MATHS

BOOKS - CENGAGE MATHS (ENGLISH)

COMPLEX NUMBERS

Single correct Answer

1. The value of $\sum_{n=0}^{100} i^{n!}$ equals (where $i = \sqrt{-1}$)

A. -1

B. i

C. $2i + 95$

D. $97 + i$

Answer: C

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2. Suppose n is a natural number such that $\left|i + 2i^2 + 3i^3 + ... + ni^n\right| = 18\sqrt{2}$ where i is the square root of -1. Then n is

A. 9

B. 18

C. 36

D. 72

Answer: C

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3. Let $i = \sqrt{-1}$ Define a sequence of complex number by $z_1 = 0, z_{n+1} = \left(z_n\right)^2 + i$ for $n \geq 1$. In the complex plane, how far from the origin is z_{111}?

A. 1

B. 2

C. 3

D. 4

Answer: B

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4. The complex number, $z = \dfrac{\left(-\sqrt{3} + 3i\right)(1 - i)}{\left(3 + \sqrt{3}i\right)(i)\left(\sqrt{3} + \sqrt{3}i\right)}$

A. lies on real axis

B. lies on imaginary axis

C. lies in first quadrant

D. lies in second quadrant

Answer: B

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5. a, b, c are positive real numbers forming a G.P. ILf $ax^2 + 2bx + c = 0 and dx^2 + 2ex + f = 0$ have a common root, then prove that $d/a, e/b, f/c$ are in A.P.

A. $A.P.$

B. $G.P.$

C. $H.P.$

D. None of these

Answer: A

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6. The equation $Z^3 + iZ - 1 = 0$ has

A. three real roots

B. one real roots

C. no real roots

D. no real or complex roots

Answer: C

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7. If a, b are complex numbers and one of the roots of the equation $x^2 + ax + b = 0$ is purely real whereas the other is purely imaginery, and $a^2 - \bar{a}^2 = kb$, then k is

A. 2

B. 4

C. 6

D. 8

Answer: B

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8. If Z is a non-real complex number, then find the minimum value of $\left|\frac{Imz^5}{Im^5z}\right|$

A. -1

B. -2

C. -4

D. -5

Answer: C

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9. For any complex numbers z_1, z_2 and z_3, $z_3 Im\left(\overline{z_2 z_3}\right) + z_2 Im\left(\overline{z_3 z_1}\right) + z_1 Im\left(\overline{z_1 z_2}\right)$ is

A. 0

B. $z_1 + z_2 + z_3$

C. $z_1 z_2 z_3$

D. $\left(\frac{z_1 + z_2 + z_3}{z_1 z_2 z_3}\right)$

Answer: A

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10. The modulus and amplitude of $\frac{1 + 2i}{1 - (1 - i)^2}$ are

A. $\sqrt{2}$ and $\frac{\pi}{6}$

B. 1 and $\frac{\pi}{4}$

C. 1 and 0

D. 1 and $\frac{\pi}{3}$

Answer: C

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11. If the argument of $(z - a)(\bar{z} - b)$ is equal to that $\left(\left(\sqrt{3} + i\right)\frac{1 + \sqrt{3}i}{1 + i}\right)$ where a,b,c are two real number and z is the complex conjugate o the complex number z find the locus of z in the rgand diagram. Find the value of a and b so that locus becomes a circle having its centre at $\frac{1}{2}(3 + i)$

A. $(3, 2)$

B. $(2, 1)$

C. $(2, 3)$

D. $(2, 4)$

Answer: B

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12. If a complex number z satisfies $|z|^2 + \frac{4}{(|z|)^2} - 2\left(\frac{z}{\bar{z}} + \frac{\bar{z}}{z}\right) - 16 = 0$, then the maximum value of $|z|$ is

A. $\sqrt{6} + 1$

B. 4

C. $2 + \sqrt{6}$

D. 6

Answer: C

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13. If $\cos\alpha + \cos\beta + \cos\gamma = 0 = \sin\alpha + \sin\beta + \sin\gamma$, then $\frac{\sin 3\alpha + \sin 3\beta + \sin 3\gamma}{\sin(\alpha + \beta + \gamma)}$ is equal to

A. 1

B. -1

C. 3

D. -3

Answer: C

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14. The least value of $|z - 3 - 4i|^2 + |z + 2 - 7i|^2 + |z - 5 + 2i|^2$ occurs when z=

A. $1 + 3i$

B. $3 + 3i$

C. $3 + 4i$

D. None of these

Answer: D

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15. The roots of the equation $x^4 - 2x^2 + 4 = 0$ are the vertices of a

:

A. square inscribed in a circle of radius 2

B. rectangle inscribed in a circle of radius 2

C. square inscribed in a circle of radius $\sqrt{2}$

D. rectangle inscribed in a circle of radius $\sqrt{2}$

Answer: D

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16. If z_1, z_2 are complex numbers such that $Re\left(z_1\right) = \left|z_1 - 2\right|$, $Re\left(z_2\right) = \left|z_2 - 2\right|$ and $arg\left(z_1 - z_2\right) = \pi/3$, then $Im\left(z_1 + z_2\right) =$

A. $2/\sqrt{3}$

B. $4/\sqrt{3}$

C. $2/\sqrt{3}$

D. $\sqrt{3}$

Answer: B

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17. If $z = e^{\frac{2\pi i}{5}}$, then $1 + z + z^2 + z^3 + 5z^4 + 4z^5 + 4z^6 + 4z^7 + 4z^8 + 5z^9 =$

A. 0

B. $4z^3$

C. $5z^4$

D. $-4z^2$

Answer: C

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18. If $z = (3 + 7i)(a + ib)$, where $a, b \in Z - \{0\}$, is purely imaginery, then minimum value of $|z|^2$ is

A. 74

B. 45

C. 65

D. 58

Answer: D

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19. Let z be a complex number satisfying $|z + 16| = 4|z + 1|$. Then

A. $|z| = 4$

B. $|z| = 5$

C. $|z| = 6$

D. $3 < |z| < 68$

Answer: A

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20. If $|z| = 1$ and $z' = \frac{1 + z^2}{z}$, then

A. z' lie on a line not passing through origin

B. $|z'| = \sqrt{2}$

C. $Re(z') = 0$

D. $Im(z') = 0$

Answer: D

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21. a, b,c are three complex numbers on the unit circle $|z| = 1$, such that $abc = a + b + c$. Then $|ab + bc + ca|$ is equal to

A. 3

B. 6

C. 1

D. 2

Answer: C

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22. If $|z_1| = |z_2| = |z_3| = 1$ then value of $|z_1 - z_3|^2 + |z_3 - z_1|^2 + |z_1 - z_2|^2$ cannot exceed

A. 6

B. 9

C. 12

D. none of these

Answer: B

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23. Number of ordered pairs $(s), (a, b)$ of real numbers such that $(a + ib)^{2008} = a - ib$ holds good is

A. 2008

B. 2009

C. 2010

D. 1

Answer: C

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24. The region represented by the inequality |2z-3i|<|3z-2i| is

A. the unit disc with its centre at $z = 0$

B. the exterior of the unit circle with its centre at $z = 0$

C. the inerior of a square of side 2 units with its centre at

$z = 0$

D. none of these

Answer: B

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25. If ω is any complex number such that $z\omega = |z|^2$ and $|z - \bar{z}| + |\omega + \bar{\omega}| = 4$, then as ω varies, then the area bounded by the locus of z is

A. 4 sq. units

B. 8 sq. units

C. 16 sq. units

D. 12 sq. units

Answer: B

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26. If $az^2 + bz + 1 = 0$, where $a, b \in C$, $|a| = \frac{1}{2}$ and have a root α such that $|\alpha| = 1$ then $\left|a\bar{b} - b\right| =$

A. $1/4$

B. $1/2$

C. $5/4$

D. $3/4$

Answer: D

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27. Let p and q are complex numbers such that $|p| + |q| < 1$. If z_1 and z_2 are the roots of the $z^2 + pz + q = 0$, then which one of the following is correct ?

A. $\left|z_1\right| < 1$ and $\left|z_2\right| < 1$

B. $\left|z_1\right| > 1$ and $\left|z_2\right| > 1$

C. If $\left|z_1\right| < 1$, then $\left|z_2\right| > 1$ and vice versa

D. Nothing definite can be said

Answer: A

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28. If z and w are two complex numbers simultaneously satisfying the equations, $z^3 + w^5 = 0$ and $z^2 + \bar{w}^4 = 1$, then

A. z and w both are purely real

B. z is purely real and w is purely imaginery

C. w is purely real and z is purely imaginery

D. z and w both are imaginery

Answer: A

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29. All complex numbers 'z' which satisfy the relation $|z - |z + 1|| = |z + |z - 1|$ on the complex plane lie on the

A. $y = x$

B. $y = -x$

C. circle $x^2 + y^2 = 1$

D. line $x = 0$ or on a line segment joining $(-1, 0) \rightarrow (1,0)$`

Answer: D

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30. If z_1, z_2 are two complex numbers such that $\left|\frac{z_1 - z_2}{z_1 + z_2}\right| = 1$ and $iz_1 = Kz_2$, where $K \in R$, then the angle between $z_1 - z_2$ and $z_1 + z_2$ is

A. $\tan^{-1}\left(\frac{2K}{K^2 + 1}\right)$

B. $\tan^{-1}\left(\frac{2K}{1 - K^2}\right)$

C. $-2\tan^{-1}K$

D. $2\tan^{-1}K$

Answer: D

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31. If $z + \frac{1}{z} = 2\cos 6^\circ$, then $z^{1000} + \frac{1}{z^{1000}}$ +1 is equal to

A. 0

B. 1

C. -1

D. 2

Answer: A

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32. Let z_1 and z_2q, be two complex numbers with α and β as their principal arguments such that $\alpha + \beta$ then principal $arg\left(z_1 z_2\right)$ is given by:

A. $\alpha + \beta + \pi$

B. $\alpha + \beta - \pi$

C. $\alpha + \beta - 2\pi$

D. $\alpha + \beta$

Answer: C

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33. Let $arg\left(z_k\right) = \frac{(2k+1)\pi}{n}$ where $k = 1, 2, \ldots\ldots\ldots n.$ If $arg\left(z_1, z_2, z_3, \ldots\ldots\ldots\ldots z_n\right) = \pi$, then n must be of form $(m \in z)$

A. $4m$

B. $2m - 1$

C. $2m$

D. None of these

Answer: B

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34. Suppose two complex numbers $z = a + ib$, $w = c + id$ satisfy the equation $\frac{z + w}{z} = \frac{w}{z + w}$. Then

A. both a and c are zeros

B. both b and d are zeros

C. both b and d must be non zeros

D. at least one of b and d is non zero

Answer: D

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35. If $|z| = 1$ and $z \neq \pm 1$, then one of the possible value of $arg(z) - arg(z+1) - arg(z-1)$, is

A. $-\pi/6$

B. $\pi/3$

C. $-\pi/2$

D. $\pi/4$

Answer: C

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36. If $arg\left(z^{3/8}\right) = \frac{1}{2}arg\left(z^2 + \bar{z}^{1/2}\right)$, then which of the following is not possible ?

A. $|z| = 1$

B. $z = \bar{z}$

C. $arg(z) = 0$

D. None of these

Answer: D

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37. z_1, z_2 are two distinct points in complex plane such that $2|z_1| = 3|z_2|$ and $z \in C$ be any point $z = \frac{2z_1}{3z_2} + \frac{3z_2}{2z_1}$ such that

A. $-1 \leq Rez \leq 1$

B. $-2 \leq Rez \leq 2$

C. $-3 \leq Rez \leq 3$

D. None of these

Answer: B

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38. If $\alpha, \beta, \gamma \in \left\{1, \omega, \omega^2\right\}$ (where ω and ω^2 are imaginery cube roots of unity), then number of triplets (α, β, γ) such that $\left|\frac{a\alpha + b\beta + c\gamma}{a\beta + b\gamma + c\alpha}\right| = 1$ is

A. 3

B. 6

C. 9

D. 12

Answer: C

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39. The value of $\left(3\sqrt{3}+\left(3^{5/6}\right)i\right)^3$ is (where $i=\sqrt{-1}$)

A. 24

B. -24

C. -22

D. -21

Answer: B

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40. If $\omega \neq 1$ is a cube root of unity and $a+b=21$, $a^3+b^3=105$, then the value of $\left(a\omega^2+b\omega\right)\left(a\omega+b\omega^2\right)$ is be equal to

A. 3

B. 5

C. 7

D. 35

Answer: B

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41. If $z = \frac{1}{2}\left(\sqrt{3} - i\right)$, then the least possible integral value of m such that $\left(z^{101} + i^{109}\right)^{106} = z^{m+1}$ is

A. 11

B. 7

C. 8

D. 9

Answer: D

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42. If $y_1 = \max ||z - \omega| - |z - \omega^2| |$, where $|z| = 2$ and $y_2 = \max ||z - \omega| - |z - \omega^2| |$, where $|z| = \frac{1}{2}$ and ω and ω^2 are complex cube roots of unity, then

A. $y_1 = \sqrt{3}, y_2 = \sqrt{3}$

B. $y_1 < \sqrt{3}, y_2 = \sqrt{3}$

C. $y_1 = \sqrt{3}, y_2 < \sqrt{3}$

D. $y_1 > 3, y_2 < \sqrt{3}$

Answer: C

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43. Let I, ω and ω^2 be the cube roots of unity. The least possible degree of a polynomial, with real coefficients having $2\omega^2, 3 + 4\omega, 3 + 4\omega^2$ and $5 - \omega - \omega^2$ as roots is -

A. 4

B. 5

C. 6

D. 7

Answer: B

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44. Number of imaginary complex numbers satisfying the equation, $z^2 = \bar{z}2^{1-|z|}$ is

A. 0

B. 1

C. 2

D. 3

Answer: C

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45. Least positive argument ofthe 4th root ofthe complex number $2 - i\sqrt{12}$ is

A. $\pi/6$

B. $5\pi/12$

C. $7\pi/12$

D. $11\pi/12$

Answer: B

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46. A root of unity is a complex number that is a solution to the equation, $z^n = 1$ for some positive integer nNumber of roots of unity that are also the roots of the equation $z^2 + az + b = 0$, for some integer a and b is

A. 6

B. 8

C. 9

D. 10

Answer: B

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47. If z is a complex number satisfying the equation $z^6 + z^3 + 1 = 0$. If this equation has a root $re^{i\theta}$ with $90^\circ < 0 < 180^\circ$ then the value of θ is

A. 100°

B. 110°

C. 160°

D. 170°

Answer: C

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48. Suppose A is a complex number and $n \in N$, such that $A^n = (A+1)^n = 1$, then the least value of n is 3 b. 6 c. 9 d. 12

A. 3

B. 6

C. 9

D. 12

Answer: B

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49. If $z_1, z_2, z_3 \ldots\ldots\ldots\ldots z_n$ are in $G.P$ with first term as unity such that $z_1 + z_2 + z_3 + \ldots + z_n = 0$. Now if $z_1, z_2, z_3 \ldots\ldots\ldots z_n$

represents the vertices of n-polygon, then the distance between incentre and circumcentre of the polygon is

A. 0

B. $|z_1|$

C. $2|z_1|$

D. none of these

Answer: A

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50. If $|z - 1 - i| = 1$, then the locus of a point represented by the complex number $5(z - i) - 6$ is

A. circle with centre $(1, 0)$ and radius 3

B. circle with centre $(-1, 0)$ and radius 5

C. line passing through origin

D. line passing through $(-1, 0)$

Answer: B

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51. Let $z \in C$ and if $A = \left\{z : \arg(z) = \frac{\pi}{4}\right\}$ and $B = \left\{z : \arg(z - 3 - 3i) = \frac{2\pi}{3}\right\}$. Then $n(A \quad B) =$

A. 1

B. 2

C. 3

D. 0

Answer: D

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52. $\theta \in [0, 2\pi]$ and z_1, z_2, z_3 are three complex numbers such that they are collinear and $(1 + |\sin\theta|)z_1 + (|\cos\theta| - 1)z_2 - \sqrt{2}z_3 = 0$. If at least one of the complex numbers z_1, z_2, z_3 is nonzero, then number of possible values of θ is

A. Infinite

B. 4

C. 2

D. 8

Answer: B

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53. Let $'z'$ be a comlex number and $'a'$ be a real parameter such that $z^2 + az + a^2 = 0$, then which is of the following is not true ?

A. locus of z is a pair of straight lines

B. $|z| = |a|$

C. $arg(z) = \pm \frac{2\pi}{3}$

D. None of these

Answer: D

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54. Let $z = x + iy$. Then find the locus of $P(z)$ such that $\frac{1+z}{z} \in R$.

A. union of lines with equations $x = 0$ and $y = -1/2$but excluding origin.

B. union of lines with equations $x = 0$ and $y = 1/2$but excluding origin.

C. union of lines with equations $x = -1/2$ and $y = 0$but excluding origin.

D. union of lines with equations $x = 1/2$ and $y = 0$but excluding origin.

Answer: C

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55. Let $A(z_1)$ and $B(z_2)$ are two distinct non-real complex numbers in the argand plane such that $\frac{z_1}{z_2} + \frac{\bar{z}_1}{z_2} = 2$. The value of

$|\angle ABO|$ is

A. $\frac{\pi}{6}$

B. $\frac{\pi}{4}$

C. $\frac{\pi}{2}$

D. None of these

Answer: C

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56. Complex numbers z_1 and z_2 satisfy $|z_1| = 2$ and $|z_2| = 3$. If the included angle of their corresponding vectors is 60°, then the value of $19\left|\frac{z_1 - z_2}{z_1 + z_2}\right|^2$ is

A. 5

B. 6

C. 7

D. 8

Answer: C

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57. Let $A(2, 0)$ and $B(z)$ are two points on the circle $|z| = 2$. $M(z')$ is the point on AB. If the point $\bar{z}'$ lies on the median of the triangle OAB where O is origin, then $arg(z')$ is

A. $\tan^{-1}\left(\frac{\sqrt{15}}{5}\right)$

B. $\tan^{-1}\left(\sqrt{15}\right)$

C. $\tan^{-1}\left(\frac{5}{\sqrt{15}}\right)$

D. $\frac{\pi}{2}$

Answer: A

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58. If $A(z_1)$, $B(z_2)$, $C(z_3)$ are vertices of a triangle such that $z_3 = \frac{z_2 - iz_1}{1 - i}$ and $|z_1| = 3$, $|z_2| = 4$ and $|z_2 + iz_1| = |z_1| + |z_2|$, then area of triangle ABC is

A. $\frac{5}{2}$

B. 0

C. $\frac{25}{2}$

D. $\frac{25}{4}$

Answer: D

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59. Let O, A, B be three collinear points such that $OA.OB = 1$. If O and B represent the complex numbers O and z, then A represents

A. $\frac{1}{\bar{z}}$

B. $\frac{1}{z}$

C. $\bar{z}$

D. z^2

Answer: A

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60. If the tangents at z_1, z_2 on the circle $|z - z_0| = r$ intersect at z_3, then $\frac{(z_3 - z_1)(z_0 - z_2)}{(z_0 - z_1)(z_3 - z_2)}$ equals

A. 1

B. -1

C. i

D. $-i$

Answer: B

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61. If z_1, z_2 and z_3 are the vertices of ΔABC, which is not right angled triangle taken in anti-clock wise direction and z_0 is the

circumcentre, then $\left(\frac{z_0 - z_1}{z_0 - z_2}\right)\frac{\sin 2A}{\sin 2B} + \left(\frac{z_0 - z_3}{z_0 - z_2}\right)\frac{\sin 2C}{\sin 2B}$ is equal to

A. 0

B. 1

C. -1

D. 2

Answer: C

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62. Let P denotes a complex number $z = r(\cos\theta + i\sin\theta)$ on the Argand's plane, and Q denotes a complex number $\sqrt{2|z|^2}\left(\cos\left(\theta + \frac{\pi}{4}\right) + i\sin\left(\theta + \frac{\pi}{4}\right)\right)$. If $'O'$ is the origin, then ΔOPQ is

A. isosceles but not right angled

B. right angled but not isosceles

C. right isosceles

D. equilateral

Answer: C

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Multiple Correct Answer

1. Complex numbers whose real and imaginary parts x and y are integers and satisfy the equation $3x^2 - |xy| - 2y^2 + 7 = 0$

A. do not exist

B. exist and have equal modulus

C. form two conjugate pairs

D. do not form conjugate pairs

Answer: B::C

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2. If $a, b, c, d \in R$ and all the three roots of $az^3 + bz^2 + cZ + d = 0$ have negative real parts, then

A. $ab > 0$

B. $bc > 0$

C. $ad > 0$

D. $bc - ad > 0$

Answer: A::B::C

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3. Suppose three real numbers a, b, c are in $G.P.$ Let $z = \frac{a + ib}{c - ib}$.

Then

A. $z = \frac{ib}{c}$

B. $z = \frac{ia}{b}$

C. $z = \frac{ia}{c}$

D. $z = 0$

Answer: A::B

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4. w_1, w_2 be roots of $(a + \bar{c})z^2 + (b + \bar{b})z + (\bar{a} + c) = 0$. If $|z_1| < 1, |z_2| < 1$, then

A. $\left|w_1\right| < 1$

B. $\left|w_1\right| = 1$

C. $\left|w_2\right| < 1$

D. $\left|w_2\right| = 1$

Answer: B::D

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5. A complex number z satisfies the equation $\left|Z^2 - 9\right| + \left|Z^2\right| = 41$, then the true statements among the following are

A. $|Z + 3| + |Z - 3| = 10$

B. $|Z + 3| + |Z - 3| = 8$

C. Maximum value of $|Z|$ is 5

D. Maximum value of $|Z|$ is 6

Answer: A::C

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6. Let a, b, c be distinct complex numbers with $|a| = |b| = |c| = 1$ and z_1, z_2 be the roots of the equation $az^2 + bz + c = 0$ with $\left|z_1\right| = 1$. Let P and Q represent the complex numbers z_1 and z_2 in the Argand plane with $\angle POQ = \theta, o^\circ < 180^\circ$ (where O being the origin).Then

A. $b^2 = ac, \theta = \frac{2\pi}{3}$

B. $\theta = \frac{2\pi}{3}, PQ = \sqrt{3}$

C. $PQ = 2\sqrt{3}, b^2 = ac$

D. $\theta = \frac{\pi}{3}, b^2 = ac$

Answer: A::B

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7. Let $Z_1 = x_1 + iy_1$, $Z_2 = x_2 + iy_2$ be complex numbers in fourth quadrant of argand plane and $|Z_1| = |Z_2| = 1$, $Ref(Z_1Z_2) = 0$. The complex numbers $Z_3 = x_1 + ix_2$, $Z_4 = y_1 + iy_2$, $Z_5 = x_1 + iy_2$, $Z_6 = x_6 + iy$, will always satisfy

A. $|Z_4| = 1$

B. $arg(Z_1Z_4) = -\pi/2$

C. $\dfrac{Z_5}{\cos(argZ_1)} + \dfrac{Z_6}{\sin(argZ_1)}$ is purely real

D. $Z_5^2 + (\bar{Z}_6)^2$ is purely imaginergy

Answer: A::B::C::D

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8. If the imaginery part of $\frac{z-3}{e^{i\theta}} + \frac{e^{i\theta}}{z-3}$ is zero, then z can lie on

A. a circle with unit radius

B. a circle with radius 3 units

C. a straight line through the point $(3, 0)$

D. a parabola with the vertex $(3, 0)$

Answer: A::C

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9. If α Is the fifth root of unity, then :

A. $\left|1 + \alpha + \alpha^2 + \alpha^3 + \alpha^4\right| = 0$

B. $\left|1+\alpha+\alpha^2+\alpha^3\right| = 1$

C. $\left|1+\alpha+\alpha^2\right| = 2\cos\frac{\pi}{5}$

D. $|1+\alpha| = 2\cos\frac{\pi}{10}$

Answer: A::B::C

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10. If z_1, z_2, z_3 are any three roots of the equation $z^6 = (z+1)^6$, then $arg\left(\frac{z_1 - z_3}{z_2 - z_3}\right)$ can be equal to

A. 0

B. π

C. $\frac{\pi}{4}$

D. $-\frac{\pi}{4}$

Answer: A::B

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11. Let z_1, z_2, z_3 are the vertices of ΔABC, respectively, such that $\frac{z_3 - z_2}{z_1 - z_2}$ is purely imaginery number. A square on side AC is drawn outwardly. $P\left(z_4\right)$ is the centre of square, then

A. $\left|z_1 - z_2\right| = \left|z_2 - z_4\right|$

B. $arg\left(\frac{z_1 - z_2}{z_4 - z_2}\right) + arg\left(\frac{z_3 - z_2}{z_4 - z_2}\right) = +\frac{\pi}{2}$

C. $arg\left(\frac{z_1 - z_2}{z_4 - z_2}\right) + arg\left(\frac{z_3 - z_2}{z_4 - z_2}\right) = 0$

D. z_1, z_2, z_3 and z_4 lie on a circle

Answer: C::D

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Comprehension

1. Consider the region R in the Argand plane described by the complex number. Z satisfying the inequalities $|Z - 2| \leq |Z - 4|$, $|Z - 3| \leq |Z + 3|$, $|Z - i| \leq |Z - 3i|$, $|Z + i| \leq |Z + 3i|$

Answer the followin questions :

The maximum value of $|Z|$ for any Z in R is

A. 5

B. 3

C. 1

D. $\sqrt{13}$

Answer: D

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2. Consider the region R in the Argand plane described by the complex number. Z satisfying the inequalities $|Z - 2| \leq |Z - 4|$, $|Z - 3| \leq |Z + 3|$, $|Z - i| \leq |Z - 3i|$, $|Z + i| \leq |Z + 3i|$

Answer the followin questions :

The maximum value of $|Z|$ for any Z in R is

A. 5

B. 14

C. $\sqrt{13}$

D. 12

Answer: A

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3. Consider the region R in the Argand plane described by the complex number. Z satisfying the inequalities $|Z - 2| \leq |Z - 4|$, $|Z - 3| \leq |Z + 3|$, $|Z - i| \leq |Z - 3i|$, $|Z + i| \leq |Z + 3i|$

Answer the followin questions :

Minimum of $\left|Z_1 - Z_2\right|$ given that Z_1, Z_2 are any two complex numbers lying in the region R is

A. 0

B. 5

C. $\sqrt{13}$

D. 3

Answer: A

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4. Let z_1 and z_2 be complex numbers such that $z_1^2 - 4z_2 = 16 + 20i$ and the roots α and β of $x^2 + z_1x + z_2 + m = 0$ for some complex number m satisfies $|\alpha - \beta| = 2\sqrt{7}$.

The locus of the complex number m is a curve

A. straight line

B. circle

C. ellipse

D. hyperbola

Answer: B

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5. Let z_1 and z_2 be complex numbers such that $z_1^2 - 4z_2 = 16 + 20i$ and the roots α and β of $x^2 + z_1x + z_2 + m = 0$ for some complex

number m satisfies $|\alpha - \beta| = 2\sqrt{7}$. The value of $|m|$,

A. 14

B. $2\sqrt{7}$

C. $7 + \sqrt{41}$

D. $2\sqrt{6} - 4$

Answer: C

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6. Let z_1 and z_2 be complex numbers such that $z_1^2 - 4z_2 = 16 + 20i$ and the roots α and β of $x^2 + z_1x + z_2 + m = 0$ for some complex number m satisfies $|\alpha - \beta| = 2\sqrt{7}$. The value of $|m|$,

A. 7

B. $28 - \sqrt{41}$

C. $\sqrt{41}$

D. $2\sqrt{6} - 4$

Answer: D

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7. The locus of any point $P(z)$ on argand plane is

$$arg\left(\frac{z - 5i}{z + 5i}\right) = \frac{\pi}{4}.$$

Then the length of the arc described by the locus of $P(z)$ is

A. $10\sqrt{2}\pi$

B. $\frac{15\pi}{\sqrt{2}}$

C. $\frac{5\pi}{\sqrt{2}}$

D. $5\sqrt{2}\pi$

Answer: B

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8. The locus of any point $P(z)$ on argand plane is $arg\left(\frac{z - 5i}{z + 5i}\right) = \frac{\pi}{4}$.

Total number of integral points inside the region bounded by the locus of $P(z)$ and imaginery axis on the argand plane is

A. 62

B. 74

C. 136

D. 138

Answer: C

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9. The locus of any point $P(z)$ on argand plane is

$$arg\left(\frac{z - 5i}{z + 5i}\right) = \frac{\pi}{4}.$$

Area of the region bounded by the locus of a complex number Z

satisfying $arg\left(\frac{z + 5i}{z - 5i}\right) = \pm\frac{\pi}{4}$

A. $75\pi + 50$

B. 75π

C. $\frac{75\pi}{2} + 25$

D. $\frac{75\pi}{2}$

Answer: A

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10. A person walks $2\sqrt{2}$ units away from origin in south west direction $\left(S45^{\circ}W\right)$ to reach A, then walks $\sqrt{2}$ units in south east direction $\left(S45^{\circ}E\right)$ to reach B. From B he travel is 4 units horizontally towards east to reach C. Then he travels along a circular path with centre at origin through an angle of $2\pi/3$ in anti-clockwise direction to reach his destination D.

Position of D in argand plane is (w is an imaginary cube root of unity)

A. $-\frac{\pi}{6}$

B. $\frac{\pi}{4}$

C. $-\frac{\pi}{4}$

D. $\frac{\pi}{3}$

Answer: C

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11. A person walks $2\sqrt{2}$ units away from origin in south west direction $\left(S45^\circ W\right)$ to reach A, then walks $\sqrt{2}$ units in south east direction $\left(S45^\circ E\right)$ to reach B. From B he travel is 4 units horizontally towards east to reach C. Then he travels along a circular path with centre at origin through an angle of $2\pi/3$ in anti-clockwise direction to reach his destination D.

Position of D in argand plane is (w is an imaginary cube root of unity)

A. $(3 + i)\omega$

B. $-(1 + i)\omega^2$

C. $3(1 - i)\omega$

D. $(1 - 3i)\omega$

Answer: C

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ILLUSTRATION

1. Evaluate :

(i) i^{135}

(ii) i^{-47}

(iii) $\left(-\sqrt{-1}\right)^{4n+3}, n \in N$

(iv) $\sqrt{-25} + 3\sqrt{-4} + 2\sqrt{-9}$

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2. Find the value of $i^n + i^{n+1} + i^{n+2} + i^{n+3}$ for all $n \in N$.

A. 0

B. i

C. $-i$

D. $2i^n$

Answer: A

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3. Find the value of $1 + i^2 + i^4 + i^6 + \ + i^{2n}$

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4. Show that the polynomial $x^{4p} + x^{4q+1} + x^{4r+2} + x^{4s+3}$ is divisible by $x^3 + x^2 + x + 1, wherep, q, r, s \in n$.

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5. Solve:

$ix^2 - 3x - 2i = 0,$

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6. If $z = 4 + i\sqrt{7}$, then find the value of $z^2 - 4z^2 - 9z + 91$.

A. 23

B. i

C. -1

D. 0

Answer: C

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7. Express each of the following in the standerd from $a + ib$

(i) $\frac{5 + 4i}{4 + 5i}$ (ii) $\frac{(1 + i)^2}{3 - i}$ (iii) $\frac{1}{1 - \cos\theta + 2i\sin\theta}$

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8. The root of the equation $2(1 + i)x^2 - 4(2 - i)x - 5 - 3i = 0$, where $i = \sqrt{-1}$, which has greater modulus is

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9. Find the value of $(1 + i)^6 + (1 - i)^6$

A. $16i$

B. 0

C. $-16i$

D. 1

Answer: B

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10. If $\left(\frac{1+i}{1-i}\right)^m = 1,$ then find the least positive integral value of m.

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11. Prove that the triangle formed by the points $1, \frac{1+i}{\sqrt{2}}, andi$ as vertices in the Argand diagram is isosceles.

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12. Find real q such that $\frac{3+2i\sin\theta}{1-2i\sin\theta}$ is purely real.

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13. If the imaginary part of $(2z+1)/(iz+1)$ is -2, then find the locus of the point representing in the complex plane.

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14. If z is a complex number such that $|z-\bar{z}|+|z+\bar{z}|=4$ then find the area bounded by the locus of z.

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15. If $(x+iy)^5=p+iq,$ then prove that $(y+ix)^5=q+ip$

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16. If z = x + iy lies in the third quadrant, then prove that $\frac{\bar{z}}{z}$ also lies in the third quadrant when $y < x < 0$

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17. Let $z = \left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^5 + \left(\frac{\sqrt{3}}{2} - \frac{i}{2}\right)^5$. If R(z) and I(z), respectively, denote the real and imaginary parts of z, then

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18. Find the relation if z_1, z_2, z_3, z_4 are the affixes of the vertices of a parallelogram taken in order.

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19. Let z_1, z_2, z_3 be three complex numbers and a, b, c be real numbers not all zero, such that $a + b + c = 0 and a z_1 + b z_2 + c z_3 = 0$. Show that z_1, z_2, z_3 are collinear.

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20. Find real values of x and y for which the complex numbers $-3 + ix^2y$ and $x^2 + y + 4i$ are conjugate of each other.

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21. about to only mathematics

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22. If $(x + iy)^3 = u + iv$, then show that $\frac{u}{x} + \frac{v}{y} = 4\left(x^2 - y^2\right)$.

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23. Let z be a complex number satisfying the equation $z^2 - (3 + i)z + m + 2i = 0, wherem \in R$. Suppose the equation has a real root. Then find non-real root.

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24. Show that the equation $Z^4 + 2Z^3 + 3Z^2 + 4Z + 5 = 0$ has no root which is either purely real or purely imaginary.

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25. Find the square root of the following: $5 + 12i$

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26. Find all possible values of $\sqrt{i} + \sqrt{-i}$.

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27. Solve for $z: z^2 - (3 - 2i)z = (5i - 5)$

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28. Solve the equation $(x - 1)^3 + 8 = 0$ in the set C of all complex numbers.

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29. If n is n odd integer that is greater than or equal to 3 but not a multiple of 3, then prove that $(x+1)^n - x^n - 1$ is divisible by $x^3 + x^2 + x$.

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30. ω is an imaginary root of unity.

Prove that

If $a + b + c = 0$ then prove that $\left(a + b\omega + c\omega^2\right)^3 + \left(a + b\omega^2 + c\omega\right)^3 = 27abc.$

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31. Find the complex number ω satisfying the equation $z^3 = 8i$ and lying in the second quadrant on the complex plane.

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32. $\frac{1}{a+\omega} + \frac{1}{b+\omega} + \frac{1}{c+\omega} + \frac{1}{d+\omega} = \frac{1}{\omega}$ where, a,b,c,d, $\in$ R and ω is a complex cube root of unity then find the value of $\sum \frac{1}{a^2 - a + 1}$

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33. Write the following complex number in polar form :

$-3\sqrt{2} + 3\sqrt{2}i$

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34. Let $z_1 = \cos 12^\circ + I\sin 12^\circ$ and $z_2 = \cos 48^\circ + i.\sin 48^\circ$. Write complex number $\left(z_1 + z_2\right)$ in polar form. Find its modulus and argument.

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35. Covert the complex number $z = 1 + \frac{\cos(8\pi)}{5} + i.\frac{\sin(8\pi)}{5}$ in polar form. Find its modulus and argument.

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36. Let z and w be two nonzero complex numbers such that $|z| = |w|$ and $arg(z) + arg(w) = \pi$. Then prove that $z = -\bar{w}$.

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37. Find nonzero integral solutions of $|1 - i|^x = 2^x$.

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38. Let z be a complex number satisfying $|z| = 3|z - 1|$. Then prove that $\left|z - \frac{9}{8}\right| = \frac{3}{8}$

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39. If complex number z=x +iy satisfies the equation $Re(z + 1) = |z - 1|$, then prove that z lies on $y^2 = 4x$.

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40. Solve the equation $|z| = z + 1 + 2i$.

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41. Find the range of real number α for which the equation $z + \alpha|z - 1| + 2i = 0$ has a solution.

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42. Find the Area bounded by complex numbers $arg|z| \leq \frac{\pi}{4}$ and $|z - 1| < |z - 3|$

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43. Prove that traingle by complex numbers z_1, z_2 and z_3 is equilateral if $\left|z_1\right| = \left|z_2\right| = \left|z_3\right|$ and $z_1 + z_2 + z_3 = 0$

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44. Show that $e^{2mi\theta}\left(\frac{i\cot\theta + 1}{i\cot\theta - 1}\right)^m = 1.$

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45. $Z_1 \neq Z_2$ are two points in an Argand plane. If $a\left|Z_1\right| = b\left|Z_2\right|$, then prove that $\frac{aZ_1 - bZ_2}{aZ_1 + bZ_2}$ is purely imaginary.

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46. Find the real part of $(1 - i)^{-i}$

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47. If $\left(\sqrt{8}+i\right)^{50}=3^{49}(a+ib)$, then find the value of a^2+b^2.

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48. Show that $\left(x^2+y^2\right)^4=\left(x^4-6x^2y^2+y^4\right)^2+\left(4x^3y-4xy^3\right)^2$.

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49. If $arg\left(z_1\right)=170^0 and arg\left(z_2\right)70^0$, then find the principal argument of z_1z_2.

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50. Find the value of expression

$$\left(\cos\left(\frac{\pi}{2}\right)+i\sin\left(\frac{\pi}{2}\right)\right)\left(\cos\left(\frac{\pi}{2^2}\right)+i\sin\left(\frac{\pi}{2^2}\right)\right)\ldots\ldots\infty$$

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51. Find the principal argument of the complex number

$$\frac{(1+i)^5\left(1+\sqrt{3}i\right)^2}{-1i\left(-\sqrt{3}+i\right)}$$

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52. If $z=\frac{\left(\sqrt{3}+i\right)^{17}}{(1-i)^{50}}$, then find $amp(z)$.

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53. If $z = x + iy$ and $w = \frac{1 - iz}{z - i}$, show that $|w| = 1z$ is purely real.

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54. It is given the complex numbers z_1 and z_2, $\left|z_1\right| = 2$ and $\left|z_2\right| = 3$. If the included angle of their corresponding vectors is 60°, then find value of $\left|\frac{z_1 + z_2}{z_1 - z_2}\right|$

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55. Solve the equation $z^3 = \bar{z}(z \neq 0)$

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56. If $2z_1/3z_2$ is a purely imaginary number, then find the value of

$$\left|\left(z_1 - z_2\right)/\left(z_1 + z_2\right)\right|$$

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57. Find the complex number satisfying the system of equations

$z^3 + \omega^7 = 0 and z^5\omega^{11} = 1.$

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58. Express the following in $a + ib$ form:

(i) $\left(\frac{\cos\theta + i\sin\theta}{\sin\theta + i\cos\theta}\right)^4$

(ii) $\frac{(\cos 2\theta - i\sin 2\theta)^4(\cos 4\theta + i\sin 4\theta)^{-5}}{(\cos 3\theta + i\sin 3\theta)^{-2}(\cos 3\theta - i\sin 3\theta)^{-9}}$

(iii) $\frac{(\sin\pi/8 + i\cos\pi/8)^8}{(\sin\pi/8 - i\cos\pi/8)^8}$

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59. Let $z = \left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^5 + \left(\frac{\sqrt{3}}{2} - \frac{i}{2}\right)^5$. If R(z) and I(z), respectively, denote the real and imaginary parts of z, then

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60. Prove that the roots of the equation $x^4 - 2x^2 + 4 = 0$ forms a rectangle.

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61. If $z + 1/z = 2\cos\theta$, prove that $\left|\left(z^{2n} - 1\right)/\left(z^{2n} + 1\right)\right| = |\tan n\theta|$

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62. If $z = x + iy$ is a complex number with $x, y \in Q and |z| = 1$, then show that $\left|z^{2n} - 1\right|$ is a rational number for every $n \in N$.

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63. If $z = \cos\theta + i\sin\theta$ is a root of the equation $a_0 z^n + a_2 z^{n-2} + \ldots . + a_{n-1} z + a_n = 0$, then prove that

$a_0 + a_1 \cos\theta + a_2 \overset{\cos 2}{} \theta + \; + a_n \cos n\theta = 0$

$a_1 \sin\theta + a_2 \overset{\sin 2}{} \theta + \; + a_n \sin n\theta = 0$

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64. If $\left|z_1\right| = 1, \left|z_2\right| = 2, \left|z_3\right| = 3, and \left|9z_1 z_2 + 4z_1 z_3 + z_2 z_3\right| = 12$, then find the value of $\left|z_1 + z_2 + z_3\right|$.

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65. If α *and* β are different complex numbers with $|\beta| = 1$, $f \in d\left|\frac{\beta - \alpha}{1 - \alpha\beta}\right|$

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66. Given that $\left|z_1 + z_2\right|^2 = \left|z_1\right|^2 + \left|z_2\right|^2$, prove that $\frac{z_1}{z_2}$ is purely imaginary.

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67. Let $\left|\left(z_1 - 2z_2\right)/\left(2 - z_1 z_2\right)\right| = 1$ and $\left|z_2\right| \neq 1$, where z_1 and z_2 are complex numbers. shown that $\left|z_1\right| = 2$

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68. If $z_1 and z_2$ are two complex numbers and $c > 0$, then prove that $\left|z_1 + z_2\right|^2 \leq (1 + c)\left|z_1\right|^2 + \left(1 + c^{-1}\right)\left|z_2\right|^2$.

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69. If z_1, z_2, z_3, z_4 are the affixes of four point in the Argand plane, z is the affix of a point such that $\left|z - z_1\right| = \left|z - z_2\right| = \left|z - z_3\right| = \left|z - z_4\right|$, then prove that z_1, z_2, z_3, z_4 are concyclic.

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70. if $\left|z_1 + z_2\right| = \left|z_1\right| + \left|z_2\right|$, then prove that $arg\left(z_1\right) = arg\left(z_2\right)$ if $\left|z_1 - z_2\right| = \left|z_1\right| + \left|z_2\right|$, then prove that $arg\left(z_1\right) = arg\left(z_2\right) = \pi$

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71. Show that the area of the triangle on the Argand diagram formed by the complex number $z, izandz + iz$ is $\frac{1}{2}|z|^2$

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72. Find the minimum value of $|z - 1|$ if $||z - 3| - |z + 1| | = 2.$

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73. Find the greatest and the least value of $\left|z_1 + z_2\right|$ if $z_1 = 24 + 7iand\left|z_2\right| = 6.$

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74. If z is a complex number, then find the minimum value of $|z| + |z - 1| + |2z - 3|$.

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75. If $\left|z_1 - 1\right| \leq$, $\left|z_2 - 2\right| \leq 2$, $\left|z_{33}\right| \leq 3$, then find the greatest value of $\left|z_1 + z_2 + z_3\right|$.

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76. Prove that following inequalities:

(i) $\left|\frac{z}{|z|} - 1\right| \leq |argz|$ (ii) $|z - 1| \leq |z||argz| + |z| - 1|$

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77. Identify the locus of z if $z = a + \frac{r^2}{z - a}, > 0.$

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78. If z is any complex number such that $|3z - 2| + |3z + 2| = 4$, then identify the locus of z

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79. If $|z| = 1$ and let $\omega = \frac{(1 - z)^2}{1 - z^2}$, then prove that the locus of ω is equivalent to $|z - 2| = \ | \ z + 2$

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80. Let z be a complex number having the argument θ ,$0 < \theta < \frac{\pi}{2}$, and satisfying the equation$|z - 3i| = 3$. Then find the value of $\cot\theta - \frac{6}{z}$

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81. How many solutions the system of equations $||z + 4| - |z - 3i|\ |\ \ | = 5$ and $|z| = 4$ `has ?

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82. Prove that $\left|Z - Z_1\right|^2 + \left|Z - Z_2\right|^2 = a$ will represent a real circle [with center $\left(\left|Z_1 + Z_2\right|^{/}2 + \right)$] on the Argand plane if $2a \geq \left|Z_1 - Z_1\right|^2$

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83. If $|z - 2 - 3i|^2 + |z - 5 - 7i|^2 = \lambda$ respresents the equation of circle with least radius, then find the value of λ.

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84. If $\frac{|2z - 3|}{|z - i|} = k$ is the equation of circle with complex number 'I' lying inside the circle, find the values of K.

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85. Find the point of intersection of the curves $arg(z - 3i) = \frac{3\pi}{4} and arg(2z + 1 - 2i) = \pi/4.$

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86. If complex numbers $z_1 z_2$ and z_3 are such that $|z_1| = |z_2| = |z_3|$, then prove that $arg\left(\frac{z_2}{z_1}\right) = arg\left(\frac{z_2 - z_3}{z_1 - z_3}\right)^2$.

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87. If the triangle fromed by complex numbers z_1, z_2 and z_3 is equilateral then prove that $\frac{z_2 + z_3 - 2z_1}{z_3 - z_2}$ is purely imaginary number

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88. Show that the equation of a circle passings through the origin and having intercepts a and b on real and imaginary axis, respectively, on the argand plane is $Re\left(\frac{z - a}{z - ib}\right) = 0$

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89. The triangle formed by $A\left(z_1\right), B\left(z_2\right)$ and $C\left(z_3\right)$ has its circumcentre at origin .If the perpendicular form A to BC intersect the circumference at z_4 then the value of $z_1 z_4 + z_2 z_3$ is

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90. Let vertices of an acute-angled triangle are $A\left(z_1\right), B\left(z_2\right), andC\left(z_3\right)$. If the origin O is he orthocentre of the triangle, then prove that

$z_1(z)_2 + (z)_1 z_2 =_2(z)_3 + (z)_2 z_3 = z_3(z)_1 + (z)_3 z_1$.

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91. If z_1, z_2, z_3 are three complex numbers such that $5z_1 - 13z_2 + 8z_3 = 0$, then prove that $\left|z_1(z)_1 1 z_2(z)_2 1 z_3(z)_3 1\right| = 0$

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92. If $z = z_0 + A\left(z - (z)_0\right), where A$ is a constant, then prove that locus of z is a straight line.

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93. $z_1 and z_2$ are the roots of $3z^2 + 3z + b = 0$. if $O(0), \left(z_1\right), \left(z_2\right)$ form an equilateral triangle, then find the value of b

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94. Let z_1, z_2 and z_3 be three complex number such that

$$\left|z_1 - 1\right| = \left|z_2 - 1\right| = \left|z_3 - 1\right| \text{ and } arg\left(\frac{z_3 - z_1}{z_2 - z_1}\right) = \frac{\pi}{6}$$

then prove that $z_2^3 + z_3^3 + 1 = z_2 + z_3 + z_2 z_3$.

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95. Let the complex numbers z_1, z_2 and z_3 be the vertices of an equailateral triangle. If z_0 is the circumcentre of the triangle , then prove that $z_1^2 + z_2^2 + z_3^2 = 3z_0^2$.

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96. In the Argands plane what is the locus of $z(\neq 1)$ such that

$$arg\left\{\frac{3}{2}\left(\frac{2z^2 - 5z + 3}{2z^2 - z - 2}\right)\right\} = \frac{2\pi}{3}.$$

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97. If $\left(\frac{3-z_1}{2-z_1}\right)\left(\frac{2-z_2}{3-z_2}\right)=k(k>0)$, then prove that points $A\left(z_1\right), B\left(z_2\right), C(3), andD(2)$ (taken in clockwise sense) are concyclic.

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98. If z_1, z_2, z_3 are complex numbers such that $\left(2/z_1\right)=\left(1/z_2\right)+\left(1/z_3\right)$, then show that the points represented by z_1, z_2, z_3 lie one a circle passing through the origin.

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99. $A(z_1), B(z_2), C(z_3)$ are the vertices of he triangle ABC (in anticlockwise). If $\angle ABC = \pi/4$ and $AB = \sqrt{2}(BC)$, then prove that $z_2 = z_3 + i(z_1 - z_3)$.

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100. If one of the vertices of the square circumscribing the circle $|z - 1| = \sqrt{2}$ is $2 + \sqrt{3}i$, where $i = \sqrt{-1}$. Find the other vertices of the square.

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101. Let $z_1 = 10 + 6i$ and $z_2 = 4 + 6i$. If z is any complex number such that the argument of $\frac{(z - z_1)}{(z - z_2)}$ is $\frac{\pi}{4}$, then prove that $|z - 7 - 9i| = 3\sqrt{2}$.

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102. Complex numbers z_1, z_2 and z_3 are the vertices A,B,C respectivelt of an isosceles right angled triangle with right angle at C. show that $\left(z_1 - z_2\right)^2 = 2\left(z_1 - z_3\right)\left(z_3 - z_2\right)$.

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103. Let $z_1, z_2 and z_3$ represent the vertices $A, B, and C$ of the triangle ABC, respectively, in the Argand plane, such that $\left|z_1\right| = \left|z_2\right| = 5$. Prove that $z_1 \sin 2A + z_2 \sin 2B + z_3 \sin 2C = 0$.

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104. F $a = \cos(2\pi/7) + i\sin(2\pi/7)$, then find the quadratic equation whose roots are $\alpha = a + a^2 + a^4 and \beta = a^3 + a^5 + a^7$.

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105. If ω is an imaginary fifth root of unity, then find the value of $loe_2\left|1 + \omega + \omega^2 + \omega^3 - 1/\omega\right|$.

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106. If 1, $\alpha_1, \alpha_2, \alpha_3, \ldots\ldots, \alpha_s$ are ninth roots of unity (taken in counter -clockwise sequence in the Argard plane). Then find the value of $|(2 - \alpha_1)(2 - \alpha_3), (2 - \alpha_5)(2 - \alpha_7)|$.

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107. find the sum of squares of all roots of the equation. $x^8 - x^7 + x^6 - x^5 + x^4 - x^3 + x^2 - x + 1 = 0$

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108. Find roots of the equation $(z + 1)^5 = (z - 1)^5$.

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109. If the roots of $(z - 1)^n = i(z + 1)^n$ are plotted in ten Arg and plane, then prove that they are collinear.

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110. Let $1, z_1, z_2, z_3, \ldots, z_{n-1}$ be the nth roots of unity. Then prove that $(1 - z_1)(1 - z_2)\ldots(1 - z_{n-1}) = n$. Also,deduce that $\sin.\frac{\pi}{n}\sin.\frac{2\pi}{\pi}\sin.\frac{3\pi}{n}\ldots\sin.\frac{(n-1)\pi}{n} = \frac{\pi}{2^{n-1}}$

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SLOVED EXAMPLES

1. if$\omega and \omega^2$ are the nonreal cube roots of unity and $[1/(a+\omega)] + [1/(b+\omega)] + [1/(c+\omega)] = 2\omega^2$ and $\left[1/(a+\omega)^2\right] + \left[1/(b+\omega)^2\right] + \left[1/(c+\omega)^2\right] = 2\omega$, then find the value of $[1/(a+1)] + [1/(b+1)] + [1/(c+1)]$.

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2. If $z_1 and z_2$ are complex numbers and $u = \sqrt{z_1 z_2}$, then prove that $\left|z_1\right| + \left|z_2\right| = \left|\frac{z_1 + z_2}{2} + u\right| + \left|\frac{z_1 + z_2}{2} - u\right|$

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3. If a is a complex number such that $|a| = 1$, then find the value of a, so that equation $az^2 + z + 1 = 0$ has one purely imaginary root.

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4. Let z, z_0 be two complex numbers. It is given that $|z| = 1$ and the numbers $z, z_0, z\bar{}(0), 1$ and 0 are represented in an Argand diagram by the points P,P_0,Q,A and the origin, respectively. Show that $\triangle POP_0$ and $\triangle AOQ$ are congruent. Hence, or otherwise,

prove that

$$\left|z - z_0\right| = \left|z\bar{z}_0 - 1\right| = \left|z\bar{z}_0 - 1\right|.$$

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5. Let a, b and c be any three nonzero complex number. If $|z| = 1$ and $'z'$ satisfies the equation $az^2 + bz + c = 0$, prove that $a.\bar{a} = c.\bar{c}$ and $|a||b| = \sqrt{ac\left(\bar{b}\right)^2}$

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6. Let x_1, x_2 are the roots of the quadratic equation $x^2 + ax + b = 0$, where a,b, are complex numbers and y_1, y_2 are the roots of the quadratic equation $y^2 + |a|yy + |b| = 0$. If $\left|x_1\right| = \left|x_2\right| = 1$, then prove that $\left|y_1\right| = \left|y_2\right| = 1$

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7. If $\alpha = (z - i)/(z + i)$ show that, when z lies above the real axis, α will lie within the unit circle which has centre at the origin. Find the locus of α as z travels on the real axis form $-\infty$to $+\infty$

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8. If $|z| \leq 1, |w| \leq 1,$ then show that $|z - w|^2 \leq (|z| - |w|)^2 + (argz - argw)^2$

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9. Prove that the distance of the roots of the equation $\left|\sin\theta_1\right|z^3 + \left|\sin\theta_2\right|z^2 + \left|\sin\theta_3|z + |\sin\theta_4| = |3\right|$ from z=0 is greater than $2/3$.

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10. If $|z - (4 + 3i)| = 1$, then find the complex number z for each of the following cases:

(i) $|z|$ is least

(ii) $|z|$ is greatest

(iii) $arg(z)$ is least

(iv) arg(z) is greatest

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11. If a ,b,c, and u,v,w are complex numbers representing the vertices of two triangle such that they are similar, then prove that $\frac{a - c}{a - b} = \frac{u - w}{u - v}$

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12. Let z_1 and z_2 be the roots of the equation $z^2 + pz + q = 0$, where the coefficients p and q may be complex numbers. Let A and B represent z_1 and z_2 in the complex plane, respectively. If $\angle AOB = \theta \neq 0$ and $OA = OB$, *where* O is the origin, prove that $p^2 = 4q\cos^2(\theta/2)$.

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13. The altitude form the vertices A, B and C of the triangle ABC meet its circumcircle at D,E and F, respectively . The complex number representing the points D,E, and F are z_1, z_2 and z_3, respectively. If $(z_3 - z_1)/(z_2 - z_1)$ is purely real, then show that triangle ABC is right-angled at A.

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14. Let A, B, C, D be four concyclic points in order in which $AD : AB = CD : CB$. If A, B, C are repreented by complex numbers a, b, c representively, find the complex number associated with point D.

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15. If $n \geq 3$ and $1, \alpha_1, \alpha_2, \alpha_3, \ldots, \alpha_{n-1}$ are the n,nth roots of unity, then find value of $\sum \sum_{1 \leq i < j \leq n-1} \alpha_i \alpha_j$

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EXERCISE3.1

1. Is the following computation correct? If not give the correct computation: $\left[\sqrt{(-2)}\sqrt{(-3)}\right] = \sqrt{(-2)\cdot(-3)} = \sqrt{6}$

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2. Find the value of $\frac{i^{592} + i^{590} + i^{588} + i^{586} + i^{584}}{i^{582} + i^{580} + i^{578} + i^{576} + i^{574}} - 1$

$(1 + i)^6 + (1 - i)^6$

A. -2

B. 0

C. 2

D. -1

Answer: A

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3. The value of $i^{1+3+5++(2n+1)}$ is_____.

A. i

B. 1

C. -1

D. $-i$

Answer: B

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4. Find the value of $x^4 + 9x^3 + 35x^2 - x + 4$ for $x = -5 + 2\sqrt{-4}$.

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EXERCISE3.2

1. प्रश्न 11 से 13 तक कि सम्मिश्र संख्याओं में प्रत्येक का गुणात्मक प्रतिलोम ज्ञात कीजिए।

$4 - 3i$

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2. Express the following complex numbers in $a + ib$ form:

$\frac{(3 - 2i)(2 + 3i)}{(1 + 2i)(2 - i)}$ (ii) $\frac{2 - \sqrt{-25}}{1 - \sqrt{-16}}$

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3. Find the least positive integer n such that $\left(\frac{2i}{1 + i}\right)^n$ is a positive integer.

A. n =6

B. n =5

C. n =8

D. n =4

Answer: C

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4. If one root of the equation $z^2 - az + a - 1 = 0$ is (1+i), where a is a complex number then find the root.

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5. Prove that quadrilateral formed by the complex numbers which are roots of the equation $z^4 - z^3 + 2z^2 - z + 1 = 0$ is an

equailateral trapezium.

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6. If Z is a non-real complex number, then find the minimum value of $\left|\frac{Imz^5}{Im^5z}\right|$

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7. Find the real numbers x and y, if $(x - iy)(3 + 5i)$ is the conjugate of $-6 - 24i$

A. $x = -2, y = 2$

B. $x = -3, y = 3$

C. $x = 3, y = -3$

D. $x = -4, y = 1$

Answer: C

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8. If z_1, z_2, z_3 are three nonzero complex numbers such that $z_3 = (1 - \lambda)z_1 + \lambda z_2 where \lambda \in R - \{0\}$, then prove that points corresponding to $z_1, z_2 and z_3$ are collinear .

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9. If n_1, n_2 are positive integers, then $(1 + i)^{n_1} + \left(1 + i^3\right)^{n_1} + \left(1 + i_5\right)^{n_2} + \left(1 + i^7\right)^{n_2}$ is real if and only if :

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EXERCISE3.3

1. If $(a + b) - i(3a + 2b) = 5 + 2i$ find a *and* b

A. $a = 12, b = -17$

B. $a = -12, b = -17$

C. $a = 12, b = 17$

D. $a = -12, b = 17$

Answer: D

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2. Find all non zero complex numbers z satisfying $\bar{z} = iz^2$

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3. If a, b, c are nonzero real numbers and $az^2 + bz + c + i = 0$ has purely imaginary roots, then prove that $a = b^2c$

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4. If the sum of square of roots of equation $x^2 + (p + iq)x + 3i = 0$ is 8, then find p and q, where p and q are real.

A. $p = 2, q = 2$

B. $p = -3, q = 4$

C. $p = 3, q = 1$ or $p = -3, q = -1$

D. $p = -2, q = -2$

Answer: C

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5. Find the square root $9 + 40i$.

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6. Simplify: $\dfrac{\sqrt{5 + 12i} + \sqrt{5 - 12i}}{\sqrt{5 + 12i} - \sqrt{5 - 12i}}$

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7. If $\sqrt{x + iy} = \pm (a + ib)$, then find $\sqrt{-x - iy}$.

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EXERCISE3.4

1. if α and β are imaginary cube root of unity then prove $(\alpha)^4 + (\beta)^4 + (\alpha)^{-1}.(\beta)^{-1} = 0$

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2. If ω is a complex cube roots of unity, then find the value of the $(1+\omega)\left(1+\omega^2\right)\left(1+\omega^4\right)\left(1+\omega^8\right)$... to 2n factors.

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3. Write the complex number in a + ib form using cube roots of unity: $\left(-\frac{1}{2}+\frac{\sqrt{3}}{2}i\right)^{1000}$

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4. If z is a complex number, then find the minimum value of

$|z| + |z - 1| + |2z - 3|$.

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5. Find the common roots of $x^{12} - 1 = 0$ and $x^4 + x^2 + 1 = 0$

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6. Ifα, β and γ are the roots of $X^3 - 3X^2 + 3X + 7 + 0$, find the value of $\frac{\alpha = 1}{\beta - 1} + \frac{\beta - 1}{\gamma - 1} + \frac{\gamma - 1}{\alpha - 1}$.

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7. Prove that $t^2 + 3t + 3$ is a factor of $(t + 1)^{n+1} + (t + 2)^{2n-1}$ for all intergral values of n $\in$ N.

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EXERCISE3.5

1. Find the pricipal argument of each of the following:

(a) $-1 - i\sqrt{3}$

(b) $\dfrac{1 + \sqrt{3}i}{3 + i}$

(c) $\sin\alpha + i(1 - \cos\alpha), 0 > \alpha > \pi$

(d) $\left(1 + i\sqrt{3}\right)^2$

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2. Find the modulus and argument of the following complex number: $\dfrac{1 + i}{1 - i}$

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3. If $\frac{3\pi}{2} < \alpha < 2\pi$ then the modulus argument of $(1 + \cos 2\alpha) + i\sin 2\alpha$

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4. Find the principal argument of the complex number $\frac{\sin(6\pi)}{5} + i\left(1 + \frac{\cos(6\pi)}{5}\right)$.

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5. If $z = re^{i\theta}$, then prove that $\left|e^{iz}\right| = e^{-rs\int h\eta}$.

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6. Find the complex number z satisfying $Re\left(z^2\right) = 0, |z| = \sqrt{3}.$

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7. If $|z - iRe(z)| = |z - Im(z)|$, then prove that z , lies on the bisectors of the quadrants.

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8. Find the locus of the points representing the complex number z for which$|z + 5|^2 = |z - 5|^2 = 10.$

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9. Solve that equation $z^2 + |z| = 0$, where z is a complex number.

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10. Let $z = x + iy$ be a complex number, where $xandy$ are real numbers. Let $AandB$ be the sets defined by $A = \{z : |z| \leq 2\} andB = \{z : (1 - i)z + (1 + i)z \geq 4\}$. Find the area of region $A \cup B$.

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11. Real part of $\left(e^{e}\right)^{\iota\theta}$ is

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12. Prove that $z = i^{i}, wherei = \sqrt{-1}$, is purely real.

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EXERCISE3.6

1. For $z_1 = \sqrt[6]{(1-i)/\left(1+i\sqrt{3}\right)}, z_2 = \sqrt[6]{(1-i)/\left(\sqrt{3}+i\right)}$, $z_3 = \sqrt[6]{(1+i)/\left(\sqrt{3}-i\right)}$, prove that $|z_1| = |z_2| = |z_3|$

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2. If $\sqrt{3}+i = (a+ib)(c+id)$, then find the value of $\tan^{-1}(b/a)\tan^{-1}(d/c)$.

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3. If z_1, z_2 and z_3, z_4 are two pairs of conjugate complex numbers then $arg\left(\frac{z_1}{z_4}\right) + arg\left(\frac{z_2}{z_3}\right) =$

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4. Find the modulus, argument and the principal agrument of the complex number $(\tan 1 - i)^2$

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5. If $(1+i)(1+2i)(1+3i)1+m) = (x+iy)$, then show that $2 \times 5 \times 10 \times \times \left(1+n^2\right) = x^2 + y^2$.

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6. If $a + ib = \frac{(x+i)^2}{2x+1}$, prove that $a^2 + b^2 = \frac{(x+i)^2}{(2x+1)^2}$

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7. Let z be a complex number satisfying the equation $\left(z^3 + 3\right)^2 = -16$, then find the value of $|z|$

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8. If θ is real and z_1, z_2 are connected by $z12 + z22 + 2z_1z_2\cos\theta = 0,$ then prove that the triangle formed by vertices $O, z_1 and z_2$ is isosceles.

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9. If $\left|z_1 - z_0\right| = z_2 - z_1 = \frac{\pi}{2}$, then find z_0.

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10. Show that $\left|\frac{z-2}{z-3}\right| = 2$ represents a circle. Find its centre and radius.

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EXERCISE3.7

1. Express the following in $a + ib$ form: $\frac{(\cos\alpha + i\sin\alpha)^4}{(\sin\beta + i\cos\beta)^5}$

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2. Find the value of following expression: $\left[\frac{1-\frac{\cos\pi}{10}+i\frac{\sin\pi}{10}}{1-\frac{\cos\pi}{10}-i\frac{\sin\pi}{10}}\right]^{10}$

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3. If $iz^4+1=0$, then prove that z can take the value $\cos\pi/8+is\in\pi/8$.

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4. Prove that $(1+i)^n+(1-i)^n=2^{\frac{n+2}{2}}.\cos\left(\frac{n\pi}{4}\right)$, where n is a positive integer.

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5. If $z = (a + ib)^5 + (b + ia)^5$, then prove that $Re(z) = Im(z)$, where $a, b \in R$.

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6. If $\cos\alpha + \cos\beta + \cos\gamma = 0$ and also $\sin\alpha + \sin\beta + \sin\gamma = 0$, then prove that: $\cos 3\alpha + \cos 3\beta + \cos 3\gamma = 3\cos(\alpha + \beta + \gamma)$

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EXERCISE3.8

1. a, b, c are three complex numbers on the unit circle $|z| = 1$, such that $abc = a + b + \cdot$ Then find the value of $|ab + bc + ca|$.

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2. Let z be not a real number such that $\left(1+z+z^2\right)/\left(1-z+z^2\right) \in R$, then prove tha $|z| = 1$.

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3. If z_1, z_2, z_3 are distinct nonzero complex numbers and $a, b, c \in R^+$ such that $\frac{a}{\left|z_1 - z_2\right|} = \frac{b}{\left|z_2 - z_3\right|} = \frac{c}{\left|z_3 - z_1\right|}$ Then find the value of $\frac{a^2}{\left|z_1 - z_2\right|} + \frac{b^2}{\left|z_2 - z_3\right|} + \frac{c^2}{\left|z_3 - z_1\right|}$

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4. If z_1 and z_2 are two complex numbers such that $\left|z_1\right| < 1 < \left|z_2\right|$, then prove that $\left|\left(1 - z_1\bar{z}_2\right)/\left(z_1 - z_2\right)\right| < 1$

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5. (i) If $\left|z_1 + z_2\right| = \left|z_1\right| + \left|z_2\right|$, then prove that $arg\left(z_1\right) = arg\left(z_2\right)$

(ii) If $\left|z_1 - z_2\right| = \left|z_1\right| + \left|z_2\right|$,then prove that $arg\left(z_1\right) - arg\left(z_2\right) = \pi$

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6. For any complex number z, find the minimum value of $|z| + |z - 2i|$.

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7. If is any complex number such that $|z + 4| \leq 3$, then find the greatest value of $|z + 1|$.

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8. $Z \in C$ satisfies the condition $|Z| > 3$. Then find the least value of $\left|Z + \frac{1}{Z}\right|$

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9. If a, b, c are non zero complex numbers of equal modlus and satisfy $az^2 + bz + c = 0$, hen prove that $\left(\sqrt{5} - 1\right)/2 \leq |z| \leq \left(\sqrt{5} + 1\right)/2.$

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10. If $|z| \leq 4$, then find the maximum value of $|iz + 3 - 4i|$

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11. Let $z_1, z_2, z_3, \ldots\ldots z_n$ be the complex numbers such that $|z_1| = |z_2| = \ldots\ldots = |z_n| = 1$. If $z = \left(\sum_{k=1}^{n} z_k\right)\left(\sum_{k=1}^{n} \frac{1}{z_k}\right)$ then prove that : z is a real number .

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EXERCISE3.9

1. If $\omega = \frac{z}{z - \frac{1}{3}i}$ and $|\omega| = 1$, where $i = \sqrt{-1}$,then lies on

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2. If $Im\left(\frac{z-1}{e^{\theta i}} + \frac{e^{\theta i}}{z-1}\right) = 0$, then find the locus of z .

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3. For three non-colliner complex numbers Z, Z_1 and Z_2 prove that $\left|Z - \frac{Z_1 + Z_2}{2}\right|^2 + \left|\frac{Z_1 - Z_2}{2}\right|^2 = \frac{1}{2}\left|Z - Z_1\right|^2 + \frac{1}{2}\left|Z - Z_2\right|^2$

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4. If $|z - 1| + |z + 3| \leq 8$, then prove that z lies on the circle.

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5. If $z = \frac{3}{2 + \cos\theta + I\sin\theta}$, then prove that z lies on the circle.

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6. How many solutions system of equations, $arg(z + 3 - 2i) = -\frac{\pi}{4}$ and $|z + 4| - |z - 3i| = 5$ has ?

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7. Prove that equation of perpendicular bisector of line segment joining complex numbers z_1 and z_2 is $z\left(\bar{z}_2 - \bar{z}_1\right) + \bar{z}\left(z_2 + z_1\right) + \left|z_1\right|^2 - \left|z_2\right|^2 = 0$

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8. If complex number z lies on the curve $|z - (-1 + i)| = 1$, then find the locus of the complex number $w = \frac{z + i}{1 - i}, i = \sqrt{-1}$.

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EXERCISE3.10

1. If $z_1 z_2, z_3$ and z_4 taken in order vertices of a rhombus, then proves that $Re\left(\frac{z_3 - z_1}{z_4 - z_2}\right) = 0$

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2. Find the locus of point z if z , i ,and iz , are collinear.

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3. If $|z| = 2 and \frac{z_1 - z_3}{z_2 - z_3} = \frac{z - 2}{z + 3}$, then prove that z_1, z_2, z_3 are vertices of a right angled triangle.

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4. If $\alpha, \beta, \gamma, \delta$ are four complex numbers such that $\frac{\gamma}{\delta}$ is real and $\alpha\delta - \beta\gamma \neq 0$ then z = $\frac{\alpha + \beta t}{\gamma + \delta t}$ where t is a rational number, then it represents:

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5. Prove that the complex numbers z_1, z_2 and the origin form an equilateral triangle only if $z_1^2 + z_2^2 - z_1 z_2 = 0$.

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6. The center of a regular polygon of n sides is located at the point z=0, and one of its vertex z_1 is known. If z_2 be the vertex adjacent to z_1, then z_2 is equal to _____.

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7. If one vertex of the triangle having maximum area that can be inscribed in the circle $|z - i| = 5is3 - 3i$, then find the other vertices of the triangle.

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8. If z_1, z_2 and z_3 are the vertices of an equilasteral triangle with z_0 as its circumcentre , then changing origin to z^0 ,show that $z_1^2 + z_2^2 + z_3^2 = 0,$ where$z_1, z_2, z_3,$ are new complex numbers of the vertices.

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9. P is a point on the argand diagram on the circle with OP as diameter two points taken such that $\angle POQ = \angle QOR = \theta$. If O is

the origin and P, Q, R are are represented by complex z_1, z_2, z_3 respectively then show that $z_2^2 \cos 2\theta = z_1 z_3 \cos^2\theta$

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10. Find the center of the are represented by $arg[(z - 3i)/(z - 2i + 4)] = \pi/4$.

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EXERCISE3.11

1. If α is complex fifth root of unity and $\left(1 + \alpha + \alpha^2 + \alpha^3\right)^{2005} = p + q\alpha + r\alpha^2 + s\alpha^3$ (where p,q,r,s are real), then find the value of $p + q + r + s$.

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2. Find the number of roots of the equation $z^{15} = 1$ satisfying $|argz| < \pi/2$.

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3. If z is nonreal root of $[-1]^{\frac{1}{7}}$ then,find the value of $z^{86}+z^{175}+z^{289}$

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4. Given $\alpha, \beta,$ respectively, the fifth and the fourth non-real roots of units, then find the value of $(1+\alpha)(1+\beta)\left(1+\alpha^2\right)\left(1+\beta^2\right)\left(1+\alpha^4\right)\left(1+\beta^4\right)$

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5. If the six roots of $x^6 = -64$ are written in the form $a + ib$, where a and b are real, then the product of those roots for which $a < 0$ is

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6. If $z_r : r = 1, 2, 3, , 50$ are the roots of the equation $\sum_{r=0}^{50} z^r = 0$, then find the value of $\sum_{r=0}^{50} 1/\left(zr^{-1}\right)$.

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single correct Answer type

1. If $a\ 0, b\ 0, then \sqrt{a}\sqrt{b}$ is equal to -$\sqrt{|a|b}$ b. $\sqrt{|a|b}i$ c. $\sqrt{|a|b}$ d. none of these

A. -$\sqrt{|a|b}$

B. $\sqrt{|a|b}$ i

C. $\sqrt{|a|b}$

D. none of these

Answer: B

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2. Consider the equation $10z^2$ - $3iz$ - $k = 0, wherez$ is a following complex variable and $i^2 = -1$. Which of the following statements ils true? (a)For real complex numbers k , both roots are purely imaginary. (b)For all complex numbers k , neither both

roots is real. (c)For all purely imaginary numbers k , both roots are real and irrational. (d)For real negative numbers k , both roots are purely imaginary.

A. For real positive numbers k, both roots are purely imaginary

B. For all complex numbers k, neither root is real .

C. For real negative numbers k, both roots are real and irrational .

D. For real negative numbers k, both roots are purely imaginary.

Answer: D

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3. The number of solutions of the equation $z^2 + z = 0$ where z is a a complex number, is

A. 1

B. 2

C. 3

D. 4

Answer: D

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4. If center of a regular hexagon is at the origin and one of the vertices on the Argand diagram is $1 + 2i$, then its perimeter is $2\sqrt{5}$ b. $6\sqrt{2}$ c. $4\sqrt{5}$ d. $6\sqrt{5}$

A. $2\sqrt{5}$

B. $6\sqrt{5}$

C. $4\sqrt{5}$

D. $6\sqrt{5}$

Answer: D

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5. If x and y are complex numbers, then the system of equations

$(1 + i)x + (1 - i)y = 1, 2ix + 2y = 1 + i$ has

A. unique solution

B. no solution

C. infinte number of solutions

D. none of theses

Answer: C

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6. The point $z_1 = 3 + \sqrt{3}i$ and $z_2 = 2\sqrt{3} + 6i$ are given on a complex plane. The complex number lying on the bisector of the angel formed by the vectors $z_1 and z_2$ is $z = \frac{\left(3 + 2\sqrt{3}\right)}{2} + \frac{\sqrt{3} + 2}{2}i$

$z = 5 + 5i$ $z = -1 - i$ none of these

A. $z = \frac{\left(3 + 2\sqrt{3}\right)}{2} + \frac{\sqrt{3} + 2}{2}i$

B. $z = 5 + 5i$

C. $z = -1 - i$

D. none of these

Answer: B

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7. The polynomial $x^6 + 4x^5 + 3x^4 + 2x^3 + x + 1$ is divisible by_____ where ω is one of the imaginary cube roots of unity. (a) $x + \omega$ (b) $x + \omega^2$ (c) $(x + \omega)\left(x + \omega^2\right)$ (d) $(x - \omega)\left(x - \omega^2\right)$

A. $x + \omega$

B. $x + \omega^2$

C. $(x + \omega)\left(x + \omega^2\right)$

D. $(x + \omega)\left(x - \omega^2\right)$

Answer: D

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8. about to only mathematics

A. $\frac{1}{2}(z+1)+i$

B. $\frac{1}{2}(iz+1)+i$

C. $\frac{1}{2}(iz-1)+i$

D. $\frac{1}{2}(z+i)+1$

Answer: B

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9. The complex number $\sin(x)+i\cos(2x)$ and $\cos(x)-i\sin(2x)$ are conjugate to each other for

A. $x=n\pi, n\in Z$

B. $x=0$

C. $x=(n+1/2)\pi, n\in Z$

D. no value of x

Answer: D

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10. If the equation $z^4 + a_1 z^3 + a_2 z^2 + a_3 z + a_4 = 0$ where a_1, a_2, a_3, a_4 are real coefficients different from zero has a pure imaginary root then the expression $\frac{a_3}{a_1 a_2} + \frac{a_1 a_4}{a_2 a_3}$ has the value equal to

A. 0

B. 1

C. -2

D. 2

Answer: B

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11. If $z_1, z_2 \in C, z_1^2 \in R, z_1\left(z_1^2 - 3z_2^2\right) = 2$ and $z_2\left(3z_1^2 - z_2^2\right) = 11$, then the value of $z_1^2 + z_2^2$ is

A. 10

B. 12

C. 5

D. 8

Answer: C

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12. If $a^2 + b^2 = 1 then \frac{1 + b + ia}{1 + b - ia} = 1$ b. 2 c. $b + ia$ d. $a + ib$

A. a + ib

B. a + ia

C. b+ ia

D. b + ib

Answer: C

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13. If $z(1+a) = b + icanda^2 + b^2 + c^2 = 1,$ then $[(1+iz)/(1-iz) =$

$\frac{a+ib}{1+c}$ b. $\frac{b-ic}{1+a}$ c. $\frac{a+ic}{1+b}$ d. none of these

A. $\frac{a+ib}{1+c}$

B. $\frac{b-ic}{1+a}$

C. $\frac{a+ic}{1+b}$

D. none of these

Answer: A

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14. If a and b are complex and one of the roots of the equation $x^2 + ax + b = 0$ is purely real whereas the other is purely imaginary, then

A. $a^2 - (\bar{a})^2 = 4b$

B. $a^2 - (\bar{a})^2 = 2b$

C. $b^2 - (\bar{a})^2 = 2a$

D. $b^2 - (\bar{b})^2 = 2a$

Answer: A

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15. If $z = (\lambda + 3) + i\sqrt{\left(5 - \lambda^2\right)}$; then the locus of z is a) a straight line b) a semicircle c) an ellipse d) a parabola

A. ellispe

B. semicircle

C. parabola

D. none of these

Answer: B

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16. Let $z = 1 - t + i\sqrt{t^2 + t + 2}$, where t is a real parameter.the locus of the z in arg and plane is

A. a hyperbola

B. an ellipse

C. a striaght line

D. none of these

Answer: A

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17. If z_1 and z_2 are the complex roots of the equation $(x - 3)^3 + 1 = 0$, then $z_1 + z_2$ equal to

A. 1

B. 3

C. 5

D. 7

Answer: D

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18. Which of the following is equal to $\sqrt[3]{-1}$?

A. $\frac{\sqrt{3}+\sqrt{-1}}{2}$

B. $\frac{-\sqrt{3}+\sqrt{-1}}{\sqrt{-4}}$

C. $\frac{\sqrt{3}-\sqrt{-1}}{\sqrt{-4}}$

D. $-\sqrt{-1}$

Answer: B

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19. about to only mathematics

A. 27

B. 72

C. 45

D. 54

Answer: D

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20. Sum of common roots of the equations $z^3 + 2z^2 + 2z + 1 = 0$ and $z^{1985} + z^{100} + 1 = 0$ is

A. -1

B. 1

C. 0

D. 1

Answer: A

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21. When the polynomial $5x^3 + Mx + N$ is divided by $x^2 + x + 1$, the remainder is 0. Then find the value of $M + N$.

A. 5

B. 4

C. -4

D. -5

Answer: D

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22. If $z = x + iy$ and $x^2 + y^2 = 16$, then the range of $||x| - |y||$ is

$[0, 4]$ b. $[0, 2]$ c. $[2, 4]$ d. none of these

A. $[0, 4]$

B. $[0, 2]$

C. $[2, 4]$

D. none of these

Answer: A

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23. If z is a complex number satisfying the equaiton $z^6 - 6z^3 + 25 = 0$, then the value of $|z|$ is

A. $5^{1/3}$

B. $25^{1/3}$

C. $125^{1/3}$

D. $625^{1/3}$

Answer: A

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24. If $8iz^3 + 12z^2 - 18z + 27i = 0, then\ |z| = \frac{3}{2}$ b. $|z| = \frac{2}{3}$ c.$|z| = 1$ d. $|z| = \frac{3}{4}$

A. $|z| = \frac{3}{2}$

B. $|z| = \frac{3}{4}$

C. $|z| = 1$

D. $|z| = \frac{3}{4}$

Answer: A

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25. Let $z_1 and z_2$ be complex numbers such that $z_1 \neq z_2$ and $\left|z_1\right| = \left|z_2\right|$. If z_1 has positive real part and z_2 has negative imaginary part, then $\frac{z_1 + z_2}{z_1 - z_2}$ may be (a)zero (b) real and positive (c)real and negative (d) purely imaginary

A. purely imaginary

B. real and positive

C. real and negative

D. none of these

Answer: A

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26. If $\left|z_1\right| = \left|z_2\right|$ and $arg\left(\frac{z_1}{z_2}\right) = \pi$, then $z_1 + z_2$ is equal to (a) 0 (b) purely imaginary (c) purely real (d) none of these

A. 0

B. purely imaginary

C. purely real

D. none of these

Answer: A

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27. If for complex numbers $z_1 and z_2, are\left(z_1\right) - arg\left(z_2\right) = 0$, then show that $\left|z_1 - z_2\right| = | = |\left|z_1\right| - \left|z_2\right| |$.

A. $\left|z_1\right| + \left|z_2\right|$

B. $\left|z_1\right| - \left|z_2\right|$

C. $\left|\left|z_1\right| - \left|z_2 | |\right.\right.$

D. 0

Answer: C

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28. If $\left|\frac{z_1}{z_2}\right| = 1$ and $arg\left(z_1 z_2\right) = 0$, then a. $z_1 = z_2$ b. $\left|z_2\right|^2 = z_1 \cdot z_2$ $c. z_1 \cdot z_2 = 1$ d. none of these

A. $z_1 = z_2$

B. $\left|z_2\right|^2 = z_1 z_2$

C. $z_1 z_2 = 1$

D. more than 8

Answer: B

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29. Suppose A is a complex number and $n \in N$, such that $A^n = (A+1)^n = 1$, then the least value of n is 3 b. 6 c. 9 d. 12

A. 3

B. 6

C. 9

D. 12

Answer: B

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30. about to only mathematics

A. 4

B. 6

C. 8

D. more than 8

Answer: C

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31. Let z, w be complex numbers such that $\bar{z} + i\bar{w} = 0$ and $argzw = \pi$ Then $argz$ equals

A. $\frac{\pi}{4}$

B. $\frac{\pi}{2}$

C. $\frac{3\pi}{4}$

D. $\frac{5\pi}{4}$

Answer: C

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32. If $z = (3 + 7i)(a + ib)$, where $a, b \in Z$ - $\{0\}$, is purely imaginery, then minimum value of $|z|^2$ is

A. 74

B. 45

C. 58

D. 65

Answer: C

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33. about to only mathematics

A. $4m\pi$

B. $\frac{2m\pi}{n(n+1)}$

C. $\frac{4m\pi}{n(n+1)}$

D. $\frac{m\pi}{n(n+1)}$

Answer: C

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34. Given $z = \left(1 + i\sqrt{3}\right)^{100}$, then $[RE(z)/IM(z)]$ equals 2^{100} b. 2^{50} c. $\frac{1}{\sqrt{3}}$ d. $\sqrt{3}$

A. 2^{100}

B. 2^{50}

C. $\frac{1}{\sqrt{3}}$

D. $\sqrt{3}$

Answer: C

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35. The expression $\left[\frac{1+\sin\left(\frac{\pi}{8}\right)+i\cos\left(\frac{\pi}{8}\right)}{1+\sin\left(\frac{\pi}{8}\right)-i\cos\left(\frac{\pi}{8}\right)}\right]^8$ is equal is

A. 1

B. -1

C. i

D. $-i$

Answer: B

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36. The number of complex numbers z satisfying $|z-3-i|=|z-9-i| and |z-3+3i|=3$ are a. one b. two c. four d. none of these

A. one

B. two

C. four

D. none of these

Answer: A

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37. $P(z)$ be a variable point in the Argand plane such that $|z| = m \in i\mu m\{|z - 1, |z + 1|\}, thenz + z$ will be equal to a. -1 or 1 b. 1 but not equal to-1 c. -1 but not equal to 1 d. none of these

A. -1 or 1

B. 1 but not equal to -1

C. -1 but not equal to 1

D. none of these

Answer: A

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38. If $\left|z^2 - 1\right| = |z|^2 + 1$, then z lies on (a) The Real axis (b)The imaginary axis (c)A circle (d)An ellipse

A. a circle

B. a parabola

C. an ellipse

D. none of these

Answer: D

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39. about to only mathematics

A. 0

B. 1

C. 2

D. 3

Answer: B

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40. about to only mathematics

A. 2

B. 3

C. 6

D. 5

Answer: D

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41. Number of ordered pairs (s), (a, b) of real numbers such that $(a + ib)^{2008} = a - ib$ holds good is

A. 2008

B. 2009

C. 2010

D. 1

Answer: C

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42. The equation $az^3 + bz^2 + \bar{b}z + \bar{a} = 0$ has a root α, where a, b,z and α belong to the set of complex numbers. The number value of $|\alpha|$

A. is 1/2

B. is 1

C. is 2

D. can't be determined

Answer: B

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43. If $k > 0$, $|z| = |w| = k$, and $\alpha = \frac{z - \bar{w}}{k^2 + z\bar{w}}$, then $Re(\alpha)$ (A) 0 (B) $\frac{k}{2}$ (C) k (D) None of these

A. 0

B. $k/2$

C. k

D. none of these

Answer: A

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44. $z_1 and z_2$ are two distinct points in an Argand plane. If $a\left|z_1\right| = b\left|z_2\right| (where a, b \in R)$, then the point $\left(az_1/bz_2\right) + \left(bz_2/az_1\right)$ is a point on the line segment [-2, 2] of

the real axis line segment [-2, 2] of the imaginary axis unit circle $|z| = 1$ the line with $argz = \tan^{-1}2$

A. line segment $[-2, 2]$ of the real axis

B. line segment $[-2, 2]$ of the imaginary axis

C. unit circle $|z| = 1$

D. the line with $\arg z = \tan^{-1}2$

Answer: A

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45. If z is a comple number such that $-\frac{\pi}{2} < \arg z \leq \frac{\pi}{2}$, then which of the following inequalities is ture ?

A. $\left|z - \bar{z}\right| \leq |z|\left(argz - arg\bar{z}\right)$

B. $\left|z - \bar{z}\right| \geq |z|\left(argz - arg\bar{z}\right)$

C. $\left|z - \bar{z}\right| < \left(argz - arg\bar{z}\right)$

D. None of these

Answer: A

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46. If $\cos\alpha + 2\cos\beta + 3\cos\gamma = \sin\alpha + 2\sin\beta + 3\sin\gamma y = 0$, then the value of $\sin 3\alpha + 8\sin 3\beta + 27\sin 3\gamma$ is

A. $\sin(a + b + \gamma)$

B. $3\sin(\alpha + \beta + \gamma)$

C. $18\sin(\alpha + \beta + \gamma)$

D. $\sin(\alpha + \beta + \gamma)$

Answer: C

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47. If α, β be the roots of the equation $u^2 - 2u + 2 = 0$ and if $\cot\theta = x + 1$, then $\frac{(x+\alpha)^n - (x+\beta)^n}{\alpha - \beta}$ is equal to (a) $\begin{pmatrix} \sin n\theta \\ \sin^n\theta \end{pmatrix}$ (b) $\begin{pmatrix} \cos n\theta \\ \cos^n\theta \end{pmatrix}$ (c) $\left((\sin n\theta), \cos^n\theta\right)\Big)$ (d) $\begin{pmatrix} \cos n\theta \\ \sin\theta^n\theta \end{pmatrix}$

A. $\frac{\sin nn\theta}{\sin^n\theta}$

B. $\frac{\cos n\theta}{\cos^n\theta}$

C. $\frac{\sin n\theta}{\cos^n\theta}$

D. $\frac{\cos n\theta}{\sin^n\theta}$

Answer: A

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48. If $z = (i)^{i} \wedge (((i)))where i = \sqrt{-1}, then |z|$ is equal to 1 b. $e^{-\pi/2}$ c. $e^{-\pi}$ d. none of these

A. 1

B. $e^{-\pi/2}$

C. $e^{-\pi}$

D. none of these

Answer: A

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49. If $z = i\log\left(2 - \sqrt{3}\right)$, then $\cos z =$

A. -1

B. $-1/2$

C. 1

D. 2

Answer: D

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50. If $|z| = 1$, then the point representing the complex number $-1 + 3z$ will lie on a. a circle b. a parabola c. a straight line d. a hyperbola

A. a circle

B. a straight line

C. a parabola

D. a hyperbola

Answer: A

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51. The locus of point z satisfying $Re\left(\frac{1}{z}\right) = k, wherek$ is a non zero real number, is a. a straight line b. a circle c. an ellipse d. a hyperbola

A. a stringht line

B. a circle

C. an ellispe

D. a hyperbola

Answer: B

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52. If z is complex number, then the locus of z satisfying the condition $|2z - 1| = |z - 1|$ is perpendicular bisector of line segment joining 1/2 and 1 circle parabola none of the above curves

A. perpeciular bisector of line segment joining 1/2 and 1

B. circle

C. parabola

D. none of the above curves

Answer: B

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53. The greatest positive argument of complex number satisfying $|z - 4| = Re(z)$ is $\frac{\pi}{3}$ b. $\frac{2\pi}{3}$ c. $\frac{\pi}{2}$ d. $\frac{\pi}{4}$

A. $\frac{\pi}{3}$

B. $\frac{2\pi}{3}$

C. $\frac{\pi}{2}$

D. $\frac{\pi}{4}$

Answer: D

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54. If $tandc$ are two complex numbers such that $|t| \neq |c|, |t| = 1andz = (at + b)/(t - c), z = x + iy$. Locus of z is (where a, b are complex numbers) a. line segment b. straight line c. circle d. none of these

A. line segment

B. straight line

C. circle

D. none of these

Answer: C

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55. If $z^2 + z|z| + \left|z^2\right| = 0,$ then the locus z is a. a circle b. a straight line c. a pair of straight line d. none of these

A. a circle

B. a straight line

C. a pair of straing line

D. none of these

Answer: C

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56. Let C_1 and C_2 are concentric circles of radius 1 and $\frac{8}{3}$ respectively having centre at $(3, 0)$ on the argand plane. If the complex number z satisfies the inequality $\log_{\frac{1}{3}}\left(\frac{|z-3|^2+2}{11|z-3|-2}\right) > 1$, then (a) z lies outside C_1 but inside C_2 (b) z line inside of both C_1 and C_2 (c) z line outside both C_1 and C_2 (d) none of these

A. z lies outside C_1 but inside C_2

B. z line inside of both C_1 and C_2

C. z line outside both C_1 and C_2

D. none of these

Answer: A

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57. about to only mathematics

A. a pair of straing lines

B. circle

C. parabola

D. ellispe

Answer: C

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58. If $|z - 1| \leq 2 and \left|\omega z - 1 - \omega^2\right| = a \quad \left(where \omega is a cube \sqrt[o]{-} funity\right)$,

then complete set of values of a

A. $0 \leq a \leq 2$

B. $\frac{1}{2} \leq a \leq \frac{\sqrt{3}}{2}$

C. $\frac{\sqrt{3}}{2} - \frac{1}{2} \leq a \leq \frac{1}{2} + \frac{\sqrt{3}}{2}$

D. $0 \leq a \leq 4$

Answer: D

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59. If $\left|z^2 - 3\right| = 3|z|$, then the maximum value of $|z|$ is 1 b. $\frac{3 + \sqrt{21}}{2}$ c. $\frac{\sqrt{21} - 3}{2}$ d. none of these

A. 1

B. $\frac{3 + \sqrt{21}}{2}$

C. $\frac{\sqrt{21} - 3}{2}$

D. none of these

Answer: B

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60. If $|2z - 1| = |z - 2| and z_1, z_2, z_3$ are complex numbers such that

`|z_1-alpha||z|d. >2|z|`

A. $< |z|$

B. $< 2|z|$

C. $> |z|$

D. $> 2|z|$

Answer: B

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61. If z_1 is a root of the equation $a_0 z^n + a_1 z^{n-1} + \ + a_{n-1} z + a_n = 3, where \left|a_i\right| < 2f$ or $i = 0, 1, , n, then$ $|z| = \frac{3}{2}$ b. $|z| < \frac{1}{4}$ c.$|z| > \frac{1}{4}$ d. $|z| < \frac{1}{3}$

A. $\left|z_1\right| > \frac{1}{2}$

B. $\left|z_1\right| < \frac{1}{2}$

C. $\left|z_1\right| > \frac{1}{4}$

D. $|z| < \frac{1}{2}$

Answer: A

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62. If $|z| < \sqrt{2} - 1, then \left|z^2 + 2z\cos\alpha\right| is$ a. less than 1 b. $\sqrt{2} + 1$ c. $\sqrt{2} - 1$ d. none of these

A. less than 1

B. $\sqrt{2} + 1$

C. $\sqrt{2 - 1}$

D. none of these

Answer: A

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63. Let $\left|Z_r - r\right| \leq r$, for all $r = 1, 2, 3\ldots., n$. Then $\left|\sum_{r=1}^{n} z_r\right|$ is less than

A. n

B. 2n

C. n(n+1)

D. $\frac{n(n+1)}{2}$

Answer: C

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64. All the roots of the equation $1lz^{10} + 10iz^9 + 10iz - 11 = 0$ lie

A. inside $|z| = 1$

B. one $|z| = 1$

C. outside $|z| = 1$

D. cannot say

Answer: B

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65. Let $\lambda \in R$. If the origin and the non-real roots of $2z^2 + 2z + \lambda = 0$ form the three vertices of an equilateral triangle in the Argand lane, then λ is 1 b. $\frac{2}{3}$ c. 2 d. -1

A. 1

B. $\frac{2}{3}$

C. 2

D. -1

Answer: B

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66. The roots of the equation $t^3 + 3at^2 + 3bt + c = 0 are z_1, z_2, z_3$ which represent the vertices of an equilateral triangle. Then $a^2 = 3b$ b. $b^2 = a$ c. $a^2 = b$ d. $b^2 = 3a$

A. $a^2 = 3b$

B. $b^2 = a$

C. $a^2 = a$

D. $b^2 = 3a$

Answer: C

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67. The roots of the cubic equation $(z + ab)^3 = a^3, a \neq 0$ represents the vertices of an equilateral triangle of sides of length

A. $\frac{1}{\sqrt{3}}|ab|$

B. $\sqrt{3}|a|$

C. $\sqrt{3}|b|$

D. $|a|$

Answer: B

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68. If $\left|z_1\right| + \left|z_2\right| = 1 and z_1 + z_2 + z_3 = 0$ then the area of the triangle whose vertices are z_1, z_2, z_3 is $3\sqrt{3}/4$ b. $\sqrt{3}/4$ c. 1 d. 2

A. $3\sqrt{3/4}$

B. $\sqrt{3/4}$

C. 1

D. 2

Answer: A

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69. Let $zand\omega$ be two complex numbers such that $|z| \leq 1, |\omega| \leq 1and|z - i\omega| = |z - i\omega| = 2, thenz$ equals 1 or i b. i or $-i$ c. 1 or -1 d. i or -1

A. $\frac{2}{3}$

B. $\frac{\sqrt{5}}{3}$

C. $\frac{3}{2}$

D. $\frac{2\sqrt{5}}{3}$

Answer: C

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70. Let z_1, z_2, z_3, z_4 are distinct complex numbers satisfying $|z| = 1$ and $4z_3 = 3(z_1 + z_2)$, then $|z_1 - z_2|$ is equal to

A. 1 or i

B. i or $-i$

C. 1 or i

D. i or -1

Answer: D

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71. z_1, z_2, z_3, z_4 are distinct complex numbers representing the vertices of a quadrilateral $ABCD$ taken in order. If $z_1 - z_4 = z_2 - z_3$ and $\arg\left[(z_4 - z_1)/(z_2 - z_1)\right] = \pi/2$, the quadrilateral is

A. rectangle

B. rhombus

C. square

D. trapezium

Answer: A

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72. If $k + \left|k + z^2\right| = |z|^2 \left(k \in R^-\right)$, then possible argument of z is

A. 0

B. π

C. $\pi/2$

D. none of these

Answer: C

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73. If z_1, z_2, z_3 are the vertices of an equilational triangle ABC such that $|z_1 - i| = |z_2 - i| = |z_3 - i|$, then $|z_1 + z_2 + z_3|$ equals to

A. $3\sqrt{3}$

B. $\sqrt{3}$

C. 3

D. $\frac{1}{3\sqrt{3}}$

Answer: C

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74. If z is a complex number having least absolute value and $|z - 2 + 2i = 1, then z =$ $\left(2 - 1/\sqrt{2}\right)(1 - i)$ b. $\left(2 - 1/\sqrt{2}\right)(1 + i)$ c. $\left(2 + 1/\sqrt{2}\right)(1 - i)$ d. $\left(2 + 1/\sqrt{2}\right)(1 + i)$

A. $\left(2 - 1/\sqrt{2}\right)(1 - i)$

B. $\left(2 - 1/\sqrt{2}\right)(1 + i)$

C. $\left(2 + 1/\sqrt{2}(1 - i)\right.$

D. $\left(2 + 1/\sqrt{2}\right)(1 + i)$

Answer: A

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75. If z is a complex number lying in the fourth quadrant of Argand plane and $\left|\left[\frac{kz}{k+1}\right] + 2i\right| > \sqrt{2}$ for all real value of

$k(k \neq -1)$, then range of $\arg(z)$ is $\left(\frac{\pi}{8}, 0\right)$ b. $\left(\frac{\pi}{6}, 0\right)$ c. $\left(\frac{\pi}{4}, 0\right)$ d. none of these

A. $\left(-\frac{\pi}{8}, 0\right)$

B. $\left(-\frac{\pi}{6}, 0\right)$

C. $\left(-\frac{\pi}{4}, 0\right)$

D. None of these

Answer: C

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76. If $\left|z_2 + iz_1\right| = \left|z_1\right| + \left|z_2\right| and \left|z_1\right| = 3 and \left|z_2\right| = 4$, then the area of ABC, if affixes of $A, B, and Carez_1, z_2, and \left[\left(z_2 - iz_1\right)/(1 - i)\right]$ respectively, is $\frac{5}{2}$ b. 0 c. $\frac{25}{2}$ d. $\frac{25}{4}$

A. $\frac{5}{2}$

B. 0

C. $\frac{25}{2}$

D. $\frac{25}{4}$

Answer: D

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77. If a complex number z satisfies $|2z + 10 + 10i| \leq 5\sqrt{3} - 5$, then the least principal argument of z is

A. $-\frac{5\pi}{6}$

B. $-\frac{11\pi}{12}$

C. $-\frac{3\pi}{4}$

D. $-\frac{2\pi}{3}$

Answer: A

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78. about to only mathematics

A. $\frac{\pi}{3}$

B. $\frac{\pi}{4}$

C. $\frac{\pi}{6}$

D. $\frac{\pi}{2}$

Answer: B

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79. $z_1 and z_2$ lie on a circle with center at the origin. The point of intersection z_3 of he tangents at $z_1 and z_2$ is given by $\frac{1}{2}\left(z_1 + (z)_2\right)$

b. $\frac{2z_1z_2}{z_1 + z_2}$ c. $\frac{1}{2}\left(\frac{1}{z_1} + \frac{1}{z_2}\right)$ d. $\frac{z_1 + z_2}{(z)_1(z)_2}$

A. $\frac{1}{2}\left(\bar{z}_1 + \bar{z}_2\right)$

B. $\frac{2z_1z_2}{z_1 + z_2}$

C.

D.

Answer: B

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80. If $\arg\left(\frac{z_1 - \frac{z}{|z|}}{\frac{z}{|z|}}\right) = \frac{\pi}{2}$ and $\left|\frac{z}{|z|} - z_1\right| = 3$, then $\left|z_1\right|$ equals to a. $\sqrt{3}$ b. $2\sqrt{2}$ c. $\sqrt{10}$ d. $\sqrt{26}$

A. $\sqrt{26}$

B. $\sqrt{10}$

C. $\sqrt{3}$

D. $2\sqrt{2}$

Answer: B

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A. $\frac{1}{2}\left|z_1 - z_2\right|^2$

B. $\frac{1}{2}\left|z_1 - z_2\right| r$

C. $\frac{1}{2}\left|z_1 - z_2\right|^2 r^2$

D. $\frac{1}{2}\left|z_1 - z_2\right|^2$

Answer: B

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82. Consider the region S of complex numbers a such that $\left|z^2 - az + 1\right| = 1$, where $|z| = 1$. Then area of S in the Argand plane is

A. $\pi + 8$

B. $\pi + 4$

C. $2\pi + 4$

D. $\pi + 6$

Answer: A

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83. about to only mathematics

A. $e^{i\theta}$

B. $e^{-i\theta}$

C. $\omega, \bar{\omega}$

D. $\omega + \bar{\omega}$

Answer: D

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84. If $pandq$ are distinct prime numbers, then the number of distinct imaginary numbers which are pth as well as qth roots of unity are. $\min(p, q)$ b. $\min(p, q)$ c. 1 d. $zero$

A. min(p,q)

B. max(p,q)

C. 1

D. zero

Answer: D

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85. Given z is a complex number with modulus 1. Then the equation $[(1 + ia)/(1 - ia)]^4 = z$ has all roots real and distinct two

real and two imaginary three roots two imaginary one root real and three imaginary

A. all roots real and distinct

B. two real and tw imaginary

C. three roots real and one imaginary

D. one root real and three imaginary

Answer: A

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86. The value of z satisfying the equation $\log z + \log z^2 + \dot{} + \log z^n = 0 is$

A. $\cos. \frac{4m\pi}{n(n+1)} + i\sin. \frac{4m\pi}{n(n+1)}, m = 0, 1, 2, ...$

B. $\cos. \frac{4m\pi}{n(n+1)} - i\sin. \frac{4m\pi}{n(n+1)}, m = 0, 1, 2, ...$

C. $\sin. \frac{4m\pi}{n} + i\cos. \frac{4m\pi}{n}, m = 0, 1, 2, ...$

D. 0

Answer: A

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87. If $n \in N > 1$, then the sum of real part of roots of $z^n = (z + 1)^n$ is equal to

A. $\frac{n}{2}$

B. $\frac{(n - 1)}{2}$

C. $-\frac{n}{2}$

D. $\frac{(1 - n)}{2}$

Answer: D

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88. Which of the following represents a points in an Argand pane, equidistant from the roots of the equation $(z+1)^4 = 16z^4$? $(0, 0)$ b. $\left(-\frac{1}{3}, 0\right)$ c. $\left(\frac{1}{3}, 0\right)$ d. $\left(0, \frac{2}{\sqrt{5}}\right)$

A. $(0, 0)$

B. $\left(-\frac{1}{3}, 0\right)$

C. $\left(\frac{1}{3}, 0\right)$

D. $\left(0, \frac{2}{\sqrt{5}}\right)$

Answer: C

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89. Let a be a complex number such that $|a| < 1 and z_1, z_2, z_3, \ldots$ be the vertices of a polygon such that $z_k = 1 + a + a^2 + \ldots + a^{k-1}$ for all $k = 1, 2, 3, Then z_1, z_2$ lie within the circle (a) $\left|z - \frac{1}{1-a}\right| = \frac{1}{|a-1|}$ (b) $\left|z + \frac{1}{a+1}\right| = \frac{1}{|a+1|}$ (c) $\left|z - \frac{1}{1-a}\right| = |a-1|$ (d) $\left|z + \frac{1}{a+1}\right| = |a+1|$

A. $\left|z - \frac{1}{1-a}\right| = \frac{1}{|a-1|}$

B. $\left|z + \frac{1}{a+1}\right| = \frac{1}{|a+1|}$

C. $\left|z - \frac{1}{1-a}\right| = |a-1|$

D. $\left|z + \frac{1}{1-a}\right| = |a-1|$

Answer: A

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90. Let $z = x + iy$ be a complex number where $xandy$ are integers. Then, the area of the rectangle whose vertices are the roots of the equation $zz^3 + zz^3 = 350$ is 48 (b) 32 (c) 40 (d) 80

A. 48

B. 32

C. 40

D. 80

Answer: A

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91. Let z be a complex number such that the imaginary part of z is nonzero and a = z2 + z + 1 is real. Then a cannot take the value (A) –1 (B) 1 3 (C) 1 2 (D) 3 4

A. -1

B. $\frac{1}{3}$

C. $\frac{1}{2}$

D. $\frac{3}{4}$

Answer: D

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92. Let complex numbers α and $\frac{1}{\alpha}$ lies on circle $(x - x_0)^2 + (y - y_0)^2 = r^2$ and $(x - x_0)^2 + (y - y_0)^2 = 4r^2$ respectively. If $z_0 = x_0 + iy_0$ satisfies the equation $2|z_0|^2 = r^2 + 2$ then $|\alpha|$ is equal to

A. $1/\sqrt{2}$

B. $1/2$

C. $1/\sqrt{7}$

D. $1/3$

Answer: C

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MULTIPLE CORRECT ANSWERS TYPE

1. If $z = \omega, \omega^2 where \omega$ is a non-real complex cube root of unity, are two vertices of an equilateral triangle in the Argand plane, then the third vertex may be represented by $z = 1$ b. $z = 0$ c. $z = -2$ d. $z = -1$

A. $z = 1$

B. $z = 0$

C. $z = -2$

D. $z = -1$

Answer: A::C

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2. If $amp\left(z_1 z_2\right) = 0 and \left|z_1\right| = \left|z_2\right| = 1, then\ z_1 + z_2 = 0$ b. $z_1 z_2 = 1$ c. $z_1 = z_2$ d. none of these

A. $z_1 + z_2 = 0$

B. $z_1 z_2 = 1$

C. $z_1 = \bar{z}_2$

D. none of these

Answer: B::C

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3. If $\sqrt{5 - 12i} + \sqrt{-5 - 12i} = z$, then principal value of $argz$ can be

A. $-\frac{\pi}{4}$

B. $\frac{\pi}{4}$

C. $\frac{3\pi}{4}$

D. $-\frac{3\pi}{4}$

Answer: A::B::C::D

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4. Values $(s)(-i)^{1/3}$ is/are $\frac{\sqrt{3} - i}{2}$ b. $\frac{\sqrt{3} + i}{2}$ c. $\frac{-\sqrt{3} - i}{2}$ d. $\frac{-\sqrt{3} + i}{2}$

A. $s\frac{\sqrt{3} - i}{2}$

B. $\frac{\sqrt{3}+i}{2}$

C. $\frac{-\sqrt{3}-i}{2}$

D. $\frac{-\sqrt{3}+i}{2}$

Answer: A::C

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5. If $a^3+b^3+6abc=8c^3 \& \omega$ is a cube root of unity then: (a)a, b, c are in $A.P.$ (b) $a, b, c,$ are in $H.P.$ (c) $a+b\omega-2c\omega^2=0$ (d) $a+b\omega^2-2c\omega=0$

A. a, c, b are in A.P

B. a,c,b are in H.P

C. $a+b\omega-2c\omega^2=0$

D. $a + b\omega^2 - 2c\omega = 0$

Answer: A::C::D

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6. Let z_1 and z_2 be two non -zero complex number such that $|z_1 + z_2| = |z_1| = |z_2|$. Then $\frac{z_1}{z_2}$ can be equal to (ω is imaginary cube root of unity).

A. $1 + \omega$

B. $1 + \omega^2$

C. ω

D. ω^2

Answer: C::D

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7. If $p = a + b\omega + c\omega^2$, $q = b + c\omega + a\omega^2$, and $r = c + a\omega + b\omega^2$, where $a, b, c \neq 0$ and ω is the complex cube root of unity, then (a) $p + q + r = a + b + c$ (b) $p^2 + z^2 + r^2 = a^2 + b^2 + c^2$ (c) $p^2 + z^2 + r^2 = -2(pq + qr + rp)$ (d) none of these

A. If p,q,r lie on the circle |z|=2, the trinagle formed by these point is equilateral.

B. $p^2 + q^2 + r^2 = a^2 + b^2 + c^2$

C. $p^2 + q^2 + r^2 = 2(pq + qr + rp)$

D. none of these

Answer: A::C

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8. Let P(x) and Q(x) be two polynomials.Suppose that $f(x) = P\left(x^3\right) + xQ\left(x^3\right)$ is divisible by $x^2 + x + 1$, then (a) P(x) is divisible by (x-1),but Q(x) is not divisible by x -1 (b) Q(x) is divisible by (x-1), but P(x) is not divisible by x-1 (c) Both P(x) and Q(x) are divisible by x-1 (d) f(x) is divisible by x-1

A. P(x) is divisible by (x-1),but Q(x) is not divisible by x -1

B. Q(x) is divisible by (x-1), but P(x) is not divisible by x-1

C. Both P(x) and Q(x) are divisible by x-1

D. f(x) is divisible by x-1

Answer: C::D

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9. If α is a complex constant such that $az^2 + z + \alpha = 0$ has a ral root, then $\alpha + \alpha = 1$ $\alpha + \alpha = 0$ $\alpha + \alpha = -1$ the absolute value of the real root is 1

A. $alph + \bar{\alpha} = 1$

B. $\alpha + \bar{\alpha} = 0$

C. $\alpha + \bar{\alpha} = -1$

D. the absolute value of the real root is 1

Answer: A::C::D

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10. If $z^3 + (3 + 2i)z + (-1 + ia) = 0$ has one real roots, then the value of a lies in the interval $(a \in R)$ $(-2, 1)$ b. $(-1, 0)$ c. $(0, 1)$ d. $(-2, 3)$

A. $(2, -1)$

B. $(-1, 0)$

C. $(0, 1)$

D. $(-2, 3)$

Answer: A::B::D

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11. Given that the complex numbers which satisfy the equation $\left|z\bar{z}^3\right| + \left|\bar{z}z^3\right| = 350$ form a rectangle in the Argand plane with the length of its diagonal having an integral number of units, then area of rectangle is 48 sq. units if z_1, z_2, z_3, z_4 are vertices of rectangle, then $z_1 + z_2 + z_3 + z_4 = 0$ rectangle is symmetrical about the real axis $arg\left(z_1 - z_3\right) = \frac{\pi}{4}$ or $\frac{3\pi}{4}$

A. area of rectangle is 48 sq units.

B. if z_1, z_2, z_3, z_4 are vertices of rectangle, then

$$z_1 + z_2 + z_3 + z_4 = 0$$

C. rectangle is symmetrical about the real axis .

D. None of these

Answer: A::B::C

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12. If the points $A(z), B(-z), andC(1-z)$ are the vertices of an equilateral triangle $ABC,$ then sum of possible z is 1/2 sum of possible z is 1 product of possible z is 1/4 product of possible z is

A. sum of possible z is $1/2$

B. sum of possible z is

C. product of possible z is $1/4$

D. product of possibble z is $1/2$.

Answer: A::C

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13. If $a|z - 3| = \min\{|z1, |z - 5|\}, then Re(z)$ equals to 2 b. $\frac{5}{2}$ c. $\frac{7}{2}$ d. 4

A. 2

B. $\frac{5}{2}$

C. $\frac{7}{2}$

D. 4

Answer: A::D

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14. If z_1, z_2 are tow complex numberes $\left(z_1 \neq z_2\right)$ satisfying $\left|z_1^2 - z_2^2\right| = \left|\bar{z}_1^2 + \bar{z}_2^2 - 2\bar{z}_1\bar{z}_2\right|$, then

A. $\frac{z_1}{z_2}$ is purely imaginary

B. $\frac{z_1}{z_2}$ is purely real

C. $\left|argz_1 - argz_2\right| = \pi$

D. $\left|argz_1 - argz_2\right| = \frac{\pi}{2}$

Answer: A::D

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15. If $z_1 = a + ib$ and $z_2 = c + id$ are complex numbers such that $\left|z_1\right| = \left|z_2\right| = 1$ and $Re\left(z_1\bar{z}_2\right) = 0$, then the pair ofcomplex

nunmbers $\omega_1 = a + ic$ and $\omega_2 = b + id$ satisfies

A. $\left|\omega_1\right| = 1$

B. $\left|\omega_2\right| = 1$

C. $Re\left(\omega_1\bar{\omega}_2\right) = 0$

D. $Im\left(\omega_1\bar{\omega}_2\right) = 0$

Answer: A::B::C

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16. Let $z_1 and z_2$ be complex numbers such that $z_1 \neq z_2$ and $\left|z_1\right| = \left|z_2\right|$. If z_1 has positive real part and z_2 has negative imaginary part, then $\frac{z_1 + z_2}{z_1 - z_2}$ may be (a)zero (b) real and positive (c)real and negative (d) purely imaginary

A. zero

B. real and positive

C. real and negative

D. purely imaginary

Answer: A::D

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17. If $|z_1| = \sqrt{2}$, $|z_2| = \sqrt{3}$ and $|z_1 + z_2| = \sqrt{(5 - 2\sqrt{3})}$ then arg $\left(\frac{z_1}{z_2}\right)$ (not neccessarily principal) is (a) $\frac{3\pi}{4}$ (b) $\frac{2\pi}{3}$ (c) $\frac{5\pi}{4}$ (d) $\frac{5\pi}{2}$

A. $\frac{3\pi}{4}$

B. $\frac{2\pi}{3}$

C. $\frac{5\pi}{4}$

D. $\frac{5}{2}$

Answer: A::C

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18. Let four points z_1, z_2, z_3, z_4 be in complex plane such that $|z_2| = 1$, $|z_1| \leq 1$ and $|z_3| \leq 1$. If $z_3 = \frac{z_2(z_1 - z_4)}{\bar{z}_1 z_4 - 1}$, then $|z_4|$ can be (a) 2 (b) $\frac{2}{5}$ (c) $\frac{1}{3}$ (d) $\frac{5}{2}$

A. 2

B. $\frac{2}{5}$

C. $\frac{1}{3}$

D. $\frac{5}{2}$

Answer: B::C

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19. A rectangle of maximum area is inscribed in the circle $|z - 3 - 4i| = 1$. If one vertex of the rectangle is $4 + 4i$, then another adjacent vertex of this rectangle can be a. $2 + 4i$ b. $3 + 5i$ c. $3 + 3i$ d. $3 - 3i$

A. $2 + 4i$

B. $3 + 5i$

C. $3 + 3i$

D. $3 - 3i$

Answer: B::C

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20. If $\left|z_1\right| = 15$ and $\left|z_2 - 3 - 4i\right| = 5$, *then*

A. $\left|z_1 - z_2\right|_{\min} = 5$

B. $\left|z_1 - z_2\right|_{\min} = 10$

C. $\left|z_1 - z_2\right|_{\min} = 20$

D. $\left|z_1 - z_2\right|_{\min} = 25$

Answer: A::D

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21. If $P\left(z_1\right), Q\left(z_2\right), R\left(z_3\right)$ and $S\left(z_4\right)$ are four complex numbers representing the vertices of a rhombus taken in order on the complex plane, which one of the following is held good?

A. $\dfrac{z_1 - z_4}{z_2 - z_3}$ is purely real

B. $amp\frac{z_1 - z_4}{z_2 - z_4} = amp\frac{z_2 - z_4}{z_3 - z_4}$

C. $\frac{z_1 - z_3}{z_2 - z_4}$ is pureluy imaginary

D. is not necessary that $\left|z_1 - z_3\right| \neq \left|z_2 - z_4\right|$

Answer: A::B::C::D

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22. about to only mathematics

A. $|z| = a$

B. $|z| = 2a$

C. $arg(z) = \frac{\pi}{2}$

D. $arg(z) = \frac{\pi}{3}$

Answer: A::D

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23. If a complex number z satisfies $|z| = 1$ and $arg(z - 1) = \frac{2\pi}{3}$, then ($\omega$ is complex imaginary number)

A. $z^2 + z$ is purely imaginary number

B. $z = -\omega^2$

C. $z = -\omega$

D. $|z - 1| = 1$ then,

Answer: A::B::D

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24. If $|z - 1| = 1$, then

A. $arg((z - 1 - i)/z)$ can be equal to $-\pi/4$

B. $(z - 2)/z$ is purely imaaginary number

C. $(z - 2)/z$ is purely real number

D. if $arg(z) = \theta$, where $z \neq 0$ and θ is acute, then

$1 - 2/z = i\tan\theta$

Answer: A::B::D

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25. If $z_1 = 5 + 12i$ and $|z_2| = 4$, then

A. maximum $\left(|z_1 + iz_2|\right) = 17$

B. minimum $\left(|z_1 + (1 + i)z_2|\right) = 13 - 4\sqrt{2}$

C. minimum $\left|\frac{z_1}{z_2+\frac{4}{z_2}}\right| = \frac{13}{4}$

D. maximum $\left|\frac{z_1}{z_2+\frac{4}{z_2}}\right| = \frac{13}{3}$

Answer: A::B::D

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26. Let z_1, z_2, z_3 be the three nonzero comple numbers such that

$z_1 \neq 1, a = |z_1|, b = |z_2|$ and $c = |z_3|$. Let $\begin{vmatrix} a & b & c \\ b & c & a \\ c & a & b \end{vmatrix} = 0$ Then

A. $arg\left(\frac{z_3}{z_2}\right) = arg\left(\frac{z_3 - z_1}{z_2 - z_1}\right)$

B. ortho centre of triangle formed by z_1, z_2, z_3 is $z_1 + z_2 + z_3$

C. if trinagle formed by z_1, z_2, z_3 is $z_1 + z_2 + z_3$ is $\frac{3\sqrt{3}}{2}\left|z_1\right|^2$

D. if triangle formed by z_1, z_2, z_3 is equlateral, then

$z_1 + z_2 + z_3 = 0$

Answer: A::B::D

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27. z_1 and z_2 are the roots of the equation $z^2 - az + b = 0$, where $\left|z_1\right| = \left|z_2\right| = 1$ and a, b are non-zero complex numbers, then

A. $|a| \leq 1$

B. $|a| \leq 2$

C. $2arg(a) = arg(b)$

D. $agra = 2arg(b)$

Answer: B::C

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28. If $\left|\left(z - z_1\right)/\left(z - z_2\right)\right| = 3$, where z_1 and z_2 are fixed complex numbers and z is a variable complex complex number, then z lies on a

A. circle with z_1 as its interior point

B. circle with z_2 as its interior point

C. circle with z_1 as its exterior point

D. circle with z_2 as its exterior point

Answer: B::C

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29. If $z = x + iy$, then the equation $\left|\frac{2z - i}{z + 1}\right| = m$ does not represents a circle, when m is (a) $\frac{1}{2}$ (b). 1 (c). 2 (d). `3

A. $1/2$

B. 1

C. 2

D. 3

Answer: A::B::C

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30. System of equaitons $|z + 3| - |z - 3| = 6$ and $|z - 4| = r$ where $r \in R^+$ has

A. one solution if $r > 1$

B. one solution if $r < 1$

C. two solutions if $r = 1$

D. at leat one solution

Answer: A::C::D

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31. Let the equation of a ray be $|z - 2| - |z - 1 - i| = \sqrt{2}$. If it strikes the y-axis, then the equation of reflected ray (including or excluding the point of incidence) is .

A. $arg(z - 2i) = \frac{\pi}{4}$

B. $|z - 2i| - |z - 3 - i| = \sqrt{2}$

C. $arg(z - 2i) = \frac{3\pi}{4}$

D. $|z - 1i| - |z - 1 - 3i| = 2\sqrt{2}$

Answer: A::B

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32. Given that the two curves $arg(z) = \frac{\pi}{6}$ and $\left|z - 2\sqrt{3}i\right| = r$ intersect in two distinct points, then a. $[r] \neq 2$ b. $0 < r < 3$ c. $r = 6$ d. $3 < r < 2\sqrt{3}$ (Note : [r] represents integral part of r)

A. $[r] \neq 2$ where [.] represents greatest integer

B. $0 < r < 3$

C. $r = 6$

D. $3 < r < 2\sqrt{3}$

Answer: A::D

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33. On the Argand plane ,let $z_1 = -2 + 3z, z_2 = -2 - 3z$ and $|z| = 1$. Then (a) z 1 moves on circle with centre at (− 2 , 0) and radius 3 (b) z 1 and z 2 describle the same locus (c) z 1 and z 2 move on differenet circles (d) z 1 − z 2 moves on a circle concetric with | z | = 1

A. z_1 moves on circle with centre at $(-2, 0)$ and radius 3

B. z_1 and z_2 describle the same locus

C. z_1 and z_2 move on differenet circles

D. $z_1 - z_2$ moves on a circle concetric with $|z| = 1$

Answer: A::B::D

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34. Let $S = \left\{z : x = x + iy, y \geq 0, \left|z - z_0\right| \leq 1\right\}$, where $\left|z_0\right| = \left|z_0 - \omega\right| = \left|z_0 - \omega^2\right|$, ω and ω^2 are non-real cube roots of unity. Then

A. $z_0 = -1$

B. $z_0 = -1/2$

C. if $z \in S$, then least value of $|z|$ is 1

D. $\left|arg\left(\omega - z_0\right)\right| = \pi/3$

Answer: A::D

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35. If P and Q are represented by the complex numbers z_1 and z_2 such that $\left|\frac{1}{z_2} + \frac{1}{z_1}\right| = \left|\frac{1}{z_2} - \frac{1}{z_1}\right|$, then

A. (a) ΔOPQ (where O is the origin) is equilateral.

B. (b) ΔOPQ is right angled

C. (c) the circumcentre of ΔOPQ is $\frac{1}{2}\left(z_1 + z_2\right)$

D. (d) the circumcentre of ΔOPQ is $\frac{1}{2}\left(z_1 - z_2\right)$

Answer: B::C

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36. Locus of complex number satisfying $\arg[(z - 5 + 4i)/(z + 3 - 2i)] = \pi/4$ is the arc of a circle whose radius is $5\sqrt{2}$ whose radius is 5 whose length (of arc) is $\frac{15\pi}{\sqrt{2}}$ whose centre is $-2 - 5i$

A. whose radius is $5\sqrt{2}$

B. whose radius is 5

C. whose length (of arc) is $\frac{15\pi}{\sqrt{2}}$

D. whose centre is -2-5i

Answer: A::B::C

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37. Equation of tangent drawn to circle $|z| = r$ at the point $A\left(z_0\right)$, is

A. $Re\left(\frac{z}{z_0}\right. = 1$

B. $z\bar{z}_0 + z_0\bar{z} = 2r^3$

C. $Im\left(\frac{z}{z_0}\right. = 1$

D. $Im\left(\frac{z_0}{z}\right) = 1$

Answer: A::B

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38. If n is a natural number > 2, such that $z^n = (z+1)^n$, then (a) roots of equation lie on a straight line parallel to the y-axis (b) roots of equaiton lie on a straight line parallel to the x-axis (c) sum of the real parts of the roots is $-[(n-1)/2]$ (d) none of these

A. roots of equation lie on a straight line parallel to the y-axis

B. roots of equaiton lie on a straight line parallel to the x-axis

C. sum of the real parts of the roots is $-[(n-1)/2]$

D. none of these

Answer: A::C

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39. If $\left|z - \left(\frac{1}{z}\right)\right| = 1$, then a. $(|z|)_{max} = \frac{1+\sqrt{5}}{2}$ b. $(|z|)_{m\in} = \frac{\sqrt{5}-1}{2}$ c. $(|z|)_{max} = \frac{\sqrt{5}-2}{2}$ d. $(|z|)_{m\in} = \frac{\sqrt{5}-1}{\sqrt{2}}$

A. $|z|_{\max} = \frac{1+\sqrt{5}}{2}$

B. $|z|_{\min} = \frac{\sqrt{5}-1}{2}$

C. $|z|_{\max} = \frac{\sqrt{4}-2}{2}$

D. $|z|_{\min} = \frac{\sqrt{5}-1}{2}$

Answer: A::B

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40. about to only mathematics

A. 0

B. 1

C. -1

D. $1 + \omega$

Answer: A::B::C

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41. Let z be a complex number satisfying equation $z^p - z^{-q} = 0,\ where\ p, q \in N, then$ (A) if $p = q$, then number of solutions of equation will be infinite. (B) if $p = q$, then number of solutions of equation will be finite. (C) if $p \neq q$, then number of solutions of equation will be $p + q + 1$. (D) if $p \neq q$, then number of solutions of equation will be $p + q$.

A. if p=q, then number of solution of equation will infinte.

B. if p=q, then number of solutions of equaiton will finite

C. if $p \neq q$, then number of solutions of equaiton will $p + q + 1$

.

D. if $p \neq q$, then number of solutions of equaiton will be $p + q$

Answer: A::B

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42. Which of the following is true ?

A. (a) The number of common roots of $z^{144} = 1$ and $z^{24} = 1$ is

24

B. (b) The number of common roots of $z^{360} = 1$ and $z^{315} = 1$ is 45

C. (c) The number of roots common to $z^{24} = 1, z^{20} = 1$ and $z^{56} = 1$ is 4

D. (d) The number of roots common to $z^{27} = 1, z^{125} = 1$ and $z^{49} = 1$ is 1

Answer: A::B::C::D

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43. about to only mathematics

A. complex number $\left(z_1 + z_2 + z_3\right)/3$ will be on the curve $|z| = 1$

B. $\left(\frac{4}{\bar{z}_1}+\frac{1}{\bar{z}_2}+\frac{1}{\bar{z}_3}\right)\left(\frac{4}{z_1}+\frac{1}{z_2}+\frac{1}{z_3}\right)=9$

C. $arg\left(\frac{z_2}{z_3}\right)=\frac{2\pi}{3}$

D. orth ocenre and circumcenter of ΔPQR wil coincide

Answer: A::B::C::D

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44. about to only mathematics

A. z' , z' . z'' are in G.P

B. z',z',z'' are H.P

C. $z' + z'' = 2z\cos\alpha$

D. $z'^2 + z''^2 = 2z^2\cos 2\alpha$

Answer: A::C::D

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45. z_1, z_2, z_3 and z'_1, z'_2, z'_3 are nonzero complex numbers such that $z_3 = (1 - \lambda)z_1 + \lambda z_2$ and $z'_3 = (1 - \mu)z'_1 + \mu z'_2$, then which of the following statements is/are ture?

A. If $\lambda, \mu \in R - \{0\}$, then z_1, z_2 and z_3 are colliner and z_1, z_2, z_3 are colliner separately.

B. If λ, μ are complex numbers, where $\lambda = \mu$, then triangles formed by points z_1, z_2, z_3 and z'_1, z'_2, z'_3 are similare.

C. If λ, μ are distinct complex numbers, then points z_1, z_2, z_3 and z'_1, z'_2, z_3 are not connectd by any well defined gemetry.

D. If $0 < \lambda < 1$, then z_3 divides the line joining z_1 and z_2 internally and if $\mu > 1$, then z_3 divides the following of z'_1, z'_2 extranlly

Answer: A::B::C::D

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46. Given $z = f(x) + ig(x)$ where $f, g: (0, 1) \rightarrow (0, 1)$ are real valued functions. Then which of the following does not hold good?

a. $z = \frac{1}{1 - ix} + i\frac{1}{1 + ix}$

b. $z = \frac{1}{1 + ix} + i\frac{1}{1 - ix}$

c. $z = \frac{1}{1 + ix} + i\frac{1}{1 + ix}$

d. $z = \frac{1}{1 - ix} + i\frac{1}{1 - ix}$

A. $z = \frac{1}{1 - ix} + i\left(\frac{1}{1 + ix}\right)$

B. $z = \frac{1}{1 + ix} + i\left(\frac{1}{1 - ix}\right)$

C. $z = \frac{1}{1 + ix} + i\left(\frac{1}{1 + ix}\right)$

D. $z = \frac{1}{1 - ix} + i\left(\frac{1}{1 - ix}\right)$

Answer: A::C::D

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47. Let a, b, c be distinct complex numbers with $|a| = |b| = |c| = 1$ and z_1, z_2 be the roots of the equation $az^2 + bz + c = 0$ with $\left|z_1\right| = 1$. Let P and Q represent the complex numbers z_1 and z_2 in the Argand plane with $\angle POQ = \theta, o^\circ < 180^\circ$ (where O being the origin).Then

A. $b^2 = ac$

B. $PQ = \sqrt{3}$

C. $\theta = \frac{\pi}{3}$

D. $\theta = \frac{2\pi}{3}$

Answer: A::B::D

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48. If all the three roots of $az^3 + bz^2 + cz + d = 0$ have negative real parts $(a, b, c, \in R)$, then

A. $ab > 0$

B. $bv > 0$

C. $ad > 0$

D. $bc - ad > 0$

Answer: A::B::C::D

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49. If $\frac{3}{2+e^{i\theta}} = ax + iby$, then the locous of $P(x, y)$ will represent

A. (a) ellipse of a =1,b=2

B. (b) circle if a=b=1

C. (c) pair of straight line if a=1,b=0

D. (d) None of these

Answer: A::B::C

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LINKED COMPREHENSION TYPE

1. Consider the complex number $z = \frac{1 - i\sin\theta}{1 + i\cos\theta}$.

The value of θ for which z is purely real are

A. $n\pi - \frac{\pi}{4}, n \in I$

B. $\pi n + \frac{\pi}{4}, n \in I$

C. $n\pi, n \in I$

D. None of these

Answer: A

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2. Consider the complex number $z = (1 - i\sin\theta)/(1 + i\cos\theta)$.

The value of θ for which z is purely imaginary are

A. $n\pi - \frac{\pi}{4}, n \in I$

B. $\pi n + \frac{\pi}{4}, n \in I$

C. $n\pi, n \in I$

D. no real values of θ

Answer: D

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3. Consider the complex number $z = (1 - i\sin\theta)/(1 + i\cos\theta)$.

The value of θ for which z is unimodular give by

A. $n\pi \pm \frac{\pi}{6}, n \in I$

B. $n\pi \pm \frac{\pi}{3}, n \in I$

C. $n\pi \pm \frac{\pi}{4}, n \in I$

D. no real values of θ

Answer: C

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4. Consider the complex number $z = \frac{1 - i\sin\theta}{1 + i\cos\theta}$.

If agrument of z is $\frac{\pi}{4}$, then (a) $\theta = n\pi, n \in I$ only (b) $\theta = (2n + 1), n \in I$only (c) both $\theta = n\pi$ and $\theta = (2n + 1)\frac{\pi}{2}, n \in I$ (d) none of these

A. $\theta = n\pi, n \in I$ only

B. $\theta = (2n + 1), n \in I$only

C. both $\theta = n\pi$ and $\theta = (2n + 1)\frac{\pi}{2}, n \in I$

D. none of these

Answer: D

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5. Consider the complex numbers z_1 and z_2 Satisfying the relation $|z_1 + z_2|^2 = |z_1|^2 + |z_2|^2$ Complex number $\frac{z_1}{z_2}$ is

A. purely real

B. purely imaginary

C. zero

D. none of theses

Answer: B

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6. Consider the complex numbers z_1 and z_2 Satisfying the relation $|z_1 + z_2|^2 = |z_1| + |z_2|^2$

Complex number z_1/z_2 is

A. purely real

B. purely imaginary

C. zero

D. none of these

Answer: B

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7. Consider the complex numbers z_1 and z_2 Satisfying the relation $\left|z_1 + z_2\right|^2 = \left|z_1\right| + \left|z_2\right|^2$

One of the possible argument of complex number $i\left(z_1/z_2\right)$

A. $\frac{\pi}{2}$

B. $-\frac{\pi}{2}$

C. 0

D. none of these

Answer: C

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8. Consider the complex numbers z_1 and z_2 Satisfying the relation $\left|z_1 + z_2\right|^2 = \left|z_1\right|^2 + \left|z_2\right|^2$ Possible difference between the argument of z_1 and z_2 is

A. 0

B. π

C. $-\frac{\pi}{2}$

D. none of these

Answer: C

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9. Let z be a complex number satisfying $z^2 + 2z\lambda + 1 = 0$, where λ is a parameter which can take any real value.

The roots of this equation lie on a certain circle if

A. $-1 < \lambda < 1$

B. $\lambda > 1$

C. $\lambda < 1$

D. none of these

Answer: A

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10. Let z be a complex number satisfying $z^2 + 2z\lambda + 1 = 0$, where λ is a parameter which can take any real value.

The roots of this equation lie on a certain circle if

A. $-1 < \lambda < 1$

B. $\lambda > 1$

C. $\lambda < 1$

D. none of these

Answer: B

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11. Let z be a complex number satisfying $z^2 + 2z\lambda + 1 = 0$, where λ is a parameter which can take any real value.

For every large value of λ the roots are approximately.

A. $-2\lambda, 1/\lambda$

B. $-\lambda, -1/\lambda$

C. $-2\lambda, -\frac{1}{2\lambda}$

D. none of these

Answer: C

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12. The roots of the equation $z^4 + az^3 + (12 + 9i)z^2 + bz = 0$ (where a and b are complex numbers) are the vertices of a square. Then

The value of $|a - b|$ is

A. $5\sqrt{5}$

B. $\sqrt{130}$

C. 12

D. $\sqrt{175}$

Answer: B

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13. The roots of the equation $z^4 + az^3 + (12 + 9i)z^2 + bz = 0$ (where a and b are complex numbers) are the vertices of a square. Then The area of the square is

A. 25 sq.units

B. 20 sq.units

C. 5 sq.unit

D. 4 sq .units

Answer: C

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14. Consider a quadratic equation $az^2bz + c = 0,$ where a,b and c are complex numbers.

the condition that equation has two purely imaginary roots, is

A. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} + c\bar{b})(a\bar{a} - \bar{a}b)$

B. $(c\bar{c} - a\bar{c})^2 = (b\bar{c} - c\bar{a})^2(a\bar{b} + \bar{a}b)$

C. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} + c\bar{b})(a\bar{b} + a\bar{b})$

D. None of these

Answer: A

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15. Consider a quadratic equaiton $az^2 + bz + c = 0$, where a,b,c are complex number. If equaiton has two purely imaginary roots, then which of the following is not ture.

A. $a\bar{b}$ is purely imaginary

B. $b\bar{c}$ is purely imaginary

C. $c\bar{a}$ is purely real

D. none of these

Answer: D

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16. Consider a quadratic equation $az^2bz + c = 0$, where a,b and c are complex numbers.

The condition that the equation has one purely real root, is

A. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} + c\bar{b})(a\bar{a} - \bar{a}b)$

B. $(c\bar{c} - a\bar{c})^2 = (b\bar{c} - c\bar{a})^2(a\bar{b} + \bar{a}b)$

C. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} + c\bar{b})(a\bar{b} + a\bar{b})$

D. $(c\bar{a} - a\bar{c})^2 = (b\bar{c} - c\bar{b})(a\bar{b} - \bar{a}b)$

Answer: D

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17. Suppose z and ω are two complex number such that $|z + i\omega| = 2$. Which of the following is ture about $|z|$ and $|\omega|$?

A. $|z| = |\omega| = \frac{1}{2}$

B. $|z| = \frac{1}{2}, |\omega|, |\omega| = \frac{3}{4}$

C. $|z| = |\omega| = \frac{3}{4}$

D. $|z| = |\omega| = 1$

Answer: D

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18. Suppose z and ω are two complex number such that Which of the following is true for z and ω?

A. $Re(z) = Re(\omega) = \frac{1}{2}$

B. $Im(z) = Im(\omega)$

C. $Re(z) = Im(\omega)$

D. $Im(z) = Re(\omega)$

Answer: D

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19. Let $zand\omega$ be two complex numbers such that $|z| \leq 1, |\omega| \leq 1and|z - i\omega| = |z - i\omega| = 2, thenz$ equals 1 or i b. i or $-i$ c. 1 or -1 d. i or -1

A. 1 or -i

B. -1

C. I or $-i$

D. ω or ω^2 (where ω is the cube root of unity)

Answer: C

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20. Consider the equaiton of line $a\bar{z} + a\bar{z} + a\bar{z} + b = 0$, where b is a real parameter and a is fixed non-zero complex number.

The intercept of line on real axis is given by

A. $\frac{-2b}{a+\bar{a}}$

B. $\frac{-b}{2(a+\bar{a})}$

C. $\frac{-b}{a+\bar{a}}$

D. $\frac{b}{a+\bar{a}}$

Answer: C

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21. Consider the equaiton of line $a\bar{z}+a\bar{z}+a\bar{z}+b=0$, where b is a real parameter and a is fixed non-zero complex number.

The intercept of line on imaginary axis is given by

A. $\frac{b}{\bar{a}-a}$

B. $\frac{2b}{\bar{a}-a}$

C. $\frac{b}{2(\bar{a}-a)}$

D. $\frac{b}{a - \bar{a}}$

Answer: D

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22. Consider the equaiton of line $a\bar{z} + \bar{a}z + b = 0$, where b is a real parameter and a is fixed non-zero complex number.

The locus of mid-point of the line intercepted between real and imaginary axis is given by

A. (a) $a\bar{z} - \bar{a}z = 0$

B. (b) $a\bar{z} + \bar{a}z = 0$

C. (c) $a\bar{z} - \bar{a}z + b = 0$

D. (d) $a\bar{z} - \bar{a}z + 2b = 0$

Answer: B

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23. Consider the equation $az + b\bar{z} + c = 0$, where a,b,c $\in$ Z

If $|a| \neq |b|$, then z represents

A. circle

B. straight line

C. one point

D. ellispe

Answer: C

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24. Consider the equation $az + b\bar{z} + c = 0$, where a,b,c $\in$ Z

If $|a| = |b|$ and $\bar{a}c \neq b\bar{c}$, then z has

A. infnite solutions

B. no solutions

C. finite solutions

D. cannot say anything

Answer: B

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25. Consider the equation $az + b\bar{z} + c = 0$, where a,b,c $\in$ Z

If $|a| \neq |b|$, then z represents

A. an ellipse

B. a circle

C. a point

D. a straight line

Answer: D

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26. Complex number z satisfy the equation $\left|z - \left(\frac{4}{z}\right)\right| = 2$

The difference between the least and the greatest moduli of complex number is (a) 2 (b) 4 (c) 1 (d) 3

A. 2

B. 4

C. 1

D. 3

Answer: A

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27. Complex numbers z satisfy the equaiton $|z - (4/z)| = 2$

The value of $arg\left(z_1/z_2\right)$ where z_1 and z_2 are complex numbers with the greatest and the least moduli, can be

A. (a) 2π

B. (b) π

C. (c) $\pi/2$

D. (d) none of these

Answer: B

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28. Complex numbers z satisfy the equaiton $|z - (4/z)| = 2$

Locus of z if $\left|z - z_1\right| = \left|z - z_2\right|$, where z_1 and z_2 are complex numbers with the greatest and the least moduli, is

A. line parallel to the real axis

B. line parallel to the imaginary axis

C. line having a positive slope

D. line having a negative slope

Answer: B

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29. In an Agrad plane z_1, z_2 and z_3 are, respectively, the vertices of an isosceles trinagle ABC with AC= BC and $\angle CAB = \theta$. If z_4 is incentre of triangle, then

The value of $AB \times AC/(IA)^2$ is

A. $\dfrac{(z_2 - z_1)(z_3 - z_1)}{(z_4 - z_1)^2}$

B. $\dfrac{(z_2 - z_1)(z_1 - z_3)}{(z_4 - z_1)^2}$

C. $\dfrac{(z_4 - z_1)^2}{(z_2 - z_1)(z_3 - z_1)}$

D. none of these

Answer: A

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30. In the Argand plane Z_1, Z_2 and Z_3 are respectively the verticles of an isosceles triangle ABC with AC=BC and $\angle CAB = \theta$. If $I\left(Z_4\right)$ is the incentre of triangle , then :

The value of $\left(Z_4 - Z_1\right)^2(1 + \cos\theta)\sec\theta$ is :

A. $\dfrac{\left(z_2 - z_1\right)\left(z_3 - z_1\right)}{\left(z_4 - z_1\right)}$

B. $\left(z_2 - z_1\right)\left(z_3 - z_1\right)$

C. $\left(z_2 - z_1\right)\left(z_3 - z_1\right)^2$

D. $\dfrac{\left(z_2 - z_1\right)\left(z_1 - z_3\right)}{\left(z_4 - z_1\right)^2}$

Answer: B

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31. In an Agrad plane z_1, z_2 and z_3 are, respectively, the vertices of an isosceles trinagle ABC with AC= BC and $\angle CAB = \theta$. If z_4 is incentre of triangle, then

The value of $\left(z_2 - z_1\right)^2 \tan\theta \tan\theta/2$ is

A. $\left(z_1 + z_2 - 2z_3\right)$

B. $\left(z_1 + z_2 - z_3\right)\left(z_1 + z_2 - z_4\right)$

C. $-\left(z_1 + z_2 - 2z_3\right)\left(z_1 + z_2 - 2z_4\right)$

D. $z_4 = \sqrt{z_2 z_3}$

Answer: C

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32. $A\left(z_1\right), B\left(z_2\right)$ and $C\left(z_3\right)$ are the vertices of triangle ABC inscribed in the circle |z|=2,internal angle bisector of angle A

meets the circumcircle again at $D(z_4)$.Point D is:

A. $z_4 = \frac{1}{z_2} + \frac{1}{z_3}$

B. $\sqrt{\frac{z_2 + z_3}{z_1}}$

C. $\sqrt{\frac{z_2 z_3}{z_1}}$

D. $z_4 = \sqrt{z_2 z_3}$

Answer: D

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33. $A(z_1), B(z_2), C(z_3)$ are the vertices of a triangle ABC inscrible in the circle $|z| = 2$. Internal angle bisector of the angle A meets the circumcircle again at $D(z_4)$.

A. $\frac{\pi}{2}$

B. $\frac{\pi}{3}$

C. $\frac{\pi}{2}$

D. $\frac{2\pi}{3}$

Answer: C

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34. $A(z_1), B(z_2), C(z_3)$ are the vertices of a triangle ABC inscrible in the circle $|z| = 2$. Internal angle bisector of the angle A meets the circumcircle again at $D(z_4)$.

Complex number representing point $D(z_4)$

A. H.M of z_2 and z_3

B. A.M of z_2 and z_3

C. G.M of z_2 and z_3

D. none of these

Answer: C

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35. Let $S = S_1 \cap S_2 \cap S_3$, where $s_1 = \{z \in C : |z| < 4\}, S_2 = \left\{z \in C : \ln\left[\frac{z - 1 + \sqrt{3}i}{1 - \sqrt{31}}\right] > 0\right\}$ and $S_3 = \{z \in C : Rez > 0\}$ Area of S=

A. $\frac{10\pi}{3}$

B. $\frac{20\pi}{3}$

C. $\frac{16\pi}{3}$

D. $\frac{32\pi}{3}$

Answer: B

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36. Let $S = S_1 \cap S_2 \cap S_3$, where $S_1 = \{z \text{ in } C : |z| < 4\}$,

$$S_2 = \left\{ z \text{ in } C : Im\left[\frac{z - 1 + \sqrt{3}i}{1 - \sqrt{3}i}\right] > 0 \right\} \text{ and } S_3 = \{z \text{ in } C : Rez > 0\}$$

$\min_{z \in S} |1 - 3i - z| =$

A. $\frac{2 - \sqrt{3}}{2}$

B. $\frac{2 + \sqrt{3}}{2}$

C. $\frac{3 - \sqrt{3}}{2}$

D. $\frac{3 + \sqrt{3}}{2}$

Answer: C

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NUMERICAL VALUE TYPES

1. If $x = a + bi$ is a complex number such that $x^2 = 3 + 4i$ and $x^3 = 2 + 1i, where i = \sqrt{-1}, then (a + b)$ equal to _____.

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2. If the complex numbers x and y satisfy $x^3 - y^3 = 98i$ and $x - y = 7i, then xy = a + ib, where a, b, \in R$. The value of $(a + b)/3$ equals _____.

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3. If $x = \omega - \omega^2 - 2$ then , the value of $x^4 + 3x^3 + 2x^2 - 11x - 6$ is (where ω is a imaginary cube root of unity)

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4. Let $z = 9 + bi, whereb$ is nonzero real and $i^2 = -1$. If the imaginary part of $z^2 andz^3$ are equal, then $b/3$ is _____.

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5. Modulus of nonzero complex number z satifying $\bar{z} + z = 0$ and $|z|^2 - 4iz = z^2$ is ____.

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7. If complex number $z(z \neq 2)$ satisfies the equation $z^2 = 4z + |z|^2 + \frac{16}{|z|^3}$,then the value of $|z|^4$ is_____.

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9. Let $|z| = 2$ and $w = \frac{z+1}{z-1}$, $where z, w, \in C$ (where C is the set of complex numbers). Then product of least and greatest value of modulus of w is_____.

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10. If z is a complex number satisfying $z^4 + z^3 + 2z^2 + z + 1 = 0$ then the set of possible values of z is

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11. Let $1, , w^2$ be the cube root of unity. The least possible degree of a polynomial with real coefficients having roots $2w, (2 + 3w), \left(2 + 3w^2\right), \left(2 - w - w^2\right)$ is _____.

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12. If ω is the imaginary cube roots of unity, then the number of pair of integers (a,b) such that $|a\omega + b| = 1$ is _____.

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13. Suppose that z is a complex number the satisfies $|z - 2 - 2i| \leq 1$. The maximum value of $|2iz + 4|$ is equal to _____.

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14. If $|z + 2 - i| = 5$ and maxium value of $|3z + 9 - 7i|$ is M, then the value of M is _____.

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15. Let $Z_1 = (8 + i)\sin\theta + (7 + 4i)\cos\theta$ and $Z_2 = (1 + 8i)\sin\theta + (4 + 7i)\cos\theta$ are two complex numbers. If $Z_1 \cdot Z_2 = a + ib$ where $a, b \in R$ then the largest value of $(a + b)\,\forall\,\theta \in R$, is

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16. Let $A = \{a \in R\}$ the equation $(1 + 2i)x^3 - 2(3 + i)x^2 + (5 - 4i)x + a^2 = 0$ has at least one real root. Then the value of $\frac{\sum a^2}{2}$ is_____.

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17. Find the minimum value of the expression $E = |z|^2 + |z - 3|^2 + |z - 6i|^2$ (where $z = x + iy, x, y \in R$)

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18. If z_1 lies on $|z - 3| + |z + 3| = 8$ such that arg $z_1 = \pi/6$, then $37\left|z_1\right|^2 =$ _____.

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19. If z satisfies the condition $\arg(z+i) = \frac{\pi}{4}$. Then the minimum value of $|z+1-i| + |z-2+3i|$ is _____.

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20. Let $\omega \neq 1$ be a complex cube root of unity. If

$$\left(4+5\omega+6\omega^2\right)^{n^2+2} + \left(6+5\omega^2+4\omega\right)^{n^2+2} + \left(5+6\omega+4\omega^2\right)^{n^2+2} = 0$$

, and $n \in N$, where $n \in [1, 100]$, then number of values of n is _____.

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21. Let z be a non - real complex number which satisfies the equation $z^{23} = 1$. Then the value of $\sum_{22}^{k=1} \frac{1}{1+z^{8k}+z^{16k}}$

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22. If z, z_1 and z_2 are complex numbers such that $z = z_1 z_2$ and $\left|\bar{z}_2 - z_1\right| \leq 1$, then maximum value of $|z|$ - Re(z) is _____.

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23. Let z_1, z_2 and z_3 be three complex numbers such that $z_1 + z_2 + z_3 = z_1 z_2 + z_2 z_3 + z_1 z_3 = z_1 z_2 z_3 = 1$. Then the area of triangle formed by points $A\left(z_1\right), B\left(z_2\right)$ and $C\left(z_3\right)$ in complex plane is _____.

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24. Let α be the non-real 5 th root of unity. If z_1 and z_2 are two complex numbers lying on $|z| = 2$, then the value of

$\sum_{t=0}^{4} \left|z_1 + \alpha^t z_2\right|^2$ is _____ .

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25. Let $z_1, z_2, z_3 \in C$ such that $\left|z_1\right| = \left|z_2\right| = \left|z_3\right| = \left|z_1 + z_2 + z_3\right| = 4.$

If $\left|z_1 - z_2\right| = \left|z_1 + z_3\right|$ and $z_2 \neq z_3$, then values of $\left|z_1 + z_2\right| \cdot \left|z_1 + z_3\right|$ is _____.

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26. Let $A\left(z_1\right)$ and $B\left(z_2\right)$ be lying on the curve $|z - 3 - 4i| = 5$, where $\left|z_1\right|$ is maximum. Now, $A\left(z_1\right)$ is rotated about the origin in anticlockwise direction through 90° reaching at $P\left(z_0\right)$. If A, B and P are collinear then the value of $\left(\left|z_0 - z_1\right| \cdot \left|z_0 - z_2\right|\right)$ is _____.

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27. If z_1, z_2, z_3 are three points lying on the circle $|z| = 2$ then the minimum value of the expression $\left|z_1 + z_2\right|^2 + \left|z_2 + z_3\right|^2 + \left|z_3 + z_1\right|^2 =$

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28. Minimum value of $\left|z_1 + 1\right| + \left|z_2 + 1\right| + \left|z_1 z_2 + 1\right|$ if $\left[z_1\right| = 1$ and $|z_2| = 1$ is _____.

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29. If $\left|z_1\right| = 2$ and $(1 - i)z_2 + (1 + i)\bar{z}_2 = 8\sqrt{2}$, then the minimum value of $\left|z_1 - z_2\right|$ is _____.

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30. Given that $1 + 2|z|^2 = \left|z^2 + 1\right|^2 + 2|z + 1|^2$, then the value of $|z(z + 1)|$ is _____.

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33. For any integer k, let $\alpha_k = \frac{\cos(k\pi)}{7} + i\frac{\sin(k\pi)}{7}$, $where i = \sqrt{-1}$.

Value of the expression $\frac{\sum k = 112 \left|\alpha_{k+1} - \alpha_k\right|}{\sum k = 13 \left|\alpha_{4k-1} - \alpha_{4k-2}\right|}$ is

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ARCHIVES (SINGLE CORRECT ANSWER TYPE)

1. If $\left|z - \frac{4}{z}\right| = 2$, then the maximum value of $|Z|$ is equal to (1) $\sqrt{3} + 1$ (2) $\sqrt{5} + 1$ (3) 2 (4) $2 + \sqrt{2}$

A. $\sqrt{3} + 1$

B. $\sqrt{5} + 1$

C. 2

D. $2 + \sqrt{2}$

Answer: B

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2. The number of complex numbersd z, such that $|z - 1| = |z + 1| = |z - i|$, where $i = \sqrt{-1}$ equals to

A. ∞

B. 0

C. 1

D. 2

Answer: C

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3. Let α and β be real and z be a complex number. If $z^2 + az + \beta = 0$ has two distinct roots on the line Re(z)=1, then it is necessary that

A. $\beta \in (1, \infty)$

B. $\beta \in (0, 1)$

C. $\beta \in (-1, 0)$

D. $|\beta| = 1$

Answer: A

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4. If $\omega(\neq 1)$ is a cube root of unity, and $(1+\omega)^7 = A + B\omega$. Then (A, B) equals

A. $(-1, 1)$

B. $(0, 1)$

C. $(1, 1)$

D. $(1, 0)$

Answer: C

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5. If $z \neq 1$ and $\frac{z^2}{z-1}$ is real, then the point represented by the complex number z lies (1) either on the real axis or on a circle passing through the origin (2) on a circle with centre at the

origin (3) either on the real axis or on a circle not passing through the origin (4) on the imaginary axis

A. either on the real axis or on a circle passing thorugh the origin.

B. on a circle with centre at the origin.

C. either on the real axis or an a circle not possing through the origin .

D. on the imaginary axis .

Answer: A

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6. If z is a complex number of unit modulus and argument q, then $arg\left(\frac{1+z}{1+\bar{z}}\right)$ equal (1) $\frac{\pi}{2}$ - θ (2) θ (3) π - θ (4) -θ

A. $-\theta$

B. $\frac{\pi}{2} - \theta$

C. θ

D. $\pi - \theta$

Answer: C

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7. If z is a complex number such that $|z| \geq 2$, then the minimum value of $\left|z + \frac{1}{2}\right|$ (1) is equal to $\frac{5}{2}$ (2) lies in the interval (1, 2) (3) is strictly greater than $\frac{5}{2}$ (4) is strictly greater than $\frac{3}{2}$ but less than $\frac{5}{2}$

A. is equal to $\frac{5}{2}$

B. lies in the interval (1,2)

C. is strictly gerater than $\frac{5}{2}$

D. is strictly greater than $\frac{3}{2}$ but less than $\frac{5}{2}$

Answer: B

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8. If z_1 and z_2 are two complex numbers such that $\frac{z_1 - 2z_2}{2 - z_1\bar{z}_2}$ is unimodular whereas z_1 is not unimodular then $|z_1|=$

A. Straight line parallel to x-axis

B. sraight line parallel to y-axis

C. circle of radius 2

D. circle of radius $\sqrt{2}$

Answer: C

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9. A value of for which $\frac{2+3i\sin\theta}{1-2i\sin\theta}$ purely imaginary, is : (1) $\frac{\pi}{3}$ (2) $\frac{\pi}{6}$ (3) $\sin^{-1}\left(\frac{\sqrt{3}}{4}\right)$ (4) $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right)$

A. $\frac{\pi}{6}$

B. $\sin^{-1}\left(\frac{Sqrt(3)}{4}\right)$

C. $\sin^{-1}\left(\frac{1}{\sqrt{3}}\right.$

D. $\frac{\pi}{3}$

Answer: C

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10. Let ω be a complex number such that $2\omega + 1 = z$ where $z = \sqrt{-3}$. $If \left| 1111 - \omega^2 - 1\omega^2 1\omega^2 \omega^7 \right| = 3k$, then k is equal to : -1 (2) 1 (3) $-z$ (4) z

A. 1

B. z

C. $-z$

D. -1

Answer: B

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11. If $\alpha, \beta \in C$ are distinct roots of the equation $x^2 + 1 = 0$ then $\alpha^{101} + \beta^{107}$ is equal to

A. 2

B. -1

C. 0

D. 1

Answer: D

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MULTIPLE CORRECT ANSWER TYPE

1. Let z_1 and z_2 be two distinct complex numbers and $z = (1 - t)z_1 + tz_2$, for some real number t with $0 < t < 1$ and $i = \sqrt{-1}$. If arg(w) denotes the principal argument of a non-zero compolex number w, then

A. $\left|z - z_1\right| + \left|z - z_2\right| = \left|z_1 - z_2\right|$

B. $\left(z - z_1\right) = \left(z - z_2\right)$

C. $\begin{vmatrix} z - z_1 & \bar{z} - \bar{z}_1 \\ z_2 - z_1 & \bar{z}_2 - \bar{z}_1 \end{vmatrix} = 0$

D. $arg\left(z - z_1\right) = arg\left(z_2 - z_1\right)$

Answer: A::C::D

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A. $\pi/2$

B. $\pi/6$

C. $2\pi/3$

D. $5\pi/6$

Answer: C::D

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3. Let $a, b \in R$ and $a^2 + b^2 \neq 0$.

Suppose $S = \left\{ z \in C : z = \frac{1}{a + ibt}, t \in R, t \neq 0 \right\}$, where $i = \sqrt{-1}$. If z=x+iy and $z \in S$, then (x,y) lies on

A. the circle with radius $\frac{1}{2a}$ and centre $\left(\frac{1}{2a}, 0\right)$ for $a > 0be \neq 0$

B. the circle with radius $-\frac{1}{2a}$ and centre $\left(-\frac{1}{2}, 0\right)a < 0, b \neq 0$

C. the axis for $a \neq 0, b = 0$

D. the y-axis for $a = 0, b \neq 0$

Answer: A::C::D

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4. Let $a, b, xandy$ be real numbers such that $a - b = 1andy \neq 0$. If the complex number $z = x + iy$ satisfies $Im\left(\frac{az + b}{z + 1}\right) = y$, then which of the following is (are) possible value9s) of x?| $-1 - \sqrt{1 - y^2}$ (b) $1 + \sqrt{1 + y^2}$ $-1 + \sqrt{1 - y^2}$ (d) $-1 - \sqrt{1 + y^2}$

A. $-1 - \sqrt{1 - y^2}$

B. $1 + \sqrt{1 + y^2}$

C. $1 - \sqrt{1 + y^2}$

D. $-1 + \sqrt{1 - y^2}$

Answer: A::D

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5. For a non-zero complex number z, let $arg(z)$ denote the principal argument with $-\pi < arg(z) \leq \pi$ Then, which of the following statement(s) is (are) FALSE? $arg(-1, -i) = \frac{\pi}{4}$, where $i = \sqrt{-1}$ (b) The function $f: R \rightarrow (-\pi, \pi]$, defined by $f(t) = arg(-1 + it)$ for all $t \in R$, is continuous at all points of $\mathbb{R}$, where $i = \sqrt{-1}$ (c) For any two non-zero complex numbers z_1 and z_2, $arg\left(\frac{z_1}{z_2}\right) - arg\left(z_1\right) + arg\left(z_2\right)$ is an integer multiple of 2π (d) For any three given distinct complex numbers z_1, z_2 and z_3, the locus of the point z satisfying the condition $arg\left(\frac{\left(z - z_1\right)\left(z_2 - z_3\right)}{\left(z - z_3\right)\left(z_2 - z_1\right)}\right) = \pi$, lies on a straight line

A. $arg(-1 - i) = \frac{\pi}{4}$, where $i = \sqrt{-1}$

B. The function $f: R \rightarrow (-\pi, \pi]$, defined by $f(t) = arg(-1 + it)$ for all $t \in R$, is continous at all points of R, where $i = \sqrt{-1}$

C. For any tow non-zero complex number z_1 and z_2, $arg\left(\frac{z_1}{z_2}\right) - arg\left(z_1\right) + arg\left(z_2\right)$ is an integer multiple of 2π

D. For any three given distinct complex numbers z_1, z_2 and z_3 the locus of the point z satisfying the condition $\left(\frac{\left(z - z_1\right)\left(z_2 - z_3\right)}{\left(z - z_3\right)\left(z_2 - z_1\right)}\right) = \pi$, lies on a strainght line.

Answer: A::B::D

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6. Let $s,\ t,\ r$ be non-zero complex numbers and L be the set of solutions $z = x + iy\ \left(x,\ y \in \mathbb{R},\ i = \sqrt{-1}\right)$ of the equation $sz + tz + r = 0$, where $z = x - iy$. Then, which of the following statement(s) is (are) TRUE? If L has exactly one element, then

$|s| \neq |t|$ (b) If $|s| = |t|$, then L has infinitely many elements (c) The number of elements in $\ln n\{z : |z - 1 + i| = 5\}$ is at most 2 (d) If L has more than one element, then L has infinitely many elements

A. If L has exactly one element, then $|s| \neq |t|$

B. If $|s| = |t|$ then L has infinitely many elements

C. The number of elements in $L \cap \{z : |z - 1 + i| = 5\}$ is at most 2

D. If L has most than one elements, then L has infinitely many elements.

Answer: A::C::D

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Matching Column

1. z_1, z_2, z_3 are vertices of a triangle. Match the condition in List I with type of triangle in List II.

	List I		List II
(p)	$z_1^2 + z_2^2 + z_3^2 = z_2z_3 + z_3z_1 + z_1z_2$	(1)	right angled but not necessarily iscosceles
(q)	$\text{Re}\left(\frac{z_3 - z_1}{z_3 - z_2}\right) = 0$	(2)	obtuse angled
(r)	$\text{Re}\left(\frac{z_3 - z_1}{z_3 - z_2}\right) < 0$	(3)	isosceles and right angled
(s)	$\frac{z_3 - z_1}{z_3 - z_2} = i$	(4)	equilateral

Codes

A.

p	q	r	s
3	2	1	4

B.

p	q	r	s
1	2	4	3

C.

p	q	r	s
4	1	2	3

D.

p	q	r	s
2	1	4	3

Answer: C

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MATRIX MATCH TYPE

1. The graph of the quadrationc funtion $y = ax^2 + bx + c$ is as shown in the following figure.

Now,match the complex numbers given in List I with the corresponding arguments in List II.

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2. Let z_1, z_2 and z_3 be the vertices of trinagle . Then match following lists.

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3. Match the following lists:

List I	List II
a. If $f(x)$ is an integrable function for $x \in \left[\frac{\pi}{6}, \frac{\pi}{3}\right]$ and $I_1 = \int_{\pi/6}^{\pi/3} \sec^2\theta f(2\sin 2\theta)\, d\theta$, and $I_2 = \int_{\pi/6}^{\pi/3} \operatorname{cosec}^2\theta f(2\sin 2\theta) d\theta$, then $I_1/I_2 =$	**p.** 3
b. If $f(x+1) = f(3+x)\ \forall\, x$, and the value of $\int_a^{a+b} f(x)dx$ is independent of a, then the value of b can be	**q.** 1
c. The value of $2\int_1^4 \frac{\tan^{-1}[x^2]}{\tan^{-1}[x^2] + \tan^{-1}[25 + x^2 - 10x]}\, dx$ (where [.]denotes the greatest integer function) is	**r.** 2
d. If $I = \int_0^2 \sqrt{x + \sqrt{x + \sqrt{x + \cdots\infty}}}\, dx$ (where $x > 0$), then $[\, I\,]$ is equal to (where [.] denotes the greatest integer function)	**s.** 4

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4. Complex number z satisfies the equation $||z - 5i| + m|z - 12i| | = n$. Then match the value of m and n in List I with the corresponding locus in List II.

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5. Complex number z lies on the curve $S \equiv ar\frac{g(z+3)}{z+3i} = -\frac{\pi}{4}$

A.

	a	b	c	d
(1)	p	q	p	r

B.

	a	b	c	d
(2)	s	r	q	p

C.

	a	b	c	d
(3)	q	p	q	r

D.

	a	b	c	d
(4)	s	p	q	r

Answer: A

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6. Consider sets

$A = \left\{z \in C : z^{27} - 1 = 0\right\}$ and $B = \left\{z \in C : z^{36} - 1 = 0\right\}$

Now ,match the following lists.

A.

	a	b	c	d
(1)	p	q	p	r

B.

	a	b	c	d
(2)	r	q	s	p

C.

	a	b	c	d
(3)	q	p	q	r

D.

	a	b	c	d
(4)	s	p	q	r

Answer: B

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7. Match the statements in List I with those in List II

[Note: Here z take the values in the complex place and Im(z) and Re(z) denote, repectively, the imaginary part and the real part of z].

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8. Let $z_k = \cos\left(\frac{2k\pi}{10}\right) - i\sin\left(\frac{2k\pi}{10}\right), k = 1, 2, \ldots\ldots, 9$

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9. Match the conics in List I with the statements/expressions in List II

List I	List II
a. Circle	**p.** The locus of the point (h, k) for which the line $hx + ky = 1$ touches the circle $x^2 + y^2 = 4$
b. Parabola	**q.** Points z in the complex plane satisfying $\lvert z+2 \rvert - \lvert z-2 \rvert = \pm 3$
c. Ellipse	**r.** Points of the conic have parametric representation $x = \sqrt{3}\left(\frac{1-t^2}{1+t^2}\right),\ y = \frac{2t}{1+t^2}$
d. Hyperbola	**s.** The eccentricity of the conic lies in the interval $1 \le x < \infty$
	t. Points z in the complex plane satisfying $\text{Re}\,(z+1)^2 = \lvert z \rvert^2 + 1$

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