# びdoubtnut 

## MATHS

## BOOKS - CENGAGE MATHS (ENGLISH)

## DIFFERENT PRODUCTS OF VECTORS AND THEIR GEOMETRICAL APPLICATIONS

## Illustration

1. Find the angle between the following pairs of vectors $3 \hat{i}+2 \hat{j}-6 \hat{k}, 4 \hat{i}-3 \hat{j}+\hat{k}, \hat{i}-2 \hat{j}+3 \hat{k}, 3 \hat{i}-2 \hat{j}+\hat{k}$

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2. If $\vec{a}$, $\vec{b}$ and $\vec{c}$ are non-zero vectors such that $\vec{a} . \vec{b}=\vec{a}$. $\vec{c}$, then find the goemetrical relation between the vectors.
3. if $\vec{r} \cdot \vec{i}=\vec{r} \cdot \vec{j}=\vec{r} \cdot \vec{k}$ and $|\vec{r}|=3$, then find vector $\vec{r}$.

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4. If $\vec{a}, \vec{b}$ and $\vec{c}$ are unit vectors such that $\vec{a}+\vec{b}+\vec{c}=0$, then the value of $\vec{a} \cdot \vec{b}+\vec{b} \cdot \vec{c}+\vec{c} \cdot \vec{a}$ is

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5. if $\vec{a}, \vec{b}$ and $\vec{c}$ are mutally perpendicular vectors of equal magnitudes, then find the angle between vectors and $\vec{a}+\vec{b}+\vec{c}$.

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6. If $|\vec{a}|+|\vec{b}|=|\vec{c}|$ and $\vec{a}+\vec{b}=\vec{c}$ then find the angle between $\vec{a}$ and $\vec{b}$.
7. If three unit vectors $\vec{a}, \vec{b}$ and $\vec{c}$ satisfy $\vec{a}+\vec{b}+\vec{c}=\overrightarrow{0}$. Then find the angle between $\vec{a}$ and $\vec{b}$.

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8. If $\theta$ is the angle between the unit vectors $\vec{a}$ and $\vec{b}$, then prove that
i. $\cos \left(\frac{\theta}{2}\right)=\frac{1}{2}|\vec{a}+\vec{b}|$
ii. $\sin \left(\frac{\theta}{2}\right)=\frac{1}{2}|\vec{a}-\vec{b}|$

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9. find the projection of the vector $\hat{i}+3 \hat{j}+7 \hat{k}$ on the vector $7 \hat{i}-\hat{j}+8 \hat{k}$

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10. If the scalar projection of vector $x \hat{i}-\hat{j}+\hat{k} 1$ on vector $2 \hat{i}-\hat{j}+5 \hat{k} i s \frac{1}{\sqrt{30}}$. The find the value of $x$.

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11. If $\vec{a}=x \hat{i}+(x-1) \hat{j}+\hat{k}$ and $\vec{b}=(x+1) \hat{i}+\hat{j}+a \hat{k}$ make an acute angle $\forall x \in R$, then find the values of $a$

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12. If $\vec{a} . \vec{i}=\vec{a} .(\hat{i}+\hat{j})=\vec{a}$. $(\hat{i}+\hat{j}+\hat{k})$. Then find the unit vector $\vec{a}$.

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13. Prove by vector method that $\cos (A+B)=\cos A \cos B-\sin A \sin B$
14. In any triangle $A B C$, prove the projection formula $a=b \cos C+c \cos B$ using vector method.

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15. Prove that an angle inscribed in a semi-circle is a right angle using vector method.

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16. Using dot product of vectors, prove that a parallelogram, whose diagonals are equal, is a rectangle

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17. If $a+2 b+3 c=4$, then find the least value of $a^{2}+b^{2}+c^{2}$
18. A unit vector a makes an angle $\frac{\pi}{4}$ with $z$-axis. If $a+i+j$ is a unit vector, then a can be equal to

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19. vectors $\vec{a}, \vec{b}$ and $\vec{c}$ are of the same length and when take they form equal angles. If $\vec{a}=\hat{i}+\hat{j}$ and $\vec{b}=\hat{j}+\hat{k}$ then find vector $\vec{c}$.

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20. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three mutually perpendicular unit vectors and $\vec{d}$ is a unit vector which makes equal angle with $\vec{a}, \vec{b}$ and $\vec{c}$, then find the value of $|\vec{a}+\vec{b}+\vec{c}+\vec{d}|^{2}$.

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21. A particle acted on by constant forces $4 \vec{i}+\vec{j}-3 \vec{k}$ and $3 \vec{i}+\vec{j}-\vec{k}$ is displaced from the point $\vec{i}+2 \vec{j}+3 \vec{k}$ to the point $5 \vec{i}+4 \vec{j}+\vec{k}$. Find the total work done by the forces

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22. If $\vec{a}, \vec{b}, \vec{c}$ are mutually perpendicular vectors of equal magnitude show that $\vec{a}+\vec{b}+\vec{c}$ is equally inclined to $\vec{a}, \vec{b}$ and $\vec{c}$

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23. If $\vec{a}=4 \hat{i}+6 \hat{j}$ and $\vec{b}=3 \hat{i}+4 \hat{k}$ find the vector component of $\vec{a}$ along $\vec{b}$.

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24. If $|\vec{a}|=|\vec{b}|=|\vec{a}+\vec{b}|=1$ then find the value of $|\vec{a}-\vec{b}|$

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25. If $\vec{a}=-\hat{i}+\hat{j}+\hat{k}$ and $\vec{b}=2 \hat{i}+0 \hat{j}+\hat{k}$ then find vector $\vec{c}$ satisfying the following conditions, (i) that it is coplaner with $\vec{a}$ and $\vec{b}$, (ii) that it is $\perp$ to $\vec{b}$ and (iii) that $\vec{a} \cdot \vec{c}=7$.

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26. If $\vec{a}, \vec{b}$ and $\vec{c}$ are vectors such that $|\vec{a}|=3,|\vec{b}|=4$ and $|\vec{c}|=5$ and $(\vec{a}+\vec{b})$ is perpendicular to $\vec{c},(\vec{b}+\vec{c})$ is perpendicular to $\vec{a}$ and $(\vec{c}+\vec{a})$ is perpendicular to $\vec{b}$ then $|\vec{a}+\vec{b}+\vec{c}|=$ (A) $4 \sqrt{3}$ (B) $5 \sqrt{2}$ (C) 2 (D) 12

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27. Prove that in a tetrahedron if two pairs of opposite edges are perpendicular , then the third pair is also perpendicular.
28. In the isosceles triangle $A B C,|\overrightarrow{A B}|=|\overrightarrow{B C}|=8$,a point $E$ divide $A B$ internally in the ratio $1: 3$, then the cosine of the angle between $C E$ and
$\overrightarrow{C A}$ is (where $|\overrightarrow{C A}|=12$ )

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29. An arc $A C$ of a circle subtends a right angle at then the center $O$. the point $B$ divides the arc in the ratio $1: 2$, If $\vec{O} A=a \& \vec{O} B=b$. then the vector $\vec{O} C$ in terms of $a \& b$, is

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30. Vector $\vec{O} A=\hat{i}+2 \hat{j}+2 \hat{k}$ turns through a right angle passing through the positive $x$-axis on the way. Show that the vector in its new position is

## $4 \hat{i}-\hat{j}-\hat{k}$. $\sqrt{2}$

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31. The base of the pyramid $A O B C$ is an equilateral triangle $O B C$ with each side equal to $4 \sqrt{2}, O$ is the origin of reference, $A O$ is perpendicualar to the plane of $O B C$ and $|\vec{A} O|=2$. Then find the cosine of the angle between the skew straight lines, one passing though $A$ and the midpoint of $O B a n d$ the other passing through $O$ and the mid point of $B C$

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32. Find $|\vec{a} \times \vec{b}|$, if $\vec{a}=\hat{i}-7 \hat{j}+7 \hat{k}$ and $\vec{b}=3 \hat{i}-2 \hat{j}+2 \hat{k}$.

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33. Let the vectors $\vec{a}$ and $\vec{b}$ be such that $|\vec{a}|=3$ and $|\vec{b}|=\frac{\sqrt{2}}{3}$ then $\mid \vec{a} \times \vec{b}$ is a unit vector. If the angle between $\vec{a}$ and $\vec{b}$ is ?

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34. Prove that $(\vec{a}-\vec{b}) \times(\vec{a}+\vec{b})=2(\vec{a} \times \vec{b})$ also interpret this result.

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35. Let $\vec{a}=\hat{i}+4 \hat{j}+2 \hat{k}, \vec{b}=3 \hat{i}-2 \hat{j}+7 \hat{k}$ and $\vec{c}=2 \hat{i}-2 \hat{j}+4 \hat{k}$. Find a vector
$\vec{d}$ which perpendicular to both $\vec{a}$ and $\vec{b}$ and $\vec{c} . \vec{d}=15$.

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36. If $A$, $B a n d C$ are the vetices of a triangle $A B C$, then prove sine rule

$$
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}
$$

37. Using cross product of vectors, prove that $\sin (A+B)=\sin A \cos B+\cos A \sin B$

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38. Find a unit vector perpendicular to the plane determined by the points (1, - 1, 2), (2, 0, - 1) and( $0,2,1$ )

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39. If $\vec{a}$ and $\vec{b}$ are two vectors, then prove that $(\vec{a} \times \vec{b})^{2}=\left|\begin{array}{ll}\vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b}\end{array}\right|$

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40. If $|\vec{a}|=2$ then find the value of $|\vec{a} \times \vec{i}|^{2}+|\vec{a} \times \vec{j}|^{2}+|\vec{a} \times \vec{k}|^{2}$

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41. $\vec{r} \times \vec{a}=\vec{b} \times \vec{a}, \vec{r} \times \vec{b}=\vec{a} \times \vec{b}, \vec{a} \neq \overrightarrow{0}, \vec{b} \neq \overrightarrow{0}, \vec{a} \neq \lambda \vec{b}$ and $\vec{a}$ is not perpendicular to $\vec{b}$, then find $\vec{r}$ in terms of $\vec{a}$ and $\vec{b}$.

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42. $A, B, C a n d D$ are any four points in the space, then prove that
$|\vec{A} B \times \vec{C} D+\vec{B} C \times \vec{A} D+\vec{C} A \times \vec{B} D|=4$ (area of $A B C$.

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43. If $\vec{a}, \vec{b}$ and $\vec{c}$ are the position vectors of the vertices $A, B$ and $C$. respectively, of $\triangle A B C$. Prove that the perpendicualar distance of the vertex $A$ from the base $B C$ of the triangle $A B C$ is $\frac{|\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}|}{}$

$$
|\vec{c}-\vec{b}|
$$

44. Using vectors, find the area of the triangle with vertices $A(1,1,2), B(2,3,5)$ and $C(1,5,5)$

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45. Find the area of the parallelogram whose adjacent sides are given by the vectors $\vec{a}=\hat{i}-\hat{j}+3 \hat{k}$ and $\vec{b}=2 \hat{i}-7 \hat{j}+\hat{k}$

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46. Area of a parallelogram, whose diagonals are $3 \hat{i}+\hat{j}-2 \hat{k}$ and $\hat{i}-3 \hat{j}+4 \hat{k}$ will be:
47. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be three vectors such that $\vec{a} \neq 0,|\vec{a}|=|\vec{c}|=1,|\vec{b}|=4$ and $|\vec{b} \times \vec{c}|=\sqrt{15}$. If $\vec{b}-2 \vec{c}=\lambda \vec{a}$ then find the value of $\lambda$.

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48. Find the moment about (1,-1,-1) of the force $3 \hat{i}+4 \hat{j}-5 \hat{k}$ acting at $(1,0,-2)$

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49. A rigid body is spinning about a fixed point ( $3,-2,-1$ ) with an angular velocity of $4 \mathrm{rad} / \mathrm{s}$, the axis of rotation being in the direction of $(1,2,2)$. Find the velocity of the particle at point $(4,1,1)$.

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50. If $\vec{a} \times \vec{b}=\vec{c} \times \vec{d}$ and $\vec{a} \times \vec{c}=\vec{b} \times \vec{d}$ show that $(\vec{a}-\vec{d})$ is parallel to $(\vec{b}-\vec{c})$.

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51. Show by a numerical example that $\vec{a} \times \vec{b}=\vec{a} \times \vec{c}$ does not imply $\vec{b}=\vec{c}$

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52. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are the position vectors of the vertices of a cycle quadrilateral

> ABCD,
prove
that

$$
\frac{|\vec{a} \times \vec{b}+\vec{b} \times \vec{d}+\vec{d} \times \vec{a}|}{(\vec{b}-\vec{a}) \cdot(\vec{d}-\vec{a})}+\frac{|\vec{b} \times \vec{c}+\vec{c} \times \vec{d}+\vec{d}+\vec{d} \times \vec{b}|}{(\vec{b}-\vec{c}) \cdot(\vec{d}-\vec{c})}
$$

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53. The postion vectors of the vertrices fo aquadrilateral with $A$ as origian are $B(\vec{b}), D(\vec{d})$ and $C(\vec{b}+m \vec{d})$. Prove that the area of the quadrilateral is $\frac{1}{2}(l+m)|\vec{b} \times \vec{d}|$.

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54. Let $\vec{a}$ and $\vec{b}$ be unit vectors such that $|\vec{a}+\vec{b}|=\sqrt{3}$. Then find the value of $(2 \vec{a}+5 \vec{b}) \cdot(3 \vec{a}+\vec{b}+\vec{a} \times \vec{b})$

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55. uandv are two non-collinear unit vectors such that $\left|\frac{\hat{u}+\hat{v}}{2}+\hat{u} \times \hat{v}\right|=1$. Prove that $|\hat{u} \times \hat{v}|=\left|\frac{\hat{u}-\hat{v}}{2}\right|$.

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56. In a $\triangle A B C$ points $D, E, F$ are taken on the sides $B C, C A$ and $A B$ respectively such that $\frac{B D}{D C}=\frac{C E}{E A}=\frac{A F}{F B}=n$ prove that $\triangle D E F=\frac{n^{2}-n+1}{(n+1)^{2}} \triangle A B C$

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57. Let $A, B, C$ be points with position vectors
$2 \hat{i}-\hat{j}+\hat{k}, \hat{i}+2 \hat{j}+\hat{k}$ and $3 \hat{i}+\hat{j}+2 \hat{k}$ respectively. Find the shortest distance between point B and plane OAC.

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58. Let $\vec{a}=x \hat{i}+12 \hat{j}-\hat{k}, \vec{b}=2 \hat{i}+2 x \hat{j}+\hat{k}$ and $\vec{c}=\hat{i}+\hat{k}$. If the ordered set $[\vec{b} \vec{c} \vec{a}]$ is left handed, then find the value of $x$.

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59. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar vectors, then find the value of $\frac{\vec{a} \cdot(\vec{b} \times \vec{c})}{\vec{b} \cdot(\vec{c} \times \vec{a})}+\frac{\vec{b} \cdot(\vec{c} \times \vec{a})}{\vec{c} \cdot(\vec{a} \times \vec{b})}+\frac{\vec{c} \cdot(\vec{b} \times \vec{a})}{\vec{a} \cdot(\vec{b} \times \vec{c})}$

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60. if the vectors $2 \hat{i}-3 \hat{j}, \hat{i}+\hat{j}-\hat{k}$ and $3 \hat{i}-\hat{k}$ from three concurrent edges of a parallelpiped, then find the volume of the parallelepied.

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61. The postion vectors of the four angular points of a tetrahedron are $A(\hat{j}+2 \hat{k}), B(3 \hat{i}+\hat{k}), C(4 \hat{i}+3 \hat{j}+6 \hat{k})$ and $D(2 \hat{i}+3 \hat{j}+2 \hat{k})$ find the volume of the tetrahedron $A B C D$.

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62. Let $\vec{a}, \vec{b}, \vec{c}$ be three unit vectors and $\vec{a} \cdot \vec{b}=\vec{a} \cdot \vec{c}=0$. If the angle between $\vec{b}$ and $\vec{c}$ is $\frac{\pi}{3}$ then find the value of $|[\vec{a} \vec{b} \vec{c}]|$

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63. Prove that $[\vec{a}+\vec{b} \vec{b}+\vec{c} \vec{c}+\vec{a}]=2[\vec{a} \vec{b} \vec{c}]$

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64. Show that: $[\vec{l} \vec{m} \vec{n}][\vec{a} \vec{b} \vec{c}]=\left|\begin{array}{lll}\vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \cdot \vec{c} \\ \vec{m} \cdot \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \cdot \vec{c} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n} \cdot \vec{c}\end{array}\right|$

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65. If $\vec{a}=\hat{i}+\hat{j}+\hat{k}, \hat{b}=\hat{i}-\hat{j}+\hat{k}, \vec{c}=\hat{i}+2 \hat{j}-\hat{k}$, then find the value of
$\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} . \vec{a} & \vec{c} . \vec{b} & \vec{c} \cdot \vec{c}\end{array}\right|$

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66. The value of a so thast the volume of parallelpiped formed by vectors
$\hat{i}+a \hat{j}+\hat{k}, \hat{j}+a \hat{k}, a \hat{i}+\hat{k}$ becomes minimum is (A) $\sqrt{93}$ ) (B) 2 (C) $\frac{1}{\sqrt{3}}$ (D) 3

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67. If $\vec{u}, \vec{v}$ and $\vec{w}$ are three non coplanar vectors then
$(\vec{u}+\vec{v}-\vec{w}) .(\vec{u}-\vec{v}) \times(\vec{v}-\vec{w})$ equals
(A) $\vec{u} \cdot(\vec{v} \times \vec{w})$
(B) $\vec{u} \cdot \vec{w} \times \vec{v}$
$2 \vec{u} .(\vec{v} \times \vec{w})(\mathrm{D}) 0$
68. If $\vec{a}$ and $\vec{b}$ are two vectors, such that $|\vec{a} \times \vec{b}|=2$, then find the value of $[\vec{a} \vec{b} \vec{a}] \times \vec{b}$.

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69. Find th altitude of a parallelepiped whose three coterminous edges are vectors $\vec{A}=\hat{i}+\hat{j}+\hat{k}, \vec{B}=2 \hat{i}+4 \hat{j}-\hat{k}$ and $\vec{C}=\hat{i}+\hat{j}+3 \hat{k} w i t h \vec{A}$ and $\vec{B}$ as the sides of the base of the parallelepiped.

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70. If $[\vec{a} \vec{b} \vec{c}]=2$, then find the value of $[(\vec{a}+2 \vec{b}-\vec{c})(\vec{a}-\vec{b})(\vec{a}-\vec{b}-\vec{c})]$

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71. If $\vec{a}, \vec{b}$ and $\vec{c}$ are , mutually perpendicular vcetors and $\vec{a}=\alpha(\vec{a} \times \vec{b})+\beta(\vec{b} \times \vec{c})+\gamma(\vec{c} \times \vec{a})$ and $[\vec{a} \vec{b} \vec{c}]=1$, then find the value
of $\alpha+\beta+\gamma$

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72. If $\vec{a}, \vec{b} a$ and $\vec{c}$ are non- coplanar vecotrs, then prove that $(\vec{a} \cdot \vec{d})(\vec{b} \times \vec{c})+(\vec{b} \cdot \vec{d})(\vec{c} \times \vec{a})+(\vec{c} \cdot \vec{d})(\vec{a} \times \vec{b})$ is independent of $\vec{d}$ where $\vec{d}$ is a unit vector.

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73. Prove that vectors $\vec{u}=\left(a l+a_{1} l_{1}\right) \hat{i}+\left(a m+a_{1} m_{1}\right) \hat{j}+\left(a n+a_{1} n_{1}\right) \hat{k}$ $\vec{v}=\left(b l+b_{1} l_{1}\right) \hat{i}+\left(b m+b_{1} m_{1}\right) \hat{j}+\left(b n+b_{1} n_{1}\right) \hat{k}$
$\vec{w}=\left(c l+c_{1} l_{1}\right) \hat{i}+\left(c m+c_{1} m_{1}\right) \hat{j}+\left(c n+c_{1} n_{1}\right) \hat{k}$ are coplanar.

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74. Let $G_{1}, G_{2}$ and $G_{3}$ be the centroids of the trianglular faces OBC,OCA and OAB , respectively, of a tetrahedron OABC . If $V_{1}$ denotes the volume of
the tetrahedron $O A B C$ and $V_{2}$ that of the parallelepiped with $O G_{1}, O G_{2}$ and $O G_{3}$ as three concurrent edges, then prove that $4 V_{1}=9 V_{2}$.

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75. Prove that $\hat{i} \times(\vec{a} \times \vec{i})+\hat{j} \times(\vec{a} \times \vec{j})+\hat{k} \times(\vec{a} \times \vec{k})=2 \vec{a}$

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76. If $\hat{i} \times[(\vec{a}-\hat{j}) \times \hat{i}] \times[(\vec{a}-\hat{k}) \times \hat{j}]+\vec{k} \times[(\vec{a}-\vec{i}) \times \hat{k}]=0$, then find vector $\vec{a}$.

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77. Let vea, $\vec{b}$ and $\vec{c}$ be any three vectors, then prove that
$\left[\begin{array}{lll}\vec{a} \times \vec{b} & \vec{b} \times \vec{c} & \vec{c} \times \vec{a}\end{array}\right]=[\vec{a} \vec{b} \vec{c}]^{2}$
78. For any four vectors prove that
$(\vec{b} \times \vec{c}) \cdot(\vec{a} \times \vec{d})+(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{d})+(\vec{a} \times \vec{b}) \cdot(\vec{c} \times \vec{d})=0$

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79. If $\vec{b}$ and $\vec{c}$ are two non-collinear such that $\vec{a}|\mid(\vec{b} \times \vec{c})$. Then prove that $(\vec{a} \times \vec{b}) \cdot(\vec{a} \times \vec{c})$ is equal to $|\vec{a}|^{2}(\vec{b} \cdot \vec{c})$ '

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80. Find the vector of length 3 unit which is perpendicular to $\hat{i}+\hat{j}+\hat{k}$ and lies in the plane of $\hat{i}+\hat{j}+\hat{k}$ and $2 \hat{i}-3 \hat{j}$

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81. Let $\hat{a}, \hat{b}$,and $\hat{c}$ be the non-coplanar unit vectors. The angle between $\hat{b}$ and $\hat{c}$ is $\alpha$, between $\hat{c}$ and $\hat{a}$ is $\beta$ and between $\hat{a}$ and $\hat{b}$ is $\gamma$. If $A(\hat{a} \cos \alpha, 0), B(\hat{b} \cos \beta, 0)$ and $C(\hat{c} \cos \gamma, 0)$, then show that in triangle $A B C, \frac{|\hat{a} \times(\hat{b} \times \hat{c})|}{\sin A}=\frac{|\hat{b} \times(\hat{c} \times \hat{a})|}{\sin B}=\frac{|\hat{c} \times(\hat{a} \times \hat{b})|}{\sin C}$

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82. find the cosine of the angle between the vectors $\vec{a}=3 \hat{i}+2 \hat{k}$ and
$\vec{b}=2 \hat{i}-2 \hat{j}+4 \hat{k}$

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83. If $\vec{b}$ is not perpendicular to $\vec{c}$. Then find the vector $\vec{r}$ satisfying the equation $\vec{r} \times \vec{b}=\vec{a} \times \vec{b}$ and $\vec{r} \cdot \vec{c}=0$

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84. If $\vec{a}$ and $\vec{b}$ are two given vectors and k is any scalar,then find the vector $\vec{r}$ satisfying $\vec{r} \times \vec{a}+k \vec{r}=\vec{b}$.

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85. $\vec{r} \times \vec{a}=\vec{b} \times \vec{a}, \vec{r} \times \vec{b}=\vec{a} \times \vec{b}, \vec{a} \neq \overrightarrow{0}, \vec{b} \neq \overrightarrow{0}, \vec{a} \neq \lambda \vec{b}$ and $\vec{a}$ is not perpendicular to $\vec{b}$, then find $\vec{r}$ in terms of $\vec{a}$ and $\vec{b}$.

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86. if vectors $3 \hat{i}-2 \hat{j}+m \hat{k}$ and $-2 \hat{i}+\hat{j}+4$ hat $k$ are perpendicular to each other, find the value of $m$

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87. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be three non- coplanar vectors and $\vec{r}$ be any arbitrary vector. Then $(\vec{a} \times \vec{b}) \times(\vec{r} \times \vec{c})+(\vec{b} \times \vec{c}) \times(\vec{r} \times \vec{a})+(\vec{c} \times \vec{a})(\vec{r} \times \vec{b})$ is always equal to

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88. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non coplanar and unit vectors such that $\vec{a} \times(\vec{b} \times \vec{c})=\frac{\vec{b}+\vec{c}}{\sqrt{2}}$ then the angle between $\vec{a}$ and $\vec{b}$ is (A) $\frac{3 \pi}{4}$ (B) $\frac{\pi}{4}$ (C) $\frac{\pi}{2}$ (D) $\pi$

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89. 

Prove
that

$$
\frac{[\vec{R} \vec{\beta} \times(\vec{\beta} \times \vec{\alpha})] \vec{\alpha}}{|\vec{\alpha} \times \vec{\beta}|^{2}}+\frac{[\vec{R} \vec{\alpha} \times(\vec{\alpha} \times \vec{\beta})] \vec{\beta}}{|\vec{\alpha} \times \vec{\beta}|^{2}}=\frac{[\vec{R} \vec{\alpha} \vec{\beta}](\vec{\alpha} \times \vec{\beta})}{|\vec{\alpha} \times \vec{\beta}|^{2}}
$$

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90. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar non-zero vectors, then prove that $(\vec{a} \cdot \vec{a}) \vec{b} \times \vec{c}+(\vec{a} \cdot \vec{b}) \vec{c} \times \vec{a}+(\vec{a} \cdot \vec{c}) \vec{a} \times \vec{b}=[\vec{b} \vec{c} \vec{a}] \vec{a}$

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91. Find a set of vectors reciprocal to the set $-\hat{i}+\hat{j}+\hat{k}, \hat{i}-\hat{j}+\hat{k}, \hat{i}+\hat{j}+\hat{k}$

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92. find the scalar and vector projection of $3 \hat{i}-\hat{j}+4 \hat{k} o n 2 \hat{i}+3 \hat{j}-6 \hat{k}$

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93. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{a}^{\prime}, \vec{b}^{\prime}, \vec{c}^{\prime}$ are reciprocal system of vectors, then prove
that $\vec{a}^{\prime} \times \vec{b}^{\prime} \times \vec{b}, \times \vec{c}^{\prime}+\vec{c}^{\prime} \times \vec{a}^{\prime}=\frac{\vec{a}+\vec{b}+\vec{c}}{}$

$$
[\vec{a} \vec{b} \vec{c}]
$$

94. $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar vectors and $\vec{r}$. Is any arbitrary vector. Prove that $[\vec{b} \vec{c} \vec{r}] \vec{a}+[\vec{c} \vec{a} \vec{r}] \vec{b}+[\vec{a} \vec{b} \vec{r}] \vec{c}=[\vec{a} \vec{b} \vec{c}] \vec{r}$.

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95. Find the angle between the following pairs of vectors $3 \hat{i}+2 \hat{j}-6 \hat{k}, 4 \hat{i}-3 \hat{j}+\hat{k}, \hat{i}-2 \hat{j}+3 \hat{k}, 3 \hat{i}-2 \hat{j}+\hat{k}$

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96. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non-zero vectors such that $\vec{a} . \vec{b}=\vec{a}$. $\vec{c}$, then find the goemetrical relation between the vectors.

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97. if $\vec{r} . \vec{i}=\vec{r} . \vec{j}=\vec{r} . \vec{k}$ and $|\vec{r}|=3$, then find vector $\vec{r}$.
98. If $\vec{a}, \vec{b}$ and $\vec{c}$ are unit vectors such that $\vec{a}+\vec{b}+\vec{c}=0$, then the value of $\vec{a} \cdot \vec{b}+\vec{b} \cdot \vec{c}+\vec{c} . \vec{a}$ is

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99. if $\vec{a}, \vec{b}$ and $\vec{c}$ are mutally perpendicular vectors of equal magnitudes, then find the angle between vectors and $\vec{a}+\vec{b}=\vec{c}$.

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100. If $|\vec{a}|+|\vec{b}|=|\vec{c}|$ and $\vec{a}+\vec{b}=\vec{c}$ then find the angle between $\vec{a}$ and $\vec{b}$
101. If three unit vectors $\vec{a}, \vec{b}$ and $\vec{c}$ satisfy $\vec{a}+\vec{b}+\vec{c}=\overrightarrow{0}$. Then find the angle between $\vec{a}$ and $\vec{b}$.

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102. If $\theta$ is the angle between the unit vectors $\vec{a}$ and $\vec{b}$, then prove that
i. $\cos \left(\frac{\theta}{2}\right)=\frac{1}{2}|\vec{a}+\vec{b}|$
ii. $\sin \left(\frac{\theta}{2}\right)=\frac{1}{2}|\vec{a}-\vec{b}|$

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103. find the projection of the vector $\hat{i}+3 \hat{j}=7 \hat{k}$ on the vector $7 \hat{i}-\hat{j}+8 \hat{k}$

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104. If the scalar projection of vector $x \hat{i}-\hat{j}+\hat{k} 1$ on vector $2 \hat{i}-\hat{j}+5 \hat{k} i s \frac{1}{\sqrt{30}}$. The find the value of $x$.

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105. If $\vec{a}=x \hat{i}+(x-1) \hat{j}+\hat{k}$ and $\vec{b}=(x+1) \hat{i}+\hat{j}+a \hat{k}$ make an acute angle $\forall x \in R$, then find the values of $a$.

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106. If $\vec{a}$. $\vec{i}=\vec{a} .(\hat{i}+\hat{j})=\vec{a} .(\hat{i}+\hat{j}+\hat{k})$. Then find the unit vector $\vec{a}$.

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107. Prove by vector method that $\cos (A+B)=\cos A \cos B-\sin A \sin B$

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108. In any triangle $A B C$, prove the projection formula $a=b \cos C+c \cos B$ using vector method.

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109. Prove that an angle inscribed in a semi-circle is a right angle using vector method.

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110. Using dot product of vectors, prove that a parallelogram, whose diagonals are equal, is a rectangle

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111. If $a+2 b+3 c=4$, then find the least value of $a^{2}+b^{2}+c^{2}$
112. about to only mathematics

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113. Vectors $\vec{a}, \vec{b}$ and $\vec{c}$ are of the same length and when taken paire they form equal angles. If $\vec{a}=\hat{i}+\hat{j}$ and $\vec{b}=\hat{j}+\hat{k}$ then find vector $\vec{c}$.

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114. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three mutually perpendicular unit vectors and $\vec{d}$ is a unit vector which makes equal angle with $\vec{a}, \vec{b}$ and $\vec{c}$, then find the value of $|\vec{a}+\vec{b}+\vec{c}+\vec{d}|^{2}$.

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115. A particle acted upon by constant forces $4 \hat{i}+\hat{j}-3 \hat{k}$ and $3 \hat{i}+\hat{j}-\hat{k}$ is displaced from the point $\hat{i}+2 \hat{j}+3 \hat{k}$ to point $5 \hat{i}+4 \hat{j}+\hat{k}$. The total work done by the forces in Sl unit is

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116. If $\vec{a}, \vec{b}, \vec{c}$ are mutually perpendicular vectors of equal magnitudes, show that the vector $\vec{a}+\vec{b}+\vec{c}$ is equally inclined to $\vec{a}, \vec{b}$ and $\vec{c}$.

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117. If $\vec{a}=4 \hat{i}+6 \hat{j}$ and $\vec{b}=3 \hat{i}+4 \hat{k}$ find the vector component of $\vec{a}$ along $\vec{b}$.

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118. If $|\vec{a}|=|\vec{b}|=|\vec{a}+\vec{b}|=1$ then find the value of $|\vec{a}-\vec{b}|$
119. If $\vec{a}=-\hat{i}+\hat{j}+\hat{k}$ and $\vec{b}=2 \hat{i}+0 \hat{j}+\hat{k}$ then find vector $\vec{c}$ satisfying the following conditions, (i) that it is coplaner with $\vec{a}$ and $\vec{b}$, (ii) that it is $\perp$ to $\vec{b}$ and (iii) that $\vec{a} . \vec{c}=7$.

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120. Let $\vec{a}, \vec{b}$ and $\vec{c}$ are vectors such that
$|\vec{a}|=3,|\vec{b}|=4$ and $|\vec{c}|=5$, and $(\vec{a}+\vec{b})$ is perpendicular to $\vec{c},(\vec{b}+\vec{c})$ is perpendiculatr to $\vec{a}$ and $(\vec{c}+\vec{a})$ is perpendicular to $\vec{b}$. Then find the value of $|\vec{a}+\vec{b}+\vec{c}|$.

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121. Prove that in a tetrahedron if two pairs of opposite edges are perpendicular, then the thrid pair is also perpendicular.
122. In isosceles triangle $A B C|\overrightarrow{A B}|=|\overrightarrow{B C}|=8$ a point $E$ divides $A B$ internally in the ratio $1: 3$, then find the angle between $C E$ and $C A$ ( where $|\overrightarrow{C A}|=12)$

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123. An $\operatorname{arc} A C$ of a circle subtends a right angle at then the center $O$. the point $B$ divides the arc in the ratio $1: 2$, If $\vec{O} A=a \& \vec{O} B=b$. then the vector $\vec{O} C$ in terms of $a \& b$, is

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124. Vector $\vec{O} A=\hat{i}+2 \hat{j}+2 \hat{k}$ turns through a right angle passing through the positive $x$-axis on the way. Show that the vector in its new position is

## $4 \hat{i}-\hat{j}-\hat{k}$. $\sqrt{2}$

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125. The base of the pyramid $A O B C$ is an equilateral triangle $O B C$ with each side equal to $4 \sqrt{2}, O$ is the origin of reference, $A O$ is perpendicualar to the plane of $O B C$ and $|\vec{A} O|=2$. Then find the cosine of the angle between the skew straight lines, one passing though $A$ and the midpoint of $O B a n d$ the other passing through $O$ and the mid point of $B C$

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126. Find $|\vec{a} \times \vec{b}|$, if $\vec{a}=2 \hat{i}-7 \hat{j}+7 \hat{k}$ and $\vec{b}=3 \hat{i}-2 \hat{j}+2 \hat{k}$

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127. Let the vectors $\vec{a}$ and $\vec{b}$ be such that $|\vec{a}|=3$ and $|\vec{b}|=\frac{\sqrt{2}}{3}$ then $\mid \vec{a} \times \vec{b}$ is a unit vector. If the angle between $\vec{a}$ and $\vec{b}$ is ?

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128. Show that $(\vec{a}-\vec{b}) \times(\vec{a}+\vec{b})=2(\vec{a} \times \vec{b})$

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129. Let $\vec{a}=\hat{i}+4 \hat{j}+2 \hat{k}, \vec{b}=3 \hat{i}-2 \hat{j}+7 \hat{k}$ and $\vec{c}=2 \hat{i}-2 \hat{j}+4 \hat{k}$. Find a vector $\vec{d}$ which perpendicular to both $\vec{a}$ and $\vec{b}$ and $\vec{c} . \vec{d}=15$.

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130. If $A, B$ and $C$ are the vetices of a triangle $A B C$, then prove sine rule

$$
\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}
$$

131. Using cross product of vectors , prove that $(\sin A+B)-\sin A \cos B+\cos A \sin B$.

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132. Find a unit vector perpendicular to the plane determined by the points (1, - 1, 2), (2, 0, - 1) and( $0,2,1$ )

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133. If $\vec{a}$ and $\vec{b}$ are two vectors, then prove that $(\vec{a} \times \vec{b})^{2}=\left|\begin{array}{ll}\vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b}\end{array}\right|$

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134. If $|\vec{a}|=2$ then find the value of $|\vec{a} \times \vec{i}|^{2}+|\vec{a} \times \vec{j}|^{2}+|\vec{a} \times \vec{k}|^{2}$

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135. $\vec{r} \times \vec{a}=\vec{b} \times \vec{a}, \vec{r} \times \vec{b}=\vec{a} \times \vec{b}, \vec{a} \neq \overrightarrow{0}, \vec{b} \neq \overrightarrow{0}, \vec{a} \neq \lambda \vec{b}$ and $\vec{a}$ is not perpendicular to $\vec{b}$, then find $\vec{r}$ in terms of $\vec{a}$ and $\vec{b}$.

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136. $A, B, C a n d D$ are any four points in the space, then prove that
$|\vec{A} B \times \vec{C} D+\vec{B} C \times \vec{A} D+\vec{C} A \times \vec{B} D|=4$ (area of $A B C$.)

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137. If $\vec{a}, \vec{b}$ and $\vec{c}$ are the position vectors of the vertices $A, B$ and $C$. respectively of $\triangle A B C$. Prove that the perpendicualar distance of the
vertex $A$ from the base $B C$ of the triangle $A B C$ is $\underline{|\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}|}$

$$
|\vec{c}-\vec{b}|
$$

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138. Using vectors, find the area of the triangle with vertices $A(1,1,2), B(2,3,5)$ and $C(1,5,5)$

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139. Find the area of the parallelogram whose adjacent sides are given by the vectors $\vec{a}=\hat{i}-\hat{j}+3 \hat{k}$ and $\vec{b}=2 \hat{i}-7 \hat{j}+\hat{k}$

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140. find the area of a parallelogram whose diagonals are $\vec{a}=3 \hat{i}+\hat{j}-2 \hat{k}$ and $\vec{b}=\hat{i}-3 \hat{j}+4 \hat{k}$.
141. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be three vectors such that $\vec{a} \neq 0,|\vec{a}|=|\vec{c}|=1,|\vec{b}|=4$ and $|\vec{b} \times \vec{c}|=\sqrt{15}$. If $\vec{b}-2 \vec{c}=\lambda \vec{a}$ then find the value of $\lambda$.

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142. Find the moment about (1,-1,-1) of the force $3 \hat{i}+4 \hat{j}-5 \hat{k}$ acting at (1,0,-2)

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143. A rigid body is spinning about a fixed point ( $3,-2,-1$ ) with an angular velocity of $4 \mathrm{rad} / \mathrm{s}$, the axis of rotation being in the direction of $(1,2,2)$.

Find the velocity of the particle at point $(4,1,1)$.
144. If $\vec{a} \times \vec{b}=\vec{c} \times \vec{d}$ and $\vec{a} \times \vec{c}=\vec{b} \times \vec{d}$ show that $(\vec{a}-\vec{d})$ is parallel to $(\vec{b}-\vec{c})$.

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145. Show by a numerical example and geometrically also that $\vec{a} \times \vec{b}=\vec{a} \times \vec{c}$ does not imply $\vec{b}=\overrightarrow{.}$

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146. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are the position vectors of the vertices of a cycle quadrilateral

$$
A B C D, \quad \text { prove }
$$ that

$$
\frac{|\vec{a} \times \vec{b}+\vec{b} \times \vec{d}+\vec{d} \times \vec{a}|}{}+\frac{|\vec{b} \times \vec{c}+\vec{c} \times \vec{d}+\vec{d} \times \vec{b}|}{}=0
$$

$$
(\vec{b}-\vec{a}) \cdot(\vec{d}-\vec{a}) \quad(\vec{b}-\vec{c}) \cdot(\vec{d}-\vec{c})
$$

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147. The postion vectors of the vertices of a quadrilateral with A as origin are $B(\vec{b}), D(\vec{d})$ and $C(\vec{b}+m \vec{d})$. Prove that the area of the quadrilateral is $\frac{1}{2}(l+m)|\vec{b} \times \vec{d}|$.

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148. Let $\vec{a}$ and $\vec{b}$ be unit vectors such that $|\vec{a}+\vec{b}|=\sqrt{3}$. Then find the value of $(2 \vec{a}+5 \vec{b}) \cdot(3 \vec{a}+\vec{b}+\vec{a} \times \vec{b})$

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149. $\hat{u}$ and $\hat{v}$ are two non-collinear unit vectors such that $\left|\frac{\hat{u}+\hat{v}}{2}+\hat{u} \times \vec{v}\right|=1$. Prove that $|\hat{u} \times \hat{v}|=\left|\frac{\hat{u}-\hat{v}}{2}\right|$

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150. In a $\triangle A B C$ points $D, E, F$ are taken on the sides $B C, C A$ and $A B$ respectively such that $\frac{B D}{D C}=\frac{C E}{E A}=\frac{A F}{F B}=n \quad$ prove that $\triangle D E F=\frac{n^{2}-n+1}{(n+1)^{2}} \triangle A B C$

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151. Let $A, B, C$ be points with position vectors $2 \hat{i}-\hat{j}+\hat{k}, \hat{i}+2 \hat{j}+3 \hat{k}$ and $3 \hat{i}+\hat{j}+2 \hat{k}$ respectively. Find the shortest distance between point $B$ and plane OAC.

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152. Let $\vec{a}=x \hat{i}+12 \hat{j}-\hat{k}, \vec{b}=2 \hat{i}+2 x \hat{j}+\hat{k}$ and $\vec{c}=\hat{i}+\hat{k}$. If the ordered set $[\vec{b} \vec{c} \vec{a}]$ is left handed, then find the value of x .

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153. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar vectors, then find the value of $\frac{\vec{a} \cdot(\vec{b} \times \vec{c})}{\vec{b} \cdot(\vec{c} \times \vec{a})}+\frac{\vec{b} \cdot(\vec{c} \times \vec{a})}{\vec{c} \cdot(\vec{a} \times \vec{b})}+\frac{\vec{c} \cdot(\vec{b} \times \vec{a})}{\vec{a} \cdot(\vec{b} \times \vec{c})}$

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154. if the vectors $2 \hat{i}-3 \hat{j}, \hat{i}+\hat{j}-\hat{k}$ and $3 \hat{i}-\hat{k}$ from three concurrent edges of a parallelpiped, then find the volume of the parallelepied.

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155. The postion vectors of the four angular points of a tetrahedron are $A(\hat{j}+2 \hat{k}), B(3 \hat{i}+\hat{k}), C(4 \hat{i}+3 \hat{j}+6 \hat{k})$ and $D(2 \hat{i}+3 \hat{j}+2 \hat{k})$ find the volume of the tetrahedron $A B C D$.

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156. Let $\vec{a}, \vec{b}, \vec{c}$ be three unit vectors and $\vec{a} \cdot \vec{b}=\vec{a}$. $\vec{c}=0$. If the angle between $\vec{b}$ and $\vec{c}$ is $\frac{\pi}{3}$ then find the value of $|[\vec{a} \vec{b} \vec{c}]|$

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157. Prove that $[\vec{a}+\vec{b} \vec{b}+\vec{c} \vec{c}+\vec{a}]=2[\vec{a} \vec{b} \vec{c}]$

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158. Prove that $[\vec{l} \vec{m} \vec{n}][\vec{a} \vec{b} \vec{c}]=\left|\begin{array}{lll}\vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \cdot \vec{c} \\ \vec{m} \cdot \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \cdot \vec{c} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n} \cdot \vec{c}\end{array}\right|$

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159. If $\vec{a}=\hat{i}+\hat{j}+\hat{k}, \hat{b}=\hat{i}-\hat{j}+\hat{k}, \vec{c}=\hat{i}+2 \hat{j}-\hat{k}$, then find the value of
$\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c} \\ \vec{c} \cdot \vec{a} & \vec{c} \cdot \vec{b} & \vec{c} \cdot \vec{c}\end{array}\right|$

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160. Find the value of a so that the volume of the parallelopiped formed by vectors $\hat{i}+a \hat{j}+\hat{k}, \hat{j}+a \hat{k}$ and $a \hat{i}+\hat{k}$ becomes minimum.

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161. If $\vec{u}, \vec{v}$ and $\vec{w}$ are three non-coplanar vectors, then prove that $(\vec{u}+\vec{v}-\vec{w}) \cdot[[(\vec{u}-\vec{v}) \times(\vec{v}-\vec{w})]]=\vec{u} \cdot \vec{v} \times \vec{w}$

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162. If $\vec{a}$ and $\vec{b}$ are two vectors, such that $|\vec{a} \times \vec{b}|=2$, then find the value of $[\vec{a} \vec{b} \vec{a}] \times \vec{b}$.

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163. Find the altitude of a parallelopiped whose three coterminous edges are vectors $\vec{A}=\hat{i}+\hat{j}+\hat{k}, \vec{B}=2 \hat{i}+4 \hat{j}-\hat{k}$ and $\vec{C}=\hat{i}+\hat{j}+3 \hat{k}$ with $\vec{A}$ and $\vec{B}$ as the sides of the base of the parallelopiped .

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164. If $[\vec{a} \vec{b} \vec{c}]=2$, then find the value of $[(\vec{a}+2 \vec{b}-\vec{c})(\vec{a}-\vec{b})(\vec{a}-\vec{b}-\vec{c})]$

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165. If $\vec{a}, \vec{b}, \vec{c}$ are mutually perpendicular vector and $\vec{a}=\alpha(\vec{a} \times \vec{b})+\beta(\vec{b} \times \vec{c})+\gamma(\vec{c} \times \vec{a})$ and $[\vec{a} \vec{b} \vec{c}]=1$ then $\vec{\alpha}+\vec{\beta}+\vec{\gamma}=$
$|\vec{a}|^{2}$ (B) $-|\vec{a}|^{2}$ (C) 0 (D) none of these

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166. i. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non-coplanar vectors, prove that vectors $3 \vec{a}-7 \vec{b}-4 \vec{c}, 3 \vec{a}-2 \vec{b}+\vec{c}$ and $\vec{a}+\vec{b}+2 \vec{c}$ are coplanar.

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167. Prove that vectors

$$
\begin{aligned}
& \vec{u}=\left(a l+a_{1} l_{1}\right) \hat{i}+\left(a m+a_{1} m_{1}\right) \hat{j}+\left(a n+a_{1} n_{1}\right) \hat{k} \\
& \vec{v}=\left(b l+b_{1} l_{1}\right) \hat{i}+\left(b m+b_{1} m_{1}\right) \hat{j}+\left(b n+b_{1} n_{1}\right) \hat{k} \\
& \vec{w}=\left(w l+c_{1} l_{1}\right) \hat{i}+\left(c m+c_{1} m_{1}\right) \hat{j}+\left(c n+c_{1} n_{1}\right) \hat{k}
\end{aligned}
$$

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168. Let $G_{1}, G_{2}$ and $G_{3}$ be the centroids of the triangular faces $O B C, O C A a n d O A B$, respectively, of a tetrahedron $O A B C$ If $V_{1}$ denotes the volumes of the tetrahedron $O A B C a n d V_{2}$ that of the parallelepiped with $O G_{1}, O G_{2}$ and $O G_{3}$ as three concurrent edges, then prove that $4 V_{1}=9 V_{2}$

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169. Prove that $\hat{i} \times(\vec{a} \times \vec{i})+\hat{j} \times(\vec{a} \times \vec{j})+\hat{k} \times(\vec{a} \times \vec{k})=2 \vec{a}$

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170. If $\hat{i} \times[(\vec{a}-\hat{j}) \times \hat{i}]+\hat{j} \times[(\vec{a}-\hat{k}) \times \hat{j}]+\vec{k} \times[(\vec{a}-\vec{i}) \times \hat{k}]=0$, then find vector $\vec{a}$.

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171. Prove that: $[\vec{a} \times \vec{b} \vec{b} \times \vec{c} \vec{c} \times \vec{a}]=[\vec{a} \vec{b} \vec{c}]^{2}$

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172. For any four vectors prove that

$$
(\vec{b} \times \vec{c}) \cdot(\vec{a} \times \vec{d})+(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{d})+(\vec{a} \times \vec{b}) \cdot(\vec{c} \times \vec{d})=0
$$

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173. If $\vec{b}$ and $\vec{c}$ are two non-collinear such that $\vec{a}|\mid(\vec{b} \times \vec{c})$. Then prove that $(\vec{a} \times \vec{b}) \cdot(\vec{a} \times \vec{c})$ is equal to $|\vec{a}|^{2}(\vec{b} \cdot \vec{c})$ '

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174. Find the vector of length 3 unit which is perpendicular to $\hat{i}+\hat{j}+\hat{k}$ and lies in the plane of $\hat{i}+\hat{j}+\hat{k}$ and $2 \hat{i}-3 \hat{j}$
175. Let $\hat{a}, \hat{b}$, and $\hat{c}$ be the non-coplanar unit vectors. The angle between $\hat{b}$ and $\hat{c}$ is $\alpha$, between $\hat{c}$ and $\hat{a}$ is $\beta$ and between $\hat{a}$ and $\hat{b}$ is $\gamma$. If $A(\hat{a} \cos \alpha, 0), B(\hat{b} \cos \beta, 0)$ and $C(\hat{c} \cos \gamma, 0)$, then show that in triangle
$A B C, \frac{|\hat{a} \times(\hat{b} \times \hat{c})|}{\sin A}=\frac{|\hat{b} \times(\hat{c} \times \hat{a})|}{\sin B}=\frac{|\hat{c} \times(\hat{a} \times \hat{b})|}{\sin C}$

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176. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplannar vectors, then prove that $\frac{|\hat{a} \times(\hat{b} \times \hat{c})|}{\sin A}=\frac{|\hat{b} \times(\hat{c} \times \hat{a})|}{\sin B}=\frac{|\hat{c} \times(\hat{a} \times \hat{b})|}{\sin C}=\frac{\Pi|\hat{a} \times(\hat{b} \times \hat{c})|}{\left|\sum \hat{n}_{1} \sin \alpha \cos \beta \cos \gamma\right|}$

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177. If $\vec{b}$ is not perpendicular to $\vec{c}$. Then find the vector $\vec{r}$ satisfying the equation $\vec{r} \times \vec{b}=\vec{a} \times \vec{b}$ and $\vec{r} . \vec{c}=0$
178. If $\vec{a}$ and $\vec{b}$ are two given vectors and k is any scalar,then find the vector $\vec{r}$ satisfying $\vec{r} \times \vec{a}+k \vec{r}=\vec{b}$.

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179. If $\vec{r} \cdot \vec{a}=0, \vec{r} \cdot \vec{b}=1$ and $[\vec{r} \vec{a} \vec{b}]=1, \vec{a} \cdot \vec{b} \neq 0,(\vec{a} \cdot \vec{b})^{2}-|\vec{a}|^{2}|\vec{b}|^{2}=1$, then find $\vec{r}$ in terms of $\vec{a}$ and $\vec{b}$.

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180. If vector $\vec{x}$ satisfying $\vec{x} \times \vec{a}+(\vec{x} \cdot \vec{b}) \vec{c}=\vec{d}$ is given by $\vec{x}=\lambda \vec{a}+\vec{a} \times \frac{\vec{a} \times(\vec{d} \times \vec{c})}{(\vec{a} \cdot \vec{c})|\vec{a}|^{2}}$, then find out the value of $\lambda$

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181. $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar vectors and $\vec{r}$. Is any arbitrary vector. Prove that $[\vec{b} \vec{c} \vec{r}] \vec{a}+[\vec{c} \vec{a} \vec{r}] \vec{b}+[\vec{a} \vec{b} \vec{r}] \vec{c}=[\vec{a} \vec{b} \vec{c}] \vec{r}$.

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182. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non -coplanar unit vectors such that
$\vec{a} \times(\vec{b} \times \vec{c})=\frac{\vec{b} \times \vec{c}}{\sqrt{2}}, \vec{b}$ and $\vec{c}$ are non- parallel, then prove that the angle between $\vec{a}$ and $\vec{b} \mathrm{is} 3 \pi / 4$

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183. 

Prove
that

$$
\frac{[\vec{R} \vec{\beta} \times(\vec{\beta} \times \vec{\alpha})] \vec{\alpha}}{|\vec{\alpha} \times \vec{\beta}|^{2}}+\frac{[\vec{R} \vec{\alpha} \times(\vec{\alpha} \times \vec{\beta})] \vec{\beta}}{|\vec{\alpha} \times \vec{\beta}|^{2}}=\frac{[\vec{R} \vec{\alpha} \vec{\beta}](\vec{\alpha} \times \vec{\beta})}{|\vec{\alpha} \times \vec{\beta}|^{2}}
$$

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184. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar non-zero vectors, then prove that $(\vec{a} \cdot \vec{a}) \vec{b} \times \vec{c}+(\vec{a} \cdot \vec{b}) \vec{c} \times \vec{a}+(\vec{a} \cdot \vec{c}) \vec{a} \times \vec{b}=[\vec{b} \vec{c} \vec{a}] \vec{a}$

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185. Find a set of vectors reciprocal to the set $-\hat{i}+\hat{j}+\hat{k}, \hat{i}+\hat{k}, \hat{i}+\hat{j}+\hat{k}$

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186. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be a set of non- coplanar vectors and $\vec{a}^{\prime} \vec{b}^{\prime}$ and $\vec{c}^{\prime}$ be its reciprocal set.
prove that $\vec{a}=\frac{\overrightarrow{b^{\prime}} \times \vec{c}^{\prime}}{\left[\vec{a}^{\prime} \vec{b}^{\prime} \vec{c}^{\prime}\right]}, \vec{b}=\frac{\vec{c}^{\prime} \times \vec{a}^{\prime}}{\left[\vec{a}^{\prime} \vec{b}^{\prime} \vec{c}^{\prime}\right]}$ and $\vec{c}=\frac{\vec{a} \vec{a}^{\prime} \times \vec{b}^{\prime}}{\left[\vec{a}^{\prime} \vec{b}^{\prime} \vec{c}^{\prime}\right]}$

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187. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{a}^{\prime}, \vec{b}^{\prime}, \vec{c}^{\prime}$ are reciprocal system of vectors, then prove that $\vec{a}^{\prime} \times \vec{b}^{\prime}+\vec{b}^{\prime} \times \vec{c}^{\prime}+\vec{c}^{\prime} \times \vec{a}^{\prime}=\frac{\vec{a}+\vec{b}+\vec{c}}{[\vec{a} \vec{b} \vec{c}]}$

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188. If $\vec{a}, \vec{b}$ and $\vec{c}$ be three non-coplanar vectors and $\mathrm{a}^{\prime}, \mathrm{b}$ ' and $\mathrm{c}^{\prime}$ constitute the reciprocal system of vectors, then prove that
i. $\vec{r}=\left(\vec{r} \cdot \vec{a}^{\prime}\right) \vec{a}+\left(\vec{r} \cdot \vec{b}^{\prime}\right) \vec{b}+\left(\vec{r} \cdot \vec{c}^{\prime}\right) \vec{c}$
ii. $\vec{r}=(\vec{r} \cdot \vec{a}) \vec{a}^{\prime}+(\vec{r} \cdot \vec{b}) \vec{b}^{\prime}+(\vec{r} \cdot \vec{c}) \vec{c}^{\prime}$

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## Exercise 2.1

1. Find '|veca| and |vecb| if (veca+vecb).(veca-vecb) $=8$ and |veca|=8|vecb|.
2. Show that $|\vec{a}| \vec{b}+|\vec{b}| \vec{a}$ is perpendicular to $|\vec{a}| \vec{b}-|\vec{b}| \vec{a}$ for any two non zero vectors `veca and vecb.

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3. If the vectors $A, B, C$ of a triangle $A B C$ are $(1,2,3),(-1,0,0),(0,1,2)$, respectively then find $\angle A B C$

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4. If $|\vec{a}|=3,|\vec{b}|=4$ and the angle between $\vec{a}$ and $\vec{b}$ is $120^{\circ}$. Then find the value of $|4 \vec{a}+3 \vec{b}|$

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5. If vectors $\hat{i}-2 x \hat{j}-3 y \hat{k}$ and $\hat{i}+3 x \hat{j}+2 y \hat{k}$ are orthogonal to each other, then find the locus of th point ( $\mathrm{x}, \mathrm{y}$ ).

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6. Let $\vec{a} \vec{b}$ and $\vec{c}$ be pairwise mutually perpendicular vectors, such that $|\vec{a}|=1,|\vec{b}|=2,|\vec{c}|=2$, the find the length of $\vec{a}+\vec{b}+\vec{c}$.

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7. If $\vec{a}+\vec{b}+\vec{c}=0,|\vec{a}|=3,|\vec{b}|=5,|\vec{c}|=7$, then find the angle between $\vec{a}$ and $\vec{b}$.

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8. If the angle between unit vectors $\vec{a}$ and $\vec{b} i s 60^{\circ}$. Then find the value of $|\vec{a}-\vec{b}|$.

## ( Watch Video Solution

9. Let $\vec{u}=\hat{i}+\hat{j}, \vec{v}=\hat{i}-\hat{j}$ and $\vec{w}=\hat{i}+2 \hat{j}+3 \hat{k}$. If $\hat{n}$ is a unit vector such that $\vec{u} . \hat{n}=0$ and $\vec{v} . \hat{n}=0,|\vec{w} . \hat{n}|$ is equal to (A) 0 (B) 1 (C) 2 (D) 3

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10. $A, B, C, D$ are any four points, prove that $\vec{A} B \vec{C} D+\vec{B} C \vec{A} D+\vec{C} A \vec{B} D=0$.

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11. $P(1,0,-1), Q(2,0,-3), R(-1,2,0)$ andS( $,-2,-1)$, then find the projection length of $\vec{P}$ Qon $\vec{R} S$

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12. If the vectors $3 \vec{p}+\vec{q} ; 5 p-3 \vec{q}$ and $2 \vec{p}+\vec{q} ; 3 \vec{p}-2 \vec{q}$ are pairs of mutually perpendicular vectors, then find the angle between vectors $\vec{p}$ and $\vec{q}$

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13. Let $\vec{A}$ and $\vec{B}$ be two non-parallel unit vectors in a plane. If $(\alpha \vec{A}+\vec{B})$ bisects the internal angle between $\vec{A}$ and $\vec{B}$ then find the value of $\alpha$.

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14. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be unit vectors such that $\vec{a}+\vec{b}+\vec{c}=\vec{x}, \vec{a} \cdot \vec{x}=1, \vec{b} \cdot \vec{x}=\frac{3}{2},|\vec{x}|=2$ then find theh angle between $\vec{c}$ and $\vec{x}$.

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15. If $\vec{a}$ and $\vec{b}$ are unit vectors, then find the greatest value of $|\vec{a}+\vec{b}|+|\vec{a}-\vec{b}|$.

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16. Constant forces $P_{1}=\hat{i}-\hat{j}+\hat{k}, P_{2}=-\hat{i}+2 \hat{j}-\hat{i} k$ and $P_{3}=\hat{j}-\hat{k}$ act on a particle at a point A. Determine the work done when particle is displaced from position $A(4 \hat{i}-3 \hat{j}-2 \hat{k})$ to $B(6 \hat{i}+\hat{j}-3 \hat{k})$

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17. Find $|\vec{a}|$ and $|\vec{b}|$, if $(\vec{a}+\vec{b}) \cdot(\vec{a}-\vec{b})=8$ and $|\vec{a}|=8|\vec{b}|$

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18. If $A, B, C$ and $D$ are four distinct points in space that $A B$ is not perpendicular to $\overrightarrow{C D}$ and satisfies (AB). $(C D)=k\left(|\overrightarrow{A D}|^{2}+|\overrightarrow{B C}|^{2}-|\overrightarrow{B D}|^{2}\right)$, then find the value of $k$.

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## Exercise 2.2

1. If $\vec{a}=2 \hat{i}+3 \hat{j}-5 \hat{k}, \vec{b}=m \hat{i}+n \hat{j}+12 \hat{k}$ and $\vec{a} \times \vec{b}=\overrightarrow{0}$ then find (m,n)

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2. Find $\vec{a}$. $\vec{b}$ if $|\vec{a}|=2,|\vec{b}|=5$, and $|\vec{a} \times \vec{b}|=8$

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3. If $\vec{a} \times \vec{b}=\vec{b} \times \vec{c} \neq 0$ where $\vec{a}, \vec{b}$ and $\vec{c}$ are coplanar vectors, then for some scalar k prove that $\vec{a}+\vec{c}=k b \vec{b}$.

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4. If $\vec{a}=2 \vec{i}+3 \vec{j}-\vec{k}, \vec{b}=-\vec{i}+2 \vec{j}-4 \vec{k}$ and $\vec{c}=\vec{i}+\vec{j}+\vec{k}$, then find the value of $(\vec{a} \times \vec{b}) \cdot(\vec{a} \times \vec{c})$

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5. If the vectors $\vec{c}, \vec{a}=x \hat{i}+y \hat{j}+z \hat{k}$ and $\vec{b}=\hat{j}$ are such that $\vec{a}, \vec{c}$ and $\vec{b}$ form a right handed system then $\vec{c}$ is
A. (a) $z \hat{i}-x \hat{k}$
B. (b) $\overrightarrow{0}$
C. (c) $y \hat{j}$
D. (d) $-z \hat{i}+x \hat{k}$

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6. given that $\vec{a} . \vec{b}=\vec{a} . \vec{c}, \vec{a} \times \vec{b}=\vec{a} \times \vec{c}$ and $\vec{a}$ is not a zero vector. Show that $\vec{b}=\vec{c}$.

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7. Show that $(\vec{a}-\vec{b}) \times(\vec{a}+\vec{b})=2 \vec{a} \times \vec{b}$ and give a genometrical interpretation of it.

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8. If $\vec{x}$ and $\vec{y}$ are unit vectors and $|\vec{z}|=\frac{2}{\sqrt{7}}$ such that $\vec{z}+\vec{z} \times \vec{x}=\vec{y}$ then find the angle $\theta$ between $\vec{x}$ and $\vec{z}$
9. prove that $(\vec{a} . \hat{i})(\vec{a} \times \hat{i})+(\vec{a} . \hat{j})(\vec{a} \times \hat{j})+(\vec{a} . \hat{k})(\vec{a} \times \hat{k})=\overrightarrow{0}$

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10. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be three non-zero vectors such that $\vec{a}+\vec{b}+\vec{c}=\overrightarrow{0}$ and $\lambda \vec{b} \times \vec{a}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}=\overrightarrow{0}$ then find the value of $\lambda$.

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11. A particle has an angular speed of $3 \mathrm{rad} / \mathrm{s}$ and the axis of rotation passes through the points $(1,1,2)$ and $(1,2,-2)$ Find the velocity of the particle at point $P(3,6,4)$

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12. Let vea, $\vec{b}$ and $\vec{c}$ be unit vectors such that $\vec{a}$. $\vec{b}=0=\vec{a}$. $\vec{c}$. It the angle between $\vec{b}$ and $\vec{c} i s \frac{\pi}{6}$ then find $\vec{a}$.

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13. If $|\vec{a} \times \vec{b}|^{2}+(\vec{a} \cdot \vec{b})^{2}=144$ and $|\vec{a}|=4$, then $|\vec{b}|$ is equal to

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14. Given $|\vec{a}|=|\vec{b}|=1$ and $|\vec{a}+\vec{b}|=\sqrt{3} \operatorname{iff} \vec{c}$ is a vector such that $\vec{c}-\vec{a}-2 \vec{b}=3(\vec{a} \times \vec{b})$ then find the value of $\vec{c}$. Vecb.

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15. Find the moment of $\vec{F}$ about point $(2,-1,3)$, where force $\vec{F}=3 \hat{i}+2 \hat{j}-4 \hat{k}$ is acting on point ( $1,-1,2$ ).

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1. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are four non-coplanar unit vectors such that $\vec{d}$ makes equal angles with all the three vectors $\vec{a}, \vec{b}, \vec{c}$ then prove that $[\vec{d} \vec{a} \vec{b}]=[\vec{d} \vec{c} \vec{b}]=[\vec{d} \vec{c} \vec{a}]$

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2. prove that if $[\vec{l} \vec{m} \vec{n}]$ are three non-coplanar vectors, then $[\vec{l} \vec{m} \vec{n}](\vec{a} \times \vec{b})=\left|\begin{array}{lll}\vec{l} \cdot \vec{a} & \vec{l} \cdot \vec{b} & \vec{l} \\ \vec{m} \cdot \vec{a} & \vec{m} \cdot \vec{b} & \vec{m} \\ \vec{n} \cdot \vec{a} & \vec{n} \cdot \vec{b} & \vec{n}\end{array}\right|$

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3. if the volume of a parallelepiped whose adjacent ages are $\vec{a}=2 \hat{i}+3 \hat{j}+4 \hat{k}, \vec{b}=\hat{i}+\alpha \hat{j}+2 \hat{k}, \vec{c}=\vec{i}+2 \hat{j}+\alpha \hat{k} i s 15$ then find of $\alpha$ if $(\alpha>0)$
4. If $\vec{a}=\hat{i}+\hat{j}+\hat{k}$ and $\vec{b}=\hat{i}-2 \hat{j}+\hat{k}$ then find the vector $\vec{c}$ such that $\vec{a} \cdot \vec{c}=2$ and $\vec{a} \times \vec{c}=\vec{b}$.

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5. If $\vec{x}$. $\vec{a}=0 \vec{x} \cdot \vec{b}=0$ and $\vec{x} \cdot \vec{c}=0$ for some non zero vector $\vec{x}$ then show that $[\vec{a} \vec{b} \vec{c}]=0$

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6. If $\vec{a}=\hat{i}+\hat{j}+\hat{k}$ and $\vec{b}=\hat{i}-2 \hat{j}+\hat{k}$ then find the vector $\vec{c}$ such that $\vec{a} . \vec{c}=2$ and $\vec{a} \times \vec{c}=\vec{b}$.

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7. If $\vec{a}, \vec{b}, \vec{c}$ are three non-coplanar vectors such that $\vec{a} \times \vec{b}=\vec{c}, \vec{b} \times \vec{c}=\vec{a}, \vec{c} \times \vec{a}=\vec{b}$, then the value of $|\vec{a}|+|\vec{b}|+|\vec{c}|$ is

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$$
\frac{\vec{b} \times(\vec{a} \times \vec{b})}{\vec{b} \cdot \vec{b}}
$$

8. If $\vec{a}=\vec{P}+\vec{q}, \vec{P} \times \vec{b}=\overrightarrow{0}$ and $\vec{q} \cdot \vec{b}=0$ then prove that $=\vec{q}$

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9. Prove that $(\vec{a} .(\vec{b} \times \hat{i})) \hat{i}+(\vec{a} \cdot(\vec{b} \times \hat{j})) \hat{j}+(\vec{a} \cdot(\vec{b} \times \hat{k})) \hat{k}=\vec{a} \times \vec{b}$

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10. for any four vectors $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ prove that
$\vec{d} .(\vec{a} \times(\vec{b} \times(\vec{c} \times \vec{d})))=(\vec{b} . \vec{d})[\vec{a} \vec{c} \vec{d}]$
11. If $\vec{a}$ and $\vec{b}$ be two non-collinear unit vectors such that $\vec{a} \times(\vec{a} \times \vec{b})=-\frac{1}{2} \vec{b}$,then find the angle between $\vec{a}$ and $\vec{b}$.

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12. show that $(\vec{a} \times \vec{b}) \times \vec{c}=\vec{a} \times(\vec{b} \times \vec{c})$ if and only if $\vec{a}$ and $\vec{c}$ are collinear or $(\vec{a} \times \vec{c}) \times \vec{b}=\overrightarrow{0}$

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13. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be the non zero vectors such that $(\vec{a} \times \vec{b}) \times \vec{c}=\frac{1}{3}|\vec{b}||\vec{c}| \vec{a}$. if theta is the acute angle between the vectors
$\vec{b}$ and $\vec{a}$ then theta equals (A) $\frac{1}{3}$ (B) $\frac{\sqrt{2}}{3}$ (C) $\frac{2}{3}$ (D) $2 \frac{\sqrt{2}}{3}$

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14. If $\vec{p}, \vec{q}, \vec{r}$ denote vectors $\vec{b} \times \vec{c}, \vec{c} \times \vec{c} \times \vec{a}, \vec{a} \times \vec{b}$. Respectively, show that $\vec{a}$ is parallel to $\vec{q} \times \vec{r}, \vec{b}$ is parallel to $\vec{r} \times \vec{p}, \vec{c}$ is parallel to $\vec{p} \times \vec{q} . \$

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15. Let $\vec{a}, \vec{b}, \vec{c}$ be non -coplanar vectors and let equations $\vec{a}^{\prime}, \vec{b}^{\prime}, \vec{c}^{\prime}$ are reciprocal system of vector $\vec{a}, \vec{b}, \vec{c}$ then prove that $\vec{a} \times \vec{a}^{\prime}+\vec{b} \times \vec{b}^{\prime}+\vec{c} \times \vec{c}^{\prime}$ is a null vector.

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16. Given unit vectors $\hat{m} \hat{n}$ and $\hat{p}$ such that angle between $\hat{m}$ and $\hat{n} i s \alpha$ and angle between $\hat{p}$ and $\hat{m} X \hat{n}$ isoxif $[\mathrm{n} \mathrm{p} \mathrm{m}]=1 / 4$ find alpha

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17. $\vec{a}, \vec{b}, \vec{c}$ arwe threee unit vectors and every two are two inclined to each at an angle $\cos ^{-1}(3 / 5)$. If $\vec{a} \times \vec{b}=p \vec{a}+q \vec{b}+r \vec{c}$, where $p, q, r$ are scalars, then find the value of $q$.

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18. Let $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}, \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $\vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$ be three non-zero vectors such that $\vec{c}$ is a unit vector perpendicular to both vectors, $\vec{a}$ and $\vec{b}$. If the angle between $\vec{a}$ and $\vec{b}$ isл/6then $\left|\begin{array}{lll}a_{1} & a_{2} & a_{3} \\ b_{1} & b_{2} & b_{3} \\ c_{1} & c_{2} & c_{3}\end{array}\right|^{2}$ is equal to

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## Exercises

1. If $\left|\begin{array}{lll}(a-x)^{2} & (a-y)^{2} & (a-z)^{2} \\ (b-x)^{2} & (b-y)^{2} & (b-z)^{2} \\ (c-x)^{2} & (c-y)^{2} & (c-a)^{2}\end{array}\right|=0$ and vectors $\vec{A}, \vec{B}$ and $\vec{C}$, where
$\vec{A}=a^{2} \hat{i}=a \hat{j}+\hat{k}$ etc. are non-coplanar, then prove that vectors $\vec{X}, \vec{Y}$ and $\vec{Z}$ where $\vec{X}=x^{2} \hat{i}+x \hat{j}+\hat{k}$. etc.may be coplanar.

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2. $O A B C$ is a tetrahedron where $O$ is the origin and $A, B, C$ have position vectors $\vec{a}, \vec{b}, \vec{c}$ respectively prove that circumcentre of tetrahedron OABC
is $\frac{a^{2}(\vec{b} \times \vec{c})+b^{2}(\vec{c} \times \vec{a})+c^{2}(\vec{a} \times \vec{b})}{2[\vec{a} \vec{b} \vec{c}]}$

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3. Let $k$ be the length of any edge of a regular tetrahedron (a tetrahedron whose edges are equal in length is called a regular tetrahedron). Show
that the angel between any edge and a face not containing the edge is $\cos ^{-1}(1 / \sqrt{3})$.

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4. In $\triangle A B C$, a point $P$ is taken on $A B$ such that $A P / B P=1 / 3$ and point $Q$ is taken on $B C$ such that $C Q / B Q=3 / 1$. If $R$ is the point of intersection of the lines AQandCP, using vector method, find the area of $A B C$ if the area of $B R C$ is 1 unit

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5. Let $O$ be an interior points of $\triangle A B C$ such that $O A+O B+3 \vec{O} C=\overrightarrow{0}$, then the ratio of $\triangle A B C$ to area of $\triangle A O C$ is

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6. The length of two opposite edges of a tetrahedrom are $a$ and $b$, the shortest distance between these edges is d , and the angle between them is $\theta$. Prove using vectors that the volume of the tetrahedron is $\frac{a b d \sin \theta}{6}$

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7. Find the volume of a parallelopiped having three coterminus vectors of equal magnitude $|a|$ and equal inclination $\theta$ with each other.

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8. Let $\vec{p}$ and $\vec{q}$ any two othogonal vectors of equal magnitude 4 each. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be any three vectors of lengths $7 \sqrt{15}$ and $2 \sqrt{33}$, mutually perpendicular to each other. Then find the distance of the vector $(\vec{a} \cdot \vec{p}) \vec{p}+(\vec{a} \cdot \vec{q}) \vec{q}+(\vec{a} \cdot(\vec{p} \times \vec{q}))(\vec{p} \times \vec{q})+(\vec{b} \cdot \vec{p}) \vec{p}+(\vec{b} \cdot \vec{p}) \vec{q}+$ $(\vec{b} .(\vec{b} \cdot \vec{q}))(\vec{p} \times \vec{q})+(\vec{c} \cdot \vec{p}) \vec{p}+(\vec{c} \cdot \vec{q}) \vec{q}+(\vec{c} .(\vec{p} \times \vec{q}))(\vec{p} \times \vec{q})$ from the origin.
9. Given that vectors $\vec{A}, \vec{B}$ and $\vec{C}$ from a triangle such that $\vec{A}=\vec{B}+\vec{C}$. Find $a, b, c$ and $d$ such that the area of the triangle is $5 \sqrt{16}$ where.
$\vec{A}=a \hat{i}+b \vec{j}+c \hat{k}$
$\vec{B}=d \hat{i}+3 \hat{j}+4 \hat{k}$
$\vec{C}=3 \hat{i}+\hat{j}-2 \hat{k}$

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10. A line $I$ is passing through the point $\vec{b}$ and is parallel to vector $\vec{c}$. Determine the distance of point $A(\vec{a})$ from the line 1 in from $\left|\vec{b}-\vec{a}+\frac{(\vec{a}-\vec{b}) \vec{c}}{|\vec{c}|^{2}} \vec{c}\right|$ or $\frac{|(\vec{b}-\vec{a}) \times \vec{c}|}{|\vec{c}|}$
11. If $\vec{e}_{1}, \vec{e}_{2}, \vec{e}_{3}$ and $\vec{E}_{1}, \vec{E}_{2}, \vec{E}_{3}$ are two sets of vectors such that $\vec{e}_{i} \vec{E}_{j}=1$, if $i=j$ and $\vec{e}_{i} \vec{E}_{j}=0$ and if $i \neq j$, then prove that $\left[\begin{array}{lll}\vec{e}_{1} & \vec{e}_{2} & \vec{e}_{3}\end{array}\right]\left[\begin{array}{lll}\vec{E}_{1} & \vec{E}_{2} & \vec{E}_{3}\end{array}\right]=1$.

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12. In a quadrillateral $A B C D$, it is given that $A B \| C D$ and the diagonals $A C$ and $B D$ are perpendiclar to each other . Show that $A D . B C \geq A B . C D$.

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13. $O A B C$ is regular tetrahedron in which $D$ is the circumcentre of $O A B$ and E is the midpoint of edge $A C$ Prove that $D E$ is equal to half the edge of tetrahedron.

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14. If $\mathrm{A}(\vec{a})$. $B(\vec{b})$ and $C(\vec{c})$ are three non-collinear point and origin does not lie in the plane of the points $A, B$ and $C$, then for any point $P(\vec{P})$ in the plane of the $\triangle A B C$ such that vector $O P$ is $\perp$ to plane of triangIABC, show that $\overrightarrow{O P}=\frac{[\vec{a} \vec{b} \vec{c}](\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a})}{4 \Delta^{2}}$

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15. If $\vec{a}, \vec{b}, \vec{c}$ are three given non-coplanar vectors and any arbitrary vector
$\vec{r}$ in space, where $\Delta_{1}=\left|\begin{array}{lll}\vec{r} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{r} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{r} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{c} \cdot \vec{c}\end{array}\right|, \Delta_{2}=\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{r} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{r} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{r} \cdot \vec{c} & \vec{c} \cdot \vec{c}\end{array}\right|$
$\Delta_{3}=\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{r} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{r} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{r} \cdot \vec{c}\end{array}\right|, \Delta=\left|\begin{array}{lll}\vec{a} \cdot \vec{a} & \vec{b} \cdot \vec{a} & \vec{c} \cdot \vec{a} \\ \vec{a} \cdot \vec{b} & \vec{b} \cdot \vec{b} & \vec{c} \cdot \vec{b} \\ \vec{a} \cdot \vec{c} & \vec{b} \cdot \vec{c} & \vec{c} \cdot \vec{c}\end{array}\right|$,
then prove that $\vec{r}=\frac{\Delta_{1}}{\Delta} \vec{a}+\frac{\Delta_{2}}{\Delta} \vec{b}+\frac{\Delta_{3}}{\Delta} \vec{c}$
16. Two vectors in space are equal only if they have equal component in
A. a given direction
B. two given directions
C. three given direction
D. in any arbitrary direaction

## Answer: c

## - Watch Video Solution

2. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be the three vectors having magnitudes, 1,5 and 3 , respectively, such that the angle between $\vec{a}$ and $\vec{b}$ is $\theta$ and $\vec{a} \times(\vec{a} \times \vec{b})=\vec{c}$. Then $\tan \theta$ is equal to
A. 0
B. $\frac{2}{3}$
C. $\frac{3}{5}$
D. $\frac{3}{4}$

## Answer: d

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3. $\vec{a}, \vec{b}$ and $\vec{c}$ are three vectors of equal magnitude. The angle between each pair of vectors is $\pi / 3$ such that $|\vec{a}+\vec{b}+\vec{c}|=\sqrt{6}$ then $|\vec{a}|$ is equal to
A. 2
B. -1
C. 1
D. $\sqrt{6} / 3$

## Answer: c

4. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three mutually perpendicular vectors, then the vector which is equally inclined to these vectors is
A. $\vec{a}+\vec{b}+\vec{c}$
B. $\frac{\vec{a}}{|\vec{a}|}+\frac{\vec{b}}{|\vec{b}|}+\frac{\vec{c}}{|\vec{c}|}$
C. $\frac{\vec{a}}{|\vec{a}|^{2}}+\frac{\vec{b}}{|\vec{b}|^{2}}+\frac{\vec{c}}{|\vec{c}|^{2}}$
D. $|\vec{a}| \vec{a}-|\vec{b}| \vec{b}+|\vec{c}| \vec{c}$

## Answer: b

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5. Let $\vec{a}=\hat{i}+\hat{j}$ and $\vec{b}=2 \hat{i}-\hat{k}$. Then the point of intersection of the lines
$\vec{r} \times \vec{a}=\vec{b} \times \vec{a}$ and $\vec{r} \times \vec{b}=\vec{a} \times \vec{b}$ is
(A) $(3,-1,10$
(B) $(3,1,-1)$
$(-3,1,1)(\mathrm{D})(-3,-1,-1)$
A. $\hat{i}-\hat{j}+\hat{k}$
B. $3 \hat{i}-\hat{j}+\hat{k}$
C. $3 \hat{i}+\hat{j}-\hat{k}$
D. $\hat{i}-\hat{j}-\hat{k}$

## Answer: c

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6. If $\vec{a}$ and $\vec{b}$ are two vectors, such that $\vec{a} \cdot \vec{b}<0$ and $|\vec{a} \cdot \vec{b}|=|\vec{a} \times \vec{b}|$ then the angle between the vectors $\vec{a}$ and $\vec{b}$ is (a) $\pi$ (b) $\frac{7 \pi}{4}$ (c) $\frac{\pi}{4}$ (d) $\frac{3 \pi}{4}$
A. $\pi$
B. $7 \pi / 4$
C. $\pi / 4$
D. $3 \pi / 4$

## (D) Watch Video Solution

7. If $\hat{a}, \hat{b}$ and $\hat{c}$ are three unit vectors such that $\hat{a}+\hat{b}+\hat{c}$ is also a unit vector and $\theta_{1}, \theta_{2}$ and $\theta_{3}$ are angles between the vectors $\hat{a}, \hat{b}, \hat{b}, \hat{c}$ and $\hat{c}, \hat{a}$, respectively m then among $\theta_{1}, \theta_{2}$ and $\theta_{3}$
A. all are acute angles
B. all are right angles
C. at least one is obtuse angle
D. none of these

## Answer: c

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8. If $\vec{a}, \vec{b}, \vec{c}$ are unit vectors such that $\vec{a} . \vec{b}=0=\vec{a} . \vec{c}$ and the angle between $\vec{b}$ and $\vec{c} i s \pi / 3$ then the value of $|\vec{a} \times \vec{b}-\vec{a} \times \vec{c}|$ is
A. $1 / 2$
B. 1
C. 2
D. none of these

## Answer: b

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9. $\mathrm{P}(\vec{p})$ and $Q(\vec{q})$ are the position vectors of two fixed points and $R(\vec{r})$ is the postion vector of a variable point. If $R$ moves such that $(\vec{r}-\vec{p}) \times(\vec{r}-\vec{q})=\overrightarrow{0}$ then the locus of R is
A. a plane containing the origian O and parallel to two non-collinear vectors $\overrightarrow{O P}$ and $\overrightarrow{O Q}$
B. the surface of a sphere described on PQ as its diameter
C. a line passing through points $P$ and $Q$
D. a set of lines parallel to line PQ

Answer: c

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10. Two adjacent sides of a parallelogram ABCD are
$2 \hat{i}+4 \hat{j}-5 \hat{k}$ and $\hat{i}+2 \hat{j}+3 \hat{k}$. Then the value of $|\overrightarrow{A C} \times \overrightarrow{B D}|$ is
A. $20 \sqrt{5}$
B. $22 \sqrt{5}$
C. $24 \sqrt{5}$
D. $26 \sqrt{5}$

Answer: b
11. If $\hat{a}, \hat{b}$ and $\hat{c}$ are three unit vectors inclined to each other at an angle $\theta$.

The maximum value of $\theta$ is
A. $\frac{\pi}{3}$
B. $\frac{\pi}{2}$
C. $\frac{2 \pi}{3}$
D. $\frac{5 \pi}{5}$

## Answer: c

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12. Let the pair of vector $\vec{a}, \vec{b}$ and $\vec{c}, \vec{d}$ each determine a plane. Then the planes are parallel if
A. $(\vec{a} \times \vec{c}) \times(\vec{b} \times \vec{d})=\overrightarrow{0}$
B. $(\vec{a} \times \vec{c}) \cdot(\vec{b} \times \vec{d})=\overrightarrow{0}$
C. $(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d})=\overrightarrow{0}$
D. $(\vec{a} \times \vec{c}) \cdot(\vec{c} \times \vec{d})=\overrightarrow{0}$

Answer: c

## - Watch Video Solution

13. If $\vec{r}$. $\vec{a}=\vec{r} \cdot \vec{b}=\vec{r} \cdot \vec{c}=0$ where $\vec{a}, \vec{b}$ and $\vec{c}$ are non-coplanar, then
A. $\vec{r} \perp(\vec{c} \times \vec{a})$
B. $\vec{r} \perp(\vec{a} \times \vec{b})$
C. $\vec{r} \perp(\vec{b} \times \vec{c})$
D. $\vec{r}=\overrightarrow{0}$

## Answer: d

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14. If $\vec{a}$ satisfies $\vec{a} \times(\hat{i}+2 \hat{j}+\hat{k})=\hat{i}-\hat{k}$ then $\vec{a}$ is equal to
A. $\lambda \hat{i}+(2 \lambda-1) \hat{j}+\lambda \hat{k}, \lambda \in R$
B. $\lambda \hat{i}+(1-2 \lambda) \hat{j}+\lambda \hat{k}, \lambda \in R$
C. $\lambda \hat{i}+(2 \lambda+1) \hat{j}+\lambda \hat{k}, \lambda \in R$
D. $\lambda \hat{i}+(1+2 \lambda) \hat{j}+\lambda \hat{k}, \lambda \in R$

## Answer: c

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15. Vectors $3 \vec{a}-5 \vec{b}$ and $2 \vec{a}+\vec{b}$ are mutually perpendicular. If $\vec{a}+4 \vec{b}$ and $\vec{b}-\vec{a}$ are also mutually perpendicular, then the cosine of the angle between $\vec{a}$ and $\vec{b}$ is (a) $\frac{19}{5 \sqrt{43}}$ (b) $\frac{19}{3 \sqrt{43}}$ (c) $\frac{19}{\sqrt{45}}$ (d) $\frac{19}{6 \sqrt{43}}$
A. $\frac{19}{5 \sqrt{43}}$
B. $\frac{19}{3 \sqrt{43}}$
C. $\frac{19}{\sqrt{45}}$
D. $\frac{19}{6 \sqrt{43}}$

## Answer: a

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16. the unit vector orthogonal to vector $-\hat{i}+2 \hat{j}+2 \hat{k}$ and making equal angles with the $x$ - and $y$-axes is
A. $\pm \frac{1}{3}(2 \hat{i}+2 \hat{j}-\hat{k})$
B. $\frac{19}{5 \sqrt{43}}$
C. $\pm \frac{1}{3}(\hat{i}+\hat{j}-\hat{k})$
D. none of these

## Answer: a

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17. The value of $x$ for which the angle between $\vec{a}=2 x^{2} \hat{i}+4 x \hat{j}+\hat{k}$ and $\vec{b}=7 \hat{i}-2 \hat{j}+\hat{k}$ is obtuse and the angle between $\vec{b}$
and the $z$-axis is acute and less then $\pi / 6$
A. $a<x<1 / 2$
B. $1 / 2<x<15$
C. $x<1 / 2$ or $x<0$
D. none of these

## Answer: b

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18. If vectors $\vec{a}$ and $\vec{b}$ are two adjecent sides of a paralleogram, then the vector representing the altitude of the parallelogram which is perpendicular to $\vec{a}$ is
A. $\vec{b}+\frac{\vec{b} \times \vec{a}}{|\vec{a}|^{2}}$
B. $\frac{\vec{a} . \vec{b}}{}$
$|\vec{b}|^{2}$
C. $\vec{b}-\frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}$
$\vec{a} \times(\vec{b} \times \vec{a})$
$|\vec{b}|^{2}$

## Answer: a

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19. A parallelogram is constructed on
$3 \vec{a}+\vec{b}$ and $\vec{a}-4 \vec{b}$, where $|\vec{a}|=6$ and $|\vec{b}|=8$ and $\vec{a}$ and $\vec{b}$ are anti parallel then the length of the longer diagonal is (A) 40 (B) 64 (C) 32 (D) 48
A. 40
B. 64
C. 32
D. 48

## Answer: c

20. Let $\vec{a} \cdot \vec{b}=0$ where $\vec{a}$ and $\vec{b}$ are unit vectors and the vector $\vec{c}$ is inclined an anlge $\theta$ to both
$\vec{a}$ and $\vec{b}$. Ifc $=m \vec{a}+n \vec{b}+p(\vec{a} \times \vec{b}),(m, n, p \in R)$ then
A. $\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$
B. $\frac{\pi}{4} \leq \theta \leq \frac{3 \pi}{4}$
C. $0 \leq \theta \leq \frac{\pi}{4}$
D. $0 \leq \theta \leq \frac{3 \pi}{4}$

## Answer: a

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21. $\vec{a}$ and $\vec{c}$ are unit vectors and $|\vec{b}|=4$ the angle between $\vec{a}$ and $\vec{b}$ iscos $^{-1}(1 / 4)$ and $\vec{b}-2 \vec{c}=\lambda \vec{a}$ the value of $\lambda$ is
A. 3,-4
B. 1/4,3/4
C. $-3,4$
D. $-1 / 4, \frac{3}{4}$

## Answer: a

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22. Let the position vectors of the points PandQ be $4 \hat{i}+\hat{j}+\lambda \hat{k}$ and $2 \hat{i}-\hat{j}+\lambda \hat{k}$, respectively. Vector $\hat{i}-\hat{j}+6 \hat{k}$ is perpendicular to the plane containing the origin and the points PandQ. Then $\lambda$ equals $1 / 2$ b. 1/2 c. 1 d. none of these
A. $-1 / 2$
B. $1 / 2$
C. 1
D. none of these

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23. A vector of magnitude $\sqrt{2}$ coplanar with the vectors $\vec{a}=\hat{i}+\hat{j}+2 \hat{k}$ and $\vec{b}=\hat{i}+\hat{j}+\hat{k}$, and perpendicular to the vector $\vec{c}=\hat{i}+\hat{j}+\hat{k}$ is
A. $-\hat{j}+\hat{k}$
B. $\hat{i}$ and $\hat{k}$
C. $\hat{i}-\hat{k}$
D. hat- hat j

## Answer: a

24. Let $P$ be a point interior to the acute triangle $A B C$ If $P A+P B+P C$ is a null vector, then w.r.t traingel $A B C$, point $P$ is its $a$. centroid b . orthocentre c. incentre d. circumcentre
A. centroid
B. orthocentre
C. incentre
D. circumcentre

## Answer: a

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25. G is the centroid of triangle ABC and $A_{1}$ and $B_{1}$ are the midpoints of sides $A B$ and $A C$, respectively. If $\Delta_{1}$ is the area of quadrilateral $G A_{1} A B_{1}$ and $\Delta$ is the area of triangle $A B C$, then $\frac{\Delta}{\Delta_{1}}$ is equal to
A. $\frac{3}{2}$
B. 3
C. $\frac{1}{3}$
D. none of these

## Answer: b

## D Watch Video Solution

$$
\begin{aligned}
& \text { 26. Points } \vec{a}, \vec{b} \vec{c} \text { and } \vec{d} \text { are coplanar and } \\
& (\sin \alpha) \vec{a}+(2 \sin 2 \beta) \vec{b}+(3 \sin 3 \gamma) \vec{c}-\vec{d}=\overrightarrow{0} \quad \text {. Then the least value of } \\
& \sin ^{2} \alpha+\sin ^{2} 2 \beta+\sin ^{2} 3 \gamma \text { is }
\end{aligned}
$$

A. $1 / 14$
B. 14
C. 6
D. $1 / \sqrt{6}$

## Answer: a

27. If $\vec{a}$ and $\vec{b}$ are any two vectors of magnitudes 1and 2. respectively, and $(1-3 \vec{a} \cdot \vec{b})^{2}+|2 \vec{a}+\vec{b}+3(\vec{a} \times \vec{b})|^{2}=47$ then the angle between $\vec{a}$ and $\vec{b}$ is
A. $\pi / 3$
B. $\pi-\cos ^{-1}(1 / 4)$
C. $\frac{2 \pi}{3}$
D. $\cos ^{-1}(1 / 4)$

## Answer: c

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28. If $\vec{a}$ and $\vec{b}$ are any two vectors of magnitude 2 and 3 respectively such that $|2(\vec{a} \times \vec{b})|+|3(\vec{a} \cdot \vec{b})|=k$ then the maximum value of k is
A. $\sqrt{13}$
B. $2 \sqrt{13}$
C. $6 \sqrt{13}$
D. $10 \sqrt{13}$

## Answer: c

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29. $\vec{a}, \vec{b}$ and $\vec{c}$ are unit vecrtors such that $|\vec{a}+\vec{b}+3 \vec{c}|=4$ Angle between $\vec{a}$ and $\vec{b} i s \theta_{1}$, between $\vec{b}$ and $\vec{c} i s \theta_{2}$ and between $\vec{a}$ and $\vec{b}$ varies $[\pi / 6,2 \pi / 3]$. Then the maximum value of $\cos \theta_{1}+3 \cos \theta_{2}$ is
A. 3
B. 4
C. $2 \sqrt{2}$
D. 6

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30. If the vector product of a constant vector $\vec{O} A$ with a variable vector $\vec{O} B$ in a fixed plane $O A B$ be a constant vector, then the locus of $B$ is (a).a straight line perpendicular to $\vec{O} A(b)$. a circle with centre $O$ and radius equal to $|\vec{O} A|$ (c). a straight line parallel to $\vec{O} A$ (d). none of these
A. a straight line perpendicular to $O A$
B. a circle with centre $O$ and radius equal to $|\overrightarrow{O A}|$
C. a striaght line parallel to $O A$
D. none of these

## Answer: c

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31. Let $\vec{u}, \vec{v}, \vec{w}$ be such that $|\vec{u}|=1,|\vec{v}|=2,|\vec{w}| 3$. If the projection of $\vec{v}$ along $\vec{u}$ is equal to that of $\vec{w}$ along $\vec{v}, \vec{w}$ are perpendicular to each other then $|\vec{u}-\vec{v}+\vec{w}|$ equals (A) 2 (B) $\sqrt{7}$ (C) $\sqrt{14}$ (D) 14
A. 2
B. $\sqrt{7}$
C. $\sqrt{14}$
D. 14

## Answer: c

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32. If $\vec{a}, \vec{b}, \vec{c}$ are non-coplanar vectors and $\vec{u}$ and $\vec{v}$ are any two vectors.

Prove that $\vec{u} \times \vec{v}=\frac{1}{[\vec{a} \vec{b} \vec{c}]}\left|\begin{array}{lll}\vec{u} \cdot \vec{a} & \vec{v} \cdot \vec{a} & \vec{a} \\ \vec{u} \cdot \vec{b} & \vec{v} \cdot \vec{b} & \vec{b} \\ \vec{u} \cdot \vec{c} & \vec{v} \cdot \vec{c} & \vec{c}\end{array}\right|$
A. $-\cos ^{-1}\left(\frac{19}{5 \sqrt{43}}\right)$
B. $\cos ^{-1}\left(\frac{19}{5 \sqrt{43}}\right)$
C. $\pi \cos ^{-1}\left(\frac{19}{5 \sqrt{43}}\right)$
D. cannot of these

Answer: b

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33. if $\vec{\alpha}|\mid(\vec{\beta} \times \vec{\gamma})$, then $(\vec{\alpha} \times \vec{\gamma})$ equal to
A. $|\vec{\alpha}|^{2}(\vec{\beta} \cdot \vec{\gamma})$
B. $|\vec{\beta}|^{2}(\vec{\gamma} \cdot \vec{\alpha})$
C. $|\vec{\gamma}|^{2}(\vec{\alpha} \cdot \vec{\beta})$
D. $|\vec{\alpha}||\vec{\beta}||\vec{\gamma}|$

Answer: a
34. The position vectors of points $\mathrm{A}, \mathrm{B}$ and C are $\hat{i}+\hat{j}, \hat{i}+5 \hat{j}-\hat{k}$ and $2 \hat{i}+3 \hat{j}+5 \hat{k}$, respectively the greatest angle of triangle $A B C$ is
A. $120^{\circ}$
B. $90^{\circ}$
C. $\cos ^{-1}(3 / 4)$
D. none of these

Answer: b

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35. Given three vectors e $\vec{a}, \vec{b}$ and $\vec{c}$ two of which are non-collinear. Futrther if $(\vec{a}+\vec{b})$ is collinear with $\vec{c},(\vec{b}+\vec{c})$ is collinear with $\vec{a},|\vec{a}|=|\vec{b}|=|\vec{c}|=\sqrt{2}$ find the value of $\vec{a}$. Vecb $+\vec{b} \cdot \vec{c}+\vec{c} \cdot \vec{a}$
A. 3
B. -3
C. 0
D. cannot of these

## Answer: b

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36. If $\vec{a}$ and $\vec{b}$ are unit vectors such that $(\vec{a}+\vec{b}) \cdot(2 \vec{a}+3 \vec{b}) \times(3 \vec{a}-2 \vec{b})=\overrightarrow{0}$ then angle between $\vec{a}$ and $\vec{b}$ is
A. 0
B. $\pi / 2$
C. $\pi$
D. indeterminate

## (D) Watch Video Solution

37. If in a right-angled triangle $A B C$, the hypotenuse
$A B=p$, then $\vec{A} B A C+\vec{B} C \vec{B} A+\vec{C} A \vec{C} B$ is equal to $2 p^{2}$ b. $\frac{p^{2}}{2}$ c. $p^{2}$ d. none of these
A. $2 p^{2}$
B. $\frac{p^{2}}{2}$
C. $p^{2}$
D. none of these

## Answer: c

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38. Resolved part of vector $\vec{a}$ and along vector $\vec{b}$ is $\vec{a} 1$ and that prependicular to $\vec{b}$ is $\vec{a} 2$ then $\vec{a} 1 \times \vec{a} 2$ is equl to
$\underline{(\vec{a} \times \vec{b}) \cdot \vec{b}}$
$|\vec{b}|^{2}$
B. $\frac{(\vec{a} \cdot \vec{b}) \vec{a}}{}$
$|\vec{a}|^{2}$
$(\vec{a} \cdot \vec{b})(\vec{b} \times \vec{a})$
C.
$|\vec{b}|^{2}$
D. $\underline{(\vec{a} \cdot \vec{b})(\vec{b} \times \vec{a})}$
$|\vec{b} \times \vec{a}|$

## Answer: c

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39. $\vec{a}=2 \hat{i}-\hat{j}+\hat{k}, \vec{b}=\hat{j}+2 \hat{j}-\hat{k}, \vec{c}=\hat{i}+\hat{j}-2 \hat{k}$. A vector coplanar with
$\vec{b}$ and $\vec{c}$. Whose projection on $\vec{a}$ is magnitude $\sqrt{\frac{2}{3}}$ is
A. $2 \hat{i}+3 \hat{j}-3 \hat{k}$
B. $-2 \hat{i}-\hat{j}+5 \hat{k}$
C. $2 \hat{i}+3 \hat{j}+3 \hat{k}$
D. $2 \hat{i}+\hat{j}+5 \hat{k}$

## Answer: b

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40. If $P$ is any arbitary point on the circumcurcle of the equilateral
triangle of side length I units, then $|\overrightarrow{P A}|^{2}+|\overrightarrow{P B}|^{2}+|\overrightarrow{P C}|^{2}$ is always equal to
A. $2 l^{2}$
B. $2 \sqrt{3} I^{2}$
C. $l^{2}$
D. $3 l^{2}$

## Answer: a

41. If $\vec{r}$ and $\vec{s}$ are non-zero constant vectors and the scalar b is chosen such that $|\vec{r}+b \vec{s}|$ is minimum, then the value of $|b \vec{s}|^{2}+|\vec{r}+b \vec{s}|^{2}$ is equal to
A. $2|\vec{r}|^{2}$
B. $|\vec{r}|^{2 / 2}$
C. $3|\vec{r}|^{2}$
D. $|\vec{r}|^{2}$

## Answer: d

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42. $\vec{a}$ and $\vec{b}$ are two unit vectors that are mutually perpendicular. A unit vector that if equally inclined to $\vec{a}, \vec{b}$ and $\vec{a} \times \vec{b}$ is equal to
A. $\frac{1}{\sqrt{2}}(\vec{a}+\vec{b}+\vec{a} \times \vec{b})$
B. $\frac{1}{2}(\vec{a} \times \vec{b}+\vec{a}+\vec{b})$
C. $\frac{1}{\sqrt{3}}(\vec{a}+\vec{b}+\vec{a} \times \vec{b})$
D. $\frac{1}{3}(\vec{a}+\vec{b}+\vec{a} \times \vec{b})$

## Answer: a

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43. Given that $\vec{a}, \vec{b}, \vec{p}, \vec{q}$ are four vectors such that $\vec{a}+\vec{b}=\mu \vec{p}, \vec{b} \cdot \vec{q}=0$ and $|\vec{b}|^{2}=1 \quad$ where $\quad \mu \quad$ is a sclar. Then $|(\vec{a} \cdot \vec{q}) \vec{p}-(\vec{p} \cdot \vec{q}) \vec{a}|$ is equal to
(a) $2|\vec{p} \vec{q}|$ (b)(1/2) $|\vec{p} \cdot \vec{q}|$
(c) $|\vec{p} \times \vec{q}|$
(d) $|\vec{p} \cdot \vec{q}|$
A. $2|\vec{p} \vec{q}|$
B. $(1 / 2)|\vec{p} . \vec{q}|$
C. $|\vec{p} \times \vec{q}|$
D. $|\vec{p} \cdot \vec{q}|$

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44. The position vectors of the vertices $A, B$ and $C$ of a triangle are three unit vectors $\vec{a}, \vec{b}$ and $\vec{c}$ respectively. A vector $\vec{d}$ is such that $\vec{d} \cdot \hat{a}=\vec{d}$. Hatb $=\vec{d} . \hat{c}$ and $\vec{d}=\lambda(\hat{b}+\hat{c})$. Then triangle $A B C$ is
A. acute angled
B. obtuse angled
C. right angled
D. none of these

## Answer: a

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45. If $a$ is real constant $A$, BandC are variable angles and $\sqrt{a^{2}-4} \tan A+a \tan B+\sqrt{a^{2}+4} \tan c=6 a$, then the least vale of $\tan ^{2} A+\tan ^{2} b+\tan ^{2}$ Cis 6 b. 10 c. 12 d. 3
A. 6
B. 10
C. 12
D. 3

## Answer: d

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46. The vertex $A$ triangle $A B C$ is on the line $\vec{r}=\hat{i}+\hat{j}+\lambda \hat{k}$ and the vertices

BandC have respective position vectors $\hat{i} a n d \hat{j}$ Let Delta be the area of the triangle and Delta $[3 / 2, \sqrt{33} / 2]$. Then the range of values of $\lambda$ corresponding to $a$ is $[-8,4] \cup[4,8]$ b. $[-4,4]$ c. $[-2,2]$ d. $[-4,-2] \cup[2,4]$
A. $[-8,-4]$ cup $[4,8]^{`}$
B. $[-4,4]$
C. $[-2,2]$
D. $[-4,-2] \cup[2,4]$

## Answer: c

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47. A non-zero vecto $\vec{a}$ is such tha its projections along vectors $\frac{\hat{i}+\hat{j}}{\sqrt{2}}, \frac{-\hat{i}+\hat{j}}{\sqrt{2}}$ and $\hat{k}$ are equal , then unit vector along $\vec{a}$ us
A. $\frac{\sqrt{2} \hat{j}-\hat{k}}{\sqrt{3}}$
$\hat{j}-\sqrt{2} \hat{k}$
B. $\frac{\sqrt{3}}{\sqrt{3}}$
C. $\frac{\sqrt{2}}{\sqrt{3}} \hat{j}+\frac{\hat{k}}{\sqrt{3}}$
D. $\frac{\hat{j}-\hat{k}}{\sqrt{2}}$

## Answer: a

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48. Position vector $\hat{k}$ is rotated about the origin by angle $135^{\circ}$ in such a way that the plane made bt it bisects the angle between $\hat{i}$ and $\hat{j}$. Then its new position is
A. $\pm \frac{\hat{i}}{\sqrt{2}} \pm \frac{\hat{j}}{\sqrt{2}}$
B. $\pm \frac{\hat{i}}{2} \pm \frac{\hat{j}}{2}-\frac{\hat{k}}{\sqrt{2}}$
C. $\frac{\hat{i}}{\sqrt{2}}-\frac{\hat{k}}{\sqrt{2}}$
D. none of these

## Answer: d

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49. In a quadrilateral $A B C D, \vec{A} C$ is the bisector of $\vec{A} B a n d \vec{A} D$, angle between $\vec{A} B$ and $\vec{A} D$ is $2 \pi / 3,15|\vec{A} C|=3|\vec{A} B|=5|\vec{A} D|$ Then the angle between $\vec{B}$ Aand $\vec{C} D$ is $\frac{\cos ^{-1}(\sqrt{14})}{7 \sqrt{2}}$ b. $\frac{\cos ^{-1}(\sqrt{21})}{7 \sqrt{3}}$ c. $\frac{\cos ^{-1} 2}{\sqrt{7}}$ d. $\cos ^{-1}(2 \sqrt{7})$

14
$\sqrt{14}$
A. $\cos ^{-1} \frac{\sqrt{14}}{7 \sqrt{2}}$
B. $\cos ^{-1} \frac{\sqrt{21}}{7 \sqrt{3}}$
C. $\cos ^{-1} \frac{2}{\sqrt{7}}$
D. $\cos ^{-1} \frac{2 \sqrt{7}}{14}$

## Answer: c

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50. In AB, DE and GF are parallel to each other and AD, BG and EF ar parallel to each other. If $C D: C E=C G: C B=2: 1$ then the value of area
( $\triangle A E G$ ): area $(\triangle A B D)$ is equal to (a) $7 / 2$ (b)3 (c) 4 (d) $9 / 2$
A. $7 / 2$
B. 3
C. 4
D. 9/2

## Answer: b

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51. Vectors $\hat{a}$ in the plane of $\vec{b}=2 \hat{i}+\hat{j}$ and $\vec{c}=\hat{i}-\hat{j}+\hat{k}$ is such that it equally inclined to $\vec{b}$ and $\vec{d}$ where $\vec{d}=\hat{j}+2 \hat{k}$ the value of $\hat{a}$ is (a) $\frac{\hat{i}+\hat{j}+\hat{k}}{\sqrt{3}}$
(b) $\frac{\hat{i}-\hat{j}+\hat{k}}{\sqrt{3}}$ (c) $\frac{2 \hat{i}+\hat{j}}{\sqrt{5}}$ (d) $\frac{2 \hat{i}+\hat{j}}{\sqrt{5}}$
A. $\frac{\hat{i}+\hat{j}+\hat{k}}{\sqrt{3}}$
B. $\frac{\hat{i}-\hat{j}+\hat{k}}{\sqrt{3}}$
c. $\frac{2 \hat{i}+\hat{j}}{\sqrt{5}}$
D. $\frac{2 \hat{i}+\hat{j}}{\sqrt{5}}$

## Answer: b

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52. Let $A B C D$ be a tetrahedron such that the edges $A B, A C a n d A D$ are mutually perpendicular. Let the area of triangles $A B C, A C D a n d A D B$ be 3 , 4 and 5 sq. units, respectively. Then the area of triangle $B C D$ is a. $5 \sqrt{2}$ b. 5
c. $\frac{\sqrt{5}}{2}$ d. $\frac{5}{2}$
A. $5 \sqrt{2}$
B. 5
C. $\frac{\sqrt{5}}{2}$
D. $\frac{5}{2}$

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53. Let $f(t)=[t] \hat{i}+(t-[t]) \hat{j}+[t+1] \hat{k}$, where[.] denotes the greatest integer
function. Then the vectors $f\left(\frac{5}{4}\right) \operatorname{andf}(t), 0<t<1$ are(a) parallel to each other(b) perpendicular(c) inclined at $\cos ^{-1} 2\left(\sqrt{7\left(1-t^{2}\right)}\right)$ (d)inclined at $\cos ^{-1}\left(\frac{8+t}{\sqrt{1+t^{2}}}\right) ;$
A. parallel to each other
B. perpendicular to each other
C. inclined at $\xrightarrow{\cos ^{-1} 2}$

$$
\sqrt{7}\left(1-t^{2}\right)
$$

D. inclined at $\frac{\cos ^{-1}(8+t)}{9 \sqrt{1+t^{2}}}$

## Answer: d

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54. If $\vec{a}$ is parallel to $\vec{b} \times \vec{c}$, then $(\vec{a} \times \vec{b}) .(\vec{a} \times \vec{c})$ is equal to (a) $|\vec{a}|^{2}(\vec{b} . \vec{c})$
(b) $|\vec{b}|^{2}(\vec{a} \cdot \vec{c})$ (c) $|\vec{c}|^{2}(\vec{a} \cdot \vec{b})$ (d) none of these
A. $|\vec{a}|^{2}(\vec{b} . \vec{c})$
B. $|\vec{b}|^{2}(\vec{a} \cdot \vec{c})$
C. $|\vec{c}|^{2}(\vec{a} . \vec{b})$
D. none of these

## Answer: a

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55. The three vectors $\hat{i}+\hat{j}, \hat{j}+\hat{k}, \hat{k}+\hat{i}$ taken two at a time form three planes, The three unit vectors drawn perpendicular to these planes form a parallelopiped of volume: $\qquad$
A. $1 / 3$
B. 4
c. $(3 \sqrt{3}) / 4$
D. $4 \sqrt{3}$

## Answer: d

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56. If $\vec{d}=\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c}+\vec{c} \times \vec{a}$ is a non- zero vector and $\mid(\vec{d} \cdot \vec{c})(\vec{a} \times \vec{b})+(\vec{d} \cdot \vec{a})(\vec{b} \times \vec{c})+(\vec{d} \cdot \vec{b})(\vec{c} \times \vec{a})=0$ then
A. $|\vec{a}|=|\vec{b}|=|\vec{c}|$
B. $|\vec{a}|+|\vec{b}|+|\vec{c}|=|\vec{d}|$
C. $\vec{a}, \vec{b}$ and $\vec{c}$ are coplanar
D. none of these

## Answer: c

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57. If $|\vec{a}|=2$ and $|\vec{b}|=3$ and $\vec{a} \cdot \vec{b}=0$, then $(\vec{a} \times(\vec{a} \times(\vec{a} \times(\vec{a} \times \vec{b}))))$ is equal to the given diagonal is $\vec{c}=4 \hat{k}=8 \hat{k}$ then, the volume of a parallelpiped is
A. $48 \hat{b}$
B. $-48 \hat{b}$
C. $48 a ̂$
D. $-48 \hat{a}$

## Answer: a

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58. If two diagonals of one of its faces are $6 \hat{i}+6 \hat{k}$ and $4 \hat{j}+2 \hat{k}$ and of the edges not containing the given diagonals is $\vec{c}=4 \hat{j}-8 \hat{k}$, then the volume of a parallelpiped is
A. 60
B. 80
C. 100
D. 120

## Answer: d

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59. The volume of a tetrahedron fomed by the coterminus edges $\vec{a}, \vec{b}$ and $\vec{c} i s 3$. Then the volume of the parallelepiped formed by the coterminus edges $\vec{a}+\vec{b}, \vec{b}+\vec{c}$ and $\vec{c}+\vec{a}$ is
A. 6
B. 18
C. 36
D. 9

## Answer: c

60. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three mutually orthogonal unit vectors, then the triple product $\left[\begin{array}{lll}\vec{a}+\vec{b}+\vec{c} & \vec{a}+\vec{b} & \vec{b}+\vec{c}\end{array}\right]$ equals
A. 0
B. 1 or -1
C. 1
D. 3

## Answer: b

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61. vector $\vec{c}$ are perpendicular to vectors $\vec{a}=(2,-3,1)$ and $\vec{b}=(1,-2,3)$ and satifies the condition $\vec{c}$. $(\hat{i}+2 \hat{j}-7 \hat{k})=10$ then vector $\vec{c}$ is equal to $(a)(7,5,1)(b)(-7,-5,-1)(c)(1,1,-1)(d)$ none of these
A. $7,5,1$
B. $(-7,-5,-1)$
C. 1,1,-1
D. none of these

## Answer: a

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62. Given $\vec{a}=x \hat{i}+y \hat{j}+2 \hat{k}, \vec{b}=\hat{i}-\hat{j}+\hat{k}, \vec{c}=\hat{i}+2 \hat{j}, \vec{a} \perp \vec{b}, \vec{a} . \vec{c}=4$ then find the value of $\left[\begin{array}{lll}\vec{a} & \vec{b} & \vec{c}\end{array}\right]$.
A. $[\vec{a} \vec{b} \vec{c}]^{2}=|\vec{a}|$
B. $[\vec{a} \vec{b} \vec{c}]=|\vec{a}|$
C. $[\vec{a} \vec{b} \vec{c}]=0$
D. $[\vec{a} \vec{b} \vec{c}]=0$

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63. Let $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}, \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $\vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$ be three non-zero vectors such that $\vec{c}$ is a unit vector perpendicular to both
$\vec{a}$ and $\vec{b}$. If the angle between $\vec{a}$ and $\vec{b}$ ism/6 then the value of $\left|\begin{array}{lll}a_{1} & b_{1} & c_{1} \\ a_{2} & b_{2} & c_{2} \\ a_{3} & b_{3} & c_{3}\end{array}\right|$ is
A. 0
B. 1
C. $\frac{1}{4}\left(a_{1}^{2}+a_{2}^{2}+a_{3}^{2}\right)\left(b_{1}^{2}+b_{2}^{2}+b_{3}^{2}\right)$
D. $\frac{3}{4}\left(a_{1}^{2}+a_{2}^{2}+a_{3}^{2}\right)\left(b_{1}^{2}+b_{2}^{2}+b_{3}^{2}\right)$

## Answer: c

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64. Let $\vec{r}, \vec{a}, \vec{b}$ and $\vec{c}$ be four non-zero vectors such that $\vec{r} \cdot \vec{a}=0,|\vec{r} \times \vec{b}|=|\vec{r}||\vec{b}|,|\vec{r} \times \vec{c}|=|\vec{r}||\vec{c}|$ then $\left[\begin{array}{lll}\vec{a} & \vec{b} & \vec{c}\end{array}\right]=$
A. $|a||b||c|$
B. $-|a||b||c|$
C. 0
D. none of these

## Answer: c

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65. If $\vec{a}, \vec{b}$ and $\vec{c}$ are such that $[\vec{a} \vec{b} \vec{c}]=1, \vec{c}=\lambda(\vec{a} \times \vec{b})$, angle between $\vec{c}$ and $\vec{b}$ is $2 \pi / 3,|\vec{a}|=\sqrt{2},|\vec{b}|=\sqrt{3}$ and $|\vec{c}|=\frac{1}{\sqrt{3}}$ then the angle between $\vec{a}$ and $\vec{b}$ is
A. (a) $\frac{\pi}{6}$
B. (b) $\frac{\pi}{4}$
C. (c) $\frac{\pi}{3}$
D. (d) $\frac{\pi}{2}$

## Answer: b

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66. If $4 \vec{a}+5 \vec{b}+9 \vec{c}=0$ then $(\vec{a} \times \vec{b}) \times[(\vec{b} \times \vec{c}) \times(\vec{c} \times \vec{a})]$ is equal to
A. a vector perpendicular to the plane of $\vec{a}, \vec{b}$ and $\vec{c}$
B. a scalar quantity
C. $\overrightarrow{0}$
D. none of these

## Answer: c

67. Value of $[\vec{a} \times \vec{b}, \vec{a} \times \vec{c}, \vec{d}]$ is always equal to (a) $(\vec{a} \overrightarrow{.} \mathrm{d})[\vec{a} \vec{b} \mathrm{c}](\mathrm{b})($ $\vec{a} \overrightarrow{\cdot c})[\vec{a} \vec{b} d](c)(\vec{a} \vec{\cdot} b)[\vec{a} \vec{b} d]$ (d) none of these
A. $(\vec{a} . \vec{d})[\vec{a} \vec{b} \vec{c}]$
B. `(veca.vecc)[veca vecb vecd]
C. $(\vec{a} . \vec{b})[\vec{a} \vec{b} \vec{d}]$
D. none of these

## Answer: a

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68. Let $\hat{a}$ and $\hat{b}$ be mutually perpendicular unit vectors. Then for ant arbitrary $\vec{r}$.
A. $\vec{r}=(\vec{r} \cdot \hat{a}) \hat{a}+(\vec{r} \cdot \hat{b}) \hat{b}+(\vec{r} \cdot(\vec{a} \times \hat{b}))(\hat{a} \times \hat{b})$
B. $\vec{r}=(\vec{r} . \hat{a})-(\vec{r} . \hat{b}) \hat{b}-(\vec{r} .(\vec{a} \times \hat{b}))(\hat{a} \times \hat{b})$
C. $\vec{r}=(\vec{r} \cdot \hat{a}) \hat{a}-(\vec{r} \cdot \hat{b}) \hat{b}-(\vec{r} \cdot(\vec{a} \times \hat{b}))(\hat{a} \times \hat{b})$
D. none of these

## Answer: a

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69. Let $\vec{a}$ and $\vec{b}$ be unit vectors that are perpendicular to each other, then $[\vec{a}+(\vec{a} \times \vec{b})+(\vec{a} \times \vec{b})]$ is equal to
A. 1
B. 0
C. -1
D. none of these

## Answer: a

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70. $\vec{a}$ and $\vec{b}$ are two vectors such that $|\vec{a}|=1,|\vec{b}|=4$ and $\vec{a}$. Vecb $=2$. If vecc $=(2 \vec{a} \times \vec{b})-3 \vec{b}$ then find angle between $\vec{b}$ and $\vec{c}$.
A. $\frac{\pi}{3}$
B. $\frac{\pi}{6}$
C. $\frac{3 \pi}{4}$
D. $\frac{5 \pi}{6}$

## Answer: d

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71. If $\vec{b}$ and $\vec{c}$ are unit vectors, then for any arbitary vector $\vec{a},(((\vec{a} \times \vec{b})+(\vec{a} \times \vec{c})) \times(\vec{b} \times \vec{c})) \cdot(\vec{b}-\vec{c})$ is always equal to
72. If $\vec{a} \cdot \vec{b}=\beta$ and $\vec{a} \times \vec{b}=\vec{c}$, then $\vec{b}$ is
A. $\underline{(\beta \vec{a}-\vec{a} \times \vec{c})}$
$|\vec{a}|^{2}$
B. $\frac{(\beta \vec{a}+\vec{a} \times \vec{c})}{|\vec{a}|^{2}}$
C. $\frac{(\beta \vec{c}+\vec{a} \times \vec{c})}{|\vec{a}|^{2}}$
D. $\frac{(\beta \vec{c}+\vec{a} \times \vec{c})}{|\vec{a}|^{2}}$

## Answer: a

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73. If $a(\vec{\alpha} \times \vec{\beta}) \times(\vec{\beta} \times \vec{\gamma})+c(\vec{\gamma} \times \vec{\alpha})=0$ and at leasy one of $a, b$ and $c$ is non-zerp, then vector $\vec{\alpha}, \vec{\beta}$ and $\gamma$ are
A. parallel
B. coplanar
C. mutually perpendicular
D. none of these

## Answer: b

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74. If $(\vec{a} \times \vec{b}) \times(\vec{b} \times \vec{c})=\vec{b}$, where $\vec{a}, \vec{b}$ and $\vec{c}$ are non zero vectors then (A) $\vec{a}, \vec{b}$ and $\vec{c}$ canbecoplanar(B)veca,vecb and veccustbecoplanar( $C$ ) veca,vecb and vecc cannot be coplanar (D) none of these
A. $\vec{a}, \vec{b}$ and $\vec{v}$ can be coplanar
B. $\vec{a}, \vec{b}$ and $\vec{c}$ must be coplanar
C. $\vec{a}, \vec{b}$ and $\vec{c}$ cannot be coplanar
D. none of these

## Answer: c

75. If $\vec{r} \cdot \vec{a}=\vec{r} \cdot \vec{b}=\vec{r} \cdot \vec{c}=\frac{1}{2}$ for some non zero vector $\vec{r}$ and $\vec{a}, \vec{b}, \vec{c}$ are non coplanar, then the area of the triangle whose vertices are $A(\vec{a}), B(\vec{b})$ and $C(\vec{c})$ is
A. $|[\vec{a} \vec{b} \vec{c}]|$
B. $|\vec{r}|$
C. $|[\vec{a} \vec{b} \vec{c}] \vec{r}|$
D. none of these

## Answer: c

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76. A vector of magnitude 10 along the normal to the curve $3 x^{2}+8 x y+2 y^{2}-3=0$ at its point $P(1,0)$ can be (a) $\cdot 6 \hat{i}+8 \hat{j}$ (b). $-8 \hat{i}+3 \hat{j}$ (c).
$6 \hat{i}-8 \hat{j}(\mathrm{~d}) .8 \hat{i}+6 \hat{j}$
A. $6 \hat{i}+8 \hat{j}$
B. $-8 \hat{i}+3 \hat{j}$
C. $6 \hat{i}-8 \hat{j}$
D. $8 \hat{i}+6 \hat{j}$

## Answer: a

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77. If $\vec{a}$ and $\vec{b}$ are two unit vectors inclined at an angle $\frac{\pi}{3}$ then
$\{\vec{a} \times(\vec{b}+\vec{a} \times \vec{b})\} \cdot \vec{b}$ is equal to (a) $-\frac{3}{4}$ (b) $\frac{1}{4}$ (c) $\frac{3}{4}$ (d) $\frac{1}{2}$
A. $\frac{-3}{4}$
B. $\frac{1}{4}$
C. $\frac{3}{4}$
D. $\frac{1}{2}$

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78. If $\vec{a}$ and $\vec{b}$ are othogonal unit vectors, then for a vector $\vec{r}$ non coplanar with $\vec{a}$ and $\vec{b}$ vector $\vec{r} \times \vec{a}$ is equal to
A. $[\vec{r} \vec{a} \vec{b}] \vec{b}-(\vec{r} \cdot \vec{b})(\vec{b} \times \vec{a})$
B. $[\vec{r} \vec{a} \vec{b}](\vec{a}+\vec{b})$
C. $[\vec{r} \vec{a} \vec{b}] \vec{a}+(\vec{r} . \vec{a}) \vec{a} \times \vec{b}$
D. none of these

## Answer: a

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79. If $\vec{a}+\vec{b}, \vec{c}$ are any three non- coplanar vectors then the equation $[\vec{b} \times \vec{c} \vec{c} \times \vec{a} \vec{a} \times \vec{b}] x^{2}+[\vec{a}+\vec{b} \vec{b}+\vec{c} \vec{c}+\vec{a}] x+1+[\vec{b}-\vec{c} \vec{c}-\vec{c}-\vec{a} \vec{a}-\vec{b}]=0$ has roots
A. real and distinct
B. real
C. equal
D. imaginary

## Answer: c

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80. Sholve the simultasneous vector equations for $\vec{x}$ and $\vec{y}: \vec{x}+\vec{c} \times \vec{y}=\vec{a}$ and $\vec{y}+\vec{c} \times \vec{x}=\vec{b}, \vec{c} \neq 0$
A. $\vec{x}=\frac{\vec{b} \times \vec{c}+\vec{a}+(\vec{c} \cdot \vec{a}) \vec{c}}{1+\vec{c} \cdot \vec{c}}$
B. $\vec{x}=\underline{\vec{c} \times \vec{b}+\vec{b}+(\vec{c} \cdot \vec{a}) \vec{c}}$
B. $\vec{x}=$
C. $\vec{y}=\frac{\vec{a} \times \vec{c}+\vec{b}+(\vec{c} \cdot \vec{b}) \vec{c}}{1+\vec{c} \cdot \vec{c}}$
D. none of these

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81. The condition for equations $\vec{r} \times \vec{a}=\vec{b}$ and $\vec{r} \times \vec{c}=\vec{d}$ to be consistent is
A. $\vec{b} \cdot \vec{c}=\vec{a} \cdot \vec{d}$
B. $\vec{a} \cdot \vec{b}=\vec{c} \cdot \vec{d}$
C. $\vec{b} \cdot \vec{c}+\vec{a} \cdot \vec{d}=0$
D. $\vec{a} \cdot \vec{b}+\vec{c} \cdot \vec{d}=0$

## Answer: c

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82. If $\vec{a}=2 \hat{i}+3 \hat{j}+\hat{k}, \vec{b}=\hat{i}-2 \hat{j}+\hat{k}$ and $\vec{c}=-3 \hat{i}+\hat{j}+2 \hat{k}$, then $[\vec{a} \vec{b} \vec{c}]=$
83.
$\vec{a}=2 \hat{i}+\hat{j}+\hat{k}, \vec{b}=\hat{i}+2 \hat{j}+2 \hat{k}, \vec{c}=\hat{i}+\hat{j}+2 \hat{k}$ and $(1+\alpha) \hat{i}+\beta(1+\alpha) \hat{j}+\gamma(1+\alpha)($
A. $-2,-4,-\frac{2}{3}$
B. $2,-4, \frac{2}{3}$
C. $-2,4, \frac{2}{3}$
D. $2,4,-\frac{2}{3}$

## Answer: a

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84. Let $(\vec{a}(x)=(\sin x) \hat{i}+(\cos x) \hat{j}$ and $\vec{b}(x)=(\cos 2 x) \hat{i}+(\sin 2 x) \hat{j}$ be two variable vectors $(x \in R)$. Then $\vec{a}(x)$ and $\vec{b}(x)$ are
A. collinear for unique value of $x$
B. perpendicular for infinte values of x .
C. zero vectors for unique value of $x$
D. none of these

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85. For any
vectors
$\vec{a}$ and $\vec{b},(\vec{a} \times \hat{i})+(\vec{b} \times \hat{i})+(\vec{a} \times \hat{j}) \cdot(\vec{b} \times \hat{j})+(\vec{a} \times \hat{k}) \cdot(\vec{b} \times \hat{k})$ is always equal to
A. $\vec{a} \cdot \vec{b}$
B. $2 \vec{a}$. Vecb
C. zero
D. none of these

Answer: b
86. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non coplanar vectors and $\vec{r}$ is any vector in space, then $(\overrightarrow{\times} \vec{b}),(\vec{r} \times \vec{c})+(\vec{b} \times \vec{c}) \times(\vec{r} \times \vec{a})+(\vec{c} \times \vec{a}) \times(\vec{r} \times \vec{b})=$
(A) $[\vec{a} \vec{b} \vec{c}]$
(B) $2[\vec{a} \vec{b} \vec{c}] \vec{r}$
(C) $3[\vec{a} \vec{b} \vec{c}] \vec{r}$
(D) $4[\vec{a} \vec{b} \vec{c}] \vec{r}$
A. $[\vec{a} \vec{b} \vec{c}] \vec{r}$
B. $2[\vec{a} \vec{b} \vec{c}] \vec{r}$
C. $3[\vec{a} \vec{b} \vec{c}] \vec{r}$
D. none of these

## Answer: b

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87. If $\vec{P}=\frac{\vec{b} \times \vec{c}}{[\vec{a} \vec{b} \vec{c}]} \cdot \vec{q}=\frac{\vec{c} \times \vec{a}}{[\vec{a} \vec{b} \vec{c}]}$ and $\vec{r}=\frac{\vec{a} \times \vec{b}}{[\vec{a} \vec{b} \vec{c}]}$, where $\vec{a}, \vec{b}$ and $\vec{c}$ are three non- coplanar vectors then the value of the expression $(\vec{a}+\vec{b}+\vec{c}) \cdot(\vec{q}+\vec{q}+\vec{r})$ is
A. 3
B. 2
C. 1
D. 0

## Answer: a

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88. $A(\vec{a}), B(\vec{b})$ and $C(\vec{c})$ are the vertices of triangle $A B C$ and $R(\vec{r})$ is any point in the plane of triangle ABC, then $\vec{r},(\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a})$ is always equal to
A. zero
B. $[\vec{a} \vec{b} \vec{c}]$
C. $-[\vec{a} \vec{b} \vec{c}]$
D. none of these

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89. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non- coplanar vectors and $\vec{a} \times \vec{c}$ is perpendicular to $\vec{a} \times(\vec{b} \times \vec{c})$, then the value of $[\vec{a} \times(\vec{b} \times \vec{c})] \times \vec{c}$ is equal to
A. $[\vec{a} \vec{b} \vec{c}] \vec{c}$
B. $[\vec{a} \vec{b} \vec{c}] \vec{b}$
C. $\overrightarrow{0}$
D. $[\vec{a} \vec{b} \vec{c}] \vec{a}$

## Answer: c

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90. If $V$ be the volume of a tetrahedron and $V^{\prime}$ be the volume of another tetrahedran formed by the centroids of faces of the previous tetrahedron
and $V=K V^{\prime}$, then $K$ is equal to a. 9 b .12 c .27 d .81
A. 9
B. 12
C. 27
D. 81

## Answer: c

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91. $[(\vec{a} \times \vec{b}) \times(\vec{b} \times \vec{c})(\vec{b} \times \vec{c}) \times(\vec{c} \times \vec{a})(\vec{c} \times \vec{a}) \times(\vec{a} \times \vec{b})]$ is equal to ( where $\vec{a}, \vec{b}$ and $\vec{c}$ are non - zero non- colanar vectors). (a) $[\vec{a} \vec{b} \vec{c}]^{2}$
(b) $[\vec{a} \vec{b} \vec{c}]^{3}(c)[\vec{a} \vec{b} \vec{c}]^{4}(d)[\vec{a} \vec{b} \vec{c}]$
A. $[\vec{a} \vec{b} \vec{c}]^{2}$
B. $[\vec{a} \vec{b} \vec{c}]^{3}$
C. $[\vec{a} \vec{b} \vec{c}]^{4}$
D. $[\vec{a} \vec{b} \vec{c}]$

Answer: c

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92. 

$\vec{r}=x_{1}(\vec{a} \times \vec{b})+x_{2}(\vec{b} \times \vec{a})+x_{3}(\vec{c} \times \vec{d})$ and $4[\vec{a} \vec{b} \vec{c}]=1$ then $x_{1}+x_{2}+x_{3}$ is equal to
A. $\frac{1}{2} \vec{r} .(\vec{a}+\vec{b}+\vec{c})$
B. $\frac{1}{4} \vec{r} .(\vec{a}+\vec{b}+\vec{c})$
C. $2 \vec{r} \cdot(\vec{a}+\vec{b}+\vec{c})$
D. $4 \vec{r} \cdot(\vec{a}+\vec{b}+\vec{c})$

## Answer: d

93. If $\vec{a} \perp \vec{b}$ then vector $\vec{v}$ in terms of $\vec{a}$ and $\vec{b}$ satisfying the equations
$\vec{v} \cdot$ Veca $=0 n a d \vec{v}$. Vecb $=1$ and $[\vec{a} \vec{a} \vec{b}]=1$ is
A. $\frac{\vec{b}}{|\vec{b}|^{2}}+\frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|^{2}}$
B. $\frac{\vec{b}}{|\vec{b}|}+\frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|^{2}}$
C. $\frac{\vec{b}}{|\vec{b}|}+\frac{\vec{a} \times \vec{b}}{|\vec{a} \times \vec{b}|}$
D. none of these

## Answer: a

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94. If $\vec{a}^{\prime}=\hat{i}+\hat{j}, \vec{b}^{\prime}=\hat{i}-\hat{j}+2 \hat{k}$ and $\vec{c}^{\prime}=2 \hat{i}-\hat{j}-\hat{k}$ then the altitude of the parallelepiped formed by the vectors, $\vec{a}, \vec{b}$ and $\vec{c}$ having base formed by $\vec{b}$ and $\vec{c}$ is (where $\vec{a}^{\prime}$ is recipocal vector $\vec{a}$ ) (a) 1 (b) $3 \sqrt{2} / 2 \quad(c) 1 / \sqrt{6}$ (d) $1 / \sqrt{2}$
A. 1
B. $3 \sqrt{2} / 2$
C. $1 / \sqrt{6}$
D. $1 / \sqrt{2}$

## Answer: d

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95. If $\vec{a}=\hat{i}+\hat{j}, \vec{b}=\hat{j}+\hat{k}, \vec{c}=\hat{k}+\hat{i}$ then in the reciprocal system of vectors
$\vec{a}, \vec{b}, \vec{c}$ reciprocal $\vec{a}$ of vector $\vec{a}$ is
A. $\frac{\hat{i}+\hat{j}+\hat{k}}{2}$
B. $\frac{\hat{i}-\hat{j}+\hat{k}}{2}$
C. $\frac{-\hat{i}-\hat{j}+\hat{k}}{2}$
D. $\frac{\hat{i}+\hat{j}-\hat{k}}{2}$

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96. If unit vectors $\vec{a}$ and $\vec{b}$ are inclined at an angle $2 \theta$ such that $|\vec{a}-\vec{b}|<1$ and $0 \leq \theta \leq \pi$, then $\theta$ lies in the interval
A. $[0, \pi / 6)$
B. $(5 \pi / 6, \pi]$
C. $[\pi / 6, \pi / 2]$
D. $(\pi / 2,5 \pi / 6]$

## Answer: a,b

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97. 

$\vec{b}$ and $\vec{c}$
are
non- collinear
if
$\vec{a} \times(\vec{b} \times \vec{c})+(\vec{a} \cdot \vec{b}) \vec{b}=(4-2 x-\sin y) \vec{b}+\left(x^{2}-1\right) \vec{c} \operatorname{nad}(\vec{a} \cdot \vec{c}) \vec{a}=\vec{a} \quad$ then
a. $\mathrm{x}=1 \mathrm{~b} . \mathrm{x}=-1 \mathrm{c} \cdot \mathrm{y}=(4 n+1) \frac{\pi}{2}, n \in I$ d. $y(2 n+1) \frac{\pi}{2}, n \in I$
A. $x=1$
B. $x=-1$
C. $y=(4 n+1) \frac{\pi}{2}, n \in I$
D. $y(2 n+1) \frac{\pi}{2}, n \in I$

## Answer: a,c

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98. Unit vectors $\vec{a}$ and $\vec{b}$ ar perpendicular, and unit vector $\vec{c}$ is inclined at an angle $\theta$ to both $\vec{a}$ and $\vec{b}$. If $\alpha \vec{a}+\beta \vec{b}+\gamma(\vec{a} \times \vec{b})$ then.
A. $\alpha=\beta$
B. $\gamma^{2}=1-2 \alpha^{2}$
C. $y^{2}=-\cos 2 \theta$
D. $\beta^{2}=\frac{1+\cos 2 \theta}{2}$

## D Watch Video Solution

99. If vectors $\vec{a}$ and $\vec{b}$ are two adjecent sides of a paralleogram, then the vector representing the altitude of the parallelogram which is perpendicular to $\vec{a}$ is
A. $\frac{(\vec{a} \cdot \vec{b})}{\vec{a}-\vec{b}}$
$|\vec{a}|^{2}$
B. $\frac{1}{|\vec{a}|^{2}}\left\{|\vec{a}|^{2} \vec{b}-(\vec{a} \cdot \vec{b}) \vec{a}\right\}$
$\vec{a} \times(\vec{a} \times \vec{b})$
C.
$|\vec{a}|^{2}$
$\vec{a} \times(\vec{b} \times \vec{a})$
D.

$$
|\vec{b}|^{2}
$$

## Answer: a,b,c

100. If $\vec{a} \times(\vec{b} \times \vec{c})$ is perpendicular to $(\vec{a} \times \vec{b}) \times \vec{c}$, we may have
A. $(\vec{a} \cdot \vec{b})|\vec{b}|^{2}=(\vec{a} \cdot \vec{b})(\vec{b} \cdot \vec{c})$
B. $\vec{a} \cdot \vec{b}=0$
C. $\vec{a} \cdot \vec{c}=0$
D. $\vec{b} \cdot \vec{c}=0$

## Answer: a,c

## - Watch Video Solution

101. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be vectors forming right- hand triad . Let $\vec{P}=\frac{\vec{b} \times \vec{c}}{[\vec{a} \vec{b} \vec{c}]}, \vec{q} \frac{\vec{c} \times \vec{a}}{[\vec{a} \vec{b} \vec{c}]}$ and $\vec{r}=\frac{\vec{a} \times \vec{b}}{[\vec{a} \vec{b} \vec{c}]} I f x \cup R^{+}$then
A. $x[\vec{a} \vec{b} \vec{c}]+\frac{[\vec{p} \vec{q} \vec{r}]}{x}$ has least value 2
B. $x^{2}[\vec{a} \vec{b} \vec{c}]^{2}+\frac{[\vec{p} \vec{q} \vec{r}]}{x^{2}}$ has least value $\left(3 / 2^{2 / 3}\right)$
C. $[\vec{p} \vec{q} \vec{r}]>0$
D. none of these

## Answer: a,c

## - Watch Video Solution

102. $a_{1}, a_{2}, a_{3} \in R-\{0\}$ and $a_{1}+a_{2} \cos 2 x+a_{3} \sin ^{2} x=0$ " for all " x in R then (a) vectors $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ and $\vec{b}=4 \hat{i}+2 \hat{j}+\hat{k}$ are perpendicular to each other (b)vectors $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ and $\vec{b}=\hat{i}+\hat{j}+2 \hat{k}$ are parallel to each each other (c)if vector $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ is of length $\sqrt{6}$ units, then on of the ordered trippplet $\left(a_{1}, a_{2}, a_{3}\right)=(1,-1,-2) \quad$ (d) if $2 a_{1}+3 a_{2}+6 a_{3}=26$, then $\left|\vec{a} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}\right| i s 2 \sqrt{6}$
A. vectors $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ and $\vec{b}=4 \hat{i}+2 \hat{j}+\hat{k}$ are perpendicular to each other
B. vectors $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ and $\vec{b}=\hat{i}+\hat{j}+2 \hat{k}$ are parallel to each
C. if vector $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}$ is of length $\sqrt{6}$ units, then on of the ordered trippplet $\left(a_{1}, a_{2}, a_{3}\right)=(1,-1,-2)$
D. if $2 a_{1}+3 a_{2}+6 a_{3}+6 a_{3}=26$, then $\left|\vec{a} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}\right| i s 2 \sqrt{6}$

## Answer: a,b,c,d

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103. If $\vec{a}$ and $\vec{b}$ are two vectors and angle between them is $\theta$, then
A. $|\vec{a} \times \vec{b}|^{2}+(\vec{a} \cdot \vec{b})^{2}=|\vec{a}|^{2}|\vec{b}|^{2}$
B. $|\vec{a} \times \vec{b}|^{2}+(\vec{a} \cdot \vec{b})^{2}$, if $\theta=\pi / 4$
C. $\vec{a} \times \vec{b}=(\vec{a} . \operatorname{Vecb}) \hat{n}($ where $\hat{n}$ is a normal unit vector) if $\theta f=\pi / 4$
D. $(\vec{a} \times \vec{b}) \cdot(\vec{a}+\vec{b})=0$

## Answer: a,b,c,d

## D Watch Video Solution

104. Let $\vec{a}$ and $\vec{b}$ be two non- zero perpendicular vectors. A vector $\vec{r}$ satisfying the equation $\vec{r} \times \vec{b}=\vec{a}$ can be
A. $\vec{b}-\frac{\vec{a} \times \vec{b}}{|\vec{b}|^{2}}$
B. $2 \vec{b}-\frac{\vec{a} \times \vec{b}}{}$

$$
|\vec{b}|^{2}
$$

C. $|\vec{a}| \vec{b}-\frac{\vec{a} \times \vec{b}}{|\vec{b}|^{2}}$
D. $|\vec{b}| \vec{b}-\frac{\vec{a} \times \vec{b}}{|\vec{b}|^{2}}$

## Answer: a,b,cd,

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105. If vector $\vec{b}=(\tan \alpha,-1,2 \sqrt{\sin \alpha / 2})$ and $\vec{c}=\left(\tan \alpha, \tan \alpha,-\frac{3}{\sqrt{\sin \alpha / 2}}\right)$ are orthogonal and vector $\vec{a}=(1,3, \sin 2 \alpha)$ makes an obtuse angle with the $z-$ axis, then the value of $\alpha$ is
A. $\alpha=(4 n+1) \pi+\tan ^{-1} 2$
B. $\alpha=(4 n+1) \pi-\tan ^{-1} 2$
C. $\alpha=(4 n+2) \pi+\tan ^{-1} 2$
D. $\alpha=(4 n+2) \pi-\tan ^{-1} 2$

## Answer: bsd

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106. Let $\vec{r}$ be a unit vector satisfying

$$
\begin{equation*}
\vec{r} \times \vec{a}=\vec{b}, \text { where }|\vec{a}|=\sqrt{3} \text { and }|\vec{b}|=\sqrt{2}, \text { then }(a) \vec{r}=\frac{2}{3}(\vec{a}+\vec{a} \times \vec{b}) \tag{b}
\end{equation*}
$$

$\vec{r}=\frac{1}{3}(\vec{a}+\vec{a} \times \vec{b})(\mathrm{c}) \vec{r}=\frac{2}{3}(\vec{a}-\vec{a} \times \vec{b})(\mathrm{d}) \vec{r}=\frac{1}{3}(-\vec{a}+\vec{a} \times \vec{b})$
A. $\vec{r}=\frac{2}{3}(\vec{a}+\vec{a} \times \vec{b})$
B. $\vec{r}=\frac{1}{3}(\vec{a}+\vec{a} \times \vec{b})$
C. $\vec{r}=\frac{2}{3}(\vec{a}-\vec{a} \times \vec{b})$
D. $\vec{r}=\frac{1}{3}(-\vec{a}+\vec{a} \times \vec{b})$

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107. If $\vec{a}$ and $\vec{b}$ are unequal unit vectors such that $(\vec{a}-\vec{b}) \times[(\vec{b}+\vec{a}) \times(2 \vec{a}+\vec{b})]=\vec{a}+\vec{b}$ then angle $\theta$ between $\vec{a}$ and $\vec{b}$ is
A. 0
B. $\pi / 2$
C. $\pi / 4$
D. $\pi$

## Answer: b,d

## - Watch Video Solution

108. If $\vec{a}$ and $\vec{b}$ are two unit vectors perpenicualar to each other and $\vec{c}=\lambda_{1} \vec{a}+\lambda_{2} \vec{b}+\lambda_{3}(\vec{a} \times \vec{b})$, then which of the following is (are) true ?
A. $\lambda_{1}=\vec{a} \cdot \vec{c}$
B. $\lambda_{2}=|\vec{b} \times \vec{c}|$
C. $\lambda_{3}=\mid(\vec{a} \times \vec{b}|\times \vec{c}|$
D. $\lambda_{1} \vec{a}+\lambda_{2} \vec{b}+\lambda_{3}(\vec{a} \times \vec{b})$

## Answer: a,d

## - Watch Video Solution

109. If vectors $\vec{a}$ and $\vec{b}$ are non collinear then $\frac{\vec{a}}{|\vec{a}|}+\frac{\vec{b}}{|\vec{b}|}$ is (A) a unit vector (B) in the plane of $\vec{a}$ and $\vec{b}$ (C) equally inclined to $\vec{a}$ and $\vec{b}$ (D) perpendicular to $\vec{a} \times \vec{b}$
A. a unit vector
B. in the plane of $\vec{a}$ and $\vec{b}$
C. equally inclined to $\vec{a}$ and $\vec{b}$
D. perpendicular to $\vec{a} \times \vec{b}$

## - Watch Video Solution

110. If $\vec{a}$ and $\vec{b}$ are non-zero vectors such that $|\vec{a}+\vec{b}|=|\vec{a}-2 \vec{b}|$ then
A. $2 \vec{a} \cdot \vec{b}=|\vec{b}|^{2}$
B. $\vec{a} \cdot \vec{b}=|\vec{b}|^{2}$
C. least value of $\vec{a}$. Vecb $+\frac{1}{|\vec{b}|^{2}+2}$ is $\sqrt{2}$
D. least value of $\vec{a} . \vec{b}+\frac{1}{|\vec{b}|^{2}+2}$ is $\sqrt{2}-1$

## Answer: add

## - Watch Video Solution

111. Let $\vec{a} \vec{b}$ and $\vec{c}$ be non- zero vectors ane $\vec{V}_{1}=\vec{a} \times(\vec{b} \times \vec{c})$ and $\vec{V}_{2}=(\vec{a} \times \vec{b}) \times \vec{c}$. vectors $\vec{V}_{1}$ and $\vec{V}_{2}$ are equal.

Then
A. $\vec{a}$ and $\vec{b}$ ar orthogonal
B. $\vec{a}$ and $\vec{c}$ are collinear
C. $\vec{b}$ and $\vec{c}$ ar orthogonal
D. $\vec{b}=\lambda(\vec{a} \times \vec{c})$ when $\lambda$ is a scalar

## Answer: b,d

## - Watch Video Solution

112. Vectors $\vec{A}$ and $\vec{B}$ satisfying the vector equation $\vec{A}+\vec{B}=\vec{a}, \vec{A} \times \vec{B}=\vec{b}$ and $\vec{A} . \vec{a}=1$. where veca and $\vec{b}$ are given vectosrs, are
A. $\vec{A}=\frac{(\vec{a} \times \vec{b})-\vec{a}}{a^{2}}$
B. $\vec{B}=\frac{(\vec{b} \times \vec{a})+\vec{a}\left(a^{2}-1\right)}{a^{2}}$
C. $\vec{A}=\frac{(\vec{a} \times \vec{b})+\vec{a}}{a^{2}}$
D. $\vec{B}=\frac{(\vec{b} \times \vec{a})-\vec{a}\left(a^{2}-1\right)}{a^{2}}$

Answer: b,c,

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113. A vector $(\vec{d})$ is equally inclined to three vectors $\vec{a}=\hat{i}-\hat{j}+\hat{k}, \vec{b}=2 \hat{i}+\hat{j}$ and $\vec{c}=3 \hat{j}-2 \hat{k}$ let $\vec{x}, \vec{y}, \vec{z}$ be three in the plane of $\vec{a}, \vec{b}, \vec{b}, \vec{c}, \vec{c}, \vec{a}$ respectively, then
A. $\vec{x} \cdot \vec{d}=-1$
B. $\vec{y} \cdot \vec{d}=1$
C. vecz.vecd=0`
D. vecr.vecd=0, " where " vecr=lambda vecx +mu vecy +deltavecz
114. Vectors Perpendicular to $\hat{i}-\hat{j}-\hat{k}$ and in the plane of $\hat{i}+\hat{j}+\hat{k}$ and $-\hat{i}+\hat{j}+\hat{k}$ are
A. $\hat{i}+\hat{k}$
B. $2 \hat{i}+\hat{j}+\hat{k}$
C. $3 \hat{i}+2 \hat{j}+\hat{k}$
D. $-4 \hat{i}-2 \hat{j}-2 \hat{k}$

## Answer: b,d

## Watch Video Solution

115. if side $A B$ of an equilateral triangle $A B C$ lying in the $x-y$ plane is $3 \hat{i}$.

Then side $C B$ can be
A. $-\frac{3}{2}(\hat{i}-\sqrt{3} \hat{j})$
B. $-\frac{3}{2}(\hat{i}-\sqrt{3} \hat{j})$
C. $-\frac{3}{2}(\hat{i}+\sqrt{3} \hat{j})$
D. $\frac{3}{2}(\hat{i}+\sqrt{3} \hat{j})$

## Answer: b,d

## - Watch Video Solution

116. The angles of a triangle, two of whose sides are respresented by vectors $\sqrt{3}(\hat{a} \times \vec{b})$ and $\hat{b}-(\hat{a}$. Vecb) $\hat{a}$ where $\vec{b}$ is a non - zero vector and $\vec{a}$ is a unit vector in the direction of $\vec{a}$. Are
A. $\tan ^{-1}(\sqrt{3})$
B. $\tan ^{-1}(1 / \sqrt{3})$
C. $\cot ^{-1}(0)$
D. $\operatorname{tant}^{\wedge}(-1)(1)^{\wedge}$
117. $\vec{a}, \vec{b}$ and $\vec{c}$ are unimodular and coplanar. A unit vector $\vec{d}$ is perpendicualt to them, $(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d})=\frac{1}{6} \hat{i}-\frac{1}{3} \hat{j}+\frac{1}{3} \hat{k}$, and the angle between $\vec{a}$ and $\vec{b}$ is $30^{\circ}$ then $\vec{c}$ is
A. $(\hat{i}-2 \hat{j}+2 \hat{k}) / 3$
B. $(-\hat{i}+2 \hat{j}-2 \hat{k}) / 3$
C. $(-\hat{i}+2 \hat{j}-\hat{k}) / 3$
D. $(-2 \hat{i}-2 \hat{j}+\hat{k}) / 3$

Answer: a,b

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118. If $\vec{a}+2 \vec{b}+3 \vec{c}=\overrightarrow{0}$ then $\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}=$
A. $2(\vec{a} \times \vec{b})$
B. $6(\vec{b} \times \vec{c})$
C. $3(\vec{c} \times \vec{a})$
D. $\overrightarrow{0}$

## Answer: c,d

## - Watch Video Solution

119. Let $\vec{a}$ and $\vec{b}$ be two non-collinear unit vectors. If $\vec{u}=\vec{a}-(\vec{a} \cdot \vec{b}) \vec{b}$ and $\vec{v}=\vec{a} \times \vec{b}$, then $|\vec{v}|$ is
A. $|\vec{u}|$
B. $|\vec{u}|+|\vec{u} . \vec{b}|$
C. $|\vec{u}|+|\vec{u} . \vec{a}|$
D. none of these

## Answer: b,d

120. if $\vec{a} \times \vec{b}=\vec{c}, \vec{b} \times \vec{c}=\vec{a}$, where $\vec{c} \neq \overrightarrow{0}$ then (a) $|\vec{a}|=|\vec{c}|$ (b) $|\vec{a}|=|\vec{b}|$
(c) $|\vec{b}|=1$ (d) $|\vec{a}|=|\vec{b}|=|\vec{c}|=1$
A. $|\vec{a}|=|\vec{c}|$
B. $|\vec{a}|=|\vec{b}|$
c. $|\vec{b}|=1$
D. $|\vec{a}|=\vec{b}|=|\vec{c}|=1$

## Answer: ac

## - Watch Video Solution

121. Let $\vec{a}, \vec{b}$, and $\vec{c}$ be three non-coplanar vectors and $\vec{d}$ be a non -zero, which is perpendicular to
$(\vec{a}+\vec{b}+\vec{c})$. Now $\vec{d}=(\vec{a} \times \vec{b}) \sin x+(\vec{b} \times \vec{c}) \cos y+2(\vec{c} \times \vec{a})$. Then
$\vec{d} \cdot(\vec{a}+\vec{c})$
A. $\xrightarrow{(a+\vec{c})}=2$
$[\vec{a} \vec{b} \vec{c}]$
B. $\frac{\vec{d} \cdot(\vec{a}+\vec{c})}{[\vec{a} \vec{b} \vec{c}]}=-2$
C. minimum value of $x^{2}+y^{2} i s \pi^{2} / 4$
D. minimum value of $x^{2}+y^{2} i s 5 \pi^{2} / 4$

## Answer: b,d

## D Watch Video Solution

122. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three unit vectors such that $\vec{a} \times(\vec{b} \times \vec{c})=\frac{1}{2} \vec{b}$, then $(\vec{b}$ and $\vec{c}$ being non parallel)
A. angle between $\vec{a}$ and $\vec{b} i s \pi / 3$
B. angle between $\vec{a}$ and $\vec{c} i s \pi / 3$
C. angle between $\vec{a}$ and $\vec{b} i s \pi / 2$
D. angle between $\vec{a}$ and $\vec{c} i s \pi / 2$

## - Watch Video Solution

123. If in triangle $A B C, \overrightarrow{A B}=\frac{\vec{u}}{|\vec{u}|}-\frac{\vec{v}}{|\vec{v}|}$ and $\overrightarrow{A C}=\frac{2 \vec{u}}{|\vec{u}|}$, where $|\vec{u}| \neq|\vec{v}|$, then $(a) 1+\cos 2 A+\cos 2 B+\cos 2 C=0(b) \sin A=\cos C(c)$ projection of $A C$ on $B C$ is equal to $B C$ (d) projection of $A B$ on $B C$ is equal to $A B$
A. $1+\cos 2 A+\cos 2 B+\cos 2 C=0$
B. $\sin A=\cos C$
C. projection of $A C$ on $B C$ is equal to $B C$
D. projection of $A B$ on $B C$ is equal to $A B$

## Answer: a,b,c

124. $\left[\begin{array}{lll}\vec{a} \times \vec{b} & \vec{c} \times \vec{d} & \vec{e} \times \vec{f}\end{array}\right]$ is equal to
(a) $[\vec{a} \vec{b} \vec{d}][\vec{c} \vec{e} \vec{f}]-[\vec{a} \vec{b} \vec{c}][\vec{d} \vec{e} \vec{f}]$
(b) $[\vec{a} \vec{b} \vec{e}][\vec{f} \vec{c} \vec{d}]-[\vec{a} \vec{b} \vec{f}][\vec{e} \vec{c} \vec{d}]$
(c) $[\vec{c} \vec{d} \vec{a}][\vec{b} \vec{e} \vec{f}]-[\vec{a} \vec{d} \vec{b}][\vec{a} \vec{e} \vec{f}]$
(d) $[\vec{a} \vec{c} \vec{e}][\vec{b} \vec{d} \vec{f}]$
A. $[\vec{a} \vec{b} \vec{d}][\vec{c} \vec{e} \vec{f}]-[\vec{a} \vec{b} \vec{c}][\vec{d} \vec{e} \vec{f}]$
B. $[\vec{a} \vec{b} \vec{e}][\vec{f} \vec{c} \vec{d}]-[\vec{a} \vec{b} \vec{f}][\vec{e} \vec{c} \vec{d}]$
C. $[\vec{c} \vec{d} \vec{a}][\vec{b} \vec{e} \vec{f}]-[\vec{a} \vec{d} \vec{b}][\vec{a} \vec{e} \vec{f}]$
D. $[\vec{a} \vec{c} \vec{e}][\vec{b} \vec{d} \vec{f}]$

## Answer: a,b,c

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125. The scalars $I$ and m such that $l \vec{a}+m \vec{b}=\vec{c}$, where $\vec{a}, \vec{b}$ and $\vec{c}$ are given vectors, are equal to
A. I $=\frac{(\vec{c} \times \vec{b}) \cdot(\vec{a} \times \vec{b})}{(\vec{a} \times \vec{b})^{2}}$
B. $l=\frac{(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})}$
$(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{a})$
C. $m=$

$$
(\vec{b} \times \vec{a})^{2}
$$

D. $m=\frac{(\vec{c} \times \vec{a}) \cdot(\vec{b} \times \vec{a})}{(\vec{b} \times \vec{a})}$

## Answer: ac

## - Watch Video Solution

126. If $(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d}) \cdot(\vec{a} \times \vec{d})=0$ then which of the following may be true?
A. $\vec{a}, \vec{b}$ and $\vec{d}$ are nenessarily coplanar
B. $\vec{a}$ lies in the plane of $\vec{c}$ and $\vec{d}$
C. $\vec{v} b$ lies in the plane of $\vec{a}$ and $\vec{d}$
D. $\vec{c}$ lies in the plane of $\vec{a}$ and $\vec{d}$

Answer: b,c,d

## - Watch Video Solution

127. $A, B$ and $d D$ are four points such that
$\overrightarrow{A B}=m(2 \hat{i}-6 \hat{j}+2 \hat{k}) \overrightarrow{B C}=(\hat{i}-2 \hat{j})$ and $\overrightarrow{C D}=n(-6 \hat{i}+15 \hat{j}-3 \hat{k}) . \quad$ If $\quad C D$ intersects $A B$ at some points $E$, then
A. $m \geq 1 / 2$
B. $n \geq 1 / 3$
C. $m=n$
D. $m<n$

## Answer: a,b

128. If the vectors $\vec{a}, \vec{b}, \vec{c}$ are non-coplanar and $l, m, n$ are distinct scalars such that

$$
[l \vec{a}+m \vec{b}+n \vec{c} \quad l \vec{b}+m \vec{c}+n \vec{a} \quad l \vec{c}+m \vec{a}+n \vec{b}]=0 \text { then }
$$

A. $l+m+n=0$
B. roots of the equation $l x^{2}+m x+n=0$ are equal
C. $l^{2}+m^{2}+n^{2}=0$
D. $l^{3}+m^{2}+n^{3}=3 l m n$

## Answer: a,b,d

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129. Let $\vec{\alpha}=a \hat{i}+b \hat{j}+c \hat{k}, \vec{\beta}=b \hat{i}+c \hat{j}+a \hat{k}$ and $\vec{\gamma}=c \hat{i}+a \hat{j}+b \hat{k}$ be three coplnar vectors with $a \neq b$, and $\vec{v}=\hat{i}+\hat{j}+\hat{k}$. Then $\vec{v}$ is perpendicular to
A. $\vec{\alpha}$
B. $\vec{\beta}$
C. $\vec{\gamma}$
D. none of these

## Answer: a,b,c

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130. If vectors $\vec{A}=2 \hat{i}+3 \hat{j}+4 \hat{k}, \vec{B}=\hat{i}+\hat{j}+5 \hat{k}$ and $\vec{C}$ form a left handed system then $\vec{C}$ is (A) $11 \hat{i}-6 \hat{j}-\hat{k}$
(B) $-11 \hat{i}+6 \hat{j}+\hat{k} \quad$ (C) $-11 \hat{i}+6 \hat{j}-\hat{k}$
$-11 \hat{i}+6 \hat{j}-\hat{k}$
A. $11 \hat{i}-6 \hat{j}-\hat{k}$
B. $-11 \hat{i}-6 \hat{j}-\hat{k}$
C. $-11 \hat{i}-6 \hat{j}+\hat{k}$
D. $-11 \hat{i}+6 \hat{j}-\hat{k}$

Answer: b,d
131. If $\vec{a}=x \hat{i}+y \hat{j}+z \hat{k}, \vec{b}=y \hat{i}+z \hat{j}+x \hat{k}$ and $\vec{c}=z \hat{i}+x \hat{j}+y \hat{k}$, then $\vec{a} \times(\vec{b} \times \vec{c})$ is
(a)parallel to $(y-z) \hat{i}+(z-x) \hat{j}+(x-y) \hat{k} \quad$ (b)orthogonal to $\hat{i}+\hat{j}+\hat{k}$
(c)orthogonal to $(y+z) \hat{i}+(z+x) \hat{j}+(x+y) \hat{k}$ (d)orthogonal to $x \hat{i}+y \hat{j}+z \hat{k}$
A. parallel to $(y-z) \hat{i}+(z-x) \hat{j}+(x-y) \hat{k}$
B. orthogonal to $\hat{i}+\hat{j}+\hat{k}$
C. orthogonal to $(y+z) \hat{i}+(z+x) \hat{j}+(x+y) \hat{k}$
D. orthogonal to $x \hat{i}+y \hat{j}+z \hat{k}$

## Answer: a,b,c,d

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132. If $\vec{a} \times(\vec{b} \times \vec{c})=(\vec{a} \times \vec{b}) \times \vec{c}$ then
A. $(\vec{c} \times \vec{a}) \times \vec{b}=\overrightarrow{0}$
B. $\vec{c} \times(\vec{a} \times \vec{b})=\overrightarrow{0}$
C. $\vec{b} \times(\vec{c} \times \vec{a})=\overrightarrow{0}$
D. $\vec{c} \times \vec{a} \times \vec{b}=\vec{b} \times(\vec{c} \times \vec{a})=\overrightarrow{0}$

## Answer: a,c,d

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133. A vector $(\vec{d})$ is equally inclined to three vectors $\vec{a}=\hat{i}-\hat{j}+\hat{k}, \vec{b}=2 \hat{i}+\hat{j}$ and $\vec{c}=3 \hat{j}-2 \hat{k}$ let $\vec{x}, \vec{y}, \vec{z}$ be three in the plane of $\vec{a}, \vec{b}, \vec{b}, \vec{c}, \vec{c}, \vec{a}$ respectively, then
A. $\vec{z} \cdot \vec{d}=0$
B. $\vec{x} \cdot \vec{d}=1$
C. $\vec{y} . \vec{d}=32$
D. $\vec{r} \cdot \vec{d}=0$, where $\vec{r}=\lambda \vec{x}+\mu \vec{y}+\gamma \vec{z}$
134. A parallelogram is constructed on the vectors $\vec{a}=3 \vec{\alpha}-\vec{\beta}, \vec{b}=\vec{\alpha}+3 \vec{\beta}$. If $|\vec{\alpha}|=|\vec{\beta}|=2$ and angle between $\vec{\alpha}$ and $\vec{\beta}$ is $\frac{\pi}{3}$ then the length of a diagonal of the parallelogram is
A. $4 \sqrt{5}$
B. $4 \sqrt{3}$
C. $4 \sqrt{7}$
D. none of these

Answer: b,c

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1. (a)Statement 1: Vector $\vec{c}=-5 \hat{i}+7 \hat{j}+2 \hat{k}$ is along the bisector of angle between $\vec{a}=\hat{i}+2 \hat{j}+2 \hat{k}$ and $\vec{b}=8 \hat{i}+\hat{j}-4 \hat{k}$.

Statement $2: \vec{c}$ is equally inclined to $\vec{a}$ and $\vec{b}$.
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

Answer: b

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2. Statement1: A component of vector $\vec{b}=4 \hat{i}+2 \hat{j}+3 \hat{k}$ in the direction perpendicular to the direction of vector $\vec{a}=\hat{i}+\hat{j}+\hat{k} i s \hat{i}-\hat{j}$

Statement 2: A component of vector in the direction of $\vec{a}=\hat{i}+\hat{j}+\hat{k} i s 2 \hat{i}+2 \hat{j}+2 \hat{k}$
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: c

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3. Statement 1: Distance of point $D(1,0,-1)$ from the plane of points $A($
$1,-2,0), B(3,1,2)$ and $C(-1,1,-1)$ is $\frac{8}{\sqrt{229}}$
Statement 2: volume of tetrahedron formed by the points $A, B, C$ and $D$ is $\sqrt{229}$
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: d

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4. Let $\vec{r}$ be a non-zero vector satisfying $\vec{r} \cdot \vec{a}=\vec{r} \cdot \vec{b}=\vec{r} . \vec{c}=0$ for given non-zero vectors $\vec{a} \vec{b}$ and $\vec{c}$

Statement 1: $[\vec{a}-\vec{b} \vec{b}-\vec{c} \vec{c}-\vec{a}]=0$
Statement 2: $[\vec{a} \vec{b} \vec{c}]=0$
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: b

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5. Statement 1: If $a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}, \vec{b} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$ are three mutually perpendicular unit vectors then $a_{1} \hat{i}+b_{1} \hat{j}+c_{1} \hat{k}, a_{2} \hat{i}+b_{2} \hat{j}+c_{2} \hat{k}$ and $a_{3} \hat{i}+b_{3} \hat{j}+c_{3} \hat{k}$ may be mutually perpendicular unit vectors.

Statement 2 : value of determinant and its transpose are the same.
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: a

## - Watch Video Solution

6. Statement $1: \vec{A}=2 \hat{i}+3 \hat{j}+6 \hat{k}, \vec{B}=\hat{u}+\hat{j}-2 \hat{k}$ and $\vec{C}=\hat{i}+2 \hat{j}+\hat{k}$ then
$|\vec{A} \times(\vec{A} \times(\vec{A} \times \vec{B})) \cdot \vec{C}|=243$
Statement 2: $|\vec{A} \times(\vec{A} \times(\vec{A} \times \vec{B})) \cdot \vec{C}|=|\vec{A}|^{2}|[\vec{A} \vec{B} \vec{C}]|$
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: d

## D Watch Video Solution

7. Statement $1: \vec{a}, \vec{b}$ and $\vec{c}$ arwe three mutually perpendicular unit vectors and $\vec{d}$ is a vector such that $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ are non- coplanar. If $[\vec{d} \vec{b} \vec{c}]=[\vec{d} \vec{a} \vec{b}]=[\vec{d} \vec{c} \vec{a}]=1$, then $\vec{d}=\vec{a}+\vec{b}+\vec{c}$ Statement 2: $\quad[\vec{d} \vec{b} \vec{c}]=[\vec{d} \vec{a} \vec{b}]=[\vec{d} \vec{c} \vec{a}] \Rightarrow \vec{d}$ is equally inclined to $\vec{a}, \vec{b}$ and $\vec{c}$.
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: b

## D Watch Video Solution

8. Consider three vectors $\vec{a}, \vec{b}$ and $\vec{c}$

Statement 1: $\vec{a} \times \vec{b}=((\hat{i} \times \vec{a}) \cdot \vec{b}) \hat{i}+((\hat{j} \times \vec{a}) \cdot \vec{b}) \hat{j}+(\hat{k} \times \vec{a}) \cdot \vec{b}) \hat{k}$
Statement 2: $\vec{c}=(\hat{i} \cdot \vec{c}) \hat{i}+(\hat{j} \cdot \vec{c}) \hat{j}+(\hat{k} \cdot \vec{c}) \hat{k}$
A. Both the statements are true and statement 2 is the correct explanation for statement 1.
B. Both statements are true but statement 2 is not the correct explanation for statement 1.
C. Statement 1 is true and Statement 2 is false
D. Statement 1 is false and Statement 2 is true.

## Answer: a

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## Comprehension type

1. Let $\vec{u}, \vec{v}$ and $\vec{w}$ be three unit vectors such that $\vec{u}+\vec{v}+\vec{w}=\vec{a}, \vec{u} \times(\vec{v} \times \vec{w})=\vec{b},(\vec{u} \times \vec{v}) \times \vec{w}=\vec{c}, \vec{a} \cdot \vec{u}=3 / 2, \vec{a} \cdot \vec{v}=7 / 4$ and

Vector $\vec{w}$ is
A. $\vec{a}-\frac{2}{3} \vec{b}+\vec{c}$
B. $\vec{a}+\frac{4}{3} \vec{b}+\frac{8}{3} \vec{c}$
C. $2 \vec{a}-\vec{b}+\frac{1}{3} \vec{c}$
D. $\frac{4}{3} \vec{a}-\vec{b}+\frac{2}{3} \vec{c}$

## D Watch Video Solution

2. Let $\vec{u}, \vec{v}$ and $\vec{w}$ be three unit vectors such that $\vec{u}+\vec{v}+\vec{w}=\vec{a}, \vec{u} \times(\vec{v} \times \vec{w})=\vec{b},(\vec{u} \times \vec{v}) \times \vec{w}=\vec{c}, \vec{a} \cdot \vec{u}=3 / 2, \vec{a} \cdot \vec{v}=7 / 4$ and

## Vector $\vec{w}$ is

A. (a) $\vec{a}-\frac{2}{3} \vec{b}+\vec{c}$
B. (b) $\vec{a}+\frac{4}{3} \vec{b}+\frac{8}{3} \vec{c}$
C. (c) $2 \vec{a}-\vec{b}+\frac{1}{3} \vec{c}$
D. (d) $\frac{4}{3} \vec{a}-\vec{b}+\frac{2}{3} \vec{c}$

## Answer: c

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3. Let $\vec{u}, \vec{v}$ and $\vec{w}$ be three unit vectors such that $\vec{u}+\vec{v}+\vec{w}=\vec{a}, \vec{u} \times(\vec{v} \times \vec{w})=\vec{b},(\vec{u} \times \vec{v}) \times \vec{w}=\vec{c}, \vec{a} \cdot \vec{u}=3 / 2, \vec{a} \cdot \vec{v}=7 / 4$ and Vector $\vec{u}$ is
A. (a) $\vec{a}-\frac{2}{3} \vec{b}+\vec{c}$
B. (b) $\vec{a}+\frac{4}{3} \vec{b}+\frac{8}{3} \vec{c}$
C. (c) $2 \vec{a}-\vec{b}+\frac{1}{3} \vec{c}$
D. (a) $\frac{4}{3} \vec{a}-\vec{b}+\frac{2}{3} \vec{c}$

## Answer: d

## Watch Video Solution

4. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of $60^{\circ}$ with each other. If $\vec{x} \times(\vec{y} \times \vec{z})=\vec{a}, \vec{y} \times(\vec{z} \times \vec{x})=\vec{b}$ and $\vec{x} \times \vec{y}=\vec{c}$, find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}$ and $\vec{c}$.
5. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of $60^{\circ}$ with each other. If $\vec{x} \times(\vec{y} \times \vec{z})=\vec{a}, \vec{y} \times(\vec{z} \times \vec{x})=\vec{b}$ and $\vec{x} \times \vec{y}=\vec{c}$, find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}$ and $\vec{c}$.
A. $\frac{1}{2}[(\vec{a}+\vec{c}) \times \vec{b}-\vec{b}-\vec{a}]$
B. $\frac{1}{2}[(\vec{a}-\vec{c}) \times \vec{b}+\vec{b}+\vec{a}]$
C. $\frac{1}{2}[(\vec{a}-\vec{b}) \times \vec{c}+\vec{b}+\vec{a}]$
D. $\frac{1}{2}[(\vec{a}-\vec{c}) \times \vec{a}+\vec{b}-\vec{a}]$

## Answer: c

## - Watch Video Solution

6. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of $60^{\circ}$ with each other. If $\vec{x} \times(\vec{y} \times \vec{z})=\vec{a}, \vec{y} \times(\vec{z} \times \vec{x})=\vec{b}$ and $\vec{x} \times \vec{y}=\vec{c}$. Find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}, \vec{c}$.
A. $\frac{1}{2}[(\vec{a}-\vec{c}) \times \vec{c}-\vec{b}+\vec{a}]$
B. $\frac{1}{2}[(\vec{a}-\vec{b}) \times \vec{c}+\vec{b}-\vec{a}]$
C. $\frac{1}{2}[\vec{c} \times(\vec{a}-\vec{b})+\vec{b}+\vec{a}]$
D. none of these

## Answer: b

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7. If $\vec{x} \times \vec{y}=\vec{a}, \vec{y} \times \vec{z}=\vec{b}, \vec{x} . \vec{b}=\gamma, \vec{x} . \vec{y}=1$ and $\vec{y} \cdot \vec{z}=1$ then find $x, y, z$ in terms of $\vec{a}, \vec{b}$ and $\gamma$.
A. $\frac{1}{|\vec{a} \times \vec{b}|^{2}}[\vec{a} \times(\vec{a} \times \vec{b})]$
B. $\frac{\gamma}{|\vec{a} \times \vec{b}|^{2}}[\vec{a} \times \vec{b}-\vec{a} \times(\vec{a} \times \vec{b})]$
C. $\frac{\gamma}{|\vec{a} \times \vec{b}|^{2}}[\vec{a} \times \vec{b}+\vec{a} \times(\vec{a} \times \vec{b})]$
D. none of these
8. If $\vec{x} \times \vec{y}=\vec{a}, \vec{y} \times \vec{z}=\vec{b}, \vec{x} \cdot \vec{b}=\gamma, \vec{x} \cdot \vec{y}=1$ and $\vec{y} \cdot \vec{z}=1$ then find $x, y, z$ in terms of $\vec{a}, \vec{b}$ and $\gamma$.
A. $\frac{\vec{a} \times \vec{b}}{\gamma}$
B. $\vec{a}+\frac{\vec{a} \times \vec{b}}{\gamma}$
C. $\vec{a}+\vec{b}+\frac{\vec{a} \times \vec{b}}{\gamma}$
D. none of these

## Answer: a

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9. Vectors $\vec{x}, \vec{y}, \vec{z}$ each of magnitude $\sqrt{2}$ make angles of $60^{\circ}$ with each other. If $\vec{x} \times(\vec{y} \times \vec{z})=\vec{a}, \vec{y} \times(\vec{z} \times \vec{x})=\vec{b}$ and $\vec{x} \times \vec{y}=\vec{c}$. Find $\vec{x}, \vec{y}, \vec{z}$ in terms of $\vec{a}, \vec{b}, \vec{c}$.
A. $\frac{\gamma}{|\vec{a} \times \vec{b}|^{2}}[\vec{a}+\vec{b} \times(\vec{a} \times \vec{b})]$
B. $\frac{\gamma}{|\vec{a} \times \vec{b}|^{2}}[\vec{a}+\vec{b}-\vec{a} \times(\vec{a} \times \vec{b})]$
C. $\frac{\gamma}{|\vec{a} \times \vec{b}|^{2}}[\vec{a}+\vec{b}+\vec{a} \times(\vec{a} \times \vec{b})]$
D. none of these

## Answer: c

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10. Given two orthogonal vectors $\vec{A}$ and $\vec{B}$ each of length unity. Let $\vec{P}$ be the vector satisfying the equation $\vec{P} \times \vec{B}=\vec{A}-\vec{P}$. then
$(\vec{P} \times \vec{B}) \times \vec{B}$ is equal to
A. $\vec{P}$
B. $-\vec{P}$
C. $2 \vec{B}$
D. $\vec{A}$

Answer: b

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11. Given two orthogonal vectors $\vec{A}$ and $\vec{B}$ each of length unity. Let $\vec{P}$ be the vector satisfying the equation $\vec{P} \times \vec{B}=\vec{A}-\vec{P}$. then
$\vec{P}$ is equal to
A. $\frac{\vec{A}}{2}+\frac{\vec{A} \times \vec{B}}{2}$
B. $\frac{\vec{A}}{2}+\frac{\vec{B} \times \vec{A}}{2}$
C. $\frac{\vec{A} \times \vec{B}}{2}-\frac{\vec{A}}{2}$
D. $\vec{A} \times \vec{B}$

## Answer: b

12. Given two orthogonal vectors $\vec{A}$ and VecB each of length unity. Let $\vec{P}$ be the vector satisfying the equation $\vec{P} \times \vec{B}=\vec{A}-\vec{P}$. then which of the following statements is false ?
A. vectors $\vec{P}, \vec{A}$ and $\vec{P} \times \vec{B}$ ar linearly dependent.
B. vectors $\vec{P}, \vec{B}$ and $\vec{P} \times \vec{B}$ ar linearly independent
C. $\vec{P}$ is orthogonal to $\vec{B}$ and has length $\frac{1}{\sqrt{2}}$.
D. none of these

## Answer: d

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13. Let $\vec{a}=2 \hat{i}+3 \hat{j}-6 \hat{k}, \vec{b}=2 \hat{i}-3 \hat{j}+6 \hat{k}$ and $\vec{c}=-2 \hat{i}+3 \hat{j}+6 \hat{k}$. Let $\vec{a}_{1}$ be the projection of $\vec{a}$ on $\vec{b}$ and $\vec{a}_{2}$ be the projection of $\vec{a}_{1}$ on $\vec{c}$. Then $\vec{a}_{2}$ is equal to

$$
\text { A. } \frac{943}{49}(2 \hat{i}-3 \hat{j}-6 \hat{k})
$$

B. $\frac{943}{49^{2}}(2 \hat{i}-3 \hat{j}-6 \hat{k})$
C. $\frac{943}{49}(-2 \hat{i}+3 \hat{j}+6 \hat{k})$
D. $\frac{943}{49^{2}}(-2 \hat{i}+3 \hat{j}+6 \hat{k})$

## Answer: b

## D Watch Video Solution

14. Let $\vec{a}=2 \hat{i}+3 \hat{j}-6 \hat{k}, \vec{b}=2 \hat{i}-3 \hat{j}+6 \hat{k}$ and $\vec{c}=-2 \hat{i}+3 \hat{j}+6 \hat{k}$. Let $\vec{a}_{1}$ be the projection of $\vec{a}$ on $\vec{b}$ and $\vec{a}_{2}$ be the projection of $\vec{a}_{1}$ on $\vec{c}$. Then $\vec{a}_{1} \cdot \vec{b}$ is equal to
A. -41
B. $-41 / 7$
C. 41
D. 287
15. Let $\vec{a}=2 \hat{i}+3 \hat{j}-6 \hat{k}, \vec{b}=2 \hat{i}-3 \hat{j}+6 \hat{k}$ and $\vec{c}=-2 \hat{i}+3 \hat{j}+6 \hat{k}$. Let $\vec{a}_{1}$ be the projection of $\vec{a}$ on $\vec{b}$ and $\vec{a}_{2}$ be the projection of $\vec{a}_{1}$ on $\vec{c}$. Then $\vec{a}_{2}$ is equal to
A. $\vec{a}$ and $v c e a_{2}$ are collinear
B. $\vec{a}_{1}$ and $\vec{c}$ are collinear
C. $\vec{a} m \vec{a}_{1}$ and $\vec{b}$ are coplanar
D. $\vec{a}, \vec{a}_{1}$ and $a_{2}$ are coplanar

## Answer: c

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16. Consider a triangular pyramid ABCD the position vectors of whose agular points are $A(3,0,1), B(-1,4,1), C(5,3,2)$ and $D(0,-5,4)$ Let $G$ be
the point of intersection of the medians of the triangle BCD. The length of the vector $A G$ is
A. $\sqrt{17}$
B. $\sqrt{51} / 3$
C. $3 / \sqrt{6}$
D. $\sqrt{59} / 4$

## Answer: b

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17. Consider a triangular pyramid ABCD the position vectors of whose agular points are $A(3,0,1), B(-1,4,1), C(5,3,2)$ and $D(0,-5,4)$ Let $G$ be the point of intersection of the medians of the triangle BCD. The length of the vector $A G$ is
A. 24
B. $8 \sqrt{6}$
C. $4 \sqrt{6}$
D. none of these

## Answer: c

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18. Consider a triangular pyramid ABCD the position vectors of whose agular points are $A(3,0,1), B(-1,4,1), C(5,3,2)$ and $D(0,-5,4)$ Let $G$ be the point of intersection of the medians of the triangle BCD. The length
of the vector $A G$ is
A. $14 / \sqrt{6}$
B. $2 / \sqrt{6}$
C. $3 / \sqrt{6}$
D. none of these

## Answer: a

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19. Vertices of a parallelogram taken in order are $\mathrm{A},(2,-1,4), \mathrm{B}(1,0,-1), \mathrm{C}($ $1,2,3$ ) and $D(x, y, z)$ The distance between the parallel lines $A B$ and $C D$ is
A. $\sqrt{6}$
B. $3 \sqrt{6 / 5}$
C. $2 \sqrt{2}$
D. 3

## Answer: c

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20. Vertices of a parallelogram taken in order are $\mathrm{A}(2,-1,4) \mathrm{B}(1,0,-1) \mathrm{C}(1,2,3)$ and $D$.

Distance of the point $P(8,2,-12)$ from the plane of the parallelogram is
A. $\frac{4 \sqrt{6}}{9}$
$32 \sqrt{6}$
B. $\frac{}{9}$
C. $\frac{16 \sqrt{6}}{9}$
D. none

## Answer: b

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21. Vertices of a parallelogram taken in order are A, ( 2,-1,4) , B (1,0,-1) , C (
$1,2,3$ ) and $D(x, y, z)$ The distance between the parallel lines $A B$ and $C D$ is
A. $14,4,2$
B. 2,4,14
C. $4,2,14$
D. $2,14,4$

## D Watch Video Solution

22. Let $\vec{r}$ be a position vector of a variable point in Cartesian OXY plane such that

$$
\vec{r} .(10 \hat{j}-8 \hat{i}-\vec{r})=40 \quad \text { and }
$$

$P_{1}=\max \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\}, P_{2}=\min \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\}$. A tangenty line is drawn to the curve $y=8 / x^{2}$ at point.$A$ with abscissa 2. the drawn line cuts the $x$-axis at a point $B$.
$p_{2}$ is equal to
A. 9
B. $2 \sqrt{2}-1$
C. $6 \sqrt{6}+3$
D. $9-4 \sqrt{2}$

## Answer: d

23. Let $\vec{r}$ be a position vector of a variable point in Cartesian OXY plane such that $\quad \vec{r} .(10 \hat{j}-8 \hat{i}-\vec{r})=40 \quad$ and
$P_{1}=\max \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\}, P_{2}=\min \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\}$. A tangenty line is drawn to the curve $y=8 / x^{2}$ at point.$A$ with abscissa 2. the drawn line cuts the $x$-axis at a point $B$.
$p_{2}$ is equal to
A. 2
B. 10
C. 18
D. 5

## Answer: c

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24. Let $\vec{r}$ be a position vector of a variable point in Cartesian OXY plane that $\begin{gathered}\vec{r} \cdot(10 \hat{j}-8 \hat{i}-\vec{r})=40 \\ P_{1}=\max \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\}, P_{2}=\min \left\{|\vec{r}+2 \hat{i}-3 \hat{j}|^{2}\right\} . \text { A tangenty line is }\end{gathered}$ drawn to the curve $y=8 / x^{2}$ at point .A with abscissa 2. the drawn line cuts the $x$-axis at a point $B$.
$p_{2}$ is equal to
A. 1
B. 2
C. 3
D. 4

## Answer: c

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25. $A b, A C$ and $A D$ are three adjacent edges of a parallelpiped. The diagonal of the praallelepiped passing through A and direqcted away
from it is vector $\vec{a}$. The vector of the faces containing vertices A, B, C and $\mathrm{A}, \mathrm{B}, \mathrm{D}$ are $\vec{b}$ and $\vec{c}$, respectively, i.e. $A B \times A C$ and $A D \times A B=\vec{c}$ the projection of each edge $A B$ and $A C$ on diagonal vector $\vec{a}$ is $\frac{|\vec{a}|}{3}$ vector $A D$ is
A. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}$
B. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}+\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
C. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}-\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
D. none of these

## Answer: a

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26. $A b, A C$ and $A D$ are three adjacent edges of a parallelpiped. The diagonal of the praallelepiped passing through $A$ and direqcted away
from it is vector $\vec{a}$. The vector of the faces containing vertices A, B, C and $\mathrm{A}, \mathrm{B}, \mathrm{D}$ are $\vec{b}$ and $\vec{c}$, respectively, i.e. $A B \times A C=\vec{b}$ and $A D \times \overrightarrow{A B}=\vec{c}$ the projection of each edge $A B$ and $A C$ on diagonal vector $\vec{a}$ is $\frac{|\vec{a}|}{3}$ vector $A B$ is
A. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}$
B. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}+\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
C. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}-\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
D. none of these

## Answer: b

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27. $A b, A C$ and $A D$ are three adjacent edges of a parallelpiped. The diagonal of the praallelepiped passing through $A$ and direqcted away
from it is vector $\vec{a}$. The vector of the faces containing vertices $A, B, C$ and
$\mathrm{A}, \mathrm{B}, \mathrm{D}$ are $\vec{b}$ and $\vec{c}$, respectively, i.e. $A B \times A C=\vec{b}$ and $A D \times A B=\vec{c}$ the projection of each edge $A B$ and $A C$ on diagonal vector $\vec{a}$ is $\frac{|\vec{a}|}{3}$ vector $A B$ is
A. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}$
B. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}+\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
C. $\frac{1}{3} \vec{a}+\frac{\vec{a} \times(\vec{b}-\vec{c})}{|\vec{a}|^{2}}-\frac{3(\vec{b} \times \vec{a})}{|\vec{a}|^{2}}$
D. none of these

## Answer: c

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2. 

.

- View Text Solution

3. 

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4. Given two vectors $\vec{a}=-\hat{i}+\hat{j}+2 \hat{k}$ and $\vec{b}=-\hat{i}-2 \hat{j}-\hat{k}$

Find
a. $\vec{a} \times \vec{b}$ then use this to find the area of the triangle.
b. The area of the parallelogram
c. The area of a paralleogram whose diagonals are

2 veca and 4 vecb

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5. Given two vectors $\vec{a}=-\hat{i}+2 \hat{j}+2 \hat{k}$ and $\vec{b}=-2 \hat{i}+\hat{j}+2 \hat{k}$ find $|\vec{a} \times \vec{b}|$

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6. 

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7. find $|\vec{x}|$, if for a unit vector $\vec{a},(\vec{x}-\vec{a})(\vec{x}+\vec{a})=12$

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8. 

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9. 

## - View Text Solution

10. 

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## Integer type

1. If $\vec{a}$ and $\vec{b}$ are any two unit vectors, then find the greatest postive integer in the range of $\frac{3|\vec{a}+\vec{b}|}{2}+2|\vec{a}-\vec{b}|$
2. Let $\vec{u}$ be a vector on rectangular coodinate system with sloping angle $60^{\circ}$ suppose that $|\vec{u}-\hat{i}|$ is geomtric mean of $|\vec{u}|$ and $|\vec{u}-2 \hat{i}|$, where $\hat{i}$ is the unit vector along the $x$-axis. Then find the value of $(\sqrt{2}-1)|\vec{u}|$

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3. Find the absolute value of parameter $t$ for which the area of the triangle whose vertices the $A(-1,1,2) ; B(1,2,3)$ and $C(5,1,1)$ is minimum.

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4. If $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}, \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}, \vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k} \quad$ and
$[3 \vec{a}+\vec{b} 3 \vec{b}+\vec{c} 3 \vec{c}+\vec{a}]=\lambda\left|\begin{array}{lll}a_{1} & a_{2} & a_{3} \\ b_{1} & b_{2} & b_{3} \\ c_{1} & c_{2} & c_{3}\end{array}\right|$ then find the value of $\frac{\lambda}{4}$
5. Let $\vec{a}=\alpha \hat{i}+2 \hat{j}-3 \hat{k}, \vec{b}=\hat{i}+2 \alpha \hat{j}-2 \hat{k}$ and $\vec{c}=2 \hat{i}-\alpha \hat{j}+\hat{k}$. Find the value of $6 \alpha$. Such that $\{(\vec{a} \times \vec{b}) \times(\vec{b} \times \vec{c})\} \times(\vec{c} \times \vec{a})=0$

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6. If , $\vec{x}, \vec{y}$ are two non-zero and non-collinear vectors satisfying

$$
\left[(a-2) \alpha^{2}+(b-3) \alpha+c\right] \vec{x}+[(a-2) \beta+c] \vec{y}+\left[(a-2) \gamma^{2}+(b-3) \gamma+c\right](\vec{x} \times \vec{y})=
$$ are three distinct distinct real numbers, then find the value of $\left(a^{2}+b^{2}+c^{2}-4\right)$

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7. Let $\vec{u}$ and $\vec{v}$ be unit vectors such that $\vec{u} \times \vec{v}+\vec{u}=\vec{w}$ and $\vec{w} \times \vec{u}=\vec{v}$.

Find the value of $[\vec{u} \vec{v} \vec{w}]$
8. The volume of the tetrahedron whose vertices are the points with positon vectors $\hat{i}-6 \hat{j}+10 \hat{k},-\hat{i}-3 \hat{j}+7 \hat{k}, 5 \hat{i}-\hat{j}+\lambda \hat{k}$ and $7 \hat{i}-4 \hat{j}+7 \hat{k}$ is 11 cubic units if the value of $\lambda$ is

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9. 

Given
that
$\vec{u}=\hat{i}+2 \hat{j}+3 \hat{k}, \vec{v}=2 \hat{i}+\hat{k}+4 \hat{k}, \vec{w}=\hat{i}+3 \hat{j}+3 \hat{k}$ and $(\vec{u} \cdot \vec{R}-15) \hat{i}+(\vec{c} \cdot \vec{R}-30) \hat{j}$
.Then find the greatest integer less than or equal to $|\vec{R}|$.

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10. Let a three- dimensional vector $\vec{V}$ satisfy the condition, $2 \vec{V}+\vec{V} \times(\hat{i}+2 \hat{j})=2 \hat{i}+\hat{k}$. If $3|\vec{V}|=\sqrt{m}$. Then find the value of $m$.
11. If $\vec{a}, \vec{b}, \vec{c}$ are unit vectors such that $\vec{a}, \vec{b}=0=\vec{a} . \vec{c}$ and the angle between $\vec{b}$ and $\vec{c} i s \frac{\pi}{3}$, then find the value of $|\vec{a} \times \vec{b}-\vec{a} \times \vec{c}|$

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12. Let $\vec{O} A=\vec{a}, \vec{O} B=10 \vec{a}+2 \vec{b}$ and $\vec{O} C=\vec{b}$, where $O$, Aand $C$ are noncollinear points. Let $p$ denotes the areaof quadrilateral $O A C B$, and let $q$ denote the area of parallelogram with OAandOC as adjacent sides. If $p=k q$, then find $k$

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13. Find the work done by the force $F=3 \hat{i}-\hat{j}-2 \hat{k}$ acrting on a particle such that the particle is displaced from point $A(-3,-4,1) \top o \in t B(-1,-1,-2)$
14. If $\vec{a}$ and $\vec{b}$ are vectors in space given by $\vec{a}=\frac{\hat{i}-2 \hat{j}}{\sqrt{5}}$ and $\vec{b}=\frac{2 \hat{i}+\hat{j}+3 \hat{k}}{\sqrt{14}}$ then find the value of $(2 \vec{a}+\vec{b}) \cdot[(\vec{a} \times \vec{b}) \times(\vec{a}-2 \vec{b})]$

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15. Let $\vec{a}=-\hat{i}-\hat{k}, \vec{b}=-\hat{i}+\hat{j}$ and $\vec{c}=i+2 \hat{j}+3 \hat{k}$ be three given vectors. If $\vec{r}$ is a vector such that $\vec{r} \times \vec{b}=\vec{c} \times \vec{b}$ and $\vec{r} . \vec{a}=0$ then find the value of $\vec{r} . \vec{b}$.

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16. If $\vec{a}, \vec{b}$ and $\vec{c}$ are unit vectors satisfying
$|\vec{a}-\vec{b}|^{2}+|\vec{b}-\vec{c}|^{2}+|\vec{c}-\vec{a}|^{2}=9$ then find the value of $|2 \vec{a}+5 \vec{b}+5 \vec{c}|$.

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17. Let $\vec{a}, \vec{b}$, and $\vec{c}$ be three non-coplanar ubit vectors such the angle between every pair of them is $\frac{\pi}{3}$. if $\vec{a} \times \vec{b}+\vec{b} \times \vec{c}=p \vec{a}+q \vec{b}+r \vec{c}$, where $\mathrm{p}, \mathrm{q}$ and r are scalars, then the value of $\frac{p^{2}+2 q^{2}+r^{2}}{q^{2}}$ is

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## Subjective type

1. from a point $O$ inside a triangle $A B C$, perpendiculars, $O D, O E$ and $O F$ are drawn to the sides, $B C, C A$ and $A B$ respectively, prove that the perpendiculars from $\mathrm{A}, \mathrm{B}$ and C to the sides $\mathrm{EF}, \mathrm{FD}$ and DE are concurrent.

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2. $A_{1}, A_{2}, \ldots . A_{n}$ are the vertices of a regular plane polygon with $n$ sides and $O$ ars its centre. Show that $\sum_{i=1}^{n-1}\left(\overrightarrow{O A_{i}} \times \overrightarrow{O A_{i+1}}\right)=(n-1)\left(\overrightarrow{O A_{1}} \times \overrightarrow{O A_{2}}\right)$
3. If c is a given non-zero scalar, and $\vec{A}$ and $\vec{B}$ are given non- zero, vectors such that $\vec{A} \perp \vec{B}$. Then find vector, $\vec{X}$ which satisfies the equations $\vec{A} \cdot \vec{X}=c$ and $\vec{A} \times \vec{X}=\vec{B}$.

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4. $A, B, C a n d D$ are any four points in the space, then prove that $|\vec{A} B \times \vec{C} D+\vec{B} C \times \vec{A} D+\vec{C} A \times \vec{B} D|=4$ (area of $A B C$. )

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5. If vectors $\vec{a}, \vec{b}$ and $\vec{c}$ are coplanar, show that $\left|\begin{array}{lll}\vec{a} & \vec{b} & \vec{c} \\ \vec{a} \cdot \vec{a} & \vec{a} \cdot \vec{b} & \vec{a} \cdot \vec{c} \\ \vec{b} \cdot \vec{a} & \vec{b} \cdot \vec{b} & \vec{b} \cdot \vec{c}\end{array}\right|=\overrightarrow{0}$
6. $\vec{A}=(2 \vec{i}+\vec{k}), \vec{B}=(\vec{i}+\vec{j}+\vec{k})$ and $\vec{C}=4 \vec{i}-\overrightarrow{3} j+7 \vec{k}$ determine a $\vec{R}$ satisfying $\vec{R} \times \vec{B}=\vec{C} \times \vec{B}$ and $\vec{R} \cdot \vec{A}=0$

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7. Determine the value of $c$ so that for the real $x$, vectors $c x \hat{i}-6 \hat{j}-3 \hat{k}$ and $x \hat{i}+2 \hat{j}+2 c x \hat{k}$ make an obtuse angle with each other .

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8. 

Prove
that:
$(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d})+(\vec{a} \times \vec{c}) \times(\vec{d} \times \vec{b})+(\vec{a} \times \vec{d}) \times(\vec{b} \times \vec{c})=-2[\vec{b} \vec{c} \vec{d}] \vec{a}$

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9. The position vectors of the vertices $A, B$ and $C$ of a tetrahedron $A B C D$ are $\hat{i}+\hat{j}+\hat{k}, \hat{k}, \hat{i}$ and $\hat{3} i$,respectively. The altitude from vertex D to the
opposite face $A B C$ meets the median line through Aof triangle $A B C$ at a point $E$. If the length of the side $A D$ is 4 and the volume of the tetrahedron is $2 \sqrt{ } 2 / 3$, find the position vectors of the point $E$ for all its possible positions

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10. Let $\vec{a}, \vec{b}$ and $\vec{c}$ be non-coplanar unit vectors, equally inclined to one another at an angle $\theta$. If $\vec{a} \times \vec{b}+\vec{b} \times \vec{c}=p \vec{a}+q \vec{b}+r \vec{c}$, find scalars $p, q$ and $r$ in terms of $\theta$.

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11. If $\vec{a}, \vec{b}, \vec{c}$ are vectors such that $|\vec{b}|=|\vec{c}|$ then $\{(\vec{a}+\vec{b}) \times(\vec{a}+\vec{c})\} \times(\vec{b} \times \vec{c}) \cdot(\vec{b}+\vec{c})=$

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12. For any two vectors $\vec{u}$ and $\vec{v}$ prove that $\left(1+|\vec{u}|^{2}\right)\left(1+|\vec{v}|^{2}\right)=(1-\vec{u} . \vec{v})^{2}+|\vec{u}+\vec{v}+(\vec{u} \times \vec{v})|^{2}$

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13. Let $\vec{u}$ and $\vec{v}$ be unit vectors. If $\vec{w}$ is a vector such that $\vec{w}+\vec{w} \times \vec{u}=\vec{v}$, then prove that $|(\vec{u} \times \vec{v}) . \vec{w}| \leq \frac{1}{2}$ and that the equality holds if and only if $\vec{u}$ is perpendicular to $\vec{v}$.

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14. Find 3-dimensional vectors $\vec{v}_{1}, \vec{v}_{2}, \vec{v}_{3} \quad$ satisfying $\vec{v}_{1} \cdot \vec{v}_{1}=4, \vec{v}_{1} \cdot \vec{v}_{2}=-2, \vec{v}_{1} \cdot \vec{v}_{3}=6$, $\vec{v}_{2} \cdot \vec{v}_{2}=2, \vec{v}_{2} \cdot \vec{v}_{3}=-5, \vec{v}_{3} \cdot \vec{v}_{3}=29$

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15. Let V be the volume of the parallelepied formed by the vectors,
$\vec{a}=a_{1} \hat{i}=a_{2} \hat{j}+a_{3} \hat{k}, \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $\vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k} . \quad$ if $a_{r} b_{r}$ nadc $c_{r}$ are non- negative real numbers and 3
$\sum_{r=1}\left(a_{r}+b_{r}+c_{r}\right)=3 L$ show that $V \leq L^{3}$

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16. $\vec{u}, \vec{v}$ and $\vec{w}$ are three nono-coplanar unit vectors and $\alpha, \beta$ and $\gamma$ are the angles between $\vec{u}$ and $\vec{u}, \vec{v}$ and $\vec{w}$ and $\vec{w}$ and $\vec{u}$, respectively and $\vec{x}, \vec{y}$ and $\vec{z}$ are unit vectors along the bisectors of the angles $\alpha, \beta$ and $\gamma$. respectively, prove that $[\vec{x} \times \vec{y} \vec{y} \times \vec{z} \vec{z} \times \vec{x})=\frac{1}{16}[\vec{u} \vec{v} \vec{w}]^{2} \frac{\sec ^{2} \alpha}{2} \frac{\sec ^{2} \beta}{2} \frac{\sec ^{2} \gamma}{2}$.

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17. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{d}$ ar distinct vectors such that

$$
\begin{aligned}
& \vec{a} \times \vec{c}=\vec{b} \times \vec{d} \text { and } \vec{a} \times \vec{b}=\vec{c} \times \vec{d} . \\
& (\vec{a} \times \vec{d}) \cdot(\vec{b} \cdot \vec{c}) \neq 0, \text { i.e. }, \vec{a} \cdot \vec{b}+\vec{d} \cdot \vec{c} \neq \vec{d} \cdot \vec{b}+\vec{a} . \vec{c} .
\end{aligned}
$$

Prove
that

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18. $P_{1} n d P_{2}$ are planes passing through origin $L_{1} a n d L_{2}$ are two lines on $P_{1}$ and $P_{2}$, respectively, such that their intersection is the origin. Show that there exist points $A, B a n d C$, whose permutation $A^{\prime}, B^{\prime}$ and $C^{\prime}$, respectively, can be chosen such that $A$ is on $L_{1}, B o n P_{1}$ but not on $L_{1}$ andC not on $P_{1} ; A^{\prime}$ is on $L_{2}, B^{\prime}$ on $P_{2}$ but not on $L_{2}$ and $C^{\prime}$ not on $P_{2}$

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19. about to only mathematics

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## fill in the blanks

1. Let $\vec{A}, \vec{B}$ and $\vec{C}$ be vectors of legth, 3,4 and 5 respectively. Let $\vec{A}$ be perpendicular to $\vec{B}+\vec{C}, \vec{B}$ to $\vec{C}+\vec{A}$ and $\vec{C}$ to $\vec{A}+\vec{B}$ then the length of vector $\vec{A}+\vec{B}+\vec{C}$ is $\qquad$ .

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2. The unit vector perendicular to the plane determined by $P(1,-1,2)$ , $\mathrm{C}(3,-1,2)$ is $\qquad$ .

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3. The area of the triangle whose vertices are $\mathrm{A}(1,-1,2), \mathrm{B}(1,2,-1), \mathrm{C}(3,-1$,
2) is $\qquad$ .

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4. If $\vec{A}, \vec{B}$ and $\vec{C}$ are three non - coplanar vectors, then
$\vec{A} \cdot \vec{B} \times \vec{C}$ $\vec{B} \cdot \vec{A} \times \vec{C}$
$\vec{C} \times \vec{A} \cdot \vec{B} \quad \vec{C} \cdot \vec{A} \times \vec{B}$
$\qquad$

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5. If $\vec{A}=(1,1,1)$ and $\vec{C}=(0,1,-1)$ are given vectors the vector $\vec{B}$ satisfying the equations $\vec{A} \times \vec{B}=\vec{C}$ and $\vec{A} \cdot \vec{B}=3$ is $\qquad$ .

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6. Let $\vec{b}=4 \hat{i}+3 \hat{j}$ and $\vec{c}$ be two vectors perpendicular to each other in the xy - plane. All vectors in the sme plane having projections 1 and 2 along $\vec{b}$ and $\vec{c}$, respectively, are given by $\qquad$

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7. The components of a vector $\vec{a}$ along and perpendicular to a non-zero vector $\vec{b}$ are $\qquad$ and $\qquad$ , respectively.

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8. A unit vector coplanar with $\vec{i}+\vec{j}+2 \vec{k}$ and $\vec{i}+2 \vec{j}+\vec{k}$ and perpendicular to $\vec{i}+\vec{j}+\vec{k}$ is $\qquad$

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9. A non vector $\vec{a}$ is parallel to the line of intersection of the plane determined by the vectors $\vec{i}, \vec{i}+\vec{j}$ and thepane determined by the vectors $\vec{i}-\vec{j}, \vec{i}+\vec{k}$ then angle between $\vec{a}$ and $\vec{i}-2 \vec{j}+2 \vec{k}$ is $=$ (A) $\frac{\pi}{2}$ (B) $\frac{\pi}{3}$ (C) $\frac{\pi}{6}$ (D) $\frac{\pi}{4}$

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10. Find a unit vector perpendicular to each of the vector $\vec{a}+\vec{b}$ and $\vec{a}-\vec{b}$, where $\vec{a}=3 \hat{i}+2 \hat{j}+2 \hat{k}$ and $\vec{b}=\hat{i}+2 \hat{j}-2 \hat{k}$

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11. let $\vec{a}, \vec{b}$ and $\vec{c}$ be three vectors having magnitudes 1,1 and 2 , respectively, if $\vec{a} \times(\vec{a} \times \vec{c})+\vec{b}=\overrightarrow{0}$, then the acute angle between $\vec{a}$ and $\vec{c}$ is $\qquad$

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12. A, B C and D are four points in a plane with position vectors, $\vec{a}, \vec{b} \vec{c}$ and $\vec{d}$ respectively, such that $(\vec{a}-\vec{d}) \cdot(\vec{b}-\vec{c})=(\vec{b}-\vec{d}) \cdot(\vec{c}-\vec{a})=0$ then point D is the ___ of triangle $A B C$.

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13. Let $\overrightarrow{O A}=\vec{a}, \overrightarrow{O B}=10 \vec{a}+2 \vec{b}$ and $\overrightarrow{O C}=\vec{b}$ where, $\mathrm{O}, \mathrm{A}$ and C are noncollinear points. Let $p$ denote that area of the quadrilateral OABC. And let $q$ denote the area of the parallelogram with $O A$ and $O C$ as adjacent sides. If $p=k q$, then $k=$ $\qquad$

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14. If $\vec{a}=\hat{j}+\sqrt{3} \hat{k}=-\hat{j}+\sqrt{3} \hat{k}$ and $\vec{c}=2 \sqrt{3} \hat{k}$ form a triangle, then the internal angle of the triangle between $\vec{a}$ and $\vec{b}$ is

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## True and false

1. Let $\vec{A}, \vec{B}$ and $\vec{C}$ be unit vectors such that $\vec{A} \cdot \vec{B}=\vec{A} \cdot \vec{C}=0$ and the angle between $\vec{B}$ and $\vec{C}$ be $\pi / 3$. Then $\vec{A}= \pm 2(\vec{B} \times \vec{C})$.

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2. If $\vec{X} . \vec{A}=0, \vec{X} . \vec{B}=0$ and $\vec{X} . \vec{C}=0$ for some non-zero vector $\vec{x} 1$, then[vecA vecB vecC] $=0$ `

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3. for any three vectors, $\vec{a}, \vec{b}$ and $\vec{c},(\vec{a}-\vec{b}) \cdot(\vec{b}-\vec{c}) \times(\vec{c}-\vec{a})=$

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## single correct answer type

1. The scalar $\vec{A} .(\vec{B} \cdot \vec{C}) \times(\vec{A}+\vec{B}+\vec{C})$ equals
A. 0
B. $[\vec{A} \vec{B} \vec{C}]+[\vec{B} \vec{C} \vec{A}]$
c. $[\vec{A} \vec{B} \vec{C}]$
D. none of these

## Answer: a

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2. For non-zero vectors $\vec{a}, \vec{b}$ and $\vec{c},|(\vec{a} \times \vec{b}) \cdot \vec{c}|=|\vec{a}||\vec{b}||\vec{c}|$ holds if and only if
A. $\vec{a} \cdot \vec{b}=0, \vec{b} \cdot \vec{c}=0$
B. $\vec{b} \cdot \vec{c}=0, \vec{c}, \vec{a}=0$
C. $\vec{c} \cdot \vec{a}=0, \vec{a}, \vec{b}=0$
D. $\vec{a} \cdot \vec{b}=\vec{b} \cdot \vec{c}=\vec{c} \cdot \vec{a}=0$

Answer: d
3. The volume of he parallelepiped whose sides are given by $\vec{O} A=2 i-2, j, \vec{O} B=i+j-k a n d \vec{O} C=3 i-k$ is a. $4 / 13 \mathrm{~b} .4 \mathrm{c} \cdot 2 / 7 \mathrm{~d} .2$
A. $4 / 13$
B. 4
C. $2 / 7$
D. 2

## Answer: d

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4. Let $\vec{a}, \vec{b}, \vec{c}$ be three noncolanar vectors and $\vec{p}, \vec{q}, \vec{r}$ are vectors defined
by the relations $\vec{p}=\frac{\vec{b} \times \vec{c}}{[\vec{a} \vec{c}]}, \vec{q}=\frac{\vec{c} \times \vec{a}}{[\vec{a} \vec{c}]}=\frac{\vec{a} \times \vec{b}}{[\vec{b} \vec{c}]}$ then the value of $[\vec{a} \vec{b} \vec{c}] \quad[\vec{a} \vec{b} \vec{c}] \quad[\vec{a} \vec{b} \vec{c}]$
the expression $(\vec{a}+\vec{b}) \cdot \vec{p}+(\vec{b}+\vec{c}) \cdot \vec{q}+(\vec{c}+\vec{a}) \cdot \vec{r}$. is equal to (A) 0 (B) 1
(C) 2 (D) 3
A. 0
B. 1
C. 2
D. 3

## Answer: d

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5. Let $\vec{a}=\hat{i}-\hat{j}, \vec{b}=\hat{j}-\hat{k}, \vec{c}=\hat{k}-\hat{i}$. If $\hat{d}$ is a unit vector such that $\vec{a} \cdot \hat{d}=0=[\vec{b} \vec{c} \vec{d}]$ then $\hat{d}$ equals
A. $\pm \frac{\hat{i}+\hat{j}-2 \hat{k}}{\sqrt{6}}$
B. $\pm \frac{\hat{i}+\hat{j}-\hat{k}}{\sqrt{3}}$
C. $\pm \frac{\hat{i}+\hat{j}+\hat{k}}{\sqrt{3}}$
D. $\pm \hat{k}$

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6. If $\vec{a}, \vec{b}$ and $\vec{c}$ are non coplanar and unit vectors such that $\left.\vec{a} \times(\vec{b} \times \vec{c})=\frac{\vec{b}+\vec{c}}{\sqrt{2}}\right)$ then the angle between vea and $\vec{b}$ is (A) $\frac{3 \pi}{4}$ (B) $\frac{\pi}{4}$
(C) $\frac{\pi}{2}$ (D) $\pi$
A. $3 \pi / 4$
B. $\pi / 4$
C. $\pi / 2$
D. $\pi$

Answer: a

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7. Let $\vec{u}, \vec{v}$ and $\vec{w}$ be vectors such that $\vec{u}+\vec{v}+\vec{w}=0$ if $|\vec{u}|=3,|\vec{v}|=4$ and $|\vec{w}|=5$ then $\vec{u} \cdot \vec{v}+\vec{v} \cdot \vec{w}+\vec{w} \cdot \vec{u}$ is
A. 47
B. -25
C. 0
D. 25

Answer: b

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8. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-coplanar vectors, then $(\vec{a}+\vec{b}+\vec{c}) \cdot[(\vec{a}+\vec{b}) \times(\vec{a}+\vec{c})]$ equals
A. 0
B. $[\vec{a} \vec{b} \vec{c}]$
C. $2[\vec{a} \vec{b} \vec{c}]$
D. $-[\vec{a} \vec{b} \vec{c}]$

Answer: d

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9. $\vec{p}, \vec{q}$ and $\vec{r}$ are three mutually prependicular vectors of the same magnitude . If vector $\vec{x}$ satisfies the equation $\vec{p} s \times((\vec{x}-\vec{q}) \times \vec{p})+\vec{q} \times((\vec{x}-\vec{r}) \times \vec{q})+\vec{r} \times((\vec{x}-\vec{p}) \times \vec{r})=\overrightarrow{0}$ then $\vec{x}$ is given by
A. $\frac{1}{2}(\vec{p}+\vec{q}-2 \vec{r})$
B. $\frac{1}{2}(\vec{p}+\vec{q}+\vec{r})$
C. $\frac{1}{3}(\vec{p}+\vec{q}+\vec{r})$
D. $\frac{1}{3}(2 \vec{p}+\vec{q}-\vec{r})$

## Answer: b

10. Let $\vec{a}=2 \hat{i}+\hat{j}+\hat{k}$, and $\vec{b}=\hat{i}+\hat{j}$ if c is a vector such that $\vec{a} \cdot \vec{c}=|\vec{c}|,|\vec{c}-\vec{a}|=2 \sqrt{2}$ and the angle between $\vec{a} \times \vec{b}$ and $\vec{i} s 30^{\circ}$, then $|(\vec{a} \times \vec{b})| \times \vec{c} \mid$ is equal to
A. $2 / 3$
B. $3 / 2$
C. 2
D. 3

## Answer: b

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11. Let $\vec{a}=2 i+j+k, \vec{b}=i+2 j-k$ and $a$ unit vector $\vec{c}$ be coplanar. If $\vec{c}$ is pependicular to $\vec{a}$. Then $\vec{c}$ is
A. $\frac{1}{\sqrt{2}}(-j+k)$
B. $\frac{1}{\sqrt{3}}(i-j-k)$
C. $\frac{1}{\sqrt{5}}(i-2 j)$
D. $\frac{1}{\sqrt{3}}(i-j-k)$

## Answer: a

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12. If the vectors $\vec{a}, \vec{b}$ and $\vec{c}$ form the sides, $B C, C A$ and $A B$, respectively, of triangle $A B C$, then
A. $\vec{a} \cdot \vec{b}+\vec{b} \cdot \vec{c}+\vec{c} \cdot \vec{a}=0$
B. $\vec{a} \times \vec{b}=\vec{b} \times \vec{c}=\vec{c} \times \vec{a}$
C. $\vec{a} \cdot \vec{b}=\vec{b} \cdot \vec{c}=\vec{c} \cdot \vec{a}$
D. $\vec{a} \times \vec{b}+\vec{b} \times \vec{c}+\vec{c} \times \vec{a}=\overrightarrow{0}$

## Answer: b

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13. Let vectors $\vec{a}, \vec{b} \vec{a}$ and $\vec{d}$ be such that $(\vec{a} \times \vec{b}) \times(\vec{c} \times \vec{d})=\overrightarrow{0}$. Let $P_{1}$ and $P_{2}$ be planes determined by the pairs of vectors $\vec{a}, \vec{b}$ and $\vec{c}, \vec{d}$, respectively. Then the angle between $P_{1}$ and $P_{2}$ is
A. 0
B. $\pi / 4$
C. $\pi / 3$
D. $\pi / 2$

## Answer: a

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14. If $\vec{a}, \vec{b}, \vec{c}$ are unit coplanar vectors then the scalar triple product $[2 \vec{a}-\vec{b}, 2 \vec{b}-c, \overrightarrow{2} c-\vec{a}]$ is equal to (A) 0 (B) 1 (C) $-\sqrt{3}$ (D) $\sqrt{3}$
A. 0
B. 1
C. $-\sqrt{3}$
D. $\sqrt{3}$

## Answer: a

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15. if $\hat{a}, \hat{b}$ and $\hat{c}$ are unit vectors. Then $|\hat{a}-\hat{b}|^{2}+|\hat{b}-\hat{c}|^{2}+|\vec{c}-\vec{a}|^{2}$ does not exceed
A. 4
B. 9
C. 8
D. 6

## Answer: b

16. If $\vec{a}$ and $\vec{b}$ are two unit vectors such that $\vec{a}+2 \vec{b}$ and $5 \vec{a}-4 \vec{b}$ are perpendicualar to each other, then the angle between $\vec{a}$ and $\vec{b}$ is
A. $45^{\circ}$
B. $60^{\circ}$
C. $\cos ^{-1}(1 / 3)$
D. $\cos ^{-1}(2 / 7)$

## Answer: b

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17. Let $\vec{V}=2 \hat{i}+\hat{j}-\hat{k}$ and $\vec{W}=\hat{i}+3 \hat{k}$. if $\vec{U}$ is a unit vector, then the maximum value of the scalar triple product $[\vec{U} \vec{V} \vec{W}]$ is
A. -1
B. $\sqrt{10}+\sqrt{6}$
C. $\sqrt{59}$
D. $\sqrt{60}$

## Answer: c

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18. Find the value of a so that the volume of the parallelopiped formed by vectors $\hat{i}+a \hat{j}+\hat{k}, \hat{j}+a \hat{k}$ and $a \hat{i}+\hat{k}$ becomes minimum.
A. -3
B. 3
C. $1 / \sqrt{3}$
D. $\sqrt{3}$

## Answer: c

19. If $\vec{a}=(\hat{i}+\hat{j}+\hat{k}), \vec{a} \cdot \vec{b}=1$ and $\vec{a} \times \vec{b}=\hat{j}-\hat{k}$, then $\vec{b}$ is (a) $\hat{i}-\hat{j}+\hat{k}$ (b) $2 \hat{i}-\hat{k}$ (c) $\hat{i}$ (d) $2 \hat{i}$
A. $\hat{i}-\hat{j}+\hat{k}$
B. $2 \hat{i}-\hat{k}$
c. $\hat{i}$
D. $2 \hat{i}$

## Answer: c

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20. The unit vector which is orthogonal to the vector $5 \hat{i}+2 \hat{j}+6 \hat{k}$ and is coplanar with vectors $2 \hat{i}+\hat{j}+\hat{k}$ and $\hat{i}-\hat{j}+\hat{k}$ is (a) $\frac{2 \hat{i}-6 \hat{j}+\hat{k}}{\sqrt{41}}$ (b) $\frac{2 \hat{i}-3 \hat{j}}{\sqrt{13}}$ (c)

$$
\frac{3 \hat{j}-\hat{k}}{\sqrt{10}} \text { (d) } \frac{4 \hat{i}+3 \hat{j}-3 \hat{k}}{\sqrt{34}}
$$

A. $\frac{2 \hat{i}-6 \hat{j}+\hat{k}}{\sqrt{41}}$
B. $\frac{2 \hat{i}-3 \hat{j}}{\sqrt{13}}$
C. $\frac{3 \hat{i}-\hat{k}}{\sqrt{10}}$
D. $\frac{4 \hat{i}+3 \hat{j}-3 \hat{k}}{\sqrt{34}}$

## Answer: c

## D Watch Video Solution

21. If $\vec{a}, \vec{b}$ and $\vec{c}$ are three non-zero, non- coplanar vectors and
$\vec{b}_{1}=\vec{b}-\frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}, \vec{b}_{2}=\vec{b}+\frac{\vec{b} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}, \vec{c}_{1}=\vec{c}-\frac{\vec{c} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}+\frac{\vec{b} \cdot \vec{c}}{|\vec{c}|^{2}} \vec{b}_{1}$,
$\vec{c}_{2}=\vec{c}-\frac{\vec{c} \cdot \vec{a}}{|\vec{a}|^{2}} \vec{a}-\frac{\vec{b} \vec{c}}{\left|\vec{b}_{1}\right|^{2}} \vec{b}_{1}, \vec{c}_{3}=\vec{c}-\frac{\vec{c} \cdot \vec{a}}{|\vec{c}|^{2}} \vec{a}+\frac{\vec{b} \cdot \vec{c}}{|\vec{c}|^{2}} \vec{b}_{1}$,
$\vec{c}_{4}=\vec{c}-\frac{\vec{c} \cdot \vec{a}}{|\vec{c}|^{2}} \vec{a}=\frac{\vec{b} \cdot \vec{c}^{2}}{|\vec{b}|^{2}} \vec{b}_{1}$, then the set of mutually orthogonal vectors is
A. (a) $\left(\vec{a}, \vec{b}_{1}, \vec{c}_{3}\right)$
B. (b) $\left(\vec{a}, \vec{b}_{1}, \vec{c}_{2}\right)$
C. (c) $\left(\vec{a}, \vec{b}_{1}, \vec{c}_{1}\right)$
D. (d) $\left(\vec{a}, \vec{b}_{2}, \vec{c}_{2}\right)$

## Answer: c

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22. Let $\vec{a}=\hat{i}+2 \hat{j}+\hat{k}, \vec{b}=\hat{i}-\hat{j}+\hat{k}$ and $\vec{c}=\hat{j}-\hat{k}$ A vector in the plane of $\vec{a}$ and $\vec{b}$ whose projections on $\vec{c} i s 1 / \sqrt{3}$ is
A. $4 \hat{i}-\hat{j}+4 \hat{k}$
B. $3 \hat{i}+\hat{j}-3 \hat{k}$
C. $2 \hat{i}+\hat{j}-2 \hat{k}$
D. $4 \hat{i}+\hat{j}-4 \hat{k}$

## Answer: a

23. Let two non-collinear unit vectors $\vec{a}$ and $\vec{b}$ form an acute angle. A point P moves so that at any time t , time position vector, $O P$ ( where O is the origin) is given by $\hat{a}$ cott $+\hat{b}$ sint. When $p$ is farthest fro origing $o$, let $M$ be the length of $O P$ and $\hat{u}$ be the unit vector along $O P$.then
A.,$\hat{u}=\frac{\hat{a}+\hat{b}}{|\hat{a}+\hat{b}|}$ and $M=(1+\hat{a} \cdot \hat{b})^{1 / 2}$
B. , $\hat{u}=\frac{\hat{a}-\hat{b}}{|\hat{a}-\hat{b}|}$ and $M=(1+\hat{a} . \hat{b})^{1 / 2}$
C. $\hat{u}=\frac{\hat{a}+\hat{b}}{|\hat{a}+\hat{b}|}$ and $M=(1+2 \hat{a} . \hat{b})^{1 / 2}$
D. $\hat{u}=\frac{\hat{a}-\hat{b}}{|\hat{a}-\hat{b}|}$ and $M=(1+2 \hat{a} . \hat{b})^{1 / 2}$

## Answer: a

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24. If $\vec{a}, \vec{c}, \vec{c}$ and $\vec{d}$ are unit vectors such that $(\vec{a} \times \vec{b}) \cdot(\vec{c} \times \vec{d})=1$ and $\vec{a} \cdot \vec{b}=\frac{1}{2}$ then
A. $\vec{a}, \vec{b}$ and $\vec{c}$ are non- coplanar
B. $\vec{b}, \vec{c}$ and $\vec{d}$ are non-coplanar
C. $\vec{b}$ and $\vec{d}$ are non- parallel
D. $\vec{a}$ and $\vec{d}$ are parallel and $\vec{b}$ and $\vec{c}$ are parallel

## Answer: c

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25. Two adjacent sides of a parallelogram $A B C D$ are given by $\vec{A} B=2 \hat{i}+10 \hat{j}+11 \hat{k}$ and $\vec{A} D=-\hat{i}+2 \hat{j}+2 \hat{k}$ The side $A D$ is rotated by an acute angle $\alpha$ in the plane of the parallelogram so that $A D$ becomes $A D^{\prime}$ If $A D^{\prime}$ makes a right angle with the side $A B$, then the cosine of the angel $\alpha$ is given by $\frac{8}{9}$ b. $\frac{\sqrt{17}}{9}$ c. $\frac{1}{9}$ d. $\frac{4 \sqrt{5}}{9}$
A. $\frac{8}{9}$
B. $\frac{\sqrt{17}}{9}$
C. $\frac{1}{9}$
D. $\frac{4 \sqrt{5}}{9}$

## Answer: b

## D Watch Video Solution

26. Let $P, Q, R$ and $S$ be the points on the plane with postion vectors $-2 \hat{i}-\hat{j}, 4 \hat{i}, 3 \hat{i}+3 \hat{j}$ and $-3 \hat{j}+2 \hat{j}$, respectively, the quadrilateral PQRS must be a
A. Parallelogram, which is neither a rhombus nor a rectangle
B. square
C. rectangle, but not a square
D. rhombus, but not a square.

## Answer: a

27. Let $\vec{a}=\hat{i}+\hat{j}+\hat{k}, \vec{b}=\hat{i}-\hat{j}+\hat{k}$ and $\vec{c}=\hat{i}-\hat{j}-\hat{k}$ be three vectors. A vectors $\vec{v}$ in the plane of $\vec{a}$ and $\vec{b}$, whose projection on $\vec{c}$ is $\frac{1}{\sqrt{3}}$ is given by
A. $\hat{i}-3 \hat{j}+3 \hat{k}$
B. $-3 \hat{i}-3 \hat{j}+\hat{k}$
C. $3 \hat{i}-\hat{j}+3 \hat{k}$
D. $\hat{i}+3 \hat{j}-3 \hat{k}$

## Answer: c

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28. Let $P R=3 \hat{i}+\hat{j}-2 \hat{k}$ and $S Q=\hat{i}-3 \hat{j}-4 \hat{k}$ determine diagonals of a parallelogram PQRS. And $P T=\hat{i}+2 \hat{j}+3 \hat{k}$ be onther vector. Then the volume of the parallelepiped determined by the vectors $P T, P Q$ and $P S$ is
A. 5
B. 20
C. 10
D. 30

## Answer: c

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## Multiple correct answers type

1. Let $\vec{a}=a_{1} \hat{i}+a_{2} \hat{j}+a_{3} \hat{k}, \vec{b}=b_{1} \hat{i}+b_{2} \hat{j}+b_{3} \hat{k}$ and $\vec{c}=c_{1} \hat{i}+c_{2} \hat{j}+c_{3} \hat{k}$ be three non-zero vectors such that $\vec{c}$ is a unit vector perpendicular to both $\vec{a}$ and $\vec{b}$. If the angle between $\vec{a}$ and $\vec{b} i s \pi / 6$ then the value of

$$
\left|\begin{array}{lll}
a_{1} & b_{1} & c_{1} \\
a_{2} & b_{2} & c_{2} \\
a_{3} & b_{3} & c_{3}
\end{array}\right| \text { is }
$$

A. 0
B. 1
C. $\frac{1}{4}\left(a_{1}^{2}+a_{2}^{2}+a_{2}^{2}\right)\left(b_{1}^{2}+b_{2}^{2}+b_{2}^{2}\right)$
D. $\frac{3}{4}\left(a_{1}^{2}+a_{2}^{2}+a_{2}^{2}\right)\left(b_{1}^{2}+b_{2}^{2}+b_{2}^{2}\right)\left(c_{1}^{2}+c_{2}^{2}+c_{2}^{2}\right)$

## Answer: c

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2. The number of vectors of unit length perpendicular to vectors $\vec{a}=(1,1,0) a n d \vec{b}=(0,1,1)$ is a. one b. two c. three d. infinite
A. one
B. two
C. three
D. infinite

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3. $\vec{a}=2 \hat{i}-\hat{j}+\hat{k}, \vec{b}=\hat{j}+2 \hat{j}-\hat{k}, \vec{c}=\hat{i}+\hat{j}-2 \hat{k}$. A vector coplanar with $\vec{b}$ and $\vec{c}$. Whose projection on $\vec{a}$ is magnitude $\sqrt{\frac{2}{3}}$ is
A. $2 \hat{i}+3 \hat{j}-3 \hat{k}$
B. $2 \hat{i}+3 \hat{j}+3 \hat{k}$
C. $-2 \hat{i}-\hat{j}+5 \hat{k}$
D. $2 \hat{i}+\hat{j}+5 \hat{k}$

## Answer: a,c

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4. For three vectors, $\vec{u}, \vec{v}$ and $\vec{w}$ which of the following expressions is not equal to any of the remaining three?
A. $\vec{u} .(\vec{v} \times \vec{w})$
B. $(\vec{v} \times \vec{w}) \cdot \vec{u}$
C. $\vec{v} \cdot(\vec{u} \times \vec{w})$
D. $(\vec{u} \times \vec{v}) \cdot \vec{w}$

## Answer: c

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5. Which of the following expressions are meaningful? $\vec{u} \cdot(\vec{v} \times \vec{w})$ b. $(\vec{u} \cdot \vec{v}) \cdot \vec{w} \mathrm{c} \cdot(\vec{u} \cdot \vec{v}) \cdot \vec{w} \mathrm{~d} \cdot \vec{u} \times(\vec{v} \cdot \vec{w})$
A. $\vec{u} .(\vec{v} \times \vec{w})$
B. $(\vec{u} \cdot \vec{v}) \cdot \vec{w}$
C. $(\vec{u} \cdot \vec{v}) \vec{w}$
D. $\vec{u} \times(\vec{v} . V e c w)$

## Answer: a,c

6. If $\vec{a}, \vec{b}, \vec{c}$ are non-coplanar vectors and $\vec{u}$ and $\vec{v}$ are any two vectors.

Prove that $\vec{u} \times \vec{v}=\frac{1}{[\vec{a} \vec{b} \vec{c}]}\left|\begin{array}{lll}\vec{u} \cdot \vec{a} & \vec{v} \cdot \vec{a} & \vec{a} \\ \vec{u} \cdot \vec{b} & \vec{v} \cdot \vec{b} & \vec{b} \\ \vec{u} \cdot \vec{c} & \vec{v} \cdot \vec{c} & \vec{c}\end{array}\right|$
A. $|\vec{u}|+\vec{u} .(\vec{a} \times \vec{b})$
B. $|\vec{u}|+|\vec{u} \cdot \vec{a}|$
C. $|\vec{u}|+|\vec{u} . \vec{b}|$
D. $|\vec{u}|+\vec{u} \cdot(\vec{a}+\vec{b})$

## Answer: a,c

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7. Vector $\frac{1}{3}(2 \hat{i}-2 \hat{j}+\hat{k})$ is
A. a unit vector
B. makes an angle $\pi / 3$ with vector $(2 \hat{i}-4 \hat{j}+3 \hat{k})$
C. parallel to vector $\left(-\hat{i}+\hat{j}-\frac{1}{2} \hat{k}\right)$
D. perpendicular to vector $3 \hat{i}+2 \hat{j}-2 \hat{k}$

## Answer: a,c,d

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8. Let $\vec{A}$ be a vector parallel to the line of intersection of planes $P_{1}$ and $P_{2}$
Plane
$P_{1}$
is parallel
to vectors
$2 \hat{j}+3 \hat{k}$ and $4 \hat{j}-3 \hat{k} n a d P_{2}$ is parallel to $\hat{j}-\hat{k}$ and $3 \hat{i}+3 \hat{j}$. Then the angle between vector $\vec{A}$ and a given vector $2 \hat{i}+\hat{j}-2 \hat{k}$ is
A. $\pi / 2$
B. $\pi / 4$
C. $\pi / 6$
D. $3 \pi / 4$

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9. The vector(s) which is /are coplanar with vectors $\hat{i}+\hat{j}+2 \hat{k}$ and $\hat{i}+2 \hat{j}+\hat{k}$ and perpendicular to vector $\hat{i}+\hat{j}+\hat{k}$, is /are
A. $\hat{j}-\hat{k}$
B. $-\hat{i}+\hat{j}$
C. $\hat{i}-\hat{j}$
D. $-\hat{j}+\hat{k}$

## Answer: a,d

## D Watch Video Solution

10. Let $\vec{x}, \vec{y}$ and $\vec{z}$ be three vectors each of magnitude $\sqrt{2}$ and the angle between each pair of them is $\frac{\pi}{3}$ if $\vec{a}$ is a non-zero vector perpendicular
to $\vec{x}$ and $\vec{y} \times \vec{z}$ and $\vec{b}$ is a non-zero vector perpendicular to $\vec{y}$ and $\vec{z} \times \vec{x}$, then
A. $\vec{b}=(\vec{b} \cdot \vec{z})(\vec{z}-\vec{x})$
B. $\vec{a}=(\vec{a} \cdot \vec{y})(\vec{y}-\vec{z})$
C. $\vec{a} \cdot \vec{b}=-(\vec{a} \cdot \vec{y})(\vec{b} \cdot \vec{z})$
D. $\vec{a}=(\vec{a} \cdot \vec{y})(\vec{z}-\vec{y})$

## Answer: a,b,c

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11. Let
$P Q R$ be
a triangle
Let
$\vec{a}=Q R, \vec{b}=R P$ and $\vec{c}=P Q$. if $|\vec{a}|=12,|\vec{b}|=4 \sqrt{3}$ and $\vec{b} . \vec{c}=24$ then which of the following is (are) true?
A. $\frac{|\vec{c}|^{2}}{2}-|\vec{a}|=12$
B. $\frac{|\vec{c}|^{2}}{2}-|\vec{a}|=30$
C. $|\vec{a} \times \vec{b}+\vec{c} \times \vec{a}|=48 \sqrt{3}$
D. $\vec{a} \cdot \vec{b}=-72$

Answer: a,c,d

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