{a} \times \vec{b})$ (b) $\vec{r} = \frac{1}{3}(\vec{a} + \vec{a} \times \vec{b})$ (c) $\vec{r} = \frac{2}{3}(\vec{a} - \vec{a} \times \vec{b})$ (d) $\vec{r} = \frac{1}{3}(-\vec{a} + \vec{a} \times \vec{b})$

A. $\vec{r} = \frac{2}{3}(\vec{a} + \vec{a} \times \vec{b})$

B. $\vec{r} = \frac{1}{3}(\vec{a} + \vec{a} \times \vec{b})$

C. $\vec{r} = \frac{2}{3}(\vec{a} - \vec{a} \times \vec{b})$

D. $\vec{r} = \frac{1}{3}(-\vec{a} + \vec{a} \times \vec{b})$

Answer: b,d

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107. If \vec{a} and \vec{b} are unequal unit vectors such that $(\vec{a} - \vec{b}) \times [(\vec{b} + \vec{a}) \times (2\vec{a} + \vec{b})] = \vec{a} + \vec{b}$ then angle θ between \vec{a} and \vec{b} is

A. 0

B. $\pi/2$

C. $\pi/4$

D. π

Answer: b,d



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108. If \vec{a} and \vec{b} are two unit vectors perpendicular to each other and $\vec{c} = \lambda_1 \vec{a} + \lambda_2 \vec{b} + \lambda_3 (\vec{a} \times \vec{b})$, then which of the following is (are) true ?

A. $\lambda_1 = \vec{a} \cdot \vec{c}$

B. $\lambda_2 = |\vec{b} \times \vec{c}|$

C. $\lambda_3 = |\vec{a} \times \vec{b}| \times |\vec{c}|$

D. $\lambda_1 \vec{a} + \lambda_2 \vec{b} + \lambda_3 (\vec{a} \times \vec{b})$

Answer: a,d



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109. If vectors \vec{a} and \vec{b} are non collinear then $\frac{\vec{a}}{|\vec{a}|} + \frac{\vec{b}}{|\vec{b}|}$ is (A) a unit vector (B) in the plane of \vec{a} and \vec{b} (C) equally inclined to \vec{a} and \vec{b} (D) perpendicular to $\vec{a} \times \vec{b}$

A. a unit vector

B. in the plane of \vec{a} and \vec{b}

C. equally inclined to \vec{a} and \vec{b}

D. perpendicular to $\vec{a} \times \vec{b}$

Answer: b,c,d



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110. If \vec{a} and \vec{b} are non - zero vectors such that $|\vec{a} + \vec{b}| = |\vec{a} - 2\vec{b}|$ then

A. $2\vec{a} \cdot \vec{b} = |\vec{b}|^2$

B. $\vec{a} \cdot \vec{b} = |\vec{b}|^2$

C. least value of $\vec{a} \cdot \text{Vecb} + \frac{1}{|\vec{b}|^2 + 2}$ is $\sqrt{2}$

D. least value of $\vec{a} \cdot \vec{b} + \frac{1}{|\vec{b}|^2 + 2}$ is $\sqrt{2} - 1$

Answer: a,d



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111. Let \vec{a} , \vec{b} and \vec{c} be non-zero vectors and

$\vec{V}_1 = \vec{a} \times (\vec{b} \times \vec{c})$ and $\vec{V}_2 = (\vec{a} \times \vec{b}) \times \vec{c}$. vectors \vec{V}_1 and \vec{V}_2 are equal .

Then

A. \vec{a} and \vec{b} are orthogonal

B. \vec{a} and \vec{c} are collinear

C. \vec{b} and \vec{c} are orthogonal

D. $\vec{b} = \lambda(\vec{a} \times \vec{c})$ when λ is a scalar

Answer: b,d

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112. Vectors \vec{A} and \vec{B} satisfying the vector equation $\vec{A} + \vec{B} = \vec{a}$, $\vec{A} \times \vec{B} = \vec{b}$ and $\vec{A} \cdot \vec{a} = 1$. where \vec{a} and \vec{b} are given vectors, are

A. $\vec{A} = \frac{(\vec{a} \times \vec{b}) - \vec{a}}{a^2}$

B. $\vec{B} = \frac{(\vec{b} \times \vec{a}) + \vec{a}(a^2 - 1)}{a^2}$

C. $\vec{A} = \frac{(\vec{a} \times \vec{b}) + \vec{a}}{a^2}$

D. $\vec{B} = \frac{(\vec{b} \times \vec{a}) - \vec{a}(a^2 - 1)}{a^2}$

Answer: b,c,

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113. A vector \vec{d} is equally inclined to three vectors $\vec{a} = \hat{i} - \hat{j} + \hat{k}$, $\vec{b} = 2\hat{i} + \hat{j}$ and $\vec{c} = 3\hat{j} - 2\hat{k}$. Let \vec{x} , \vec{y} and \vec{z} be three vectors in the plane of \vec{a} , \vec{b} ; \vec{b} , \vec{c} ; \vec{c} , \vec{a} , respectively. Then

A. $\vec{x} \cdot \vec{d} = -1$

B. $\vec{y} \cdot \vec{d} = 1$

C. $\vec{z} \cdot \vec{d} = 0$

D. $\vec{r} \cdot \vec{d} = 0$, where $\vec{r} = \lambda\vec{x} + \mu\vec{y} + \delta\vec{z}$

Answer: c.d

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114. Vectors perpendicular to $\hat{i} - \hat{j} - \hat{k}$ and in the plane of $\hat{i} + \hat{j} + \hat{k}$ and $-\hat{i} + \hat{j} + \hat{k}$ are (A) $\hat{i} + \hat{k}$ (B) $2\hat{i} + \hat{j} + \hat{k}$ (C) $3\hat{i} + 2\hat{j} + \hat{k}$ (D) $-4\hat{i} - 2\hat{j} - 2\hat{k}$

A. $\hat{i} + \hat{k}$

$$B. 2\hat{i} + \hat{j} + \hat{k}$$

$$C. 3\hat{i} + 2\hat{j} + \hat{k}$$

$$D. -4\hat{i} - 2\hat{j} - 2\hat{k}$$

Answer: b,d



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115. If the sides \overrightarrow{AB} of an equilateral triangle ABC lying in the xy-plane is $3\hat{i}$ then the side \overrightarrow{CB} can be (A) $-\frac{3}{2}(\hat{i} - \sqrt{3})$ (B) $\frac{3}{2}(\hat{i} - \sqrt{3})$ (C) $-\frac{3}{2}(\hat{i} + \sqrt{3})$ (D) $\frac{3}{2}(\hat{i} + \sqrt{3})$

$$A. -\frac{3}{2}(\hat{i} - \sqrt{3}\hat{j})$$

$$B. -\frac{3}{2}(\hat{i} - \sqrt{3}\hat{j})$$

$$C. -\frac{3}{2}(\hat{i} + \sqrt{3}\hat{j})$$

$$D. \frac{3}{2}(\hat{i} + \sqrt{3}\hat{j})$$

Answer: b,d



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116. Let \hat{a} be a unit vector and \hat{b} a non zero vector non parallel to \vec{a} . Find the angles of the triangle two sides of which are represented by the vectors. $\sqrt{3}(\hat{a} \times \vec{b})$ and $\vec{b} - (\hat{a} \cdot \vec{b})\hat{a}$

A. $\tan^{-1}(\sqrt{3})$

B. $\tan^{-1}(1/\sqrt{3})$

C. $\cot^{-1}(0)$

D. $\tan^{-1}(1)$

Answer: a,b,c



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117. \vec{a}, \vec{b} and \vec{c} are unimodular and coplanar. A unit vector \vec{d} is perpendicular to them, $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = \frac{1}{6}\hat{i} - \frac{1}{3}\hat{j} + \frac{1}{3}\hat{k}$, and the angle

between \vec{a} and \vec{b} is 30° then \vec{c} is

- A. $(\hat{i} - 2\hat{j} + 2\hat{k})/3$
- B. $(-\hat{i} + 2\hat{j} - 2\hat{k})/3$
- C. $(-\hat{i} + 2\hat{j} - \hat{k})/3$
- D. $(-2\hat{i} - 2\hat{j} + \hat{k})/3$

Answer: a,b



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118. If $\vec{a} + 2\vec{b} + 3\vec{c} = \vec{0}$ then $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} =$

- A. $2(\vec{a} \times \vec{b})$
- B. $6(\vec{b} \times \vec{c})$
- C. $3(\vec{c} \times \vec{a})$
- D. $\vec{0}$

Answer: c,d

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119. Let \vec{a} and \vec{b} be two non-collinear unit vectors. If $\vec{u} = \vec{a} - (\vec{a} \cdot \vec{b})\vec{b}$ and $\vec{v} = \vec{a} \times \vec{b}$, then $|\vec{v}|$ is

A. $|\vec{u}|$

B. $|\vec{u}| + |\vec{u} \cdot \vec{b}|$

C. $|\vec{u}| + |\vec{u} \cdot \vec{a}|$

D. none of these

Answer: b,d

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120. if $\vec{a} \times \vec{b} = \vec{c}$, $\vec{b} \times \vec{c} = \vec{a}$, where $\vec{c} \neq \vec{0}$ then (a) $|\vec{a}| = |\vec{c}|$ (b) $|\vec{a}| = |\vec{b}|$

(c) $|\vec{b}| = 1$ (d) $|\vec{a}| = |\vec{b}| = |\vec{c}| = 1$

A. $|\vec{a}| = |\vec{c}|$

B. $|\vec{a}| = |\vec{b}|$

C. $|\vec{b}| = 1$

D. $|\vec{a}| = |\vec{b}| = |\vec{c}| = 1$

Answer: a,c

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121. Let \vec{a} , \vec{b} , and \vec{c} be three non-coplanar vectors and \vec{d} be a non-zero, which is perpendicular to $(\vec{a} + \vec{b} + \vec{c})$. Now $\vec{d} = (\vec{a} \times \vec{b})\sin x + (\vec{b} \times \vec{c})\cos y + 2(\vec{c} \times \vec{a})$. Then

A. $\frac{\vec{d} \cdot (\vec{a} + \vec{c})}{[\vec{a}\vec{b}\vec{c}]} = 2$

B. $\frac{\vec{d} \cdot (\vec{a} + \vec{c})}{[\vec{a}\vec{b}\vec{c}]} = -2$

C. minimum value of $x^2 + y^2$ is $\pi^2/4$

D. minimum value of $x^2 + y^2$ is $5\pi^2/4$

Answer: b,d



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122. If $\vec{a}, \vec{b},$ and \vec{c} are three unit vectors such that $\vec{a} \times (\vec{b} \times \vec{c}) = \frac{1}{1}\vec{b}$, then (\vec{b} and \vec{c} being non-parallel) angle between \vec{a} and \vec{b} is $\pi/3$ b. angle between \vec{a} and \vec{c} is $\pi/3$ c. angle between \vec{a} and \vec{b} is $\pi/2$ d.

a. angle between \vec{a} and \vec{c} is $\pi/2$

A. angle between \vec{a} and \vec{b} is $\pi/3$

B. angle between \vec{a} and \vec{c} is $\pi/3$

C. angle between \vec{a} and \vec{b} is $\pi/2$

D. angle between \vec{a} and \vec{c} is $\pi/2$

Answer: b,c



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123. If in triangle ABC, $\vec{AB} = \frac{\vec{u}}{|\vec{u}|} - \frac{\vec{v}}{|\vec{v}|}$ and $\vec{AC} = \frac{2\vec{u}}{|\vec{u}|}$, where $|\vec{u}| \neq |\vec{v}|$,

then (a) $1 + \cos 2A + \cos 2B + \cos 2C = 0$ (b) $\sin A = \cos C$ (c) projection of AC on BC is equal to BC (d) projection of AB on BC is equal to AB

A. $1 + \cos 2A + \cos 2B + \cos 2C = 0$

B. $\sin A = \cos C$

C. projection of AC on BC is equal to BC

D. projection of AB on BC is equal to AB

Answer: a,b,c



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124. $[\vec{a} \times \vec{b} \quad \vec{c} \times \vec{d} \quad \vec{e} \times \vec{f}]$ is equal to



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125. The scalars l and m such that $l\vec{a} + m\vec{b} = \vec{c}$, where \vec{a} , \vec{b} and \vec{c} are given vectors, are equal to

$$\text{A. } l = \frac{(\vec{c} \times \vec{b}) \cdot (\vec{a} \times \vec{b})}{(\vec{a} \times \vec{b})^2}$$

$$\text{B. } l = \frac{(\vec{c} \times \vec{a}) \cdot (\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})}$$

$$\text{C. } m = \frac{(\vec{c} \times \vec{a}) \cdot (\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})^2}$$

$$\text{D. } m = \frac{(\vec{c} \times \vec{a}) \cdot (\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})}$$

Answer: a,c

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126. If $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) \cdot (\vec{a} \times \vec{d}) = 0$ then which of the following may be true ?

A. \vec{a} , \vec{b} , \vec{c} and \vec{d} are necessarily coplanar

B. \vec{a} lies in the plane of \vec{c} and \vec{d}

C. \vec{b} lies in the plane of \vec{a} and \vec{d}

D. \vec{c} lies in the plane of \vec{a} and \vec{d}

Answer: b,c,d

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127. A, B, C and D are four points such that

$\vec{AB} = m(2\hat{i} - 6\hat{j} + 2\hat{k})$, $\vec{BC} = (\hat{i} - 2\hat{j})$ and $\vec{CD} = n(-6\hat{i} + 15\hat{j} - 3\hat{k})$ If CD

intersects AB at some point E , then a. $m \geq 1/2$ b. $n \geq 1/3$ c. $m = n$ d. $m < n$

A. (a) $m \geq 1/2$

B. (b) $n \geq 1/3$

C. (c) $m = n$

D. (d) $m < n$

Answer: a,b



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128. If the vectors \vec{a} , \vec{b} , \vec{c} are non-coplanar and l, m, n are distinct scalars such that

$$\begin{bmatrix} l\vec{a} + m\vec{b} + n\vec{c} & l\vec{b} + m\vec{c} + n\vec{a} & l\vec{c} + m\vec{a} + n\vec{b} \end{bmatrix} = 0 \text{ then}$$

A. a) $l + m + n = 0$

B. b) roots of the equation $lx^2 + mx + n = 0$ are equal

C. c) $l^2 + m^2 + n^2 = 0$

D. d) $l^3 + m^2 + n^3 = 3lmn$

Answer: a,b,d



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129. Let $\vec{\alpha} = a\hat{i} + b\hat{j} + c\hat{k}$, $\vec{\beta} = b\hat{i} + c\hat{j} + a\hat{k}$ and $\vec{\gamma} = c\hat{i} + a\hat{j} + b\hat{k}$ be three coplanar vectors with $a \neq b$, and $\vec{v} = \hat{i} + \hat{j} + \hat{k}$. Then \vec{v} is perpendicular to

A. $\vec{\alpha}$

B. $\vec{\beta}$

C. $\vec{\gamma}$

D. none of these

Answer: a,b,c



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130. if vectors $\vec{A} = 2\hat{i} + 3\hat{j} + 4\hat{k}$, $\vec{B} = \hat{i} + \hat{j} + 5\hat{k}$ and \vec{C} form a left-handed system, then \vec{C} is

A. $11\hat{i} - 6\hat{j} - \hat{k}$

B. $-11\hat{i} - 6\hat{j} - \hat{k}$

C. $-11\hat{i} - 6\hat{j} + \hat{k}$

$$D. d) -11\hat{i} + 6\hat{j} - \hat{k}$$

Answer: b,d



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131. If $\vec{a} = x\hat{i} + y\hat{j} + z\hat{k}$, $\vec{b} = y\hat{i} + z\hat{j} + x\hat{k}$ and $\vec{c} = z\hat{i} + x\hat{j} + y\hat{k}$,

then $\vec{a} \times (\vec{b} \times \vec{c})$ is

(a) parallel to $(y - z)\hat{i} + (z - x)\hat{j} + (x - y)\hat{k}$ (b) orthogonal to $\hat{i} + \hat{j} + \hat{k}$

(c) orthogonal to $(y + z)\hat{i} + (z + x)\hat{j} + (x + y)\hat{k}$ (d) orthogonal to $x\hat{i} + y\hat{j} + z\hat{k}$

A. parallel to $(y - z)\hat{i} + (z - x)\hat{j} + (x - y)\hat{k}$

B. orthogonal to $\hat{i} + \hat{j} + \hat{k}$

C. orthogonal to $(y + z)\hat{i} + (z + x)\hat{j} + (x + y)\hat{k}$

D. orthogonal to $x\hat{i} + y\hat{j} + z\hat{k}$

Answer: a,b,c,d



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132. If $\vec{a} \times (\vec{b} \times \vec{c}) = (\vec{a} \times \vec{b}) \times \vec{c}$ then

A. $(\vec{c} \times \vec{a}) \times \vec{b} = \vec{0}$

B. $\vec{c} \times (\vec{a} \times \vec{b}) = \vec{0}$

C. $\vec{b} \times (\vec{c} \times \vec{a}) = \vec{0}$

D. $\vec{c} \times \vec{a} \times \vec{b} = \vec{b} \times (\vec{c} \times \vec{a}) = \vec{0}$

Answer: a,c,d



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133. A vector \vec{d} is equally inclined to three vectors

$\vec{a} = \hat{i} - \hat{j} + \hat{k}$, $\vec{b} = 2\hat{i} + \hat{j}$ and $\vec{c} = 3\hat{j} - 2\hat{k}$. Let \vec{x} , \vec{y} and \vec{z} be three vectors in

the plane of \vec{a} , \vec{b} ; \vec{b} , \vec{c} ; \vec{c} , \vec{a} , respectively. Then

A. (a) $\vec{z} \cdot \vec{d} = 0$

B. (b) $\vec{x} \cdot \vec{d} = 1$

C. (c) $\vec{y} \cdot \vec{d} = 32$

D. (d) $\vec{r} \cdot \vec{d} = 0$, where $\vec{r} = \lambda\vec{x} + \mu\vec{y} + \gamma\vec{z}$

Answer: a,d

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134. A parallelogram is constructed on the vectors $\vec{a} = 3\vec{\alpha} - \vec{\beta}$, $\vec{b} = \vec{\alpha} + 3\vec{\beta}$. If $|\vec{\alpha}| = |\vec{\beta}| = 2$ and angle between $\vec{\alpha}$ and $\vec{\beta}$ is $\frac{\pi}{3}$ then the length of a diagonal of the parallelogram is

A. $4\sqrt{5}$

B. $4\sqrt{3}$

C. $4\sqrt{7}$

D. none of these

Answer: b,c

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Reasoning Type

1. (a) Statement 1: Vector $\vec{c} = -5\hat{i} + 7\hat{j} + 2\hat{k}$ is along the bisector of angle between $\vec{a} = \hat{i} + 2\hat{j} + 2\hat{k}$ and $\vec{b} = 8\hat{i} + \hat{j} - 4\hat{k}$.

Statement 2 : \vec{c} is equally inclined to \vec{a} and \vec{b} .

A. (a) Both the statements are true and statement 2 is the correct explanation for statement 1.

B. (b) Both statements are true but statement 2 is not the correct explanation for statement 1.

C. (c) Statement 1 is true and Statement 2 is false

D. (d) Statement 1 is false and Statement 2 is true.

Answer: b



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2. Statement 1: A component of vector $\vec{b} = 4\hat{i} + 2\hat{j} + 3\hat{k}$ in the direction perpendicular to the direction of vector $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ is $-\hat{j}$

Statement 2: A component of vector \vec{b} in the direction of $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ is $2\hat{i} + 2\hat{j} + 2\hat{k}$

A. (a) Both the statements are true and statement 2 is the correct explanation for statement 1.

B. (b) Both statements are true but statement 2 is not the correct explanation for statement 1.

C. (c) Statement 1 is true and Statement 2 is false

D. (d) Statement 1 is false and Statement 2 is true.

Answer: c



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3. Statement 1: Distance of point D(1,0,-1) from the plane of points A(1,-2,0) , B (3, 1,2) and C(-1,1,-1) is $\frac{8}{\sqrt{229}}$

Statement 2: volume of tetrahedron formed by the points A,B, C and D is

$$\frac{\sqrt{229}}{2}$$

- A. (a) Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. (b) Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. (c) Statement 1 is true and Statement 2 is false
- D. (d) Statement 1 is false and Statement 2 is true.

Answer: d



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4. Let \vec{r} be a non - zero vector satisfying $\vec{r} \cdot \vec{a} = \vec{r} \cdot \vec{b} = \vec{r} \cdot \vec{c} = 0$ for given non-zero vectors \vec{a} , \vec{b} and \vec{c}

Statement 1: $[\vec{a} - \vec{b}, \vec{b} - \vec{c}, \vec{c} - \vec{a}] = 0$

Statement 2: $[\vec{a}, \vec{b}, \vec{c}] = 0$

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

Answer: b

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5. Statement 1: If $a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$, $b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$ and $c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$ are three mutually perpendicular unit vectors then $a_1\hat{i} + b_1\hat{j} + c_1\hat{k}$, $a_2\hat{i} + b_2\hat{j} + c_2\hat{k}$ and $a_3\hat{i} + b_3\hat{j} + c_3\hat{k}$ may be mutually perpendicular unit vectors.

Statement 2 : value of determinant and its transpose are the same.

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.
- B. Both statements are true but statement 2 is not the correct explanation for statement 1.
- C. Statement 1 is true and Statement 2 is false
- D. Statement 1 is false and Statement 2 is true.

Answer: a

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6. Statement 1: $\vec{A} = 2\hat{i} + 3\hat{j} + 6\hat{k}$, $\vec{B} = \hat{i} + \hat{j} - 2\hat{k}$ and $\vec{C} = \hat{i} + 2\hat{j} + \hat{k}$ then

$$\left| \vec{A} \times \left(\vec{A} \times \left(\vec{A} \times \vec{B} \right) \right) \cdot \vec{C} \right| = 243 \quad \text{Statement 2:}$$

$$\left| \vec{A} \times \left(\vec{A} \times \left(\vec{A} \times \vec{B} \right) \right) \cdot \vec{C} \right| = \left| \vec{A} \right|^2 \left| \left[\vec{A} \vec{B} \vec{C} \right] \right|$$

- A. Both the statements are true and statement 2 is the correct explanation for statement 1.

B. Both statements are true but statement 2 is not the correct explanation for statement 1.

C. Statement 1 is true and Statement 2 is false

D. Statement 1 is false and Statement 2 is true.

Answer: d

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7. Statement 1: \vec{a} , \vec{b} and \vec{c} are three mutually perpendicular unit vectors and \vec{d} is a vector such that \vec{a} , \vec{b} , \vec{c} and \vec{d} are non-coplanar. If

$$[\vec{d}\vec{b}\vec{c}] = [\vec{d}\vec{a}\vec{b}] = [\vec{d}\vec{c}\vec{a}] = 1, \text{ then } \vec{d} = \vec{a} + \vec{b} + \vec{c}$$

Statement 2: $[\vec{d}\vec{b}\vec{c}] = [\vec{d}\vec{a}\vec{b}] = [\vec{d}\vec{c}\vec{a}] \Rightarrow \vec{d}$ is equally inclined to \vec{a} , \vec{b} and \vec{c} .

A. (a) Both the statements are true and statement 2 is the correct explanation for statement 1.

B. (b) Both statements are true but statement 2 is not the correct explanation for statement 1.

C. (c) Statement 1 is true and Statement 2 is false

D. (d) Statement 1 is false and Statement 2 is true.

Answer: b

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8. Consider three vectors \vec{a} , \vec{b} and \vec{c}

$$\text{Statement 1: } \vec{a} \times \vec{b} = \left((\hat{i} \times \vec{a}) \cdot \vec{b} \right) \hat{i} + \left((\hat{j} \times \vec{a}) \cdot \vec{b} \right) \hat{j} + \left((\hat{k} \times \vec{a}) \cdot \vec{b} \right) \hat{k}$$

$$\text{Statement 2: } \vec{c} = \left(\hat{i} \cdot \vec{c} \right) \hat{i} + \left(\hat{j} \cdot \vec{c} \right) \hat{j} + \left(\hat{k} \cdot \vec{c} \right) \hat{k}$$

A. (a) Both the statements are true and statement 2 is the correct explanation for statement 1.

B. (b) Both statements are true but statement 2 is not the correct explanation for statement 1.

C. (c) Statement 1 is true and Statement 2 is false

D. (d) Statement 1 is false and Statement 2 is true.

Answer: a



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Comprehension Type

1. Let \vec{u} , \vec{v} and \vec{w} be three unit vectors such that $\vec{u} + \vec{v} + \vec{w} = \vec{a}$, $\vec{u} \times (\vec{v} \times \vec{w}) = \vec{b}$, $(\vec{u} \times \vec{v}) \times \vec{w} = \vec{c}$, $\vec{a} \cdot \vec{u} = 3/2$, $\vec{a} \cdot \vec{v} = 7/4$ and

Vector \vec{u} is

A. $\vec{a} - \frac{2}{3}\vec{b} + \vec{c}$

B. $\vec{a} + \frac{4}{3}\vec{b} + \frac{8}{3}\vec{c}$

C. $2\vec{a} - \vec{b} + \frac{1}{3}\vec{c}$

D. $\frac{4}{3}\vec{a} - \vec{b} + \frac{2}{3}\vec{c}$

Answer: b



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2. Let \vec{u} , \vec{v} and \vec{w} be three unit vectors such that $\vec{u} + \vec{v} + \vec{w} = \vec{a}$, $\vec{u} \times (\vec{v} \times \vec{w}) = \vec{b}$, $(\vec{u} \times \vec{v}) \times \vec{w} = \vec{c}$, $\vec{a} \cdot \vec{u} = 3/2$, $\vec{a} \cdot \vec{v} = 7/4$ and

Vector \vec{u} is

A. $2\vec{a} - 3\vec{c}$

B. $3\vec{b} - 4\vec{c}$

C. $-4\vec{c}$

D. $\vec{a} + \vec{b} + 2\vec{c}$

Answer: c



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3. Let \vec{u} , \vec{v} and \vec{w} be three unit vectors such that

$$\vec{u} + \vec{v} + \vec{w} = \vec{a}, \vec{u} \times (\vec{v} \times \vec{w}) = \vec{b}, (\vec{u} \times \vec{v}) \times \vec{w} = \vec{c}, \vec{a} \cdot \vec{u} = 3/2, \vec{a} \cdot \vec{v} = 7/4 \text{ and}$$

Vector \vec{u} is

A. $\frac{2}{3}(2\vec{c} - \vec{b})$

B. $\frac{1}{3}(\vec{a} - \vec{b} - \vec{c})$

C. $\frac{1}{3}\vec{a} - \frac{2}{3}\vec{b} - 2\vec{c}$

D. $\frac{4}{3}(\vec{c} - \vec{b})$

Answer: d



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4. Vectors \vec{x} , \vec{y} , \vec{z} each of magnitude $\sqrt{2}$ make angles of 60° with each other. If $\vec{x} \times (\vec{y} \times \vec{z}) = \vec{a}$, $\vec{y} \times (\vec{z} \times \vec{x}) = \vec{b}$ and $\vec{x} \times \vec{y} = \vec{c}$. Find \vec{x} , \vec{y} , \vec{z} in terms of \vec{a} , \vec{b} , \vec{c} .



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5. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of 60° with each other. If $\vec{x} \times (\vec{y} \times \vec{z}) = \vec{a}, \vec{y} \times (\vec{z} \times \vec{x}) = \vec{b}$ and $\vec{x} \times \vec{y} = \vec{c}$. Find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}, \vec{c}$.

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6. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of 60° with each other. If $\vec{x} \times (\vec{y} \times \vec{z}) = \vec{a}, \vec{y} \times (\vec{z} \times \vec{x}) = \vec{b}$ and $\vec{x} \times \vec{y} = \vec{c}$, find $\text{vec } x, \text{vec } y, \text{vec } z \in \text{terms of } \text{vec } a, \text{vec } b \text{ and } \text{vec } c$.

A. $\frac{1}{2} [(\vec{a} - \vec{c}) \times \vec{c} - \vec{b} + \vec{a}]$

B. $\frac{1}{2} [(\vec{a} - \vec{b}) \times \vec{c} + \vec{b} - \vec{a}]$

C. $\frac{1}{2} [\vec{c} \times (\vec{a} - \vec{b}) + \vec{b} + \vec{a}]$

D. none of these

Answer: b

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7. If $\vec{x} \cdot \vec{x}\vec{y} = \vec{a}$, $\vec{y} \times \vec{z} = \vec{b}$, $\vec{x} \cdot \vec{b} = \gamma$, $\vec{x} \cdot \vec{y} = 1$ and $\vec{y} \cdot \vec{z} = 1$ then find x,y,z in terms of \vec{a}, \vec{b} and γ .

A. $\frac{1}{|\vec{a} \times \vec{b}|^2} [\vec{a} \times (\vec{a} \times \vec{b})]$

B. $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} \times \vec{b} - \vec{a} \times (\vec{a} \times \vec{b})]$

C. $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} \times \vec{b} + \vec{a} \times (\vec{a} \times \vec{b})]$

D. none of these

Answer: b



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8. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of 60° with each other. If $\vec{x} \times (\vec{y} \times \vec{z}) = \vec{a}$, $\vec{y} \times (\vec{z} \times \vec{x}) = \vec{b}$ and $\vec{x} \times \vec{y} = \vec{c}$. Find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}, \vec{c}$.

A. $\frac{\vec{a} \times \vec{b}}{\gamma}$

B. $\vec{a} + \frac{\vec{a} \times \vec{b}}{\gamma}$

C. $\vec{a} + \vec{b} + \frac{\vec{a} \times \vec{b}}{\gamma}$

D. none of these

Answer: a



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9. If $\vec{x} \cdot \vec{y} = \vec{a}$, $\vec{y} \times \vec{z} = \vec{b}$, $\vec{x} \cdot \vec{b} = \gamma$, $\vec{x} \cdot \vec{y} = 1$ and $\vec{y} \cdot \vec{z} = 1$ then find $\vec{x}, \vec{y}, \vec{z}$ in terms of \vec{a}, \vec{b} and γ .

A. $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} + \vec{b} \times (\vec{a} \times \vec{b})]$

B. $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} + \vec{b} - \vec{a} \times (\vec{a} \times \vec{b})]$

C. $\frac{\gamma}{|\vec{a} \times \vec{b}|^2} [\vec{a} + \vec{b} + \vec{a} \times (\vec{a} \times \vec{b})]$

D. none of these

Answer: c



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10. Given two orthogonal vectors \vec{A} and \vec{B} each of length unity. Let \vec{P} be the vector satisfying the equation $\vec{P} \times \vec{B} = \vec{A} - \vec{P}$. then

\vec{P} is equal to

A. \vec{P}

B. $-\vec{P}$

C. $2\vec{B}$

D. \vec{A}

Answer: b



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11. Given two orthogonal vectors \vec{A} and \vec{B} each of length unity. Let \vec{P} be the vector satisfying the equation $\vec{P} \times \vec{B} = \vec{A} - \vec{P}$. then

\vec{P} is equal to

A. $\frac{\vec{A}}{2} + \frac{\vec{A} \times \vec{B}}{2}$

B. $\frac{\vec{A}}{2} + \frac{\vec{B} \times \vec{A}}{2}$

C. $\frac{\vec{A} \times \vec{B}}{2} - \frac{\vec{A}}{2}$

D. $\vec{A} \times \vec{B}$

Answer: B



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12. Given two orthogonal vectors \vec{A} and \vec{B} each of length unity. Let \vec{P} be the vector satisfying the equation $\vec{P} \times \vec{B} = \vec{A} - \vec{P}$. then which of the following statements is false ?

A. vectors \vec{P} , \vec{A} and $\vec{P} \times \vec{B}$ are linearly dependent.

B. vectors \vec{P} , \vec{B} and $\vec{P} \times \vec{B}$ are linearly independent

C. \vec{P} is orthogonal to \vec{B} and has length $\frac{1}{\sqrt{2}}$.

D. none of these

Answer: d

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13. Let $\vec{a} = 2\hat{i} + 3\hat{j} - 6\hat{k}$, $\vec{b} = 2\hat{i} - 3\hat{j} + 6\hat{k}$ and $\vec{c} = -2\hat{i} + 3\hat{j} + 6\hat{k}$. Let \vec{a}_1 be the projection of \vec{a} on \vec{b} and \vec{a}_2 be the projection of \vec{a}_1 on \vec{c} . Then \vec{a}_2 is equal to

A. (a) $\frac{943}{49} (2\hat{i} - 3\hat{j} - 6\hat{k})$

B. (b) $\frac{943}{49^2} (2\hat{i} - 3\hat{j} - 6\hat{k})$

C. (c) $\frac{943}{49} (-2\hat{i} + 3\hat{j} + 6\hat{k})$

D. (d) $\frac{943}{49^2} (-2\hat{i} + 3\hat{j} + 6\hat{k})$

Answer: b

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14. Let $\vec{a} = 2\hat{i} + 3\hat{j} - 6\hat{k}$, $\vec{b} = 2\hat{i} - 3\hat{j} + 6\hat{k}$ and $\vec{c} = -2\hat{i} + 3\hat{j} + 6\hat{k}$. Let \vec{a}_1 be the projection of \vec{a} on \vec{b} and \vec{a}_2 be the projection of \vec{a}_1 on \vec{c} . Then $\vec{a}_1 \cdot \vec{b}$ is equal to

A. (a) -41

B. (b) -41/7

C. (c) 41

D. (d) 287

Answer: a



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15. Let $\vec{a} = 2\hat{i} + 3\hat{j} - 6\hat{k}$, $\vec{b} = 2\hat{i} - 3\hat{j} + 6\hat{k}$ and $\vec{c} = -2\hat{i} + 3\hat{j} + 6\hat{k}$. Let \vec{a}_1 be the projection of \vec{a} on \vec{b} and \vec{a}_2 be the projection of \vec{a}_1 on \vec{c} . Then \vec{a}_2 is equal to

A. \vec{a} and \vec{a}_2 are collinear

B. \vec{a}_1 and \vec{c} are collinear

C. \vec{a}, \vec{a}_1 and \vec{b} are coplanar

D. \vec{a}, \vec{a}_1 and \vec{a}_2 are coplanar

Answer: c



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16. Consider a triangular pyramid ABCD the position vectors of whose angular points are $A(3, 0, 1), B(-1, 4, 1), C(5, 2, 3)$ and $D(0, -5, 4)$ Let G be the point of intersection of the medians of the triangle BCD. The length of the vector AG is

A. $\sqrt{17}$

B. $\sqrt{51}/3$

C. $3/\sqrt{6}$

D. $\sqrt{59}/4$

Answer: b



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17. Consider a triangular pyramid ABCD the position vectors of whose angular points are $A(3, 0, 1)$, $B(-1, 4, 1)$, $C(5, 3, 2)$ and $D(0, -5, 4)$. Let G be the point of intersection of the medians of the triangle BCT. The length of the perpendicular from the vertex D on the opposite face

A. (a) 24

B. (b) $8\sqrt{6}$

C. (c) $4\sqrt{6}$

D. (d) none of these

Answer: c



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18. Consider a triangular pyramid ABCD the position vectors of whose angular points are $A(3, 0, 1)$, $B(-1, 4, 1)$, $C(5, 3, 2)$ and $D(0, -5, 4)$ Let G be the point of intersection of the medians of the triangle BCD. The length of the vector AG is

A. $14/\sqrt{6}$

B. $2/\sqrt{6}$

C. $3/\sqrt{6}$

D. $\sqrt{5}$

Answer: a



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19. Vertices of a parallelogram taken in order are A, (2,-1,4) , B (1,0,-1) , C (1,2,3) and D (x,y,z) The distance between the parallel lines AB and CD is

A. (a) $\sqrt{6}$

B. (b) $3\sqrt{6/5}$

C. (c) $2\sqrt{2}$

D. (d) 3

Answer: c



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20. Vertices of a parallelogram taken in order are A(2,-1,4)B(1,0,-1)C(1,2,3) and D.

Distance of the point P (8, 2,-12) from the plane of the parallelogram is

A. $\frac{4\sqrt{6}}{9}$

B. $\frac{32\sqrt{6}}{9}$

C. $\frac{16\sqrt{6}}{9}$

D. none

Answer: b



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21. Vertices of a parallelogram taken in order are A(2,-1,4)B(1,0,-1)C(1,2,3) and D.

Distance of the point P (8, 2,-12) from the plane of the parallelogram is

A. 14, 4,2

B. 2,4,14

C. 4,2,14

D. 2,14,4

Answer: d



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22. Let \vec{r} is a positive vector of a variable point in cartesian OXY plane such that $\vec{r} \cdot (10\hat{j} - 8\hat{i} - \vec{r}) = 40$ and

$p_1 = \max \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}, p_2 = \min \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}$. A tangent line is drawn to the curve $y = \frac{8}{x^2}$ at the point A with abscissa 2. The drawn line cuts x-axis at a point B

A. (a) 9

B. (b) $2\sqrt{2} - 1$

C. (c) $6\sqrt{6} + 3$

D. (d) $9 - 4\sqrt{2}$

Answer: d



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23. Let \vec{r} is a positive vector of a variable point in cartesian OXY plane

such that $\vec{r} \cdot (10\hat{j} - 8\hat{i} - \vec{r}) = 40$ and

$p_1 = \max \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}, p_2 = \min \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}$. Then $p_1 + p_2$ is

equal to

A. 2

B. 10

C. 18

D. 5

Answer: c



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24. Let \vec{r} is a positive vector of a variable point in cartesian OXY plane

such that $\vec{r} \cdot (10\hat{j} - 8\hat{i} - \vec{r}) = 40$ and

$p_1 = \max \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}$, $p_2 = \min \left\{ \left| \vec{r} + 2\hat{i} - 3\hat{j} \right|^2 \right\}$. Then $p_1 + p_2$ is

equal to

A. 1

B. 2

C. 3

Answer: c


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25. \vec{a} , \vec{b} , \vec{c} and \vec{d} are three adjacent edges of a parallelepiped. The diagonal of the parallelepiped passing through A and directed away from it is vector \vec{a} . The vector of the faces containing vertices A, B, C and

A, B, D are \vec{b} and \vec{c} , respectively, i.e. $\vec{AB} \times \vec{AC} = \vec{b}$ and $\vec{AD} \times \vec{AB} = \vec{c}$ the

projection of each edge AB and AC on diagonal vector \vec{a} is $\frac{|\vec{a}|}{3}$

vector \vec{AB} is

A. $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2}$

B. $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} + \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$

C. $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} - \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$

D. none of these

Answer: a



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26. \vec{a} , \vec{b} , \vec{c} and \vec{d} are three adjacent edges of a parallelepiped. The diagonal of the parallelepiped passing through A and directed away from it is vector \vec{a} . The vector of the faces containing vertices A, B, C and

A, B, D are \vec{b} and \vec{c} , respectively, i.e. $\vec{b} \times \vec{c}$ and $\vec{d} \times \vec{b} = \vec{c}$ the

projection of each edge AB and AC on diagonal vector \vec{a} is $\frac{|\vec{a}|}{3}$ vector \vec{a}

is

A. $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2}$

B. $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} + \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$

C. $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} - \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$

D. none of these

Answer: C



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27. \vec{AB} , \vec{AC} and \vec{AD} are three adjacent edges of a parallelepiped. The diagonal of the parallelepiped passing through A and directed away from it is vector \vec{a} . The vector of the faces containing vertices A, B, C and

A, B, D are \vec{b} and \vec{c} , respectively, i.e. $\vec{AB} \times \vec{AC} = \vec{b}$ and $\vec{AD} \times \vec{AB} = \vec{c}$ the

projection of each edge AB and AC on diagonal vector \vec{a} is $\frac{|\vec{a}|}{3}$

vector \vec{AB} is

A. $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2}$

B. $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} + \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$

C. $\frac{1}{3}\vec{a} + \frac{\vec{a} \times (\vec{b} - \vec{c})}{|\vec{a}|^2} - \frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^2}$

D. none of these

Answer: A



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Martrix Match Type

1. 



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2. 



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3. 



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4. Given two vectors $\vec{a} = -\hat{i} + \hat{j} + 2\hat{k}$ and $\vec{b} = -\hat{i} - 2\hat{j} - \hat{k}$



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5. Given two vectors $\vec{a} = -\hat{i} + 2\hat{j} + 2\hat{k}$ and $\vec{b} = -2\hat{i} + \hat{j} + 2\hat{k}$

find $|\vec{a} \times \vec{b}|$

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6.

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7. Volume of parallelepiped formed by vectors $\vec{a} \times \vec{b}$, $\vec{b} \times \vec{c}$ and $\vec{c} \times \vec{a}$ is 36 sq. units.



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8. 

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9. 

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10. 

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1. If \vec{a} and \vec{b} are any two unit vectors, then find the greatest positive

integer in the range of $\frac{3|\vec{a} + \vec{b}|}{2} + 2|\vec{a} - \vec{b}|$

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2. Let \vec{u} be a vector on rectangular coordinate system with sloping angle

60° suppose that $|\vec{u} - \hat{i}|$ is geomtric mean of $|\vec{u}|$ and $|\vec{u} - 2\hat{i}|$, where \hat{i} is

the unit vector along the x-axis . Then find the value of $\frac{\sqrt{2} - 1}{|\vec{u}|}$

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3. Find the absolute value of parameter t for which the area of the triangle whose vertices the $A(-1, 1, 2)$; $B(1, 2, 3)$ and $C(t, 1, 1)$ is minimum.

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4. If $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$, $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$, $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$ and

$$[3\vec{a} + \vec{b} \quad 3\vec{b} + \vec{c} \quad 3\vec{c} + \vec{a}] = \lambda \begin{vmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{vmatrix} \text{ then find the value of } \frac{\lambda}{4}$$

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5. Let $\vec{a} = \alpha\hat{i} + 2\hat{j} - 3\hat{k}$, $\vec{b} = \hat{i} + 2\alpha\hat{j} - 2\hat{k}$ and $\vec{c} = 2\hat{i} - \alpha\hat{j} + \hat{k}$. Find the value of

$$6\alpha. \text{ Such that } \{(\vec{a} \times \vec{b}) \times (\vec{b} \times \vec{c})\} \times (\vec{c} \times \vec{a}) = 0$$

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6. If \vec{x}, \vec{y} are two non-zero and non-collinear vectors satisfying

$$[(a-2)\alpha^2 + (b-3)\alpha + c]\vec{x} + [(a-2)\beta^2 + (b-3)\beta + c]\vec{y} + [(a-2)\gamma^2 + (b-3)\gamma + c]\vec{z}$$

are three distinct real numbers, then find the value of $(a^2 + b^2 + c^2 - 4)$.

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7. Let \vec{u} and \vec{v} be unit vectors such that $\vec{u} \times \vec{v} + \vec{u} = \vec{w}$ and $\vec{w} \times \vec{u} = \vec{v}$.

Find the value of $[\vec{u}\vec{v}\vec{w}]$



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8. The volume of the tetrahedron whose vertices are the points with position vectors $\hat{i} - 6\hat{j} + 10\hat{k}$, $-\hat{i} - 3\hat{j} + 7\hat{k}$, $5\hat{i} - \hat{j} + \lambda\hat{k}$ and $7\hat{i} - 4\hat{j} + 7\hat{k}$ is 11 cubic units if the value of λ is



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9. Given that

$$\vec{u} = \hat{i} + 2\hat{j} + 3\hat{k}, \vec{v} = 2\hat{i} + \hat{k} + 4\hat{k}, \vec{w} = \hat{i} + 3\hat{j} + 3\hat{k} \text{ and } (\vec{u} \cdot \vec{R} - 15)\hat{i} + (\vec{c} \cdot \vec{R} - 30)\hat{j}$$

. Then find the greatest integer less than or equal to $|\vec{R}|$.



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10. Let a three-dimensional vector \vec{V} satisfy the condition ,
 $2\vec{V} + \vec{V} \times (\hat{i} + 2\hat{j}) = 2\hat{i} + \hat{k}$. If $3|\vec{V}| = \sqrt{m}$. Then find the value of m.

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11. If $\vec{a}, \vec{b}, \vec{c}$ are unit vectors such that $\vec{a} \cdot \vec{b} = 0 = \vec{a} \cdot \vec{c}$ and the angle
between \vec{b} and \vec{c} is $\frac{\pi}{3}$, then find the value of $|\vec{a} \times \vec{b} - \vec{a} \times \vec{c}|$

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12. Let $\vec{OA} = \vec{a}, \vec{OB} = 10\vec{a} + 2\vec{b}$ and $\vec{OC} = \vec{b}$, where O, A and C are non-
collinear points. Let p denotes the area of quadrilateral $OACB$, and let q
denote the area of parallelogram with OA and OC as adjacent sides. If
 $p = kq$, then find k

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13. Find the work done by the force $F = 3\hat{i} - \hat{j} - 2\hat{k}$ acting on a particle such that the particle is displaced from point $A(-3, -4, 1)$ to point $B(-1, -1, -2)$.

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14. If \vec{a} and \vec{b} are vectors in space given by $\vec{a} = \frac{\hat{i} - 2\hat{j}}{\sqrt{5}}$ and $\vec{b} = \frac{2\hat{i} + \hat{j} + 3\hat{k}}{\sqrt{14}}$ then find the value of $(2\vec{a} + \vec{b}) \cdot [(\vec{a} \times \vec{b}) \times (\vec{a} - 2\vec{b})]$

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15. Let $\vec{a} = -\hat{i} - \hat{k}$, $\vec{b} = -\hat{i} + \hat{j}$ and $\vec{c} = \hat{i} + 2\hat{j} + 3\hat{k}$ be three given vectors. If \vec{r} is a vector such that $\vec{r} \times \vec{b} = \vec{c} \times \vec{b}$ and $\vec{r} \cdot \vec{a} = 0$ then find the value of $\vec{r} \cdot \vec{b}$.

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16. If \vec{a} , \vec{b} and \vec{c} are unit vectors satisfying

$$|\vec{a} - \vec{b}|^2 + |\vec{b} - \vec{c}|^2 + |\vec{c} - \vec{a}|^2 = 9 \text{ then find the value of } |2\vec{a} + 5\vec{b} + 5\vec{c}|$$

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17. Let \vec{a} , \vec{b} , and \vec{c} be three non coplanar unit vectors such that the angle between every pair of them is $\frac{\pi}{3}$. If $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} = p\vec{a} + q\vec{b} + r\vec{c}$ where p, q, r are scalars then the value of $\frac{p^2 + 2q^2 + r^2}{q^2}$ is

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Subjective Type

1. From a point O inside a triangle ABC , perpendiculars OD , OE and OF are drawn to the sides BC , CA and AB , respectively. Prove that the perpendiculars from A , B , and C to the sides EF , FD and DE are concurrent.

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2. A_1, A_2, \dots, A_n are the vertices of a regular plane polygon with n sides

and O is its centre. Show that
$$\sum_{i=1}^{n-1} \left(\vec{OA}_i \times \vec{OA}_{i+1} \right) = (n-1) \left(\vec{OA}_1 \times \vec{OA}_2 \right)$$

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3. If c is a given non-zero scalar, and \vec{A} and \vec{B} are given non-zero vectors such that $\vec{A} \perp \vec{B}$. Then find vector, \vec{X} which satisfies the equations

$\vec{A} \cdot \vec{X} = c$ and $\vec{A} \times \vec{X} = \vec{B}$.

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4. A, B, C and D are any four points in the space, then prove that

$$\left| \vec{AB} \times \vec{CD} + \vec{BC} \times \vec{AD} + \vec{CA} \times \vec{BD} \right| = 4 \text{ (area of } ABC \text{.)}$$

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5. If the vectors \vec{a} , \vec{b} , and \vec{c} are coplanar show that

$$\begin{vmatrix} \vec{a} & \vec{b} & \vec{c} \\ \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \end{vmatrix} = 0$$

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6. $\vec{A} = (2\vec{i} + \vec{k})$, $\vec{B} = (\vec{i} + \vec{j} + \vec{k})$ and $\vec{C} = 4\vec{i} - 3\vec{j} + 7\vec{k}$ determine a \vec{R} satisfying $\vec{R} \times \vec{B} = \vec{C} \times \vec{B}$ and $\vec{R} \cdot \vec{A} = 0$

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7. Determine the value of c so that for the real x , vectors $c\hat{i} - 6\hat{j} - 3\hat{k}$ and $x\hat{i} + 2\hat{j} + 2cx\hat{k}$ make an obtuse angle with each other.

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8. If vectors, \vec{b} , \vec{c} and \vec{d} are not coplanar, then prove that vector $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) + (\vec{a} \times \vec{c}) \times (\vec{d} \times \vec{b}) + (\vec{a} \times \vec{d}) \times (\vec{b} \times \vec{c})$ is parallel to \vec{a} .

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9. The position vectors of the vertices A, B and C of a tetrahedron ABCD are $\hat{i} + \hat{j} + \hat{k}$, \hat{k} , \hat{i} and $3\hat{i}$, respectively. The altitude from vertex D to the opposite face ABC meets the median line through A of triangle ABC at a point E. If the length of the side AD is 4 and the volume of the tetrahedron is $2\sqrt{2}/3$, find the position vectors of the point E for all its possible positions

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10. Let a , b and c be non-coplanar unit vectors equally inclined to one another at an acute angle θ then $[a\ b\ c]$ in terms of θ is equal to :

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11. If \vec{A}, \vec{B} and \vec{C} are vectors such that $|\vec{B}| = |\vec{C}|$ prove that
- $$\left[(\vec{A} + \vec{B}) \times (\vec{A} + \vec{C}) \right] \times (\vec{B} + \vec{C}) \cdot (\vec{B} + \vec{C}) = 0$$

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12. For any two vectors \vec{u} and \vec{v} prove that
- $$(1 + |\vec{u}|^2)(1 + |\vec{v}|^2) = (1 - \vec{u} \cdot \vec{v})^2 + |\vec{u} + \vec{v} + (\vec{u} \times \vec{v})|^2$$

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13. Let \vec{u} and \vec{v} be unit vectors. If \vec{w} is a vector such that $\vec{w} + \vec{w} \times \vec{u} = \vec{v}$, then prove that $|(\vec{u} \times \vec{v}) \cdot \vec{w}| \leq \frac{1}{2}$ and that the equality holds if and only if \vec{u} is perpendicular to \vec{v} .

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14. Find 3-dimensional vectors $\vec{v}_1, \vec{v}_2, \vec{v}_3$ satisfying

$$\vec{v}_1 \cdot \vec{v}_1 = 4, \vec{v}_1 \cdot \vec{v}_2 = -2, \vec{v}_1 \cdot \vec{v}_3 = 6,$$

$$\vec{v}_2 \cdot \vec{v}_2 = 2, \vec{v}_2 \cdot \vec{v}_3 = -5, \vec{v}_3 \cdot \vec{v}_3 = 29$$

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15. Let V be the volume of the parallelepiped formed by the vectors,

$$\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}, \vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k} \text{ and } \vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}. \text{ if } a_r, b_r, \text{ and } c_r$$

are non-negative real numbers and

$$\sum_{r=1}^3 (a_r + b_r + c_r) = 3L \text{ show that } V \leq L^3$$

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16. \vec{u}, \vec{v} and \vec{w} are three non-coplanar unit vectors and α, β and γ are the angles between \vec{u} and \vec{v}, \vec{v} and \vec{w} and \vec{w} and \vec{u} , respectively and

\vec{x}, \vec{y} and \vec{z} are unit vectors along the bisectors of the angles α, β and γ .

respectively, prove that $[\vec{x} \times \vec{y} \vec{y} \times \vec{z} \vec{z} \times \vec{x}] = \frac{1}{16} [\vec{u} \vec{v} \vec{w}]^2 \frac{\sec^2 \alpha}{2} \frac{\sec^2 \beta}{2} \frac{\sec^2 \gamma}{2}$.

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17. If $\vec{a}, \vec{b}, \vec{c}$ and \vec{d} are distinct vectors such that $\vec{a} \times \vec{c} = \vec{b} \times \vec{d}$ and $\vec{a} \times \vec{b} = \vec{c} \times \vec{d}$. Prove that $(\vec{a} - \vec{d}) \cdot (\vec{c} - \vec{b}) \neq 0$, i. e., $\vec{a} \cdot \vec{b} + \vec{d} \cdot \vec{c} \neq \vec{d} \cdot \vec{b} + \vec{a} \cdot \vec{c}$.

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18. P_1 and P_2 are planes passing through origin L_1 and L_2 are two lines on P_1 and P_2 , respectively, such that their intersection is the origin. Show that there exist points A, B and C , whose permutation A', B' and C' , respectively, can be chosen such that A is on L_1 , B on P_1 but not on L_1 and C not on P_1 ; A' is on L_2 , B' on P_2 but not on L_2 and C' not on P_2 .

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19. about to only mathematics

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Fill In The Blanks

1. Let \vec{A} , \vec{B} and \vec{C} be vectors of length 3, 4 and 5 respectively. Let \vec{A} be perpendicular to $\vec{B} + \vec{C}$, \vec{B} to $\vec{C} + \vec{A}$ and \vec{C} to $\vec{A} + \vec{B}$ then the length of vector $\vec{A} + \vec{B} + \vec{C}$ is _____.



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2. The unit vector perpendicular to the plane determined by $P(1, -1, 2)$, $Q(2, 0, -1)$ and $R(0, 2, 1)$.



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3. The area of the triangle whose vertices are

$A(1, -1, 2)$, $B(2, 1, -1)$, $C(3, -1, 2)$ is



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4. If \vec{A} , \vec{B} , \vec{C} are non-coplanar vectors then $\frac{\vec{A} \cdot \vec{B} \times \vec{C}}{\vec{C} \times \vec{A} \cdot \vec{B}} + \frac{\vec{B} \cdot \vec{A} \times \vec{C}}{\vec{C} \cdot \vec{A} \times \vec{B}} =$

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5. If $\vec{A} = (1, 1, 1)$ and $\vec{C} = (0, 1, -1)$ are given vectors then find a vector \vec{B} satisfying equations $\vec{A} \times \vec{B} = \vec{C}$ and $\vec{A} \cdot \vec{B} = 3$

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6. Let $\vec{b} = 4\hat{i} + 3\hat{j}$ and \vec{c} be two vectors perpendicular to each other in the xy -plane. Find all vectors in the same plane having projection 1 and 2 along \vec{b} and \vec{c} respectively.

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7. The components of a vector \vec{a} along and perpendicular to a non-zero vector \vec{b} are _____ and _____, respectively.

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8. A unit vector coplanar with $\vec{i} + \vec{j} + 2\vec{k}$ and $\vec{i} + 2\vec{j} + \vec{k}$ and perpendicular to $\vec{i} + \vec{j} + \vec{k}$ is _____

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9. A non vector \vec{a} is parallel to the line of intersection of the plane determined by the vectors $\vec{i}, \vec{i} + \vec{j}$ and the plane determined by the vectors $\vec{i} - \vec{j}, \vec{i} + \vec{k}$ then angle between \vec{a} and $\vec{i} - 2\vec{j} + 2\vec{k}$ is = (A) $\frac{\pi}{2}$ (B) $\frac{\pi}{3}$
(C) $\frac{\pi}{6}$ (D) $\frac{\pi}{4}$

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10. If \vec{b} and \vec{c} are any two mutually perpendicular unit vectors and \vec{a} is

any vector, then $(\vec{a} \cdot \vec{b})\vec{b} + (\vec{a} \cdot \vec{c})\vec{c} + \frac{\vec{a} \cdot (\vec{b} \times \vec{c})}{|\vec{b} \times \vec{c}|^2}(\vec{b} \times \vec{c}) =$ (A) 0 (B) \vec{a} (C)

veca /2(D)2veca`



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11. Let \vec{a} , \vec{b} and \vec{c} be three vectors having magnitudes 1, 1 and 2 respectively.

If $\vec{a} \times (\vec{a} \times \vec{c}) + \vec{b} = \vec{0}$ then the acute angle between \vec{a} and \vec{c} is



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12. A, B, C and D are four points in a plane with position vectors,

\vec{a} , \vec{b} , \vec{c} and \vec{d} respectively, such that

$(\vec{a} - \vec{d}) \cdot (\vec{b} - \vec{c}) = (\vec{b} - \vec{d}) \cdot (\vec{c} - \vec{a}) = 0$ then point D is the _____ of

triangle ABC.



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13. If $\vec{A} = \lambda(\vec{u} \times \vec{v}) + \mu(\vec{v} \times \vec{w}) + \nu(\vec{w} \times \vec{u})$ and $[\vec{u} \vec{v} \vec{w}] = \frac{1}{5}$ then $\lambda + \mu + \nu =$

(A) 5 (B) 10 (C) 15 (D) none of these

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14. If $\vec{a} = \hat{j} + \sqrt{3}\hat{k}$, $\vec{b} = -\hat{j} + \sqrt{3}\hat{k}$ and $\vec{c} = 2\sqrt{3}\hat{k}$ form a triangle, then the internal angle of the triangle between \vec{a} and \vec{b} is

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True And False

1. Let \vec{A} , \vec{B} and \vec{C} be unit vectors such that $\vec{A} \cdot \vec{B} = \vec{A} \cdot \vec{C} = 0$ and the angle between \vec{B} and \vec{C} be $\pi/3$. Then $\vec{A} = \pm 2(\vec{B} \times \vec{C})$.

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2. If $\vec{x} \cdot \vec{a} = 0$, $\vec{x} \cdot \vec{b} = 0$ and $\vec{x} \cdot \vec{c} = 0$ for some non zero vector \vec{x} then show that $[\vec{a}\vec{b}\vec{c}] = 0$

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3. for any three vectors, \vec{a} , \vec{b} and \vec{c} , $(\vec{a} - \vec{b}) \cdot (\vec{b} - \vec{c}) \times (\vec{c} - \vec{a}) =$

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Exercise 2 1

1. Find $|\vec{a}|$ and $|\vec{b}|$, if $(\vec{a} + \vec{b}) \cdot (\vec{a} - \vec{b}) = 8$ and $|\vec{a}| = 8|\vec{b}|$

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2. Show that $|\vec{a}|\vec{b} + |\vec{b}|\vec{a}$ is perpendicular to $|\vec{a}|\vec{b} - |\vec{b}|\vec{a}$ for any two non zero vectors \vec{a} and \vec{b} .

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3. If the vertices A,B,C of a triangle ABC are $(1,2,3), (-1,0,0), (0,1,2)$, respectively, then find $\angle ABC$.

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4. If $|\vec{a}| = 3$, $|\vec{b}| = 4$ and the angle between \vec{a} and \vec{b} is 120° . Then find the value of $|4\vec{a} + 3\vec{b}|$

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5. If vectors $\hat{i} - 2\hat{j} - 3\hat{k}$ and $\hat{i} + 3\hat{j} + 2\hat{k}$ are orthogonal to each other, then find the locus of the point (x,y) .



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6. Let \vec{a} , \vec{b} and \vec{c} be pairwise mutually perpendicular vectors, such that $|\vec{a}| = 1$, $|\vec{b}| = 2$, $|\vec{c}| = 2$, then find the length of $\vec{a} + \vec{b} + \vec{c}$.



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7. If $\vec{a} + \vec{b} + \vec{c} = 0$, $|\vec{a}| = 3$, $|\vec{b}| = 5$, $|\vec{c}| = 7$, then find the angle between \vec{a} and \vec{b} .



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8. If the angle between unit vectors \vec{a} and \vec{b} is 60° . Then find the value of $|\vec{a} - \vec{b}|$.



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9. Let $\vec{u} = \hat{i} + \hat{j}$, $\vec{v} = \hat{i} - \hat{j}$ and $\vec{w} = \hat{i} + 2\hat{j} + 3\hat{k}$. If \hat{n} is a unit vector such that $\vec{u} \cdot \hat{n} = 0$ and $\vec{v} \cdot \hat{n} = 0$, $|\vec{w} \cdot \hat{n}|$ is equal to (A) 0 (B) 1 (C) 2 (D) 3

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10. A, B, C and d are any four points prove that
 $\vec{AB} \cdot \vec{CD} + \vec{BC} \cdot \vec{AD} + \vec{CA} \cdot \vec{BD} = 0$

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11. $P(1, 0, -1)$, $Q(2, 0, -3)$, $R(-1, 2, 0)$ and $S(3, -2, -1)$, then find the projection length of \vec{PQ} and \vec{RS} .

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12. If the vectors $3\vec{p} + \vec{q}$, $5\vec{p} - 3\vec{q}$ and $2\vec{p} + \vec{q}$, $4\vec{p} - 2\vec{q}$ are pairs of mutually perpendicular vectors, then find the angle between vectors \vec{p} and \vec{q} .



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13. Let \vec{A} and \vec{B} be two non-parallel unit vectors in a plane. If $(\alpha\vec{A} + \vec{B})$ bisects the internal angle between \vec{A} and \vec{B} then find the value of α .



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14. Let \vec{a}, \vec{b} and \vec{c} be unit vectors such that $\vec{a} + \vec{b} + \vec{c} = \vec{x}$, $\vec{a} \cdot \vec{x} = 1$, $\vec{b} \cdot \vec{x} = \frac{3}{2}$, $|\vec{x}| = 2$ then find the angle between \vec{c} and \vec{x} .



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15. If \vec{a} and \vec{b} are unit vectors, then find the greatest value of $|\vec{a} + \vec{b}| + |\vec{a} - \vec{b}|$.



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16. Constant forces $P_1 = \hat{i} - \hat{j} + \hat{k}$, $P_2 = -\hat{i} + 2\hat{j} - \hat{k}$ and $P_3 = \hat{j} - \hat{k}$ act on a particle at a point A. Determine the work done when particle is displaced from position $A(4\hat{i} - 3\hat{j} - 2\hat{k})$ to $B(6\hat{i} + \hat{j} - 3\hat{k})$

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17. If $|\vec{a}| = 5$, $|\vec{a} - \vec{b}| = 8$ and $|\vec{a} + \vec{b}| = 10$ then find $|\vec{b}|$

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18. If A, B, C, D are four distinct point in space such that AB is not perpendicular to CD and satisfies

$\vec{AB} \cdot \vec{CD} = k \left(|\vec{AD}|^2 + |\vec{BC}|^2 - |\vec{AC}|^2 - |\vec{BD}|^2 \right)$, then find the value of k

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1. If $\vec{a} = 2\hat{i} + 3\hat{j} - 5\hat{k}$, $\vec{b} = m\hat{i} + n\hat{j} + 12\hat{k}$ and $\vec{a} \times \vec{b} = \vec{0}$ then find (m,n)

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2. If $|\vec{a}| = 2$, $|\vec{b}| = 5$ and $|\vec{a} \times \vec{b}| = 8$ then find the value of $\vec{a} \cdot \vec{b}$

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3. If $\vec{a} \times \vec{b} = \vec{b} \times \vec{c} \neq 0$ where \vec{a} , \vec{b} and \vec{c} are coplanar vectors, then for some scalar k prove that $\vec{a} + \vec{c} = k\vec{b}$.

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4. If $\vec{a} = 2\vec{j} + 3\vec{j} - \vec{k}$, $\vec{b} = -\vec{i} + 2\vec{j} - 4\vec{k}$ and $\vec{c} = \vec{i} + \vec{j} + \vec{k}$, then find the value of $(\vec{a} \times \vec{b}) \cdot (\vec{a} \times \vec{c})$

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5. find the vector \vec{c} , $\vec{a} = x\hat{i} + y\hat{j} + z\hat{k}$ and $\vec{b} = \hat{j}$ are such that \vec{a} , \vec{c} and \vec{b} form a right-handed system, then find \vec{c} .

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6. given that $\vec{a} \cdot \vec{b} = \vec{a} \cdot \vec{c}$, $\vec{a} \times \vec{b} = \vec{a} \times \vec{c}$ and \vec{a} is not a zero vector. Show that $\vec{b} = \vec{c}$.

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7. Show that $(\vec{a} - \vec{b}) \times (\vec{a} + \vec{b}) = 2\vec{a} \times \vec{b}$ and give a geometrical interpretation of it.

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8. If \vec{x} and \vec{y} are unit vectors and $|\vec{z}| = \frac{2}{\sqrt{7}}$ such that $\vec{z} + \vec{z} \times \vec{x} = \vec{y}$ then find the angle θ between \vec{x} and \vec{z}



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9. Prove that $(\vec{a} \cdot \hat{i})(\vec{a} \times \hat{i}) + (\vec{a} \cdot \hat{j})(\vec{a} \times \hat{j}) + (\vec{a} \cdot \hat{k})(\vec{a} \times \hat{k}) = \vec{0}$



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10. Let a, b, c be three non-zero vectors such that $a + b + c = 0$, then $\lambda b \times a + b \times c + c \times a = 0$, where λ is



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11. A particle has an angular speed of 3 rad/s and the axis of rotation passes through the points $(1, 1, 2)$ and $(1, 2, -2)$. Find the velocity of the particle at point $P(3, 6, 4)$.



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12. Let \vec{a} , \vec{b} and \vec{c} be unit vectors such that $\vec{a} \cdot \vec{b} = 0 = \vec{a} \cdot \vec{c}$. If the angle between \vec{b} and \vec{c} is $\frac{\pi}{6}$ then find \vec{a} .

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13. If $(\vec{a} \times \vec{b})^2 + (\vec{a} \cdot \vec{b})^2 = 144$ and $|\vec{a}| = 4$ then find the value of $|\vec{b}|$

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14. Given $|\vec{a}| = |\vec{b}| = 1$ and $|\vec{a} + \vec{b}| = \sqrt{3}$ if \vec{c} is a vector such that $\vec{c} - \vec{a} - 2\vec{b} = 3(\vec{a} \times \vec{b})$ then find the value of $\vec{c} \cdot \vec{b}$.

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15. Find the moment of \vec{F} about point $(2, -1, 3)$, where force $\vec{F} = 3\hat{i} + 2\hat{j} - 4\hat{k}$ is acting on point $(1, -1, 2)$.

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Exercise 2 3

1. If $\vec{a}, \vec{b}, \vec{c}$ and \vec{d} are four non-coplanar unit vectors such that \vec{d} makes equal angles with all the three vectors $\vec{a}, \vec{b}, \vec{c}$ then prove that

$$[\vec{d}\vec{a}\vec{b}] = [\vec{d}\vec{c}\vec{b}] = [\vec{d}\vec{c}\vec{a}]$$

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2. If $\vec{l}, \vec{m}, \vec{n}$ are three non coplanar vectors prove that $\left[\begin{matrix} \vec{l} \\ \vec{m} \\ \vec{n} \end{matrix} \right] = \frac{1}{\sqrt{(\vec{l}\cdot\vec{l})(\vec{m}\cdot\vec{m})(\vec{n}\cdot\vec{n}) - (\vec{l}\cdot\vec{m})^2 - (\vec{l}\cdot\vec{n})^2 - (\vec{m}\cdot\vec{n})^2}}$

$$= \frac{1}{\sqrt{(\vec{l}\cdot\vec{l})(\vec{m}\cdot\vec{m})(\vec{n}\cdot\vec{n}) - (\vec{l}\cdot\vec{m})^2 - (\vec{l}\cdot\vec{n})^2 - (\vec{m}\cdot\vec{n})^2}}$$

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3. if the volume of a parallelepiped whose adjacent edges are $\vec{a} = 2\hat{i} + 3\hat{j} + 4\hat{k}$, $\vec{b} = \hat{i} + \alpha\hat{j} + 2\hat{k}$, $\vec{c} = \hat{i} + 2\hat{j} + \alpha\hat{k}$ is 15 then find α if $(\alpha > 0)$

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4. If $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ and $\vec{b} = \hat{i} - 2\hat{j} + \hat{k}$ then find the vector \vec{c} such that $\vec{a} \cdot \vec{c} = 2$ and $\vec{a} \times \vec{c} = \vec{b}$.

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5. If $\vec{x} \cdot \text{Veca} = 0$, $\vec{x} \cdot \text{Vecb} = 0$ and $\vec{x} \cdot \vec{c} = 0$ for some non-zero vector \vec{x} . Then prove that $[\vec{a}\vec{b}\vec{c}] = 0$

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6. If $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ and $\vec{b} = \hat{i} - 2\hat{j} + \hat{k}$ then find the vector \vec{c} such that $\vec{a} \cdot \vec{c} = 2$ and $\vec{a} \times \vec{c} = \vec{b}$.

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7. If \vec{a} , \vec{b} and \vec{c} are three vectors such that $\vec{a} \times \vec{b} = \vec{c}$, $\vec{b} \times \vec{c} = \vec{a}$, $\vec{c} \times \vec{a} = \vec{b}$ then prove that $|\vec{a}| = |\vec{b}| = |\vec{c}|$

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8. If $\vec{a} = \vec{p} + \vec{q}$, $\vec{p} \times \vec{b} = \vec{0}$ and $\vec{q} \cdot \vec{b} = 0$ then prove that $\frac{\vec{b} \times (\vec{a} \times \vec{b})}{\vec{b} \cdot \vec{b}} = \vec{q}$

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9. Prove that $(\vec{a} \cdot (\vec{b} \times \hat{i}))\hat{i} + (\vec{a} \cdot (\vec{b} \times \hat{j}))\hat{j} + (\vec{a} \cdot (\vec{b} \times \hat{k}))\hat{k} = \vec{a} \times \vec{b}$

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10. for any four vectors $\vec{a}, \vec{b}, \vec{c}$ and \vec{d} prove that

$$\vec{d} \cdot (\vec{a} \times (\vec{b} \times (\vec{c} \times \vec{d}))) = (\vec{b} \cdot \vec{d}) [\vec{a} \vec{c} \vec{d}]$$

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11. If \vec{a} and \vec{b} be two non-collinear unit vectors such that

$$\vec{a} \times (\vec{a} \times \vec{b}) = \frac{1}{2} \vec{b}, \text{ then find the angle between } \vec{a} \text{ and } \vec{b}.$$

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12. show that $(\vec{a} \times \vec{b}) \times \vec{c} = \vec{a} \times (\vec{b} \times \vec{c})$ if and only if \vec{a} and \vec{c} are collinear or $(\vec{a} \times \vec{c}) \times \vec{b} = \vec{0}$

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13. Let \vec{a} , \vec{b} and \vec{c} be non-zero vectors such that no two are collinear and $(\vec{a} \times \vec{b}) \times \vec{c} = \frac{1}{3} |\vec{b}| |\vec{c}| \vec{a}$ if θ is the acute angle between vectors \vec{b} and \vec{c} then find value of $\sin\theta$.

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14. If $\vec{p}, \vec{q}, \vec{r}$ denote vectors $\vec{b} \times \vec{c}, \vec{c} \times \vec{a}, \vec{a} \times \vec{b}$. Respectively, show that \vec{a} is parallel to $\vec{q} \times \vec{r}$, \vec{b} is parallel to $\vec{r} \times \vec{p}$, \vec{c} is parallel to $\vec{p} \times \vec{q}$.

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15. Let $\vec{a}, \vec{b}, \vec{c}$ be non-coplanar vectors and let equations $\vec{a}', \vec{b}', \vec{c}'$ are reciprocal system of vector $\vec{a}, \vec{b}, \vec{c}$ then prove that $\vec{a} \times \vec{a}' + \vec{b} \times \vec{b}' + \vec{c} \times \vec{c}'$ is a null vector.

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16. Given unit vectors \hat{m} and \hat{n} such that angle between \hat{m} and \hat{n} is α and angle between \hat{p} and \hat{m} is α if $[\hat{n} \hat{p} \hat{m}] = 1/4$ find α

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17. \vec{a} , \vec{b} , and \vec{c} are three unit vectors and every two are inclined to each other at an angle $\cos^{-1}(3/5)$. If $\vec{a} \times \vec{b} = p\vec{a} + q\vec{b} + r\vec{c}$, where p, q, r are scalars, then find the value of q

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18. Let $\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}$, $\vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k}$ and $\vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k}$ give three non-zero vectors such that \vec{c} is a unit vector perpendicular to both \vec{a} and \vec{b} . If the angle between \vec{a} and \vec{b} is $\frac{\pi}{6}$, then prove that

$$\begin{vmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{vmatrix} p = \frac{1}{4} (a_1^2 + a_2^2 + a_3^2) (b_1^2 + b_2^2 + b_3^2)$$

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Single Correct Answer Type

1. The scalar $\vec{A} \cdot (\vec{B} + \vec{C}) \times (\vec{A} + \vec{B} + \vec{C})$ equals (A) 0 (B) $[\vec{A}\vec{B}\vec{C}] + [\vec{B}\vec{C}\vec{A}]$
(C) $[\vec{A}\vec{B}\vec{C}]$ (D) none of these

A. 0

B. $[\vec{A}\vec{B}\vec{C}] + [\vec{B}\vec{C}\vec{A}]$

C. $[\vec{A}\vec{B}\vec{C}]$

D. none of these

Answer: a

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2. For non-zero vectors \vec{a} , \vec{b} and \vec{c} , $|(\vec{a} \times \vec{b}) \cdot \vec{c}| = |\vec{a}| |\vec{b}| |\vec{c}|$ holds if and only if

A. $\vec{a} \cdot \vec{b} = 0, \vec{b} \cdot \vec{c} = 0$

B. $\vec{b} \cdot \vec{c} = 0, \vec{c} \cdot \vec{a} = 0$

C. $\vec{c} \cdot \vec{a} = 0, \vec{a} \cdot \vec{b} = 0$

D. $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = \vec{c} \cdot \vec{a} = 0$

Answer: d

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3. The volume of the parallelepiped whose sides are given by

$\vec{OA} = 2i - 2j, \vec{OB} = i + j - k$ and $\vec{OC} = 3i - k$ is a. $4/13$ b. 4 c. $2/7$ d. 2

A. $4/13$

B. 4

C. $2/7$

D. 2

Answer: d



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4. Let $\vec{a}, \vec{b}, \vec{c}$ be three noncoplanar vectors and $\vec{p}, \vec{q}, \vec{r}$ are vectors defined

by the relations $\vec{p} = \frac{\vec{b} \times \vec{c}}{[\vec{a}\vec{b}\vec{c}]}, \vec{q} = \frac{\vec{c} \times \vec{a}}{[\vec{a}\vec{b}\vec{c}]}, \vec{r} = \frac{\vec{a} \times \vec{b}}{[\vec{a}\vec{b}\vec{c}]}$ then the value of

the expression $(\vec{a} + \vec{b}) \cdot \vec{p} + (\vec{b} + \vec{c}) \cdot \vec{q} + (\vec{c} + \vec{a}) \cdot \vec{r}$ is equal to (A) 0 (B) 1

(C) 2 (D) 3

A. 0

B. 1

C. 2

D. 3

Answer: d



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5. Let $\vec{a} = \hat{i} - \hat{j}$, $\vec{b} = \hat{j} - \hat{k}$, $\vec{c} = \hat{k} - \hat{i}$. If \hat{d} is a unit vector such that $\vec{a} \cdot \hat{d} = 0 = [\vec{b} \vec{c} \hat{d}]$ then \hat{d} equals

A. $\pm \frac{\hat{i} + \hat{j} - 2\hat{k}}{\sqrt{6}}$

B. $\pm \frac{\hat{i} + \hat{j} - \hat{k}}{\sqrt{3}}$

C. $\pm \frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$

D. $\pm \hat{k}$

Answer: a



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6. If \vec{a} , \vec{b} and \vec{c} are non coplanar and unit vectors such that

$\vec{a} \times (\vec{b} \times \vec{c}) = \frac{\vec{b} + \vec{c}}{\sqrt{2}}$ then the angle between \vec{a} and \vec{b} is (A) $\frac{3\pi}{4}$ (B) $\frac{\pi}{4}$

(C) $\frac{\pi}{2}$ (D) π

A. $3\pi/4$

B. $\pi/4$

C. $\pi/2$

D. π

Answer: a



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7. Let \vec{u} , \vec{v} and \vec{w} be vectors such that $\vec{u} + \vec{v} + \vec{w} = 0$ if $|\vec{u}| = 3$, $|\vec{v}| = 4$ and $|\vec{w}| = 5$ then $\vec{u} \cdot \vec{v} + \vec{v} \cdot \vec{w} + \vec{w} \cdot \vec{u}$ is (a) 47 (b) -25 (c) 0 (d) 25

A. 47

B. -25

C. 0

D. 25

Answer: b

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8. If \vec{a} , \vec{b} and \vec{c} are three non-coplanar vectors, then

$(\vec{a} + \vec{b} + \vec{c}) \cdot [(\vec{a} + \vec{b}) \times (\vec{a} + \vec{c})]$ equals

A. 0

B. $[\vec{a}\vec{b}\vec{c}]$

C. $2[\vec{a}\vec{b}\vec{c}]$

D. $-[\vec{a}\vec{b}\vec{c}]$

Answer: d

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9. Let \vec{p} , \vec{q} , \vec{r} be three mutually perpendicular vectors of the same magnitude. If a vector \vec{x} satisfies the equation

$$\vec{p} \times \{\vec{x} - \vec{q}\} \times \vec{p} + \vec{q} \times \{\vec{x} - \vec{r}\} \times \vec{q} + \vec{r} \times \{\vec{x} - \vec{p}\} \times \vec{r} = \vec{0},$$

then \vec{x} is given by

A. (a) $\frac{1}{2}(\vec{p} + \vec{q} - 2\vec{r})$

B. (b) $\frac{1}{2}(\vec{p} + \vec{q} + \vec{r})$

C. (c) $\frac{1}{3}(\vec{p} + \vec{q} + \vec{r})$

D. (d) $\frac{1}{3}(2\vec{p} + \vec{q} - \vec{r})$

Answer: b



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10. Let $\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$, and $\vec{b} = \hat{i} + \hat{j}$ if \vec{c} is a vector such that $\vec{a} \cdot \vec{c} = |\vec{c}|$, $|\vec{c} - \vec{a}| = 2\sqrt{2}$ and the angle between $\vec{a} \times \vec{b}$ and \vec{c} is 30° , then $\frac{|\vec{a} \times \vec{b}|}{|\vec{c}|}$ is equal to

A. $\frac{2}{3}$

B. $\frac{3}{2}$

C. 2

D. 3

Answer: b



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11. Let $\vec{a} = 2i + j + k$, $\vec{b} = i + 2j - k$ and a unit vector \vec{c} be coplanar. If \vec{c} is perpendicular to \vec{a} . Then \vec{c} is

A. $\frac{1}{\sqrt{2}}(-j + k)$

B. $\frac{1}{\sqrt{3}}(i - j - k)$

C. $\frac{1}{\sqrt{5}}(i - 2j)$

D. $\frac{1}{\sqrt{3}}(i - j - k)$

Answer: a



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12. If the vectors \vec{a} , \vec{b} , \vec{c} form the sides BC, CA and AB respectively of a triangle ABC then (A) $\vec{a} \cdot (\vec{b} \times \vec{c}) = \vec{0}$ (B) $\vec{a} \times (\vec{b} \times \vec{c}) = \vec{0}$ (C)

$$\vec{a} \cdot \vec{b} = \vec{c} \cdot \vec{c} = \vec{a} \cdot \vec{a}, a \neq 0 \quad (D) \vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} = \vec{0}$$

A. $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} = 0$

B. $\vec{a} \times \vec{b} = \vec{b} \times \vec{c} = \vec{c} \times \vec{a}$

C. $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = \vec{c} \cdot \vec{a}$

D. $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} = \vec{0}$

Answer: b



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13. Let the vectors $\vec{a}, \vec{b}, \vec{c}$ and \vec{d} be such that $(\vec{a} \times \vec{b}) \times (\vec{c} \times \vec{d}) = \vec{0}$. Let

P_1 and P_2 be planes determined by pairs of vectors

\vec{a}, \vec{b} and \vec{c}, \vec{d} respectively. Then the \angle between P_1 and P_2 is (A) 0 (B) $\pi/4$ (C) $\pi/3$

(D) $\pi/2$

A. 0

B. $\pi/4$

C. $\pi/3$

D. $\pi/2$

Answer: a



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14. If $\vec{a}, \vec{b}, \vec{c}$ are unit coplanar vectors then the scalar triple product

$[2\vec{a} - \vec{b}, 2\vec{b} - \vec{c}, 2\vec{c} - \vec{a}]$ is equal to (A) 0 (B) 1 (C) $-\sqrt{3}$ (D) $\sqrt{3}$

A. 0

B. 1

C. $-\sqrt{3}$

D. $\sqrt{3}$

Answer: a



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15. if \hat{a} , \hat{b} and \hat{c} are unit vectors. Then $|\hat{a} - \hat{b}|^2 + |\hat{b} - \hat{c}|^2 + |\hat{c} - \hat{a}|^2$ does not exceed

A. 4

B. 9

C. 8

D. 6

Answer: b



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16. If \vec{a} and \vec{b} are two unit vectors such that $\vec{a} + 2\vec{b}$ and $5\vec{a} - 4\vec{b}$ are perpendicular to each other then the angle between \vec{a} and \vec{b} is (A) 45°

(B) 60° (C) $\cos^{-1}\left(\frac{1}{3}\right)$ (D) $\cos^{-1}\left(\frac{2}{7}\right)$

A. 45°

B. 60°

C. $\cos^{-1}(1/3)$

D. $\cos^{-1}(2/7)$

Answer: b



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17. Let $\vec{V} = 2\hat{i} + \hat{j} - \hat{k}$ and $\vec{W} = \hat{i} + 3\hat{k}$. If \vec{U} is a unit vector, then the maximum value of the scalar triple product $[\vec{U}\vec{V}\vec{W}]$ is

A. -1

B. $\sqrt{10} + \sqrt{6}$

C. $\sqrt{59}$

D. $\sqrt{60}$

Answer: c



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18. Find the value of a so that the volume of the parallelepiped formed by vectors $\hat{i} + a\hat{j} + \hat{k}$, $\hat{j} + a\hat{k}$ and $a\hat{i} + \hat{k}$ becomes minimum.

A. -3

B. 3

C. $1/\sqrt{3}$

D. $\sqrt{3}$

Answer: c



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19. If $\vec{a} = (\hat{i} + \hat{j} + \hat{k})$, $\vec{a} \cdot \vec{b} = 1$ and $\vec{a} \times \vec{b} = \hat{j} - \hat{k}$, then \vec{b} is (a) $\hat{i} - \hat{j} + \hat{k}$ (b) $2\hat{i} - \hat{k}$ (c) \hat{i} (d) $2\hat{i}$

A. $\hat{i} - \hat{j} + \hat{k}$

B. $2\hat{i} - \hat{k}$

C. \hat{i}

D. $2\hat{i}$

Answer: c



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20. The unit vector which is orthogonal to the vector $5\hat{i} + 2\hat{j} + 6\hat{k}$ and is coplanar with vectors $2\hat{i} + \hat{j} + \hat{k}$ and $\hat{i} - \hat{j} + \hat{k}$ is (a) $\frac{2\hat{i} - 6\hat{j} + \hat{k}}{\sqrt{41}}$ (b) $\frac{2\hat{i} - 3\hat{j}}{\sqrt{13}}$ (c)

$\frac{3\hat{j} - \hat{k}}{\sqrt{10}}$ (d) $\frac{4\hat{i} + 3\hat{j} - 3\hat{k}}{\sqrt{34}}$

A. $\frac{2\hat{i} - 6\hat{j} + \hat{k}}{\sqrt{41}}$

B. $\frac{2\hat{i} - 3\hat{j}}{\sqrt{13}}$

C. $\frac{3\hat{j} - \hat{k}}{\sqrt{10}}$

D. $\frac{4\hat{i} + 3\hat{j} - 3\hat{k}}{\sqrt{34}}$

Answer: c



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21. if \vec{a}, \vec{b} and \vec{c} are three non-zero, non-coplanar vectors and

$$\vec{b}_1 = \vec{b} - \frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^2} \vec{a}, \vec{b}_2 = \vec{b} + \frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^2} \vec{a}, \vec{c}_1 = \vec{c} - \frac{\vec{c} \cdot \vec{a}}{|\vec{a}|^2} \vec{a} + \frac{\vec{b} \cdot \vec{c}}{|\vec{c}|^2} \vec{b}_1, \vec{c}_2 = \vec{c} - \frac{\vec{c} \cdot \vec{a}}{|\vec{a}|^2} \vec{a} - \frac{\vec{b} \cdot \vec{c}}{|\vec{c}|^2} \vec{b}_1$$

, then the set of orthogonal vectors is

A. $(\vec{a}, \vec{b}_1, \vec{c}_3)$

B. $(\vec{c}_1, \vec{b}_1, \vec{c}_2)$

C. $(\vec{a}, \vec{b}_1, \vec{c}_1)$

D. $(\vec{a}, \vec{b}_2, \vec{c}_2)$

Answer: c

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22. Let $\vec{a} = \hat{i} + 2\hat{j} + \hat{k}$, $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ and $\vec{c} = \hat{i} + \hat{j} - \hat{k}$. A vector in the plane of

\vec{a} and \vec{b} whose projection on \vec{c} is $\frac{1}{\sqrt{3}}$ is (A) $4\hat{i} - \hat{j} + 4\hat{k}$ (B) $\hat{i} + \hat{j} - 3\hat{k}$ (C)

$2\hat{i} + \hat{j} - 2\hat{k}$ (D) $4\hat{i} + \hat{j} - 4\hat{k}$

A. $4\hat{i} - \hat{j} + 4\hat{k}$

B. $3\hat{i} + \hat{j} - 3\hat{k}$

C. $2\hat{i} + \hat{j} - 2\hat{k}$

D. $4\hat{i} + \hat{j} - 4\hat{k}$

Answer: a

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23. Let two non collinear unit vectors \hat{a} and \hat{b} form an acute angle. A point P moves so that at any time t the position vector \vec{OP} (where O is the origin) is given by $\hat{a}\cos t + \hat{b}\sin t$. When P is farthest from origin O, let

M be the length of \vec{OP} and \hat{u} be the unit vector along \vec{OP} . Then (A)

$$\hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{\frac{1}{2}} \quad \text{(B) } \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{\frac{1}{2}} \quad \text{(C)}$$

$$\hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{\frac{1}{2}} \quad \text{(D) } \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{\frac{1}{2}}$$

$$\text{A. , } \hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{1/2}$$

$$\text{B. , } \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + \hat{a} \cdot \hat{b})^{1/2}$$

$$\text{C. } \hat{u} = \frac{\hat{a} + \hat{b}}{|\hat{a} + \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{1/2}$$

$$\text{D. , } \hat{u} = \frac{\hat{a} - \hat{b}}{|\hat{a} - \hat{b}|} \text{ and } M = (1 + 2\hat{a} \cdot \hat{b})^{1/2}$$

Answer: a



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24. If $\vec{a}, \vec{b}, \vec{c}$ and \vec{d} are unit vectors such that $(\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) = 1$ and $\vec{a} \cdot \vec{c} = \frac{1}{2}$ then (A) $\vec{a}, \vec{b}, \vec{c}$ are non coplanar (B) $\vec{b}, \vec{c}, \vec{d}$ are non coplanar (C) \vec{b}, \vec{d} are non paralel (D) \vec{a}, \vec{d} are paralel and \vec{b}, \vec{c} are parallel

A. \vec{a}, \vec{b} and \vec{c} are non- coplanar

B. \vec{b}, \vec{c} and \vec{d} are non-coplanar

C. \vec{b} and \vec{d} are non-parallel

D. \vec{a} and \vec{d} are parallel and \vec{b} and \vec{c} are parallel

Answer: c



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25. Two adjacent sides of a parallelogram $ABCD$ are given by

$\vec{AB} = 2\hat{i} + 10\hat{j} + 11\hat{k}$ and $\vec{AD} = -\hat{i} + 2\hat{j} + 2\hat{k}$. The side AD is rotated by an

acute angle α in the plane of the parallelogram so that AD becomes AD' .

If AD' makes a right angle with the side AB , then the cosine of the angle

α is given by a. $\frac{8}{9}$ b. $\frac{\sqrt{17}}{9}$ c. $\frac{1}{9}$ d. $\frac{4\sqrt{5}}{9}$

A. $\frac{8}{9}$

B. $\frac{\sqrt{17}}{9}$

C. $\frac{1}{9}$

D. $\frac{4\sqrt{5}}{9}$

Answer: b



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26. Let P, Q, R and S be the points on the plane with position vectors $-2\hat{i} - \hat{j}$, $4\hat{i}$, $3\hat{i} + 3\hat{j}$ and $-3\hat{i} + 2\hat{j}$ respectively. The quadrilateral PQRS must be a

- A. Parallelogram, which is neither a rhombus nor a rectangle
- B. square
- C. rectangle, but not a square
- D. rhombus, but not a square.

Answer: a



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27. Let $\vec{a} = \hat{i} + \hat{j} + \hat{k}$, $\vec{b} = \hat{i} - \hat{j} + \hat{k}$ and $\vec{c} = \hat{i} - \hat{j} - \hat{k}$ be three vectors. A vector \vec{v} in the plane of \vec{a} and \vec{b} , whose projection on \vec{c} is $\frac{1}{\sqrt{3}}$ is given by

A. $\hat{i} - 3\hat{j} + 3\hat{k}$

B. $-3\hat{i} - 3\hat{j} + \hat{k}$

C. $3\hat{i} - \hat{j} + 3\hat{k}$

D. $\hat{i} + 3\hat{j} - 3\hat{k}$

Answer: c



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28. Let $\vec{PR} = 3\hat{i} + \hat{j} - 2\hat{k}$ and $\vec{SQ} = \hat{i} - 3\hat{j} - 4\hat{k}$ determine diagonals of a parallelogram PQRS and $\vec{PT} = \hat{i} + 2\hat{j} + 3\hat{k}$ be another vector. Then the volume of the parallelepiped determined by the vectors \vec{PT} , \vec{PQ} and \vec{PS} is

A. 5

B. 20

C. 10

D. 30

Answer: c



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Multiple Correct Answers Type

1.

Let

$$\vec{a} = a_1\hat{i} + a_2\hat{j} + a_3\hat{k}, \quad \vec{b} = b_1\hat{i} + b_2\hat{j} + b_3\hat{k} \text{ and } \vec{c} = c_1\hat{i} + c_2\hat{j} + c_3\hat{k} \text{ be}$$

three non-zero vectors such that \vec{c} is a unit vectors perpendicular to

both the vectors \vec{a} and \vec{b} . If the angle between \vec{a} and \vec{b} is $\frac{\pi}{6}$

then

$$\left| \begin{array}{ccc} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{array} \right|^2 \text{ is equal to}$$

A. (a) 0

B. (b) 1

C. (c) $\frac{1}{4}(a_1^2 + a_2^2 + a_2^2)(b_1^2 + b_2^2 + b_2^2)$

D. (d) $\frac{3}{4}(a_1^2 + a_2^2 + a_2^2)(b_1^2 + b_2^2 + b_2^2)(c_1^2 + c_2^2 + c_2^2)$

Answer: c



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2. The number of vectors of unit length perpendicular to vectors

$\vec{a} = (1, 1, 0)$ and $\vec{b} = (0, 1, 1)$ is a. one b. two c. three d. infinite

A. one

B. two

C. three

D. infinite

Answer: b



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3. Let $\vec{a} = 2\hat{i} + \hat{j} + \hat{k}$, $\vec{b} = \hat{i} + 2\hat{j} - \hat{k}$ and $\vec{c} = \hat{i} + \hat{j} - 2\hat{k}$ be three vectors . A vector in the plane of \vec{b} and \vec{c} whose projection on \vec{a} is of magnitude $\sqrt{\left(\frac{2}{3}\right)}$ is (A) $2\hat{i} + 3\hat{j} + 3\hat{k}$ (B) $2\hat{i} + 3\hat{j} - 3\hat{k}$ (C) $-2\hat{i} - \hat{j} + 5\hat{k}$ (D) $2\hat{i} + \hat{j} + 5\hat{k}$

A. $2\hat{i} + 3\hat{j} - 3\hat{k}$

B. $2\hat{i} + 3\hat{j} + 3\hat{k}$

C. $-2\hat{i} - \hat{j} + 5\hat{k}$

D. $2\hat{i} + \hat{j} + 5\hat{k}$

Answer: a,c



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4. For three vectors, \vec{u} , \vec{v} and \vec{w} which of the following expressions is not equal to any of the remaining three ?

A. (a) $\vec{u} \cdot (\vec{v} \times \vec{w})$

B. (b) $(\vec{v} \times \vec{w}) \cdot \vec{u}$

C. (c) $\vec{v} \cdot (\vec{u} \times \vec{w})$

D. (d) $(\vec{u} \times \vec{v}) \cdot \vec{w}$

Answer: c



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5. Which of the following expressions are meaningful? $\vec{u} \cdot (\vec{v} \times \vec{w})$ b.

$(\vec{u} \cdot \vec{v}) \cdot \vec{w}$ c. $(\vec{u} \cdot \vec{v}) \cdot \vec{w}$ d. $\vec{u} \times (\vec{v} \cdot \vec{w})$

A. $\vec{u} \cdot (\vec{v} \times \vec{w})$

B. $(\vec{u} \cdot \vec{v}) \cdot \vec{w}$

C. $(\vec{u} \cdot \vec{v}) \vec{w}$

D. $\vec{u} \times (\vec{v} \cdot \vec{w})$

Answer: a,c

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6. If \vec{a} and \vec{b} are two non collinear vectors and

$\vec{u} = \vec{a} - (\vec{a} \cdot \vec{b}) \cdot \vec{b}$ and $\vec{v} = \vec{a} \times \vec{b}$ then \vec{v} is

A. $|\vec{u}|$

B. $|\vec{u}| + |\vec{u} \cdot \vec{v}|$

C. $|\vec{u}| + |\vec{u} \cdot \vec{b}|$

D. $|\vec{u}| + \vec{u} \cdot (\vec{a} + \vec{b})$

Answer: a,c

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7. $\vec{P} = (2\hat{i} - 2\hat{j} + \hat{k})$, then find $|\vec{P}|$

A. a unit vector

B. makes an angle $\pi/3$ with vector $(2\hat{i} - 4\hat{j} + 3\hat{k})$

C. parallel to vector $\left(-\hat{i} + \hat{j} - \frac{1}{2}\hat{k}\right)$

D. perpendicular to vector $3\hat{i} + 2\hat{j} - 2\hat{k}$

Answer: a,c,d

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8. Let \vec{a} be vector parallel to line of intersection of planes P_1 and P_2 through origin. If P_1 is parallel to the vectors $2\vec{j} + 3\vec{k}$ and $4\vec{j} - 3\vec{k}$ and P_2 is parallel to $\vec{j} - \vec{k}$ and $3\vec{i} + 3\vec{j}$, then the angle between \vec{a} and $2\vec{i} + \vec{j} - 2\vec{k}$ is :

A. $\pi/2$

B. $\pi/4$

C. $\pi/6$

D. $3\pi/4$

Answer: b,d

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9. The vectors which is/are coplanar with vectors $\hat{i} + \hat{j} + 2\hat{k}$ and $\hat{i} + 2\hat{j} + \hat{k}$ and perpendicular to the vector $\hat{i} + \hat{j} + \hat{k}$ is /are (A) $\hat{j} - \hat{k}$ (B) $-\hat{i} + \hat{j}$ (C) $\hat{i} - \hat{j}$ (D) $-\hat{j} + \hat{k}$

A. $\hat{j} - \hat{k}$

B. $-\hat{i} + \hat{j}$

C. $\hat{i} - \hat{j}$

D. $-\hat{j} + \hat{k}$

Answer: a,d



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10. Let \vec{x}, \vec{y} and \vec{z} be three vectors each of magnitude $\sqrt{2}$ and the angle between each pair of them is $\frac{\pi}{3}$ if \vec{a} is a non-zero vector perpendicular to \vec{x} and $\vec{y} \times \vec{z}$ and \vec{b} is a non-zero vector perpendicular to \vec{y} and $\vec{z} \times \vec{x}$, then

$$A. (a) \vec{b} = (\vec{b} \cdot \vec{z})(\vec{z} - \vec{x})$$

$$B. (b) \vec{a} = (\vec{a} \cdot \vec{y})(\vec{y} - \vec{z})$$

$$C. (c) \vec{a} \cdot \vec{b} = -(\vec{a} \cdot \vec{y})(\vec{b} \cdot \vec{z})$$

$$D. (d) \vec{a} = (\vec{a} \cdot \vec{y})(\vec{z} - \vec{y})$$

Answer: a,b,c

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11. Let PQR be a triangle. Let

$\vec{a} = QR$, $\vec{b} = RP$ and $\vec{c} = PQ$. if $|\vec{a}| = 12$, $|\vec{b}| = 4\sqrt{3}$ and $\vec{b} \cdot \vec{c} = 24$ then

which of the following is (are) true ?

$$A. (a) \frac{|\vec{c}|^2}{2} - |\vec{a}| = 12$$

$$B. (b) \frac{|\vec{c}|^2}{2} - |\vec{a}| = 30$$

$$C. (c) \left| \vec{a} \times \vec{b} + \vec{c} \times \vec{a} \right| = 48\sqrt{3}$$

$$D. (d) \vec{a} \cdot \vec{b} = -72$$

Answer: a,c,d



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