



MATHS

BOOKS - CENGAGE MATHS (ENGLISH)

CONIC SECTIONS

Others

1. Given that $A(1, 1)$ and $B(2, -3)$ are two points and D is a point on AB produced such that $AD = 3AB$. Find the coordinates of D .

[Watch Video Solution](#)

2. Find the coordinates of the point which divides the line segments joining the points $(6, 3)$ and $(-4, 5)$ in the ratio $3:2$ (i) internally and (ii) externally.

[Watch Video Solution](#)

3. Four points $A(6, 3)$, $B(-3, 5)$, $C(4, -2)$ and $D(x, 2x)$ are given in such a way that $\frac{(\text{Area of } DBC)}{(\text{Area of } ABC)} = \frac{1}{2}$.

[Watch Video Solution](#)

4. If the points $(1, 1)$, $(0, \sec^2 \theta)$; and $(\csc^2 \theta, 0)$ are collinear, then find the value of θ

[Watch Video Solution](#)

5. Given that A_1, A_2, A_3, A_n are n points in a plane whose coordinates are $(x_1, y_1), (x_2, y_2), (x_n, y_n)$, respectively. A_1A_2 is bisected at the point P_1 , P_1A_3 is divided in the ratio $1:2$ at P_2 , P_2A_4 is divided in the ratio $1:3$ at P_3 , P_3A_5 is divided in the ratio $1:4$ at P_4 , and so on until all n points are exhausted. Find the final point so obtained.

[Watch Video Solution](#)

6. If P divides OA internally in the ratio $\lambda_1 : \lambda_2$ and Q divides OA externally in the ratio $\lambda_1 : \lambda_2$, then prove that OA is the harmonic mean of OP and OQ .



[Watch Video Solution](#)

7. Prove that the point $(-2, -1)$, $(1, 0)$, $(4, 3)$ and $(1, 2)$ are the vertices of parallel-gram. Is it a rectangle?



[Watch Video Solution](#)

8. Determine the ratio in which the line $3x + y - 9 = 0$ divides the segment joining the points $(1, 3)$ and $(2, 7)$.



[Watch Video Solution](#)

9. Find the orthocentre of the triangle whose vertices are $(0, 0)$, $(3, 0)$, and $(0, 4)$.



Watch Video Solution

10. If a vertex of a triangle is $(1, 1)$, and the middle points of two sides passing through it are $(-2, 3)$ and $(5, 2)$, then find the centroid of the triangle.



Watch Video Solution

11. The vertices of a triangle are $A(-1, -7)$, $B(5, 1)$ and $C(1, 4)$. If the internal angle bisector of $\angle B$ meets the side AC in D , then find the length AD .



Watch Video Solution

12. If $\triangle ABC$ having vertices $A(a \cos \theta_1, a \sin \theta_1)$, $B(b \cos \theta_2, b \sin \theta_2)$, and $C(c \cos \theta_3, c \sin \theta_3)$ is equilateral, then prove that $\cos \theta_1 + \cos \theta_2 + \cos \theta_3 = \sin \theta_1 + \sin \theta_2 + \sin \theta_3 = 0$.



Watch Video Solution

13. If the points $(x, -1)$, $(3, y)$, $(-2, 3)$, and $(-3, -2)$ taken in order are the vertices of a parallelogram, then find the values of x and y .



Watch Video Solution

14. If the midpoints of the sides of a triangle are $(2, 1)$, $(-1, -3)$, and $(4, 5)$, then find the coordinates of its vertices.



Watch Video Solution

15. If the circumcenter of an acute-angled triangle lies at the origin and the centroid is the middle point of the line joining the points $(a^2 + 1, a^2 + 1)$ and $(2a, -2a)$, then find the orthocentre.



Watch Video Solution

16. If a vertex, the circumcenter, and the centroid of a triangle are $(0, 0)$, $(3, 4)$, and $(6, 8)$, respectively, then the triangle must be (a) a right-angled triangle (b) an equilateral triangle (c) an isosceles triangle (d) a right-angled isosceles triangle



Watch Video Solution

17. Orthocenter and circumcenter of a $\triangle ABC$ are (a, b) and (c, d) , respectively. If the coordinates of the vertex A are (x_1, y_1) , then find the coordinates of the middle point of BC .



Watch Video Solution

18. If $A(x_1, y_1)$, $B(x_2, y_2)$ and $C(x_3, y_3)$ are the vertices of triangle ABC and $x_1^2 + y_1^2 = x_2^2 + y_2^2 = x_3^2 + y_3^2$, then show that

$$x_1 \sin 2A + x_2 \sin 2B + x_3 \sin 2C = y_1 \sin 2A + y_2 \sin 2B + y_3 \sin 2C = 0$$

.



Watch Video Solution

19. The points (a, b) , (c, d) , and $\left(\frac{kc + la}{k + l}, \frac{kd + lb}{k + l}\right)$ are (a) vertices of an equilateral triangle (b) vertices of an isosceles triangle (c) vertices of a right-angled triangle (d) collinear



Watch Video Solution

20. The circumcenter of the triangle formed by the line $y = x$, $y = 2x$, and $y = 3x + 4$ is

A. (a) $(6, 8)$

B. (b) $(6, -8)$

C. (c) $(3, 4)$

D. (d) $(-3, -4)$

Answer: null



Watch Video Solution

21. The line joining $A(b \cos \alpha, b \sin \alpha)$ and $B(a \cos \beta, a \sin \beta)$ is produced to the point $M(x, y)$ so that AM and BM are in the ratio $b:a$. Then

$$x \cos \left(\frac{\alpha + \beta}{2} \right) + y \sin \left(\frac{\alpha + \beta}{2} \right)$$



Watch Video Solution

22. If the middle points of the sides of a triangle are $(-2, 3)$, $(4, -3)$, and $(4, 5)$, then find the centroid of the triangle.



Watch Video Solution

23. In what ratio does the x-axis divide the line segment joining the points $(2, -3)$ and $(5, 6)$?



Watch Video Solution

24. If $(1, 4)$ is the centroid of a triangle and the coordinates of its any two vertices are $(4, -8)$ and $(-9, 7)$, find the area of the triangle.



Watch Video Solution

25. If $(x_i, y_i), i = 1, 2, 3$, are the vertices of an equilateral triangle such that

$$(x_1 + 2)^2 + (y_1 - 3)^2 = (x_2 + 2)^2 + (y_2 - 3)^2 = (x_3 + 2)^2 + (y_3 - 3)^2,$$

then find the value of $\frac{x_1 + x_2 + x_3}{y_1 + y_2 + y_3}$.



Watch Video Solution

26. A particle just clears a wall of height b at distance a and strikes the ground at a distance c from the point of projection. The angle of projection is (1) $\frac{\tan^{-1} b}{ac}$ (2) 45° (3) $\frac{\tan^{-1}(bc)}{a(c-a)}$ (4) $\frac{\tan^{-1}(bc)}{a}$



Watch Video Solution

27. Find the locus of a point, so that the join of $(-5, 1)$ and $(3, 2)$ subtends a right angle at the moving point.



Watch Video Solution

28. The sum of the squares of the distances of a moving point from two fixed points $(a, 0)$ and $(-a, 0)$ is equal to a constant quantity $2c^2$. Find the equation to its locus.



Watch Video Solution

29. AB is a variable line sliding between the coordinate axes in such a way that A lies on the x-axis and B lies on the y-axis. If P is a variable point on AB such that $PA = b$, $PB = a$, and $AB = a + b$, find the equation of the locus of P .



Watch Video Solution

30. A rod of length l slides with its ends on two perpendicular lines. Find the locus of its midpoint.



Watch Video Solution

31. Find the locus of the point $(t^2 - t + 1, t^2 + t + 1)$, $t \in R$.



Watch Video Solution

32. Find the locus of a point such that the sum of its distance from the points $(2, 2)$ and $(2, -2)$ is 6.



Watch Video Solution

33. Two points $P(a,0)$ and $Q(-a,0)$ are given. R is a variable point on one side of the line PQ such that $\angle RPQ - \angle RQP$ is a positive constant 2α . Find the locus of the point R .



Watch Video Solution

34. If the coordinates of a variable point P are $(a \cos \theta, b \sin \theta)$, where θ is a variable quantity, then find the locus of P .



Watch Video Solution

35. Find the locus of a point whose distance from $(a, 0)$ is equal to its distance from the y -axis.



Watch Video Solution

36. The coordinates of the point A and B are $(a, 0)$ and $(-a, 0)$, respectively. If a point P moves so that $PA^2 - PB^2 = 2k^2$, when k is constant, then find the equation to the locus of the point P .



Watch Video Solution

37. The locus of the foot of perpendicular drawn from origin to a variable line passing through fixed points $(2, 3)$ is a circle whose diameter is?



Watch Video Solution

38. A variable line through the point $P(2, 1)$ meets the axes at A and B .
Find the locus of the centroid of triangle OAB (where O is the origin).



Watch Video Solution

39. If $A(\cos \alpha, \sin \alpha)$, $B(\sin \alpha, -\cos \alpha)$, $C(1, 2)$ are the vertices of ABC , then as α varies, find the locus of its centroid.



Watch Video Solution

40. Let $A(2, -3)$ and $B(-2, 1)$ be the vertices of $\triangle ABC$. If the centroid of the triangle moves on the line $2x + 3y = 1$, then find the locus of the vertex C .



Watch Video Solution

41. Convert the following points from polar coordinates to the corresponding Cartesian coordinates. (i)

(ii) (iii) $\left((iv) (v) 2, (vi) \frac{\pi}{vii} 3(viii) (ix) (x) \right) (xi)$ (xii) (ii)

(xiii) $\left((\xi v) \left((xv) (xvi) 0, (xvii) \frac{\pi}{xxviii} 2(xix) (\times) (\times i) \right) (xxii) (xxiii) (iii) \right)$

(xxiv) $\left((\times v) \left((xxvi) (\times vii) - \sqrt{(xxviii) 2(xix) (xxx)}, (\times \xi) \frac{\pi}{xxxxi} 4(x$

(xxxvii)



Watch Video Solution

42. A straight line is drawn through $P(3, 4)$ to meet the axis of x and y at A and B , respectively. If the rectangle $OACB$ is completed, then find the locus of C .



Watch Video Solution

43. A variable line passing through point $P(2, 1)$ meets the axes at A and B . Find the locus of the circumcenter of triangle OAB (where O is the origin).

[Watch Video Solution](#)

44. A point moves such that the area of the triangle formed by it with the points $(1, 5)$ and $(3, -7)$ is 21 sq units. Then, find the locus of the point.

[Watch Video Solution](#)

45. Find the locus of the point of intersection of lines $x \cos \alpha + y \sin \alpha = a$ and $x \sin \alpha - y \cos \alpha = b$ (α is a variable).

[Watch Video Solution](#)

46. Find the locus of the middle point of the portion of the line $x \cos \alpha + y \sin \alpha = p$ which is intercepted between the axes, given that p remains constant.

[Watch Video Solution](#)

47. Q is a variable point whose locus is $2x + 3y + 4 = 0$; corresponding to a particular position of Q , P is the point of section of OQ , O being the origin, such that $OP:PQ = 3:1$. Find the locus of P .



Watch Video Solution

48. Convert $y = 10$ into a polar equation.



Watch Video Solution

49. Convert the following Cartesian coordinates to the corresponding polar coordinates using positive r and negative r . (i)

(ii) (iii) ((iv) (v) $-1, 1$ (vi) (vii) (viii) (ii)

(ix) (x) ((xi) (xi) $2, -3$ (xiii) (xiv) (xv)



Watch Video Solution

50. Find the minimum distance of any point on the line $3x + 4y - 10 = 0$ from the origin using polar coordinates.



Watch Video Solution

51. If the difference between the roots of the equation $x^2 + ax + 1 = 0$ is less than $\sqrt{5}$, then the set of possible values of a is (1) $(-3, 3)$ (2) $(-3, \infty)$ (3) $(3, \infty)$ (4) $(-\infty, -3)$



Watch Video Solution

52. Express the polar equation $r = 2 \cos \theta$ in rectangular coordinates.



Watch Video Solution

53. Let L be the line of intersection of the planes $2x + 3y + z = 1$ and $x + 3y + 2z = 2$. If L makes an angles α with the positive x -axis, then \cos

α equals



Watch Video Solution

54. Convert $r \sin \theta = r \cos \theta + 4$ into its equivalent Cartesian equation.



Watch Video Solution

55. Convert $r = \sec \theta e^{r \cos \theta}$ into its equivalent Cartesian equation.



Watch Video Solution

56. A particle just clears a wall of height b at distance a and strikes the ground at a distance c from the point of projection. The angle of projection is (1) $\frac{\tan^{-1} b}{ac}$ (2) 45° (3) $\frac{\tan^{-1}(bc)}{a(c-a)}$ (4) $\frac{\tan^{-1}(bc)}{a}$



Watch Video Solution

$$\begin{aligned} & (vi)(vii)\left((viii)(ix)\sqrt{(x)2(xi)(xii)}, (\xi ii)\frac{\pi}{xiv}6(xv)(xvi)(xvii)\right)(xviii) \\ & \text{(xix)} \tag{iii} \\ & (xx)(\times i)\left((xxii)(\times iii) - 3, -(xxiv)\frac{\pi}{xxv}6(xxvi)(\times vii)(\times viii)\right)(xxix) \\ & \text{(xxx)} \end{aligned}$$


58. If $(2, 3, 5)$ is one end of a diameter of the sphere $x^2 + y^2 + z^2 - 6x - 12y - 2z + 20 = 0$, then the coordinates of the other end of the diameter are (1) $(4, 9, -3)$ (2) $(4, -3, 3)$ (3) $(4, 3, 5)$ (4) $(4, 3, -3)$



Watch Video Solution

59. Convert $r = 4 \tan \theta \sec \theta$ into its equivalent Cartesian equation.



Watch Video Solution

60. Given the equation $4x^2 + 2\sqrt{3}xy + 2y^2 = 1$. Through what angle should the axes be rotated so that the term xy is removed from the transformed equation.



Watch Video Solution

61. The equation of a curve referred to a given system of axes is $3x^2 + 2xy + 3y^2 = 10$. Find its equation if the axes are rotated through an angle 45° , the origin remaining unchanged.



Watch Video Solution

62. Determine x so that the line passing through $(3, 4)$ and $(x, 5)$ makes an angle of 135° with the positive direction of the x-axis.



Watch Video Solution

63. What does the equation $2x^2 + 4xy - 5y^2 + 20x - 22y - 14 = 0$ become when referred to the rectangular axes through the point $(-2, -3)$, the new axes being inclined at an angle at 45° with the old axes?



Watch Video Solution

64. Shift the origin to a suitable point so that the equation $y^2 + 4y + 8x - 2 = 0$ will not contain a term in y and the constant term.



Watch Video Solution

65. At what point should the origin be shifted if the coordinates of a point $(4, 5)$ become $(-3, 9)$?



Watch Video Solution

66. Find the equation to which the equation $x^2 + 7xy - 2y^2 + 17x - 26y - 60 = 0$ is transformed if the origin is shifted to the point $(2, -3)$, the axes remaining parallel to the original axes.



[Watch Video Solution](#)

67. The equation of curve referred to the new axes, axes retaining their directions, and origin $(4, 5)$ is $X^2 + Y^2 = 36$. Find the equation referred to the original axes.



[Watch Video Solution](#)

68. If the point $(2, 3)$, $(1, 1)$, and $(x, 3x)$ are collinear, then find the value of x , using slope method.



[Watch Video Solution](#)

69. Which line is having the greatest inclination with the positive direction of the x-axis?

(i) Line joining the points $(1, 3)$ and $(4, 7)$

(ii) Line $3x - 4y + 3 = 0$



Watch Video Solution

70. Find the orthocentre of $\triangle ABC$ with vertices $A(1, 0)$, $B(-2, 1)$, and $C(5, 2)$



Watch Video Solution

71. The angle between the line joining the points $(1, -2)$, $(3, 2)$ and the line $x + 2y - 7 = 0$ is



Watch Video Solution

72. The line joining the points $A(2, 1)$ and $B(3, 2)$ is perpendicular to the line $(a^2)x + (a + 2)y + 2 = 0$. Find the values of a .



Watch Video Solution

73. For what value of k are the points $(k, 2 - 2k)$, $(-k + 1, 2k)$ and $(-4 - k, 6, 6 - 2k)$ are collinear?



Watch Video Solution

74. Find the area of the quadrilateral $ABCD$ having vertices $A(1, 1)$, $B(7, -3)$, $C(12, 2)$, and $D(7, 21)$.



Watch Video Solution

75. Given that $P(3, 1)$, $Q(6, 5)$, and $R(x, y)$ are three points such that the angle PQR is a right angle and the area of RQP is 7, find the value

of $4x - 3y + 5$



Watch Video Solution

76. If O is the origin and if the coordinates of any two points Q_1 and Q_2 are (x_1, y_1) and (x_2, y_2) , respectively, prove that $OO_1 \cdot OO_2 \cos \angle Q_1 O Q_2 = x_1 x_2 + y_1 y_2$.



Watch Video Solution

77. Prove that the area of the triangle whose vertices are $(t, t - 2)$, $(t + 2, t + 2)$, and $(t + 3, t)$ is independent of t .



Watch Video Solution

78. Find the area of a triangle having vertices $A(3, 2)$, $B(11, 8)$ and $C(8, 12)$.



Watch Video Solution

79. In ABC Prove that $AB^2 + AC^2 = 2(AO^2 + BO^2)$, where O is the middle point of BC



Watch Video Solution

80. Two points $O(0, 0)$ and $A(3, \sqrt{3})$ with another point P form an equilateral triangle. Find the coordinates of P .



Watch Video Solution

81. Find the coordinate of the circumcenter of the triangle whose vertices are $A(5, -1)$, $B(-1, 5)$, and $C(6, 6)$. Find its radius also.



Watch Video Solution

82. Find the orthocentre of $\triangle ABC$ with vertices $A(1, 0)$, $B(-2, 1)$, and $C(5, 2)$



Watch Video Solution

83. If $(b_2 - b_1)(b_3 - b_1) + (a_2 - a_1)(a_3 - a_1) = 0$, then prove that the circumcenter of the triangle having vertices (a_1, b_1) , (a_2, b_2) and (a_3, b_3) is $\left(\frac{a_2 + a_3}{2}, \frac{b_2 + b_3}{2} \right)$



Watch Video Solution

84. If line $3x - ay - 1 = 0$ is parallel to the line $(a + 2)x - y + 3 = 0$ then find the value of a .



Watch Video Solution

85. If $A(2, -1)$ and $B(6, 5)$ are two points, then find the ratio in which the foot of the perpendicular from $(4, 1)$ to AB divides it.



Watch Video Solution

86. Angle of a line with the positive direction of the x-axis is θ . The line is rotated about some point on it in anticlockwise direction by angle 45° and its slope becomes 3. Find the angle θ .



Watch Video Solution

87. Let $A(6, 4)$ and $B(2, 12)$ be two given points. Find the slope of a line perpendicular to AB .



Watch Video Solution

88. If the points $(a, 0)$, $(b, 0)$, $(0, c)$, and $(0, d)$ are concyclic ($a, b, c, d > 0$), then prove that $ab = cd$.



Watch Video Solution

89. If $A(-2, 1)$, $B(2, 3)$ and $C(-2, -4)$ are three points, find the angle between BA and BC .



Watch Video Solution

90. The line joining the points $(x, 2x)$ and $(3, 5)$ makes an obtuse angle with the positive direction of the x-axis. Then find the values of x .



Watch Video Solution

91. If the line passing through $(4, 3)$ and $(2, k)$ is parallel to the line $y = 2x + 3$, then find the value of k .

[Watch Video Solution](#)

92. Find the area of the pentagon whose vertices are $A(1, 1)$, $B(7, 21)$, $C(7, -3)$, $D(12, 2)$, and $E(0, -3)$

[Watch Video Solution](#)

93. Let $A = (3, 4)$ and B is a variable point on the lines $|x| = 6$. If $AB \leq 4$, then find the number of position of B with integral coordinates.

[Watch Video Solution](#)

94. The three points $(-2, 2)$, $(8, -2)$, and $(-4, -3)$ are the vertices of (a) an isosceles triangle (b) an equilateral triangle (c) a right-angled triangle (d) none of these

[Watch Video Solution](#)

95. The points $(-a, -b), (a, b), (a^2, ab)$ are (a) vertices of an equilateral triangle (b) vertices of a right angled triangle (c) vertices of an isosceles triangle (d) collinear



Watch Video Solution

96. The distance between the point $(a \cos \alpha, a \sin \alpha)$ and $(a \cos \beta, a \sin \beta)$ is



Watch Video Solution

97. Find the length of altitude through A of the triangle ABC , where $A \equiv (-3, 0), B \equiv (4, -1), C \equiv (5, 2)$



Watch Video Solution

98. If the coordinates of two points A and B are $(3, 4)$ and $(5, -2)$, respectively, find the coordinates of any point P if $PA = PB$. Area of

PAB is 10 sq. units.



Watch Video Solution

99. If the point $(0, 0)$, $(2, 2\sqrt{3})$, and (p, q) are the vertices of an equilateral triangle, then (p, q) is

A. (a) $(0, -4)$

B. (b) $(4, 4)$

C. (c) $(4, 0)$

D. (d) $(5, 0)$

Answer: null



Watch Video Solution

100. Given points $P(2, 3)$, $Q(4, -2)$, and $R(\alpha, 0)$ (i) Find the value of α (ii) Find the value of α (iii) (iv) if $PR + RQ$ is minimum (v) Find the value of α (vi) Find the value of α (vii) Find the value of α (viii) Find the value of α (ix) Find the value of α

of $(x)\alpha(xi)$ (xii) if $(xiii)(\xi v)|(xv)PR - RQ|(xvi)$ (xvii) is maximum



[Watch Video Solution](#)

101. If the vertices of a triangle have rational coordinates, then prove that the triangle cannot be equilateral.



[Watch Video Solution](#)