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## MATHS

## BOOKS - CENGAGE MATHS (ENGLISH)

## AREA

## Illustration

1. Find the area of the closed figure bounded by the curves $y=\sqrt{x}, y=\sqrt{4-3 x} a n d y=0$

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2. Find the area, lying above the $\mathrm{x}=a \mathrm{ais}$ and included between the circle $x^{2}+y^{2}=8 x$ and the parabola $y^{2}=4 x$.
3. Find the area bounded by
(i) $\mathrm{y}=\log _{e}|x|$ and $y=0$
(ii) $y=\left|\log _{e}\right| x| |$ and $y=0$

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4. Find the area bounded by $y=\frac{1}{x^{2}-2 x+2}$ and x -axis.

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5. find the area of $y=3-2 x-x^{\wedge} 2$

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6. If the area of bounded between the $x$-axis and the graph of $y=6 x-3 x^{2}$ between the ordinates $x=1 a n d x=a$ is 19 units, then $a$
can take the value 4 or -2 two value are in $(2,3)$ and one in $(-1,0)$ two value are in $(3,4)$ and one in $(-2,-1)$ none of these

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7. Prove that area common to ellipse $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$ and its auxiliary circle $x^{2}+y^{2}=a^{2}$ is equal to the area of another ellipse of semi-axis a and ab.

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8. Let $f(x)=$ maximum $\left\{x^{2},(1-x)^{2}, 2 x(1-x)\right\}$ where $x \in[0,1]$. Determine the area of the region bounded by the curve $y=f(x)$ and the lines $y=0, x=0, x=1$.

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9. Consider the region formed by the lines $x=0, y=0, x=2, y=2$. If the area enclosed by the curves $y=e^{x} a n d y=1 n x$, within this region, is being removed, then find the area of the remaining region.

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10. Draw a rough sketch of the curve $y=\frac{x^{2}+3 x+2}{x^{2}-3 x+2}$ and find the area of the bounded region between the curve and the $x$-axis.

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11. Find the area bounded by the curve $y=(x-1)(x-2)(x-3)$ lying between the ordinates $x=0 a n d x=3$.

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12. Find the area bounded by the curve $x= \begin{cases}-2-y, & y<-1 \\ y^{3}, & -1 \leq y \leq 1 \\ 2-y, & y>1\end{cases}$ and $x=0$ is

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13. Find the area enclosed by the graph of $y=\log _{e}(x+1)$, $y$-axis, and the line $y=1$

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14. Find the area bounded by the curve $y=\sin ^{-1} x$ and the line $x=0,|y|=\frac{\pi}{2}$.

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15. Find the area of the region bounded by the curves $y=\sqrt{x+2}$ and $y=\frac{1}{x+1}$ between the lines $\mathrm{x}=0$ and $\mathrm{x}=2$.

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16. Find the area bounded by $y=\sin ^{-1} x, y=\cos ^{-1} x$, and the $X$-axis.

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17. Find the area bounded by the parabola $y=x^{2}+1$ and the straight line $x+y=3$.

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18. Find the area bounded by the curves $y=\sin x a n d y=\cos x$ between two consecutive points of the intersection.

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19. Find the ratio in which the area bounded by the curves $y^{2}=12 x$ and $x^{2}=12 y$ is divided by the line $x=3$.

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20. Find the area of the figure bounded by the parabolas $x=-2 y^{2}, x=1-3 y^{2}$.

## - Watch Video Solution

21. The area common to regions $x^{2}+y^{2}-2 x \leq 0$ and ygeq $\sin (\mathrm{pix} / 2)$

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22. Find the area of the region enclosed by the curves $y=x \log x$ and $y=2 x-2 x^{2}$.

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23. Find the area bounded by $y^{2} \leq 4 x, x^{2}+y^{2} \geq 2 x$, and $x \leq y+2$ in the first quadrant.

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24. Sketch the region bounded by the curves $y=x^{2} a n d y=\frac{2}{1+x^{2}}$. Find the area.

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25. Find the area bounded by the curves $y=x^{3}-x$ and $y=x^{2}+x$.

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26. Find the area bounded by $y=-x^{3}+x^{2}+16 x$ and $y=4 x$
27. Find the area of the region enclosed by $y=-5 x-x^{2}$ and $y=x$ on interval $[-1,5]$

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28. If the area enclosed by curve $y=f(x)$ andy $=x^{2}+2$ between the abscissa $x=2 a n d x=\alpha, \alpha>2$, is $\left(\alpha^{3}-4 \alpha^{2}+8\right) s q$. unit. It is known that curve $y=f(x)$ lies below the parabola $y=x^{2}+2$.

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29. Let $C_{1}$ and $C_{2}$ be the graphs of the functions $y=x^{2}$ and $y=2 x$, respectively, where $0 \leq x \leq 1$. Let $C_{3}$ be the graph of a function $\mathrm{y}=\mathrm{f}(\mathrm{x})$, where $0 \leq x \leq 1, f(0)=0$. For a point P on $C_{1}$, let the lines through P , parallel to the axes, meet $C_{2}$ and $C_{3}$ at Q and R , respectively (see figure). If for every position of $P\left(o n C_{1}\right)$, the areas of the shaded
regions OPQ and ORP are equal, determine the function $f(x)$.


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30. 

If
the
area
bounded
by
$f(x)=\sqrt{\tan x}, y=f(c), x=0$ and $x=a, 0<c<a<\frac{\pi}{2}$ minimum then find the value of $c$.

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31. Find the area of the region $R$ which is enclosed by the curve $y \geq \sqrt{1-x^{2}}$ and $\max \{|x|,|y|\} \leq 4$.

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32. Plot the region in the first quadrant in which points are nearer to the origin than to the line $x=3$.

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33. Consider a square with vertices at $(1,1),(-1,1),(-1,-1)$ and $(1,-1)$. Let S be the region consisting of all points inside the square which are nearer to the origin than to any edge. Sketch the region $S$ and find its area.

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34. Let $O(0,0), A(2,0), \operatorname{and} B\left(1 \frac{1}{\sqrt{3}}\right)$ be the vertices of a triangle. Let $R$ be the region consisting of all those points $P$ inside $O A B$ which satisfy $d(P, O A) \leq \min [d(p, O B), d(P, A B)]$, where $d$ denotes the distance from the point to the corresponding line. Sketch the region $R$ and find its area.

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35. Find the area enclosed by $y=g(x), \mathrm{x}$-axis, $\mathrm{x}=1$ and $\mathrm{x}=37$, where $\mathrm{g}(\mathrm{x})$ is inverse of $f(x)=x^{3}+3 x+1$.

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36. Find the area bounded by the curve $f(x)=x+\sin x$ and its inverse function between the ordinates $x=0$ to $x=2 \pi$.

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1. Find the area bounded by the curve $x^{2}=y, x^{2}=-y a n d y^{2}=4 x-3$

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2. Find the area of the region enclosed by the curve $y=\left|x-\frac{1}{x}\right|(x>0)$ and the line $\mathrm{y}=2$

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3. Find the area of the region bounded by the curves $y=x^{2}, y=\left|2-x^{2}\right|$, andy $=2$, which lies to the right of the line $x=1$.

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4. The ratio in which the line $x-1=0$ divides the area bounded by the curves $2 x+1=\sqrt{4 y+1}, y=x$ and $y=2$ is

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5. If $S_{0}, S_{1}, S_{2}, \ldots$ are areas bounded by the x-axis and half-wave of the curve $y=\sin \pi \sqrt{x}, \quad$ then prove that $S_{0}, S_{1}, S_{2}, \ldots$ are in A.P...

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6. Find the area of the figure enclosed by the curve $5 x^{2}+6 x y+2 y^{2}+7 x+6 y+6=0$.

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7. Find the area bounded by the curves $x^{2}+y^{2}=4, x^{2}=-\sqrt{2} y$ and $x=y$
8. Find the area of the region bounded by the curve $C: y=\tan x$, tan $\geq n t d r a w n \rightarrow C$ at $x=\frac{\pi}{4}$, and the $x$-axis.

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9. Compute the area of the region bounded by the curves $y-e x(\log )_{e} x a n d y=\frac{\log x}{e x}$

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10. If $A_{n}$ be the area bounded by the curve $y=(\tan x)^{n}$ and the lines $x=0, y=0, x=\pi / 4$, then for $n>2$.

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1. Find the area of the smaller part of the circle $x^{2}+y^{2}=a^{2}$ cut off by the line $x=\frac{a}{\sqrt{2}}$

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2. Find the area enclosed by the curves ${ }^{\wedge} x^{\wedge} 2=y, y=x+2$,

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3. 

## A

curve
is
given
by
byy $=\left\{\left(\sqrt{4-x^{2}}\right), 0 \leq x<1 \sqrt{(3 x)}, 1 \leq x \leq 3\right.$. Find the area lying between the curve and x -axis.

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4. Find the area bounded by $\begin{gathered} \\ x\end{gathered}=2 y-y^{\wedge} 2$
5. Find the area bounded by the x -axis, part of the curve $y=\left(1-\frac{8}{x^{2}}\right)$, and the ordinates at $x=2 a n d x=4$. If the ordinate at $x=a$ divides the area into two equal parts, then find $a$.

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6. Find the area of the region bounded by the $x$-axis and the curves defined by $y=\tan x$,
(where $\frac{-\pi}{3} \leq x \leq \frac{\pi}{3}$ ) and $y=\cot x$.(where $\frac{\pi}{6} \leq x \leq \frac{2 \pi}{3}$ )

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7. Find the area bounded by $y=\left|\sin x-\frac{1}{2}\right|$ and $y=1$ for $x \in[0, \pi]$

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8. If the area bounded by the graph of $y=x e^{-a x}(a>0)$ and the x -axis is $1 / 9$ then find the value of a.

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9. The area bounded by the curve $x y^{2}=a^{2}(a-x)$ and $y$-axis is

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## Concept Application Exercise 92

1. Find the area lying in the first quadrant and bounded by the curve $y=x^{3}$ and the line $y=4 x$.

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2. Find the area bounded by the curve $x^{2}=4 y$ and the straight line $x=4 y-2$.

## - Watch Video Solution

3. Find the area enclosed by the figure described by the equation $x^{4}+1=2 x^{2}+y^{2}$.

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4. In what ratio does the $x$-axis divide the area of the region bounded by the parabolas $y=4 x-x^{2}$ and $y=x^{2}-x$ ?

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| 5. Find $\quad$ the | area of | the | circle |
| :--- | :--- | :--- | :--- | :--- |
| $x^{2}+y^{2}=16$ whichisexteri or | $\rightarrow$ theparabolay ${ }^{2}=6 x$ | by | using |

integration.

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6. Find the area of the region bounded by the curves $y=x^{2}+2, y=x, x=0, a n d x=3$.

## - Watch Video Solution

7. Find the area of the region bounded by the limits $x=0, x=\frac{\pi}{2}, \operatorname{andf}(x)=\sin x, g(x)=\cos x$.

## ( Watch Video Solution

8. Find the area bounded by $y=\tan ^{-1} x, y=\cot ^{-1} x, a n d y-a \xi s$ in the first quadrant.
9. 

Find
the area bounded $y=-(\log )_{e} x, y=(\log )_{e} x, y=(\log )_{e}(-x)$, andy $=-(\log )_{e}(-x)$.

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10. Find the area of the region $\left\{(x, y): y^{2} \leq 4 x, 4 x^{2}+4 y^{2} \leq 9\right\}$

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11. Sketch the region bounded by the curves $y=\sqrt{5-x^{2}}$ and $y=|x-1|$ and find its area.

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12. Sketch the curves and identify the region bounded by the curves $x=\frac{1}{2}, x=2, y=\log x a n y=2^{x}$. Find the area of this region.
13. Find the area bounded by $y=x^{2}$ and $y=x^{1 / 3}$ for $x \in[-1,1]$.

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14. Find the smallest area bounded by the curves $y=x-\sin x, y=x+\cos x$.

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## Concept Application Exercise 93

1. Find the continuous function $f$ where $\left(x^{4}-4 x^{2}\right) \leq f(x) \leq\left(2 x^{2}-x^{3}\right)$ such that the area bounded by $y=f(x), y=x^{4}-4 x^{2}$. then y -axis, and the line $x=t$, where $(0 \leq t \leq 2) \quad$ is $\quad k \quad$ times the area bounded by $y=f(x), y=2 x^{2}-x^{3}, y-a \xi s$, and line $x=t(w h e r e 0 \leq t \leq 2)$.
2. If the area bounded by the $x$-axis, the curve $y=f(x),(f(x)>0)$ and the lines $x=1, x=b$ is equal to $\sqrt{b^{2}+1}-$ then find $\mathrm{f}(\mathrm{x})$.

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3. The area bounded by the graph of $y=f(x), f(x)>0$ on $[0, \mathrm{a}]$ and x axis is $\frac{a^{2}}{2}+\frac{a}{2} \sin a+\frac{\pi}{2} \cos a$ then find the value of $f\left(\frac{\pi}{2}\right)$.

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4. A curve $\mathrm{y}=\mathrm{f}(\mathrm{x})$ is such that $f(x) \geq 0$ and $f(0)=0$ and bounds a curvilinear triangle with the base $[0, x]$ whose area is proportional to $(n+1)^{\text {th }}$ power of $f(x)$. If $f(1)=1$ then find $\mathrm{f}(\mathrm{x})$.
5. Find the area of curve enclosed by : $|x+y|+|x-y| \leq 4,|x| \leq 1, y \geq \sqrt{x^{2}-2 x+1}$.

## (D) Watch Video Solution

6. Consider two regions
$R_{1}$ : points P are nearer to $(1,0)$ than to $x=-1$.
$R_{2}$ : Points P are nearer to $(0,0)$ than to $(8,0)$ Find the area of the region common to $R_{1}$ and $R_{2}$.

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7. If $f:[-1,1] \rightarrow\left[-\frac{1}{2}, \frac{1}{2}\right]: f(x)=\frac{x}{1+x^{2}}$, then find the area bounded by $y=f^{-1}(x)$, the $x$-axis and the lines $x=\frac{1}{2}, x=-\frac{1}{2}$.

## - Watch Video Solution

1. Area enclosed by the curve $y=f(x)$ defined parametrically as $x=\frac{1-t^{2}}{1+t^{2}}, y=\frac{2 t}{1+t^{2}}$ isequa $<0 \quad \pi$ sqünits $\quad$ (b) $\quad \frac{\pi}{2}$ sqünits $\frac{3 \pi}{4}$ squinits (d) $\frac{3 \pi}{2}$ squinits
A. $\pi$ sq. units
B. $\pi / 2$ sq. units
C. $\frac{3 \pi}{4}$ sq. units
D. $\frac{3 \pi}{2}$ sq. units

## Answer: A

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2. Let $f(x)=$ minimum $(x+1, \sqrt{1-x})$ for all $x \leq 1$. Then the area bounded by $y=f(x)$ and the x -axis is k units then 6 k is equal to
A. $\frac{7}{3}$ sq. units
B. $\frac{1}{6}$ sq. units
C. $\frac{11}{6}$ sq. units
D. $\frac{7}{6}$ sq. units

## Answer: D

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3. The area of the closed figure bounded by $x=-1, y=0, y=x^{2}+x+1$, and the tangent to the curve $y=x^{2}+x+1$ at $\mathrm{A}(1,3)$ is
A. (a) $4 / 3$ sq. units
B. (b) $7 / 3$ sq. units
C. (c) $7 / 6$ sq. units
D. (d) None of these

## Answer: C

4. The area bounded by the curve $a^{2} y=x^{2}(x+a)$ and the $x$-axis is
A. $a^{2} / 3$ sq. units
B. $a^{2} / 4$ sq. units
C. $3 a^{2} / 4$ sq. units
D. $a^{2} / 12$ sq. units

## Answer: D

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5. The area between the curve $y=2 x^{4}-x^{2}$, the x -axis, and the ordinates of the two minima of the curve is
A. $11 / 60$ sq. units
B. $7 / 120$ sq. units
C. $1 / 30$ sq. units
D. $7 / 90$ sq. units

## Answer: B

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6. The area of the closed figure bounded by $x=-1, x=2$, and
$y=\left\{-x^{2}+2, x \leq 12 x-1, x>1\right.$ and the ascissa axis is (a)
$\frac{16}{3}$ squinits (b) $\frac{10}{3}$ squinits (c) $\frac{13}{3}$ squinits (d) $\frac{7}{3}$ squinits
A. $16 / 3$ sq. units
B. $10 / 3$ sq. units
C. $13 / 3$ sq. units
D. $7 / 3$ sq. units

## Answer: A

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7. The value of the parameter a such that the area bounded by $y=a^{2} x^{2}+a x+1$, coordinate axes, and the line $\mathrm{x}=1$ attains its least value is equal to
A. $\frac{1}{4}$ sq. units
B. $-\frac{1}{2}$ sq. units
C. $\frac{3}{4}$ sq. units
D. -1 sq. units

## Answer: C

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8. The positive valu of the parameter ' $k$ ' for which the area of the figure bounded by the curve $y=\sin (k x), x=\frac{2 \pi}{3 k}, x=\frac{5 \pi}{3 k}$ and $x$-axis is less than 2 can be
A. $\frac{1}{8}<k<\frac{3}{8}$
B. $0<k<\frac{1}{8}$
C. $1<k<2$
D. $\frac{3}{8}<k<\frac{5}{8}$

## Answer: C

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9. The area bounded by the curve $y=x\left(1-\log _{e} x\right)$ and x -axis is
A. $\frac{e^{2}}{4}$
B. $\frac{e^{2}}{2}$
C. $\frac{e^{2}-e}{2}$
D. $\frac{e^{2}-e}{4}$

## Answer: A

10. The area inside the parabola $5 x^{2}-y=0$ but outside the parabola $2 x^{2}-y+9=0$ is (a) $12 \sqrt{3}$ sq units (b) $6 \sqrt{3}$ sq units (c) $8 \sqrt{3}$ sq units (d) $4 \sqrt{3}$ sq units
A. $12 \sqrt{3}$ sq. units
B. $6 \sqrt{3}$ sq. units
C. $8 \sqrt{3}$ sq. units
D. $4 \sqrt{3}$ sq. units

## Answer: A

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11. Area enclosed between the curves $|y|=1-x^{2}$ and $x^{2}+y^{2}=1$ is (a) $\frac{3 \pi-8}{3}$ (b) $\frac{\pi-8}{3}$ (c) $\frac{2 \pi-8}{3}$ (d) None of these
A. $\frac{3 \pi-8}{3}$ sq. units
B. $\frac{\pi-8}{3}$
C. $\frac{2 \pi-8}{3}$ sq. units
D. None of these

## Answer: A

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12. If $A_{n}$ is the area bounded by $\mathrm{y}=\mathrm{x}$ and $y=x^{n}, n \in N$, then
$A_{2} . A_{3} \ldots A_{n}=$
A. $\frac{1}{n(n+1)}$
B. $\frac{1}{2^{n} n(n+1)}$
C. $\frac{1}{2^{n-1} n(n+1)}$
D. $\frac{1}{2^{n-2} n(n+1)}$

## Answer: D

13. The area of the region is 1st quadrant bounded by the $y$-axis, $y=\frac{x}{4}, y=1+\sqrt{x}$, and $y=\frac{2}{\sqrt{x}}$ is
A. $2 / 3$ sq. units
B. $8 / 3$ sq. units
C. $11 / 3$ sq. units
D. $13 / 6$ sq. units

## Answer: C

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14. The area of the closed figure bounded by $y=\frac{x^{2}}{2}-2 x+2$ and the tangents to it at $\left(1, \frac{1}{2}\right) \operatorname{and}(4,2)$ is $\frac{9}{8}$ sqinits (b) $\frac{3}{8}$ squinits $\frac{3}{2}$ squinits (d) $\frac{9}{4}$ sqiunits
A. $9 / 8$ sq. units
B. $3 / 8$ sq. units
C. $3 / 2$ sq. units
D. $9 / 4$ sq. units

## Answer: A

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> 15. The area of the region bounded by $x^{2}+y^{2}-2 x-3=0$ and $y=|x|+1$ is
A. $\frac{\pi}{2}-1$ sq. units
B. $2 \pi$ sq. units
C. $4 \pi$ sq. units
D. $\pi / 2$ sq. units

## Answer: A

16. The area enclosed by the curve $y=\sqrt{4-x^{2}}, y \geq \sqrt{2} \sin \left(\frac{x \pi}{2 \sqrt{2}}\right)$, and the $x$-axis is divided by the $y$-axis in the ratio.
(a) $\frac{\pi^{2}-8}{\pi^{2}+8}$
(b) $\frac{\pi^{2}-4}{\pi^{2}+4}$
(c) $\frac{\pi-4}{\pi-4}$
(d) $\frac{2 \pi^{2}}{2 \pi+\pi^{2}-8}$
A. $\frac{\pi^{2}-8}{\pi^{2}+8}$
B. $\frac{\pi^{2}-4}{\pi^{2}+4}$
C. $\frac{\pi-4}{\pi-4}$
D. $\frac{2 \pi^{2}}{2 \pi+\pi^{2}-8}$

## Answer: D

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17. The area bounded by the curve $y^{2}=1-x$ and the lines $y=\frac{[x]}{x}, x=-1$, and $x=\frac{1}{2}$ is
A. $\frac{3}{\sqrt{2}}-\frac{11}{6}$ sq. units
B. $3 \sqrt{2}-\frac{11}{4}$ sq. units
C. $\frac{6}{\sqrt{2}}-\frac{11}{5}$ sq. units
D. None of these

## Answer: A

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18. The area bounded by the curves $y=(\log )_{e} x a n d y=\left((\log )_{e} x\right)^{2}$ is
A. $e-2$ sq. units
B. $3-e$ sq. units
C. e sq. units
D. $e-1$ sq. units

## Answer: B

19. The area bounded by $y=3-|3-x|$ and $y=\frac{6}{|x+1|}$ is
A. $\frac{15}{2}-6$ In 2 sq. units
B. $\frac{13}{2}-3$ In 2 sq. units
C. $\frac{13}{2}-6$ In 2 sq. units
D. None of these

## Answer: C

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20. Find the area enclosed between the curves:
$y=\log _{e}(x+e), x=\log _{e}\left(\frac{1}{y}\right) \&$ the x -axis.
A. 2 sq. units
B. 1 sq. units
C. 4 sq. units
D. None of these

## Answer: A

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21. Find the area enclosed the curve $y=\sin x$ and the $X$-axis between
$x=0$ and $x=\pi$.
A. $\frac{7}{2}$ sq. units
B. $\frac{7}{4}+\sqrt{3}$ sq. units
C. $\frac{7 \sqrt{3}}{4}$ sq. units
D. $7-\frac{\sqrt{3}}{4}$ sq. units

## Answer: A

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22. The area bounded by $y=x^{2}, y=[x+1], 0 \leq x \leq 2$ and the $y$-axis is where [.] is greatest integer function.
A. $\frac{1}{3}$
B. $\frac{\sqrt{2}}{3}$
C. 1
D. $\frac{7}{3}$

## Answer: B

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23. The area of the region bounded by the parabola $(y-2)^{2}=x-1$, the tangent to the parabola at the point $(2,3)$ and the $X$-axis is
A. 7 sq. units
B. 6 sq. units
C. 9 sq. units
D. None of these

## Answer: C

## D Watch Video Solution

24. The area bounded by the curves $y=x e^{x}, y=x e^{-x}$ and the line
$x=1$ is $\frac{2}{e}$ sqünits (b) $1-\frac{2}{e}$ sqünits $\frac{1}{e}$ squinits (d) $1-\frac{1}{e}$ squnits
A. $\frac{2}{e}$ sq. units
B. $1-\frac{2}{e}$ sq. units
C. $\frac{1}{e}$ sq. units
D. $1-\frac{1}{e}$ sq. units

## Answer: A

## D Watch Video Solution

25. The area of the region whose boundaries are defined by the curves $\mathrm{y}=2$ $\cos x, y=3 \tan x$, and the $y$-axis is
A. $1+3 \operatorname{In}\left(\frac{2}{\sqrt{3}}\right)$ sq. units
B. $1+\frac{3}{2}$ In $3-3$ In 2 sq. units
C. $1+\frac{3}{2}$ In $3-\operatorname{In} 2$ sq. units
D. In $3-\operatorname{In} 2$ sq. units

## Answer: B

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26. Area bounded by $y=\sec ^{-1} x, y=\cot ^{-1} x$ and line $\mathrm{x}=1$ is given by
A. $\log (3+2 \sqrt{2})-\frac{\pi}{2}$ sq. units
B. $\frac{\pi}{2}-\log (3+2 \sqrt{2})$ sq. units
C. $\pi-\log _{e} 3$ sq. units
D. None of these

## Answer: A

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27. The area bounded by the curve $y=\frac{3}{|x|}$ and $y+|2-x|=2$ is

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28. The area enclosed by $y=x^{2}+\cos x$ and its normal at $x=\frac{\pi}{2}$ in the first quadrant is
A. $\frac{\pi^{5}}{32}-\frac{\pi^{4}}{64}+\frac{\pi^{3}}{32}+1$
B. $\frac{\pi^{5}}{16}-\frac{\pi^{4}}{32}+\frac{\pi^{3}}{24}-1$
C. $\frac{\pi^{5}}{32}-\frac{\pi^{4}}{32}+\frac{\pi^{3}}{16}$
D. $\frac{\pi^{5}}{32}-\frac{\pi^{4}}{32}+\frac{\pi^{3}}{24}+1$

## Answer: D

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29. Given $f(x)=\int_{0}^{x} e^{t}\left(\log _{e} \sec t-\sec ^{2} t\right) d t, g(x)=-2 e^{x} \tan x$, then the area bounded by the curves $y=f(x)$ and $y=g(x)$ between the ordinates $x=0$ and $x=\frac{\pi}{3}$, is (in sq. units)
A. $\frac{1}{2} e^{\frac{\pi}{3}} \log _{e} 2$
B. $e^{\frac{\pi}{3}} \log _{e} 2$
C. $\frac{1}{4} e^{\frac{\pi}{3}} \log _{e} 2$
D. $e^{\frac{\pi}{3}} \log _{e} 3$

## Answer: B

## - Watch Video Solution

30. The area of the loop of the curve $a y^{2}=x^{2}(a-x)$ is $4 a^{2}$ squinits (b) $\frac{8 a^{2}}{15}$ squinits $\frac{16 a^{2}}{9}$ squinits (d) None of these
A. $4 a^{2}$ sq. units
B. $\frac{8 a^{2}}{15}$ sq. units
C. $\frac{16 a^{2}}{9}$ sq. units
D. None of these

## Answer: B

## - Watch Video Solution

31. Aea of the region nclosed between the curves $x=y^{2}-1$ and $x=|y| \sqrt{1-y^{2}}$ is
A. 1 sq. units
B. $4 / 3$ sq. units
C. $2 / 3$ sq. units
D. 2 sq. units

Answer: D

## - Watch Video Solution

32. The area bounded by the loop of the curve $4 y^{2}=x^{2}\left(4-x^{2}\right)$ is given by (1) $\frac{7}{3}$ (2) $\frac{8}{3}$ (3) $\frac{11}{3}$ (4) $\frac{16}{3}$
A. $7 / 3$ sq. units
B. $8 / 3$ sq. units
C. $11 / 3$ sq. units
D. $16 / 3$ sq. units
33. The area enclosed by the curves
$x y^{2}=a^{2}(a-x) \operatorname{and}(a-x) y^{2}=a^{2} x$ is
A. $(\pi-2) a^{2}$ sq. units
B. $(4-\pi) a^{2}$ sq. units
C. $\pi a^{2} / 3$ sq. units
D. None of these

## Answer: A

## - Watch Video Solution

34. The area bounded by the two branches of curve $(y-x)^{2}=x^{3}$ and the straight line $x=1$ is $\frac{1}{5}$ squinits (b) $\frac{3}{5}$ squinits $\frac{4}{5}$ squinits $\frac{8}{4}$ squinits
A. $1 / 5$ sq. units
B. $3 / 5$ sq. units
C. $4 / 5$ sq. units
D. $8 / 4$ sq. units

## Answer: C

## - Watch Video Solution

35. The area bounded by the curves
$y=\sin ^{-1}|\sin x|$ and $y=\left(\sin ^{-1}|\sin x|\right)^{2}$, where $0 \leq x \leq 2 \pi$, is
A. $\frac{1}{3}+\frac{\pi^{2}}{4}$ sq. units
B. $\frac{1}{6}+\frac{\pi^{3}}{8}$ sq. units
C. 2 sq. units
D. None of these

## Answer: D

## - Watch Video Solution

36. Consider two curves $C_{1}: y^{2}=4[\sqrt{y}] \operatorname{xandC}_{2}: x^{2}=4[\sqrt{x}] y$, where
[.] denotes the greatest integer function. Then the area of region enclosed by these two curves within the square formed by the lines $x=1, y=1, x=4, y=4$ is (a) $\frac{8}{3}$ squinits (b) $\frac{10}{3}$ squinits (c) $\frac{11}{3}$ squinits (d) $\frac{11}{4}$ squinits
A. $8 / 3$ sq. units
B. $10 / 3$ sq. units
C. $11 / 3$ sq. units
D. $11 / 4$ sq. units

## Answer: C

## - Watch Video Solution

37. The area enclosed between the curve $y^{2}(2 a-x)=x^{3}$ and the line $x=2$ above the $x$-axis is
A. $\pi a^{2}$ sq. units
B. $\frac{3 \pi a^{2}}{2}$ sq. units
C. $2 \pi a^{2}$ sq. units
D. $3 \pi a^{2}$ sq. units

## Answer: B

## D Watch Video Solution

38. The area of the region of the plane bounded by $\max (|x|,|y|) \leq 1$ and $x y \leq \frac{1}{2}$ is
(a) $\frac{1}{2}+\ln 2$ sq. units
(b) $3+\ln 2$ sq.units
(c) $\frac{31}{4}$ sq. units
(d) $1+2 \ln 2$ sq.units
A. $1 / 2+\ln 2$ sq. units
B. $3+\ln 2$ sq. units
C. $31 / 4$ sq. units
D. $1+2 \ln 2$ sq. units

## Answer: B

## - Watch Video Solution

39. Find tha area of the region containing the points $(x, y)$ satisfying $4 \leq x^{2}+y^{2} \leq 2(|x|+|y|)$.
A. 8 sq. units
B. 2 sq. units
C. $4 \pi$ sq. units
D. $2 \pi$ sq. units

## Answer: A

40. Let $f(x)$ be a non-negative continuous function such that the area bounded by the curve $y=f(x)$, the $x$-axis, and the ordinates $x=\frac{\pi}{4}$ and $x=\beta>\frac{\pi}{4}$ is $\beta \sin \beta+\frac{\pi}{4} \cos \beta+\sqrt{2} \beta$. Then $f^{\prime}\left(\frac{\pi}{2}\right)$ is
A. $\left(\frac{\pi}{2}-\sqrt{2}-1\right)$
B. $\left(\frac{\pi}{4}+\sqrt{2}-1\right)$
C. $-\frac{\pi}{2}$
D. $\left(1-\frac{\pi}{2}-\sqrt{2}\right)$

## Answer: C

## - Watch Video Solution

## Multiple Correct Answers Type

1. Let $A(k)$ be the area bounded by the curves $y=x^{2}-3$ and $y=k x+2$ The range of $A(k)$ is $\left(\frac{10 \sqrt{5}}{3}, \infty\right)$ The range of $A(k)$ is

# $\left(\frac{20 \sqrt{5}}{3}, \infty\right)$ If function $k \vec{A}(k)$ is defined for $k \in[-2, \infty)$, then $A(k)$ 

 is many-one function. The value of $k$ for which area is minimum is 1 .A. The range of $A(k)$ is $\left[\frac{10 \sqrt{5}}{3}, \infty\right)$
B. The range of $A(k)$ is $\left[\frac{20 \sqrt{5}}{3}, \infty\right)$
C. If function $k \rightarrow A(k)$ is defined for $k \in[-2, \infty)$, then $\mathrm{A}(\mathrm{k})$ is many-one function
D. The value of k for which area is minimum is 1

## Answer: B::C

## - Watch Video Solution

2. The parabolas $y^{2}=4 x a n d x^{2}=4 y$ divide the square region bounded by the lines $x=4, y=4$ and the coordinate axes. If $S_{1}, S_{2}, S_{3}$ are the areas of these parts numbered from top to bottom, respectively, then

$$
S_{1}: S_{2} \equiv 1: 1 \text { (b) } S_{2}: S_{3} \equiv 1: 2 S_{1}: S_{3} \equiv 1: 1 \text { (d) } S_{1}:\left(S_{1}+S_{2}\right)=1: 2
$$

A. $S_{1}: S_{2} \equiv 1: 1$
B. $S_{2}: S_{3} \equiv 1: 2$
C. $S_{1}: S_{3} \equiv 1: 1$
D. $S_{1}:\left(S_{1}+S_{2}\right)=1: 2$

## Answer: A::C::D

## - Watch Video Solution

3. Which of the following have the same bounded area $f(x)=s \in x, g(x)=\sin ^{2} x$, where $0 \leq x \leq 10 \pi$

$$
f(x)=s \in x, g(x)=|s \in x|, \text { where } 0 \leq x \leq 20 \pi
$$

$$
f(x)=|s \in x|, g(x)=\sin ^{3} x, \text { where } 0 \leq x \leq 10 \pi
$$

$$
f(x)=s \in x, g(x)=\sin ^{4} x, \text { where } 0 \leq x \leq 10 \pi
$$

A. $f(x)=\sin x, g(x)=\sin ^{2} x$, where $0 \leq x \leq 10 \pi$
B. $f(x)=\sin x, g(x)=|\sin |, \quad$ where $0 \leq x \leq 20 \pi$
C. $f(x)=|\sin |, g(x)=\sin ^{3} x, \quad$ where $0 \leq x \leq 10 \pi$
D. $f(x)=\sin x, g(x)=\sin ^{4} x, \quad$ where $0 \leq x \leq 10 \pi$

## Answer: A::C::D

## - Watch Video Solution

4. If the curve $y=a x^{\frac{1}{2}}+b x$ passes through the point $(1,2)$ and lies above the $x$-axis for $0 \leq x \leq 9$ and the area enclosed by the curve, the $x$ axis, and the line $x=4$ is 8 sq. units, then (a) $a=1$ (b) $b=1 a=3$ (d) $b=-1$
A. $a=1$
B. $b=1$
C. $a=3$
D. $b=-1$

## Answer: C::D

5. The area bounded by the curve $x=a \cos ^{3} t,, y=a \sin ^{3} t$, is :
A. $12 a^{2} \int_{0}^{\pi / 2} \cos ^{4} t \sin ^{2} t d t$
B. $12 a^{2} \int_{0} \cos ^{2} t \sin ^{4} t d t$
C. $2 \int_{-a}^{a}\left(a^{2 / 3}-x^{2 / 3}\right)^{3 / 2} d x$
D. $4 \int_{0}^{a}\left(a^{2 / 3}-x^{2 / 3}\right) d x$

## Answer: A::C::D

## - Watch Video Solution

6. If $A_{1}$ is the area area bounded by $\left|x-a_{i}\right|+|y|=b_{i}, i \in N$,where $a_{i+1}=a_{i}+\frac{3}{2} b_{i}$ and $b_{i+1}=\frac{b_{i}}{2}, a_{i}=0$ and $b_{i}=32$, then
A. $A_{3}=128$
B. $A_{3}=256$
C. $\lim _{n \rightarrow \infty} \sum_{i=1}^{n} A_{i}=\frac{8}{3}(32)^{2}$
D. $\lim _{n \rightarrow \infty} \sum_{i=1}^{n} A_{i}=\frac{4}{3}(16)^{2}$

## Answer: A:C

## - Watch Video Solution

7. Find the area bounded by the curve $y=2 x-x^{2}$, and the line $y=x$
A. $2 \int_{1}^{e} \sqrt{\log _{e} y} d y$
B. $2 e-\int^{1} e^{x^{2}} d x$
C. $\int_{-1}^{1}\left(e-e^{x^{2}}\right) d x$
D. $2 \int_{0} \sqrt{x} e^{x} d x$

## Answer: A::B::C::D

8. The area bounded by the curves $y=|x|-1$ and $y=-|x|+1$ is 1 sq. units (b) 2 sq. units $2 \sqrt{2}$ sq. units (d) 4 sq. units
A. $\alpha=e^{2}+1$
B. $\alpha=e^{2}-2$
C. $\beta=1+e^{-1}$
D. $\beta=1+e^{-2}$

## Answer: A: D

## - Watch Video Solution

9. 

Consider
curves
$S_{1}: \sqrt{|x|}+\sqrt{|y|}=\sqrt{a}, S_{2}: x^{2}+y^{2}=a^{2}$ and $S_{3}:|x|+|y|=a$. If $\alpha$ is the area bounded by $S_{2}$ and $S_{3}$, then
A. $\alpha=a^{2}\left(\pi-\frac{2}{3}\right)$
B. $\beta=\frac{4 a^{2}}{3}$
C. $\gamma=2 a^{2}(\pi-1)$
D. the ratio in which $S_{3}$ divides area between $S_{1}$ and $S_{2}$ is $4: 3(\pi-2)$

## Answer: A::B::D

## D Watch Video Solution

10. Let $A(k)$ be the area bounded by the curves $y=x^{2}+2 x-3$ and $y=k x+1$. Then
A. the value of $k$ for which $A(k)$ is least is 2
B. the value of $k$ for which $A(k)$ is least is $3 / 2$
C. least value of $A(k)$ is $32 / 3$
D. least value of $A(k)$ is $64 / 3$

## Answer: A::C

11. The area of the region bounded by the curve $y=e^{x}$ and lines $\mathrm{x}=0$ and $y=e$ is
A. $e-1$
B. $\int_{1}^{e} \operatorname{In}(e+1-y) d y$
C. $e-\int_{0}^{1} e^{x} d x$
D. $\int_{1}^{e} \operatorname{In} \mathrm{y} d y$

## Answer: B::C::D

12. The area of the region $R=\left\{(x, y):|x| \leq|y|\right.$ and $\left.x^{2}+y^{2} \leq 1\right\}$ is
A. $\frac{1}{2}<\alpha<1$
B. $\alpha^{4}+4 \alpha^{2}-1=0$
C. $0<\alpha \leq \frac{1}{2}$
D. $2 \alpha^{4}-4 \alpha^{2}+1=0$

## Answer: A::D

## - Watch Video Solution

13. Let $f: R \rightarrow R$ be a differentiable function such that $f(x)=x^{2}+\int_{0}^{x} e^{-t} f(x-t) d t$.
$y=f(x)$ is
A. The curve $y=f(x)$ passes through the point $(1,2)$
B. The curve $\mathrm{y}=\mathrm{f}(\mathrm{x})$ passes through the point $(2,-1)$
C. The
area
of
the
region
$\left\{(x, y) \in[0,1] \times R: f(x) \leq y \leq \sqrt{1-x^{2}}\right\}$ is $\frac{\pi-2}{4}$
D. The
area
of
the
region

$$
\left\{(x, y) \in[0,1] \times R: f(x) \leq y \leq \sqrt{1-x^{2}}\right\} \text { is } \frac{\pi-1}{4}
$$

## - Watch Video Solution

## Linkded Comprehension Type

1. Let $A_{r}$ be the area of the region bounded between the curves $y^{2}=\left(e^{-k r}\right) x($ where $k>0, r \in N)$ and the line $y=m x($ where $m \neq 0$ , k and m are some constants $A_{1}, A_{2}, A_{3}, \ldots$ are in G.P. with common ratio
A. $e^{-k}$
B. $e^{-2 k}$
C. $e^{-4 k}$
D. None of these

## Answer: B

2. Let $A_{r}$ be the area of the region bounded between the curves $y^{2}=\left(e^{-k r}\right) x($ where $k>0, r \in N)$ and the line $y=m x($ where $m \neq 0$ , $k$ and $m$ are some constants
$\lim _{n \rightarrow \infty} \Sigma_{i=1}^{n} A_{i}=\frac{1}{48\left(e^{2 k}-1\right)}$ then the value of m is
A. 3
B. 1
C. 2
D. 4

## Answer: C

## - Watch Video Solution

3. If $y=f(x)$ is a monotonic function in ( $a, b)$, then the area bounded by the ordinates at $x=a, x=b, y=f(x)$ and $y=f(c)($ where $c \in(a, b))$ is minimum whe

Proof : $A=\int_{a}^{c}(f(c)-f(x)) d x+\int_{c}^{b}(f(c)) d x$ $=f(c)(c-a)-\int_{a}^{c}(f(x)) d x+\int_{a}^{b}(f(x)) d x-f(c)(b-c)$
$\Rightarrow \quad A=[2 c-(a+b)] f(c)+\int_{c}^{b}(f(x)) d x-\int_{a}^{c}(f(x)) d x$


## Differentiating w.r.t. c, we get

$\frac{d A}{d c}=[2 c-(a+b)] f^{\prime}(c)+2 f(c)+0-f(c)-(f(c)-0)$
For maxima and minima, $\frac{d A}{d c}=0$

$$
\Rightarrow \quad f^{\prime}(c)[2 c-(a+b)]=0\left(a s f^{\prime}(c) \neq 0\right)
$$

Hence, $c=\frac{a+b}{2}$
Also for $c<\frac{a+b}{2}, \frac{d A}{d c}<0$ and for $c>\frac{a+b}{2}, \frac{d A}{d c}>0$

Hence, A is minimum when $c=\frac{a+b}{2}$.
If the area bounded by $f(x)=\frac{x^{3}}{3}-x^{2}+a$ and the straight lines $\mathrm{x}=0$, $x=2$, and the $x$-axis is minimum, then the value of $a$ is
A. $1 / 2$
B. 2
C. 1
D. $2 / 3$

## Answer: D

## - Watch Video Solution

4. If $y=f(x)$ is a monotonic function in ( $a, b)$, then the area bounded by the ordinates at $x=a, x=b, y=f(x)$ and $y=f(c)($ where $c \in(a, b))$ is min iumwhen $c=\frac{a+b}{2}$.
Proof: $A=\int_{a}^{c}(f(c)-f(x)) d x+\int_{c}^{b}(f(c)) d x$
$=f(c)(c-a)-\int_{a}^{c}(f(x)) d x+\int_{a}^{b}(f(x)) d x-f(c)(b-c)$
$\Rightarrow \quad A=[2 c-(a+b)] f(c)+\int_{c}^{b}(f(x)) d x-\int_{a}^{c}(f(x)) d x$


Differentiating w.r.t. c, we get

$$
\frac{d A}{d c}=[2 c-(a+b)] f^{\prime}(c)+2 f(c)+0-f(c)-(f(c)-0)
$$

For maxima and minima, $\frac{d A}{d c}=0$

$$
\Rightarrow \quad f^{\prime}(c)[2 c-(a+b)]=0\left(a s f^{\prime}(c) \neq 0\right)
$$

Hence, $c=\frac{a+b}{2}$
Also for $c<\frac{a+b}{2}, \frac{d A}{d c}<0$ and for $c>\frac{a+b}{2}, \frac{d A}{d c}>0$ Hence, A is minimum when $c=\frac{a+b}{2}$.

The value of the parameter a for which the area of the figure bounded by
the abscissa axis, the graph of the function $y=x^{3}+3 x^{2}+x+a$, and the straight lines, which are parallel to the axis of ordinates and cut the abscissa axis at the point of extremum of the function, which is the least, is
A. 2
B. 0
C. -1
D. 1

## Answer: C

## - Watch Video Solution

5. If $y=f(x)$ is a monotonic function in ( $a, b)$, then the area bounded by the ordinates
$x=a, x=b, y=f(x)$ and $y=f(c)($ where $c \in(a, b))$ is minimum whe

Proof : $A=\int_{a}^{c}(f(c)-f(x)) d x+\int_{c}^{b}(f(c)) d x$
$=f(c)(c-a)-\int_{a}^{c}(f(x)) d x+\int_{a}^{b}(f(x)) d x-f(c)(b-c)$
$\Rightarrow \quad A=[2 c-(a+b)] f(c)+\int_{c}^{b}(f(x)) d x-\int_{a}^{c}(f(x)) d x$


Differentiating w.r.t. c, we get
$\frac{d A}{d c}=[2 c-(a+b)] f^{\prime}(c)+2 f(c)+0-f(c)-(f(c)-0)$
For maxima and minima, $\frac{d A}{d c}=0$

$$
\Rightarrow \quad f^{\prime}(c)[2 c-(a+b)]=0\left(a s f^{\prime}(c) \neq 0\right)
$$

Hence, $c=\frac{a+b}{2}$
Also for $c<\frac{a+b}{2}, \frac{d A}{d c}<0$ and for $c>\frac{a+b}{2}, \frac{d A}{d c}>0$ Hence, A is minimum when $c=\frac{a+b}{2}$.

If the area enclosed by $f(x)=\sin x+\cos x, y=a$ between two consecutive points of extremum is minimum, then the value of a is
A. 0
B. -1
C. 1
D. 2

## Answer: A

## - Watch Video Solution

6. Consider the area $S_{0}, S_{1}, S_{2} \ldots$. bounded by the x-axis and half-waves of the curve $y=e^{-x} \sin x, \quad$ where $x \geq 0$.

The value of $S_{0}$ is
A. $\frac{1}{2}\left(1+e^{\pi}\right)$ sq. units
B. $\frac{1}{2}\left(1+e^{-\pi}\right)$ sq. units
C. $\frac{1}{2}\left(1-e^{-\pi}\right)$ sq. units
D. $\frac{1}{2}\left(e^{\pi}-1\right)$ sq. units

## Answer: A

## - Watch Video Solution

7. Consider the sequence of natural numbers $s_{0}, s_{1}, s_{2}$,... such that $s_{0}=3, s_{1}=3$ and $s_{n}=3+s_{n-1} s_{n-2}$, then
A. $\frac{e^{\pi}}{2}$
B. $e^{-\pi}$
C. $e^{\pi}$
D. $\frac{e^{-\pi}}{2}$

## Answer: C

8. Consider the area $S_{0}, S_{1}, S_{2} \ldots$. bounded by the x-axis and half-waves of the curve $y=e^{-x} \sin x, \quad$ where $x \geq 0$.

The value of $S_{0}$ is
A. $\frac{1+e^{\pi}}{1-e^{-\pi}}$
B. $\frac{\frac{1}{2}\left(1+e^{\pi}\right)}{1-e^{\pi}}$
C. $\frac{1}{2\left(1-e^{-\pi}\right)}$
D. None of these

## Answer: B

## - Watch Video Solution

9. 

Two
curves
$C_{1} \equiv[f(y)]^{2 / 3}+[f(x)]^{1 / 3}=0$ and $C_{2} \equiv[f(y)]^{2 / 3}+[f(x)]^{2 / 3}=12$,
satisfying the
relation
$(x-y) f(x+y)-(x+y) f(x-y)=4 x y\left(x^{2}-y^{2}\right)$
The area bounded by the curve $C_{1}$ and $C_{2}$ is
A. (a) $2 \pi-\sqrt{3}$ sq. units
B. (b) $2 \pi+\sqrt{3}$ sq. units
C. (c) $\pi+\sqrt{6}$ sq. units
D. (d) $2 \sqrt{3}-\pi$ sq. units

## Answer: B

## - Watch Video Solution

10. 

Two
curves
$C_{1} \equiv[f(y)]^{2 / 3}+[f(x)]^{1 / 3}=0$ and $C_{2} \equiv[f(y)]^{2 / 3}+[f(x)]^{2 / 3}=12$,
satisfying
the
relation
$(x-y) f(x+y)-(x+y) f(x-y)=4 x y\left(x^{2}-y^{2}\right)$
The area bounded by the curve $C_{2}$ and $|x|+|y|=\sqrt{12}$ is
A. (a) $12 \pi-24$ sq. units
B. (b) $6-\sqrt{12}$ sq. units
C. (c) $2 \sqrt{12}-6$ sq. units
D. (d) None of these

## Answer: A

## - Watch Video Solution

11. 

$C_{1} \equiv[f(y)]^{2 / 3}+[f(x)]^{1 / 3}=0$ and $C_{2} \equiv[f(y)]^{2 / 3}+[f(x)]^{2 / 3}=12$,
satisfying the
relation
$(x-y) f(x+y)-(x+y) f(x-y)=4 x y\left(x^{2}-y^{2}\right)$
The area bounded by $C_{1}$ and $x+y+2=0$ is
A. (a) $5 / 2$ sq. units
B. (b) $7 / 2$ sq. units
C. (c) $9 / 2$ sq. units
D. (d) None of these

## Answer: C

12. 

Consider
the
two
curves
$C_{1}: y=1+\cos x$ and $C_{2}: y=1+\cos (x-\alpha)$ for $\alpha \in\left(0, \frac{\pi}{2}\right)$, where

Also the area of the figure bounded by the curves $C_{1}, C_{2}$, and $x=0$ is same as that of the figure bounded by $C_{2}, y=1$, and $x=\pi$.

The value of $\alpha$ is
A. $\frac{\pi}{4}$
B. $\frac{\pi}{3}$
C. $\frac{\pi}{6}$
D. $\frac{\pi}{8}$

## Answer: C

## - Watch Video Solution

13. Consider two curves $C_{1}: y=\frac{1}{x} a n d C_{2}: y=1 n x$ on the $x y$ plane. Let $D_{1}$ denotes the region surrounded by $C_{1}, C_{2}$, and the line $x=1 a n d D_{2}$
denotes the region surrounded by $C_{1}, C_{2}$ and the line $x=a$. If $D_{1}=D_{2}$, then the sum of logarithm of possible value of $a$ is $\qquad$
A. 1 sq. units
B. 2 sq. units
C. $2+\sqrt{3}$ sq. units
D. None of these

## Answer: B

## - Watch Video Solution

14. Consider the function defined implicity by the equation $y^{2}-2 y e^{\sin ^{-1} x}+x^{2}-1+[x]+e^{2 \sin ^{-1} x}=0($ where $[\mathrm{x}]$ denotes the greates The area of the region bounded by the curve and the line $x=-1$ is
A. $\pi+1$ sq. units
B. $\pi-1$ sq. units
C. $\frac{\pi}{2}+1$ sq. units
D. $\frac{\pi}{2}-1$ sq. units

## Answer: A

## - Watch Video Solution

15. Consider the function defined implicity by the equation $y^{2}-2 y e^{\sin ^{-1} x}+x^{2}-1+[x]+e^{2 \sin ^{-1} x}=0$ (where $[\mathrm{x}]$ denotes the greates Line $\mathrm{x}=0$ divides the region mentioned above in two parts. The ratio of area of left-hand side of line to that of right-hand side of line is
A. $1+\pi: \pi$
B. $2-\pi: \pi$
C. 1:1
D. $\pi+2: \pi$

## Answer: D

16. Consider two functions
$f(x)=\left\{\begin{array}{ll}{[x],} & -2 \leq x \leq-1 \\ |x|+1, & -1<x \leq 2\end{array}\right.$ and $g(x)= \begin{cases}{[x],} & -\pi \leq x<0 \\ \sin x, & 0 \leq x \leq \pi\end{cases}$ where [.] denotes the greatest integer function.

The exhaustive domain of $g(f(x))$ is
A. $\frac{\sqrt{3}}{4}+\frac{\pi}{6}$ sq. units
B. $\frac{\sqrt{3}}{2}+\frac{\pi}{6}$ sq. units
C. $\frac{\sqrt{3}}{4}-\frac{\pi}{6}$ sq. units
D. $\frac{\sqrt{3}}{2}-\frac{\pi}{6}$ sq. units

## Answer: A

## (D) Watch Video Solution

17. Computing area with parametrically represented boundaries: If the boundary of a figure is represented by parametric equation, i.e., $x=x(t), y=(t)$, then the area of the figure is evaluated by one of the three formulas :
$S=-\int_{\alpha}^{\beta} y(t) x^{\prime}(t) d t$,
$S=\int_{\alpha}^{\beta} x(t) y^{\prime}(t) d t$,
$S=\frac{1}{2} \int_{\alpha}^{\beta}\left(x y^{\prime}-y x^{\prime}\right) d t$,
Where $\alpha$ and $\beta$ are the values of the parameter t corresponding respectively to the beginning and the end of the traversal of the curve corresponding to increasing t .

The area of the region bounded by an are of the cycloid $x=a(t-\sin t), y=a(1-\cos t)$ and the x -axis is
A. $6 \pi a^{2}$ sq. units
B. $3 \pi a^{2}$ sq. units
C. $4 \pi a^{2}$ sq. units
D. None of these

## Answer: B

18. Computing area with parametrically represented boundaries: If the boundary of a figure is represented by parametric equation, i.e., $x=x(t), y=(t)$, then the area of the figure is evaluated by one of the three formulas :
$S=-\int_{\alpha}^{\beta} y(t) x^{\prime}(t) d t$,
$S=\int_{\alpha}^{\beta} x(t) y^{\prime}(t) d t$,
$S=\frac{1}{2} \int_{\alpha}^{\beta}\left(x y^{\prime}-y x^{\prime}\right) d t$,
Where $\alpha$ and $\beta$ are the values of the parameter t corresponding respectively to the beginning and the end of the traversal of the curve corresponding to increasing t.

The area of the loop described as
$x=\frac{t}{3}(6-t), y=\frac{t^{2}}{8}(6-t)$ is
A. $\frac{27}{5}$ sq. units
B. $\frac{24}{5}$ sq. units
C. $\frac{27}{6}$ sq. units
D. $\frac{21}{5}$ sq. units

## D Watch Video Solution

19. Computing area with parametrically represented boundaries: If the boundary of a figure is represented by parametric equation, i.e., $x=x(t), y=(t)$, then the area of the figure is evaluated by one of the three formulas :
$S=-\int_{\alpha}^{\beta} y(t) x^{\prime}(t) d t$
$S=\int_{\alpha}^{\beta} x(t) y^{\prime}(t) d t$,
$S=\frac{1}{2} \int_{\alpha}^{\beta}\left(x y^{\prime}-y x^{\prime}\right) d t$,
Where $\alpha$ and $\beta$ are the values of the parameter t corresponding respectively to the beginning and the end of the traversal of the curve corresponding to increasing t .

If the curve given by parametric equation $x=t-t^{3}, y=1-t^{4}$ forms a loop for all values of $t \in[-1,1]$ then the area of the loop is
A. $\frac{1}{7}$ sq. units
B. $\frac{3}{5}$ sq. units
C. $\frac{16}{35}$ sq. units
D. $\frac{8}{35}$ sq. units

## Answer: C

## - Watch Video Solution

20. Let $f(x)$ be a continuous function fiven by
$f(x)=\left\{\begin{array}{ll}2 x, & |x| \leq 1 \\ x^{2}+a x+b, & |x|>1\end{array}\right.$, then
If $\mathrm{f}(\mathrm{x})$ is continuous for all real x then the value of $a^{2}+b^{2}$ is
A. 3
B. 4
C. 5
D. 11

## Answer: C

21. Let $f(x)$ be continuous function given by $f(x)=\{2 x,|x| \leq 1$ and $\left.x^{2}+a x+b,|x|>1\right\}$.

Find the area of the region in the third quadrant bounded by the curves $x=-2 y^{2}$ and $y=f(x)$ lying on the left of the line $8 x+1=0$.
A. sq. units
B. $\frac{257}{192}$ sq. units
C. $\frac{257}{96}$ sq. units
D. $\frac{289}{192}$ sq. units

## Answer: B

## - Watch Video Solution

## Matrix Match Type

1. Match the following lists :

| List I | List II |
| :--- | :--- |
| a. The area bounded by the curve <br> $y=x\|x\|, x$-axis and the ordinates <br> $x=1, x=-1$ | p. $10 / 3$ sq. units |
| b. The area of the region lying between <br> the lines $x-y+2=0, x=0$, and the <br> curve $x=\sqrt{y}$ | q. 64/3 sq. units |
| c. The area enclosed between the curves |  |
| $y^{2}=x$ and $y=\|x\|$ | r. $2 / 3$ sq. units |
| d. The area bounded by parabola $y^{2}=x$, <br> straight line $y=4$, and the $y$-axis | s. $1 / 6$ sq. units |

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2. show that the tangents to thre curve $y=2 x^{3}-3$ at the point where $x=2$ and $x=-2$ are parallel

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3. find the point on the curve $y=2 x^{2}-6 x-4$ at which the tangent is
4. Find the point on the curve $y=x^{3}-11 x+5$ at which the tangent has the equation $y=x-11$

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5. find the equation of the tangent to the curve $y=-5 x^{2}+6 x+7$ at the point $(1 / 2,35 / 4)$

## - Watch Video Solution

## Numerical Value Type

1. The area enclosed by the curve $c: y=x \sqrt{9-x^{2}}(x \geq 0)$ and the $x$-axis is $\qquad$
2. Let $S$ be the area bounded by the curve $y=\sin x(0 \leq x \leq \pi)$ and the $x$-axis and $T$ be the area bounded by the curves $y=\sin x\left(0 \leq x \leq \frac{\pi}{2}\right), y=a \cos x\left(0 \leq x \leq \frac{\pi}{2}\right), \quad$ and the $x$-axis (wherea $\in R^{+}$) The value of ( $3 a$ ) such that $S: T=1: \frac{1}{3}$ is $\qquad$

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3. Let $C$ be a curve passing through $M(2,2)$ such that the slope of the tangent at any point to the curve is reciprocal of the ordinate of the point. If the area bounded by curve $C$ and line $x=2$ is $A$, then the value of $\frac{3 A}{2}$ is..

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4. The area enclosed by $f(x)=12+a x \pm x^{2}$ coordinates axes and the ordinates at $x=3(f(3)>0)$ is 45 sq. units. If m and n are the x -axis intercepts of the graph of $y=f(x)$, then the value of $(m+n+a)$ si $\qquad$ .
5. If the area bounded by the curve $f(x)=x^{1 / 3}(x-1)$ and the $x$-axis is A, then the value of 28 A is ..

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6. If the area bounded by the curve $y=x^{2}+1$ and the tangents to it drawn from the origin is $A$, then the value of $3 A$ is

## - Watch Video Solution

7. If the area enclosed by the curve $y=\sqrt{x}$ and $x=-\sqrt{y}$, the circle $x^{2}+y^{2}=2$ above the $x$-axis is $A$, then the value of $\frac{16}{\pi} A$ is

## - Watch Video Solution

8. The value of $a(a>0)$ for which the area bounded by the curves $y=\frac{x}{6}+\frac{1}{x^{2}}, y=0, x=a$, and $x=2 a$ has the least value is $\qquad$ .

## ( Watch Video Solution

9. Area bounded by the curve $[|x|]+[|y|]=3$, where[.] denotes the greatest integer function

## - Watch Video Solution

10. The area bounded by the curves $y=x(x-3)^{2}$ and $y=x$ is $\qquad$ (in sq. units)

## - Watch Video Solution

11. 

If
the
area
of
the
region
$\left\{(x, y): 0 \leq y \leq x^{2}+1,0 \leq y \leq x+1,0 \leq x \leq 2\right\}$ is $A$, then the
$\qquad$

## - Watch Video Solution

12. If $S$ is the sum of possible values of $c$ for which the area of the figure bounded by the curves $y=\sin 2 x$, the straight lines $x=\frac{\pi}{6}, x=c$, and the abscissa axis is equal to $\frac{1}{2}$, then the value of $\pi / S$ is $\qquad$

## - Watch Video Solution

13. If $A$ is the area bounded by the curves $y=\sqrt{1-x^{2}}$ and $y=x^{3}-x$, then of $\frac{\pi}{A}$.

## - Watch Video Solution

14. Consider two curves $C_{1}: y=\frac{1}{x} a n d C_{2}: y=1 n x$ on the $x y$ plane. Let $D_{1}$ denotes the region surrounded by $C_{1}, C_{2}$, and the line $x=1$ and $D_{2}$
denotes the region surrounded by $C_{1}, C_{2}$ and the line $x=a$. If $D_{1}=D_{2}$, then the sum of logarithm of possible value of $a$ is $\qquad$

## - Watch Video Solution

15. If ' $a^{\prime}(a>0)$ is the value of parameter for each of which the area of the figure bounded by the straight line $y=\frac{a^{2}-a x}{1+a^{4}}$ and the parabola $y=\frac{x^{2}+2 a x+3 a^{2}}{1+a^{4}}$ is the greatest, then the value of $a^{4}$ is

## - Watch Video Solution

16. If $S$ is the sum of cubes of possible value of $c$ for which the area of the figure bounded by the curve $y=8 x^{2}-x^{5}$, then straight lines $x=1 a n d x=c$ and the abscissa axis is equal to $\frac{16}{3}$, then the value of $[S]$, where [.] denotest the greatest integer function, is $\qquad$

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17. For a point $P$ in the plane, let $d_{1}(P) \operatorname{andd}_{2}(P)$ be the distances of the point $P$ from the lines $x-y=0 a n d x+y=0$ respectively. The area of the region $R$ consisting of all points $P$ lying in the first quadrant of the plane and satisfying $2 \leq d_{1}(P)+d_{2}(P) \leq 4$, is

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18. A farmer $F_{1}$ has a land in the shape of a triangle with vertices at $P(0,0), Q(1,1)$ and $R(2,0)$. From this land, a neighbouring farmer $F_{2}$ takes away the region which lies between the side $P Q$ and a curve of the form $y=x^{n}(n>1)$. If the area of the region taken away by the farmer $F_{2}$ is exactly $30 \%$ of the area of $P Q R$, then the value of $n$ is
$\qquad$ .

## - Watch Video Solution

1. The area of the region bounded by the parabola $(y-2)^{2}=x-1$, the tangent to the parabola at the point $(2,3)$ and the X -axis is
A. 3
B. 6
C. 9
D. 12

## Answer: C

## - Watch Video Solution

2. The area bounded by the curves $y=\cos x$ and $y=\sin x$ between the ordinates $x=0$ and $x=\frac{3 \pi}{2}$ is
A. $4 \sqrt{2}+1$
B. $4 \sqrt{2}-1$
C. $4 \sqrt{2}+2$
D. $4 \sqrt{2}-2$

Answer: D

## - Watch Video Solution

3. The area of the region enclosed by the curve $y=x, x=e, y=\frac{1}{x}$ and the positive X -axis is
A. $\frac{5}{2}$ square units
B. $\frac{1}{2}$ square units
C. 1 square units
D. $\frac{3}{2}$ square units

## Answer: D

## - Watch Video Solution

4. The area bounded between the parabolas $x^{2}=\frac{y}{4}$ and $x^{2}=9 y$ and the straight line $\mathrm{y}=2$ is
A. $20 \sqrt{2}$
B. $\frac{10 \sqrt{2}}{3}$
C. $\frac{20 \sqrt{2}}{3}$
D. $10 \sqrt{2}$

## Answer: C

## - Watch Video Solution

5. The area (in square units) bounded by the curves $y=\sqrt{x}, 2 y-x+3=0, x$-axis, and lying in the first quadrant is
A. 9
B. 36
C. 18
D. $\frac{27}{4}$

## Answer: A

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6. The area of the region described by $A=\left\{(x, y): x^{2}+y^{2} \leq 1\right.$ and $\left.y^{2} \leq 1-x\right\}$ is
A. $\frac{\pi}{2}+\frac{4}{3}$
B. $\frac{\pi}{2}-\frac{4}{3}$
C. $\frac{\pi}{2}-\frac{2}{3}$
D. $\frac{\pi}{2}+\frac{2}{3}$

Answer: D

## - Watch Video Solution

7. The area (in sq. units) of the region described by $\{x, y): y^{2} \leq 2 x$ and $\left.y \geq 4 x-1\right\}$ is
A. $\frac{7}{32}$
B. $\frac{5}{64}$
C. $\frac{15}{64}$
D. $\frac{9}{32}$

Answer: D

## - Watch Video Solution

8. The area (in sq units) of the region
$\left\{(x, y): y^{2} \geq 2 x\right.$ and $\left.x^{2}+y^{2} \leq 4 x, x \geq 0, y \geq 0\right\}$ is
A. $\pi-\frac{8}{3}$
B. $\pi-\frac{4 \sqrt{2}}{3}$
C. $\frac{\pi}{2}-\frac{2 \sqrt{2}}{3}$
D. $\pi-\frac{4}{3}$

## Answer: A

## - Watch Video Solution

9. The area (in sq units) of the region bounded by the curve $y=\sqrt{x}$ and the lines $y=0, y=x-2$, is
A. $\frac{5}{2}$
B. $\frac{59}{12}$
C. $\frac{3}{2}$
D. $\frac{7}{3}$

## Answer: A

## - Watch Video Solution

10. Let ${ }^{g} g(x)=\cos ^{\wedge} 2 x, f(x)=s q r t x$ and alpha,beta (alpha
A. $\frac{1}{2}(\sqrt{2}-1)$
B. $\frac{1}{2}(\sqrt{3}-1)$
C. $\frac{1}{2}(\sqrt{3}+1)$
D. $\frac{1}{2}(\sqrt{3}-\sqrt{2})$

## Answer: B

## - Watch Video Solution

## Single Correct Answer Type

1. Let the straight line $x=b$ divide the area enclosed by $y=(1-x)^{2}, y=0$, and $x=0 \quad$ into two parts $R_{1}(0 \leq x \leq b)$ and $R_{2}(b \leq x \leq 1)$ such that $R_{1}-R_{2}=\frac{1}{4}$. Then b equals
A. $3 / 4$
B. $1 / 2$
C. $1 / 3$
D. $1 / 4$

## Answer: B

## - Watch Video Solution

2. The area enclosed by the curves
$y=\sin x+\cos x$ and $y=|\cos x-\sin x|$ over the interval $\left[0, \frac{\pi}{2}\right]$ is (a)
$4(\sqrt{2}-1)$ (b) $2 \sqrt{2}(\sqrt{2}-1)$ (c) $2(\sqrt{2}+1)$ (d) $2 \sqrt{2}(\sqrt{2}+1)$
A. $4(\sqrt{2}-1)$
B. $2 \sqrt{2}(\sqrt{2}-1)$
C. $2(\sqrt{2}+1)$
D. $2 \sqrt{2}(\sqrt{2}+1)$

## Answer: B

## D Watch Video Solution

3. Area of the region $\left\{(x, y) \in R^{2}: y \geq \sqrt{|x+3|}, 5 y \leq x+9 \leq 15\right\}$ is equal to
A. $\frac{1}{6}$
B. $\frac{4}{3}$
C. $\frac{3}{2}$
D. $\frac{5}{3}$

## Answer: C

## - Watch Video Solution

4. The area enclosed between the curve $y=\sin ^{2} x$ and $y=\cos ^{2} x$ in the interval $0 \leq x \leq \pi$ is $\qquad$ sq. units.
A. 2 sq unit
B. $\frac{1}{2}$ sq unit
C. 1 sq unit
D. None of these

## Answer: C

## D Watch Video Solution

5. The area of the region enclosed by $y=x^{2}$ and $y=\sqrt{|x|}$ is
A. $1 / 3$
B. $2 / 3$
C. $1 / 6$
D. 1

## Answer: B

6. The area of the region bonded by $y=e^{x}, y=e^{-x}, x=0$ and $\mathrm{x}=1$ is
(a) $e+\frac{1}{e}$ (b) $\log \left(\frac{4}{e}\right)$ (c) $4 \log \left(\frac{4}{e}\right)$ (d) $e+\frac{1}{e}-2$
A. $e+\frac{1}{e}$
B. $\log (4 / e)$
C. $4 \log (4 / e)$
D. $e+\frac{1}{e}-2$

## Answer: D

## - Watch Video Solution

7. The area bounded by the curve $y=\left|\cos ^{-1}(\sin x)\right|-\left|\sin ^{-1}(\cos x)\right|$ and axis from $\frac{3 \pi}{2} \leq x \leq 2 \pi$
A. $\pi^{2}$ sq. units
B. $\pi^{2} / 4$ sq. units
C. $\pi^{2} / 2$ sq. units
D. none of these

## Answer: B

## - Watch Video Solution

8. If $(a, 0)$, agt 0 , is the point where the curve $y=\sin 2 x-\sqrt{3} \sin x$ cuts the x -axis first, A is the area bounded by this part of the curve, the origin and the positive $x$-axis. Then
A. $4 A+8 \cos a=7$
B. $4+8 \sin a=7$
C. $4 A-8 \sin a=7$
D. $4 A-8 \cos a=7$

## Answer: A

9. The area in the first quadrant between $x^{2}+y^{2}=\pi^{2}$ and $y=\sin x$ is
(a) $\frac{\left(\pi^{3}-8\right)}{4}$
(b) $\frac{\pi^{3}}{4}$
(c) $\frac{\left(\pi^{3}-16\right)}{4}$
(d) $\frac{\left(\pi^{3}-8\right)}{2}$
A. $\frac{\left(\pi^{3}-8\right)}{4}$
B. $\frac{\pi^{3}}{4}$
C. $\frac{\left(\pi^{3}-16\right)}{4}$
D. $\frac{\left(\pi^{3}-8\right)}{2}$

## Answer: A

## - Watch Video Solution

10. The area bounded by the curves $y=\cos ^{-1} x, y=\sin ^{-1} x$ and $y=-\pi x^{3}$, where $-1 \leq x \leq 1$,is
A. $\frac{3 \pi}{2}+1-\sqrt{2}$ sq. units
B. $\frac{3 \pi}{4}+1+\sqrt{2}$ sq. units
C. $\frac{3 \pi}{4}+2-\sqrt{2}$ sq. units
D. $\frac{3 \pi}{4}+1-\sqrt{2}$ sq. units

## Answer: D

## - View Text Solution

11. The area bounded by the curve $y=\sin ^{2} x-2 \sin x$ and the $x$-axis, where $x \in[0,2 \pi]$, is
A. 4 sq. units
B. 8 sq. units
C. 16 sq. units
D. 20 sq. units

## Answer: B

12. Consider the functions $\mathrm{f}(\mathrm{x})$ and $\mathrm{g}(\mathrm{x})$, both defined from $R \rightarrow R$ and are defined as $f(x)=2 x-x^{2}$ and $g(x)=x^{n}$ where $n \in N$. If the area between $f(x)$ and $g(x)$ is $1 / 2$, then the value of $n$ is
A. 5
B. 6
C. 7
D. 8

## Answer: A

## - Watch Video Solution

13. Let a function $f(x)$ be defined in $[-2,2]$ as
$f(x)=\left\{\begin{array}{ll}\{x\}, & -2 \leq x<-1 \\ |\operatorname{sgn} x|, & -1 \leq x \leq 1 \\ \{-x\}, & 1<x \leq 2\end{array}\right.$ where $\{x\}$ and $\operatorname{sgn} x$ denote
fractional part and signum functions, respectively. Then find the area bounded by the graph of $f(x)$ an the $x$-axis.
A. 2 sq. units
B. 3 sq. units
C. 4 sq. units
D. 5 sq. units

## Answer: B

## D Watch Video Solution

14. The area bounded by $y=x^{2}+2$ and $y=2|x|-\cos \pi x$ is equal to
A. $2 / 3$
B. $8 / 3$
C. $4 / 3$
D. $1 / 3$

## Answer: B

15. Area bounded by $f(x)=\frac{x^{2}-1}{x^{2}+1}$ and the line $y=1$ is
A. $\pi$ sq. units
B. $2 \pi$ sq. units
C. $\pi / 2$ sq. units
D. none of these

## Answer: B

## Watch Video Solution

16. The area bounded by the curve $y=x e^{-x} ; x y=0$ and $x=c$ where c is the $x$-coordinate of the curve's inflection point, is
A. $1-3 e^{-2}$
B. $1-2 e^{-2}$
C. $1-e^{-2}$
D. none of these

## Answer: A

## - Watch Video Solution

17. Area of region bounded by the curve $y=\frac{16-x^{2}}{4}$ and $y=\sec ^{-1}\left[-\sin ^{2} x\right]$ (where $[\mathrm{x}]$ denotes the greatest ingeger function) is
A. $\frac{1}{3}(4-\pi)^{3 / 2}$
B. $8(4-\pi)^{3 / 2}$
C. $\frac{8}{3}(4-\pi)^{3 / 2}$
D. $\frac{8}{3}(4-\pi)^{1 / 2}$

## Answer: C

18. Suppose $y=f(x)$ and $y=g(x)$ are two continuous functiond whose graphs intersect at the three points $(0,4),(2,2)$ and $(4,0)$ with $f(x)>g(x)$ for $0<x<2$ and $f(x)<g(x)$ for $2<x<4$. If $\int_{0}^{4}[f(x)-g(x)] d x=10$ and $\int_{2}^{4}[g(x)-f(x)] d x=5 \quad$ the $\quad$ area between two curves for $0<x<2$,is (A) 5 (B) 10 (C) 15 (D) 20
A. 5
B. 10
C. 15
D. 20

## Answer: C

## - Watch Video Solution

19. The ratio of the areas of two regions of the curve $C_{1} \equiv 4 x^{2}+\pi^{2} y^{2}=4 \pi^{2} \quad$ divided by the
$C_{2} \equiv y=-\left(\operatorname{sgn}\left(x-\frac{\pi}{2}\right)\right) \cos x$ (where $\left.\operatorname{sgn}(\mathrm{x})=\operatorname{signum}(\mathrm{x})\right)$ is
A. $\frac{\pi^{2}-2}{\pi^{2}-2 \sqrt{2}}$
B. $\frac{\pi^{2}+2}{\pi^{2}-2 \sqrt{2}}$
C. $\frac{\pi^{2}+6}{\pi^{2}+3 \sqrt{2}}$
D. $\frac{\pi^{2}-1}{\pi^{2}-\sqrt{2}}$

## Answer: A

## - Watch Video Solution

20. The area bounded by the curves

$$
x \sqrt{3}+y=2 \log _{e}(x-y \sqrt{3})-2 \log _{e} 2, y=\sqrt{3} x
$$

$y=-\frac{1}{\sqrt{3}} x+2$, is
A. $2 \log _{e} 2$ sq. units
B. $2 \log _{e} 2+1$ sq. units
C. $2 \log _{e} 2-1$ sq. units
D. $4 \log _{e} 2-1$ sq. units

## - Watch Video Solution

21. Area of region bounded by the curve $y=\frac{4-x^{2}}{4+x^{2}}, 25 y^{2}=9 x$ and $y=\frac{3}{5}|x|-\frac{6}{5}$ which contains (1,0) point in its interior is
A. $\left\{\pi-4 \tan ^{-1} \cdot \frac{1}{2}+\frac{1}{10}\right\}$ sq. units
B. $\left\{\pi-2 \tan ^{-1} \cdot \frac{1}{2}-\frac{1}{5}\right\}$ sq. units
C. $\left\{\pi+4 \tan ^{-1} \cdot \frac{1}{2}-\frac{1}{5}\right\}$ sq. units
D. none of these

## Answer: A

## D Watch Video Solution

22. Area bounded by the $\min .\{|x|,|y|\}=1$ and the max. $\{|x|,|y|\}=2$ is
A. 4
B. 8
C. 16
D. 9

## Answer: A

## - Watch Video Solution

23. Consider $f(x)=\left\{\begin{array}{ll}\cos x & 0 \leq x<\frac{\pi}{2} \\ \left(\frac{\pi}{2}-x\right)^{2} & \frac{\pi}{2} \leq x<\pi\end{array}\right.$ such that f is periodic with period $\pi$. Then which of the following is not true?
A. The range of f is $\left[0, \frac{\pi^{2}}{4}\right)$.
B. $f$ is discontinuous for infinite values of $x$.
C. The area bounded by $y=f(x)$ and the $X$-axis from $x=0$ to $x=n \pi$ is $n\left(1+\frac{\pi^{3}}{24}\right)$ for a given $n \in N$.
D. none of these

## - Watch Video Solution

24. The area made by curve $f(x)=[x]+\sqrt{x-[x]}$ and $x$-axis when $0 \leq x \leq n(n \in N)$ is equal to $\{$ where $[\mathrm{x}]$ is greatest integer function\}
A. $\frac{2 n}{3}+\frac{n(n+1)}{2}$
B. $\frac{n}{3}+\frac{n(n+1)}{2}$
C. $\frac{2 n}{3}+\frac{n(n-1)}{2}$
D. $\frac{n}{3}+\frac{n(n-1)}{2}$

## Answer: C

## D View Text Solution

25. 

the
regions
$A=\left\{(x, y) \mid x^{2}+y^{2} \leq 100\right\}$ and $B=\left\lvert\, \begin{array}{ll}x \quad y \mid \sin (x+y)>0\} & \text { in the }\end{array}\right.$
plane. Then the area of the region $A \cap B$ is
A. $10 \pi$
B. 100
C. $100 \pi$
D. $50 \pi$

## Answer: D

## - Watch Video Solution

26. Let $R$ be the region containing the point ( $x, y$ ) on the $X-Y$ plane, satisfying $2 \leq|x+3 y|+|x-y| \leq 4$. Then the area of this region is
A. 5 sq. units
B. 6 sq. units
C. 7 sq. units
D. 8 sq. units

## - Watch Video Solution

27. If $f(x)=\left\{\begin{array}{ll}\sqrt{\{x\}} & \text { for } x \not \subset Z \\ 1 & \text { for } x \in Z\end{array}\right.$ and $g(x)=\{x\}^{2}$ where \{.\} denotes fractional part of x then area bounded by $\mathrm{f}(\mathrm{x})$ and $\mathrm{g}(\mathrm{x})$ for $x \in 0,6$ is
A. $\frac{2}{3}$
B. 2
C. $\frac{10}{3}$
D. 6

## Answer: B

## - Watch Video Solution

28. Let $S$ is the region of points which satisfies
$y^{2}<16 x, x<4$ and $\frac{x y\left(x^{2}-3 x+2\right)}{x^{2}-7 x+12}>0$. Its area is
A. $\frac{8}{3}$
B. $\frac{64}{3}$
C. $\frac{32}{3}$
D. none of these

## Answer: B

## - Watch Video Solution

29. The area of the region $\left\{(x, y): x^{2}+y^{2} \leq 5,||x|-|y|| \geq 1\right.$ is
A. $4\left(\pi-\tan ^{-1}\left(\frac{24}{7}\right)\right)-4$
B. $5\left(\pi-\tan ^{-1}\left(\frac{24}{7}\right)\right)-4$
C. $3\left(\pi-\tan ^{-1}\left(\frac{24}{7}\right)\right)-4$
D. $2\left(\pi-\tan ^{-1}\left(\frac{24}{7}\right)\right)-1$

## Answer: B

## - Watch Video Solution

30. The folloiwng figure shows the graph of a continuous function $y=f(x)$ on the interval $[1,3]$. The points $\mathrm{A}, \mathrm{B}, \mathrm{C}$ have coordinates $(1,1),(3,2),(2,3)$, respectively, and the lines $L_{1}$ and $L_{2}$ are parrallel, with $L_{1}$ being tangent to the curve at $C$. If the area under the graph of $y=f(x)$ from $x=1$ to $x=3$ is 4 square units, then the area of the shaded region is
A. 1
B. 2
C. 3
D. 4

## Answer: B

## (D) Watch Video Solution

## Multiple Correct Answer Type

1. If the area of bounded between the $x$-axis and the graph of $y=6 x-3 x^{2}$ between the ordinates $x=1 a n d x=a$ is 19 units, then $a$ can take the value 4 or -2 two value are in $(2,3)$ and one in $(-1,0)$ two value are in $(3,4)$ and one in $(-2,-1)$ none of these
A. one value in $(2,3)$
B. one value in $(-2,-1)$
C. one value in $(-1,0)$
D. one value in $(3,4)$

## Answer: B::D

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2. Which of the following is the possible value/values of c for which the area of the figure bounded by the curves $y=\sin 2 x$, the straight lines $x=\pi / 6, x=c$ and the abscissa axis is equal to $1 / 2$ ?
A. $-\frac{\pi}{6}$
B. $\frac{\pi}{3}$
C. $\frac{\pi}{6}$
D. none of these

## Answer: B

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3. Area of the region bounded by the curve $y=\tan x$ and lines $y=0$ and $x=1$ is
A. $\int_{0}^{1}$ and $(1-x) d x$
B. $\tan 1-\int_{0}^{\tan 1} \tan ^{-1} y d y$
C. $\int_{0}^{\tan 1} \tan ^{-1} y d y$
D. $\int_{0}^{1} \tan ^{-1} x d x$

## Answer: A: B

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## Comprehension Type

1. In the following figure, the graphs of two functions $y=f(x)$ and $y=\sin x$ are givne They intersect at origin, $A(a, f(a)), B(\pi, 0)$ and $C(2 \pi, 0) \cdot A_{i}(i=1,2,3)$ is the area bounded by the curves as shown in the figure, respectively, for $x \in(0, a), x \in(a, \pi), x \in(\pi, 2 \pi)$.

If $A_{1}=1+(a-1) \cos a-\sin$ a, then

The function $f(x)$ is
A. $x^{2} \sin x$
B. $x \sin x$
C. $2 x \sin x$
D. $x^{3} \sin x$

## Answer: B

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2. In the following figure, the graphs of two functions $y=f(x)$ and $y=\sin x$ are givne. They intersect at origin, $A(a, f(a)), B(\pi, 0)$ and $C(2 \pi, 0) \cdot A_{i}(i=1,2,3)$ is the area bounded by the curves as shown in the figure, respectively, for $x \in(0, a), x \in(a, \pi), x \in(\pi, 2 \pi)$. If $A_{1}=1+(a-1) \cos a-\sin$ a, then

The function $f(x)$ is
A. $(\pi-1)$ units $^{2}$
B. $(\pi / 2-1)$ units $^{2}$
C. $(\pi-\sin 1-1)$ units $^{2}$
D. $\pi / 2$ units $^{2}$

## Answer: C

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