



MATHS

BOOKS - CENGAGE MATHS (ENGLISH)

DIFFERENTIAL EQUATIONS

ILLUSTRATIONS

1. Find the order and degree of the following differential equations. i) $\frac{dy}{dx} + y = \frac{1}{\frac{dy}{dx}}, \text{ ii) } \frac{e^{e^3y}}{dx^3} - x\frac{d^2y}{dx^2} + y = 0 \text{ , iii) } \frac{\sin^{-1}(dy)}{dx} = x + y \text{, iv)}$ $\frac{\log_e(dy)}{dx} = ax + by$ $\text{v) } y\frac{d^2y}{dx^2} + x\left(\frac{dy}{dx}\right)^2 - 4y\frac{dy}{dx} = 0$

2. Form the differential equation of family of lines concurrent at the

origin.

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3. Form the differential equation of all circle touching the x-axis at the origin and centre on the y-axis.

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4. Form the differential equation of family of lines situated at a constant

distance p from the origin.



5. From the differential equation of the family of parabolas with focus at the origin and axis of symmetry along the x-axis. Find the order and

degree of the differential equation.



7. Form the differential equation of the family curves having equation $y = \left(\sin^{-1}x\right)^2 + A\cos^{-1}x + B.$

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8. What is the order of the differential equation whose general solution is

$$y=c_1\cos 2x+c_2\sin^2 x+c_3\cos^2 x+c_4e^{2x}+c_5e^{2x+c_6}$$

9. Find the particular solution of the differential equation $(1+e^{2x})dy+(1+y^2)e^xdx=0,$ given that y=1 when x=0.

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10. Solve
$$\log\left(\frac{dy}{dx}\right) = 4x - 2y - 2$$
 , given that $y = 1$ when $x = 1$.

11. Solve the differential equation
$$xy\frac{dy}{dx} = \frac{1+y^2}{1+x^2}(1+x+x^2)$$

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12. Solve the following differential equation:
 $\sqrt{1+x^2+y^2+x^2y^2} + xy\frac{dy}{dx} = 0$
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13. Solve
$$rac{d^2y}{dx^2}=\left(rac{dy}{dx}
ight)^2$$

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14. Solve
$$rac{dy}{dx}=\left(x+y
ight)^2$$

15. Solve :
$$rac{dy}{dx}\sqrt{1+x+y}=x+y-1$$

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16. Show that the differential equation $(x^2 + xy)dy = (x^2 + y^2)dx$ is homogenous and solve it.



17. Show that the given differential equation $xdy - ydx = \sqrt{x^2 + y^2} \; \mathsf{dx}$

is homogenous and solve it.

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18. Solve
$$x \sin\left(rac{y}{x}
ight) dy = \Big(y \sin\left(rac{y}{x}
ight) - x\Big) dx.$$

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19. Solve
$$\Big(1+e^{rac{x}{y}}\Big)dx+e^{rac{x}{y}}igg(1-rac{x}{y}igg)dy=0$$

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20. Solve
$$xdy = \left(y + x rac{f\left(rac{y}{x}
ight)}{f^{\,\prime}\left(rac{y}{x}
ight)}
ight)dx$$

21. Find the real value of m for which the substitution $y = u^m$ will transform the differential equation $2x^4y\frac{dy}{dx} + y^4 = 4x^6$ in to a homogeneous equation.

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22. Solve
$$\displaystyle rac{dy}{dx} = \displaystyle rac{x+2y+3}{2x+3y+4}$$

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23. Solve the differential equation $: xdy + ydx + rac{xdy - ydx}{x^2 + y^2} = 0$

24. Solve:

$$\Big[(x+1)rac{y}{x}+\sin y\Big]dx+[x+\log_e x+x\cos y]$$
dy

25. Solve:
$$(x\cos x - \sin x)dx = rac{x}{y}{\sin x}dy$$

26. Solve:
$$y^4 dx + 2xy^3 dy = rac{y dx - x dy}{x^3 y^3}$$

27. Solve:

$$rac{dy}{dx} = rac{yf'(x)-y^2}{f(x)}$$



28. Solve the differential equation $y e^{rac{x}{y}} dx = \Big(x e^{rac{x}{y}} + y^2 \sin y\Big) dy (y
eq 0)$

29. Solve
$$\displaystyle rac{dy}{dx} = \displaystyle rac{x-2y+5}{2x+y-1}$$

30. Solve
$$\displaystyle rac{x+yrac{dy}{dx}}{y-xrac{dy}{dx}} = x^2+2y^2+rac{y^4}{x^2}$$

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$$1igg(rac{1}{y}rac{\sin x}{y}-rac{y}{x^2}rac{\cos y}{x}+1igg)dx+igg(rac{1}{x}rac{\cos y}{x}-rac{x}{y^2}rac{\sin y}{x}+rac{1}{y^2}igg)dy=0$$

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32. Solve
$$x^2 igg(rac{dy}{dx} igg) + y = 1$$

33. Solve:

 $ydx - xdy + \log xdx = 0$



35. Solve :
$$ig(x+2y^3ig)rac{dy}{dx}=y$$

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36. Solve the differential equation: $ig(1+y^2ig)rac{dx}{dy}+x=e^{ an^{-1}y}$

37. Let u(x) and v(x) satisfy the differential equation $\frac{du}{dx} + p(x)u = f(x)$ and $\frac{dv}{dx} + p(x)v = g(x)$ are continuous functions. If $u(x_1)$ for some x_1 and f(x) > g(x) for all $x > x_1$, prove that any point (x, y), where $x > x_1$, does not satisfy the equations y = u(x) and y = v(x).

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38. Solve
$$\left(rac{dy}{dx}
ight)+\left(rac{y}{x}
ight)=y^3$$

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39. Solve
$$\left(rac{dy}{dx}
ight)=e^{x-y}(e^x-e^y)\cdot$$

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40. Solve
$$(x-1)dy + ydx = x(x-1)y^{rac{1}{3}}dx$$
.





42. The slope of a curve, passing through (3,4) at any point is the reciprocal of twice the ordinate of that point. Show that it is parabola.

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43. Find the equation of a curve passing through the point (0, 2) given that the sum of the coordinates of any point on the curve exceeds the magnitude of the slope of the tangent to the curve at that point by 5.

44. Find the curve passing through (2, 1) and which has a constant subtangent equal to 2.



45. If length of tangent at any point on th curve y = f(x) intercepted between the point and the x-axis is of length 1. Find the equation of the curve.

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46. A curve passing through the point (1,1) has the porperty that the perpendicular distance of the normal at any point P on the curve from the origin is equal to the distance of P from x-axis Determine the equation of the curve.

47. Find the equation of the curve such that the portion of the x-axis cut off between the origin and the tangent at a point is twice the abscissa and which passes through the point (1,2).

48. Find the equation of the curve passing through the point, (5,4) if the sum of reciprocal of the intercepts of the normal drawn at any point P(x,y) on it is 1.

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49. Find the equation of the curve passing through the origin if the middle point of the segment of its normal from any point of the curve to the x-axis lies on the parabola $2y^2 = x$.





51. Find the orthogonal trajectory of $y^2 = 4ax$ (a being the parameter).



52. The population of a certain is known to increase at a rate proportional to the number of people presently living in the country. If after two years the population has doubled, and after three years the population is 20,000 estimates the number of people initially living in the country.



53. What constant interest rate is required if an initial deposit placed into an account accrues interest compounded continuously is to double its value in six years? $(\ln |x| = 0.6930)$



54. Suppose that a mothball loses volume by evaporation at a rate proportional to its instantaneous area. If the diameter of the ball decreases from 2cm to 1cm in 3 months, how long will it take until the ball has practically gone?



55. A body at a temperature of $50^0 F$ is placed outdoors where the temperature is $100^0 F$. If the rate of change of the temperature of a body is proportional to the temperature difference between the body and its surrounding medium. If after 5 min the temperature of the body is $60^0 F$,

find (a) how long it will take the body to reach a temperature of 75^0 F and (b) the temperature of the body after 20 min.

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56. Find the time required for a cylindrical tank of radius r and height H to empty through a round hole of area a at the bottom. The flow through the hole is according to the law $v(t) = k\sqrt{2gh(t)}$, where v(t) and h(t), are respectively, the velocity of flow through the hole and the height of the water level above the hole at time t, and g is the acceleration due to gravity.

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57. A country has a food deficit of 10%. Its population grows continuously at a rate of 3% per year. Its annual food production every year is 4% more than that of the last year. Assuming that the average food requirement per person remains constant, prove that the country

will become self-sufficient in food after n years, where n is the smallest integer bigger than or equal to $\frac{\ln 10 - \ln 9}{\ln(1.04) - 0.03}$

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58. A hemi-spherical tank of radius 2 m is initially full of water and has an outlet of $12cm^2$ cross-sectional area at the bottom. The outlet is opened at some instant. The flow through the outlet is according to the law $v(t) = 0.6\sqrt{2gh(t)}$, where v(t) and h(t) are, respectively, the velocity of the flow through the outlet and the height of water level above the outlet and the height of water level above the outlet at time t, and g is the acceleration due to gravity. Find the time it takes to empty the tank.

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EXAMPLES

1. Solve
$$\displaystyle rac{x+yrac{dy}{dx}}{y-xrac{dy}{dx}} = x^2+2y^2+rac{y^4}{x^2}$$

2. Solve :

$$\Big\{x\cos\Big(rac{y}{x}\Big)+y\sin\Big(rac{y}{x}\Big)\Big\}ydx=\Big\{y\sin\Big(rac{y}{x}\Big)-x\cos\Big(rac{y}{x}\Big)\Big\}xdy$$

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3. Solve
$$\displaystyle rac{dy}{dx} = \displaystyle rac{\left(x+y
ight)^2}{(x+2)(y-2)}$$

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4. Solve
$$y \left(\frac{dy}{dx} \right)^2$$

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5. If
$$y+rac{d}{dx}(xy)=x(\sin x+\log x)$$
, find $y(x)$.

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6. If
$$\int_a^x ty(t)dt = x^2 + y(x), ext{ then find } y(x)$$

7. Given a function 'g' which has a derivative g'(x) for every real x and satisfies g'(0) = 2 and $g(x + y) = e^y g(x) + e^y g(y)$ for all x and y then: Find g(x).

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8. Solve
$$rac{dy}{dx} = rac{\sin y + x}{\sin 2y - x \cos y}$$

9. Solve:

$$rac{dy}{dx} + rac{3y}{x} = g(x)$$
, where $g(x) = \begin{cases} 1 & ext{if } 0 \le x \le 1 \\ rac{1}{x} & ext{if } x > 1 \end{cases}$
 $yigg(rac{1}{2}igg) = rac{1}{8}$ and $y(x)$ is continous on $[0,\infty]$.

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10. Solve: $(x\cos y - y\sin y)dy + (x\sin y + y\cos y)dx = 0$

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11. If y_1 and y_2 are the solution of the differential equation $\frac{dy}{dx} + Py = Q$, where P and Q are functions of x alone and $y_2 = y_1 z$, then prove that $z = 1 + \cdot e^{-f\frac{Q}{y_1}dx}$, where c is an arbitrary constant.

12. If y_1 and y_2 are two solutions to the differential equation $\frac{dy}{dx} + P(x)y = Q(x)$. Then prove that $y = y_1 + c(y_1 - y_2)$ is the general solution to the equation where c is any constant.

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13. Let $f(x), x \ge 0$, be a non-negative continuous function, and let $f(x) = \int_0^x f(t)dt, x \ge 0$, if for some $c > 0, f(x) \le cF(x)$ for all $x \ge 0$, then show that f(x) = 0 for all $x \ge 0$.

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14. Find a pair of curves such that (a) the tangents drawn at points with equal abscissas intersect on the y-axis. (b) the normal drawn at points with equal abscissas intersect on the x-axis. (c) one curve passes through (1,1) and other passes through (2, 3).

15. Given two curves: y = f(x) passing through the point (0, 1) and $g(x) = \int_{-\infty}^{x} f(t)dt$ passing through the point $\left(0, \frac{1}{n}\right)$. The tangents drawn to both the curves at the points with equal abscissas intersect on the x-axis. Find the curve y = f(x).

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16. A cyclist moving on a level road at 4 m/s stops pedalling and lets the wheels come to rest. The retardation of the cycle has two components: a constant 0.08 m/s^2 due to friction in the working parts and a resistance of 0. $02v^2/m$, where v is speed in meters per second. What distance is traversed by the cycle before it comes to rest? (consider 1n 5=1.61).

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17. The force of resistance encountered by water on a motor boat of mass m going in still water with velocity v is proportional to the velocity v. At t=0 when its velocity is v_0 , then engine shuts off. Find an expression

for the position of motor boat at time t and also the distance travelled by the boat before it comes to rest. Take the proportionality constant as k > 0.

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18. *A* and *B* are two separate reservoirs of water. Capacity of reservoir *A* is double the capacity of reservoir *B*. Both the reservoirs are filled completely with water, their inlets are closed and then the water is released simultaneously from both the reservoirs. The rate of flow of water out of each reservoir at any instant of time is proportional to the quantity of water in the reservoir at the time. One hour after the water is released, the quantity of water is reservoir *A* is $1\frac{1}{2}$ times the quantity of water in reservoir *B*. After how many hours do both the reservoirs have the same quantity of water?

1. Find the order and degree (if defined) of the following differential

equations:

$$rac{d^2y}{dx^2} = \left\{1+\left(rac{dy}{dx}
ight)^4
ight\}^{5/3}$$

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2. Find the order and degree (if defined) of the equation:
$$\frac{d^3y}{dx^3} = x \ln \left(\frac{dy}{dx} \right)$$

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$$\mathbf{3.}\left(rac{d^4y}{dx^4}
ight)^3+3igg(rac{d^2y}{dx^2}igg)^6+\sin x=2\cos x$$

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4. Find the order and degree (if defined) of the equation:

$$\left(\frac{d^3y}{dx^3}\right)^{\frac{2}{3}} + 4 - 3\frac{d^2}{dx^2} + 5\frac{dy}{dx} = 0$$

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5. Find the order and degree (if defined) of the equation:

$$a = \frac{1\left[1 + \left(\frac{dy}{dx}\right)^2\right]^{\frac{3}{2}}}{\frac{d^2y}{dx^2}}, \text{ where } a \text{ is constant}$$

6. Find the order and degree (if defined) of the equation: $\frac{d^4y}{dx^4} - \sin\left(\frac{d^3y}{dx^3}\right) = 0$

CONCEPT APPLICATION EXERCISES 10.2

1. Find the differential equation of All-horizontal lines in a plane. All non-

vertical lines in a plane.

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2. Form the differential equation of family of circles having center at origin.

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3. Find the differential equation of all parabolas whose axes are parallel

to the x-axis an having latus rectum a.





5. The degree of the differential equation satisfying the relation

$$\sqrt{1+x^2}+\sqrt{1+y^2}=\lambdaigg(x\sqrt{1+y^2}-y\sqrt{1+x^2}igg)$$
 is

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6. Find the differential equation whose general solution is given by $y = (c_1 + c_2)\cos(x + c_3) - c_4e^{x+c_5}$, where c_1, c_2, c_3, c_4, c_5 are arbitary constants.

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CONCEPT APPLICATION EXERCISES 10.3

1. Solve
$$e^{rac{dy}{dx}}=x+1,\,$$
 given that when $x=0,\,y=3.$

2. Solve
$$ig(x-y^2xig)dx=ig(y-x^2yig)dy.$$



5. Solve the following differential equations:
$$\frac{dy}{dx} = 1 + x + y + xy$$
 (ii)

$$y-xrac{dy}{dx}=aigg(y^2+rac{dy}{dx}igg)$$

6. Solve (x - y)(dx + dy) = dx - dy, given that y = -1, where x = 0.



7. Solve
$$\frac{dy}{dx} = yf'(x) = f(x)f'(x)$$
, where $f(x)$ is a given integrable

function of x.

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8. Solve
$$rac{dy}{dx} = \cos(x+y) - \sin(x+y).$$

9. If a function 'f' satisfies the relation
$$f(x)f^{''}(x) - f(x)f'(x) - f'(x)^2 = 0 \forall x \in R \text{ and } f(0) = 1 = f'(0).$$

Then find $f(x)$.

CONCEPT APPLICATION EXERCISES 10.4



4. Solve
$$\Big[x\sin^2\Big(rac{y}{x}\Big)-y\Big]dx+xdy=0; y=rac{\pi}{4}$$
 when $x=1$

5. Show that the differential equation $y^3 dy - (x + y^2) dx = 0$ can be reduced to a homogenous equation.

6. Solve
$$rac{dy}{dx} = rac{2x-y+1}{x+2y-3}$$

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CONCEPT APPLICATION EXERCISES 10.5

1. The solution of $ydx - xdy + 3x^2y^2e^{x^3}$ dx = 0 is

2.
$$rac{dy}{dx}=rac{2xy}{x^2-1-2y}$$



7.
$$y(xy+1)dx+xig(1+xy+x^2y^2ig)dy=0$$

CONCEPT APPLICATION EXERCISES 10.6

1. What is the integrating factor of the differential equation $ig(1-y^2ig)rac{dx}{dy}+yx=ay\,(\,-1< y<1)?$

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2. Solve
$$rac{dy}{dx} + y \cot x = \sin x$$

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3. Solve (x+y+1)(dy//dx)=1

4. Solve the equation
$$ig(1-x^2)igg(rac{dy}{dx}igg)+2xy=x\sqrt{1-x^2}$$

5. Solve the equation
$$\displaystyle rac{dy}{dx} = \displaystyle rac{y}{2y 1 n y + y - x}$$

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6. Solve the equation
$$ydx + ig(x-y^2ig)dy = 0$$

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7. Find the equation of a curve passing through (0,1) and having gradient $rac{-(y+y^3)}{1+x+xy^2}$ at (x,y).

1. Solve the equation
$$rac{dy}{dx} = rac{1}{x} = rac{e^y}{x^2}$$

2.
$$rac{dy}{dx} + x \sin 2y = x^3 \cos^2 y$$

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3.
$$rac{dy}{dx}+rac{xy}{1-x^2}=x\sqrt{y}$$

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4.
$$rac{dy}{dx} = ig(x^3 - 2x an^{-1} yig)ig(1 + y^2ig)$$
5.
$$\frac{dy}{dx} = \frac{\tan x}{1+x}e^x \sec y$$



CONCEPT APPLICATION EXERCISES 10.8

1. Find the equation of the curve in which the subnormal varies as the square of the ordinate.

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2. Find the curve for which the length of normal is equal to the radius

vector.



3. Find the curve for which the perpendicular from the foot of the ordinate to the tangent is of constant length.



4. A curve y = f(x) passes through the origin. Through any point (x, y) on the curve, lines are drawn parallel to the co-ordinate axes. If the curve divides the area formed by these lines and co-ordinates axes in the ratio m:n, find the curve.



5. A normal is drawn at a point P(x, y) of a curve. It meets the x-axis at Q. If PQ has constant length k, then show that the differential equation describing such curves is $y\frac{dy}{dx} = \pm \sqrt{k^2 - y^2}$. Find the equation of such a curve passing through (0, k). **6.** Find the orthogonal trajectories of family of curves $x^2 + y^2 = cx$

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7. A curve C has the property that if the tangent drawn at any point P on C meets the co-ordinate axis at A and B, then P is the mid-point of AB. The curve passes through the point (1,1). Determine the equation of the curve.

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CONCEPT APPLICATION EXERCISES 10.9

1. A person places Rs 500 in an account that interest compounded continuously. Assuming no additional deposits or withdrawals, how much will be in the account after seven years if the interest rate is a constant 8.5 percent for the first four year and a constant 9.25 percent for the last three years



3 m to empty through a round hole of 2.5 cm with a velocity 2. $5\sqrt{h}$ m/s,

2. Find the time required for a cylindrical tank of radius 2.5 m and height

h being the depth of the water in the tank.

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3. If the population of country double in 50 years, in how many years will it triple under the assumption that the rate of increase is proportional to the number of inhabitants.

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4. The rate at which a substance cools in moving air is proportional to the difference between the temperatures of the substance and that of the air. If the temperature of the air is 290 K and the substance cools from 370 K to 330 K in 10 min, when will the temperature be 295 K?

5. A right circular cone with radius R and height H contains a liquid which evaporates at a rate proportional to its surface area in contact with air (proportionality constant k is positive). Suppose that r(t) is the radius of the liquid cone at time t. The time after which the cone is empty is

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SINGLE CORRECT ANSWER TYPES

1. The degree of the differential equation satisfying $\sqrt{1-x^2} + \sqrt{1-y^2} = a(x-y)$ is (a) 1 (b) 2 (c) 3 (d) none of these A. 1 B. 2 C. 3

D. None of these

Answer: A

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2. Number of values of $m \in N$ for which $y = e^{mx}$ is a solution of the differential equation $\frac{d^3y}{dx^3} - 3\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 12y = 0$ (a) 0 (b) 1 (c) 2 (d) More than 2 A. 0 B. 1 C. 2 D. More than 2

Answer: C

3. The order of differential equation of family of circles passing through intersection of 3x + 4y - 7 = 0 and $S = -x^2 + y^2 - 2x + 1 = 0$ is

A. 1

B. 2

C. 3

D. 4

Answer: A

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4. The differential equation of all non-horizontal lines in a plane is (a) $(b)(c)(d) \frac{(e)(f)d^{(g)2(h)}(i)y}{j} ((k)d(l)x^{(m)2(n)}(o))(p)(q)(r) \quad (s) \quad (b)$ $(t)(u)(v) \frac{(w)(x)d^{(y)2(z)}(aa)x}{bb} ((cc)d(dd)y^{(ee)2(ff)}(gg))(hh)(ii) = 0(jj)$ $(kk) \quad (c) \quad (d)(e)(f) \frac{(g)dy}{h} ((i)dx)(j)(k) = 0(l) \quad (m) \quad (d)$ $(n)(o)(p) \frac{(q)dx}{r} ((s)dy)(t)(u) = 0(v) \text{ (w)}$

A.
$$rac{d^2y}{dx^2}$$

B. $rac{d^2x}{dy^2}=0$
C. $rac{dy}{dx}=0$
D. $rac{dx}{dy}=0$

Answer: B

(y) (z) [Math Processing Error] (xx) (yy) [Math Processing Error] (eeee) (ffff)

[Math Processing Error] (ddddd)

A.
$$rac{d^2y}{dx^2} - 2rac{dy}{dx} + 2y = 0$$

B. $rac{d^2y}{dx^2} + 2rac{dy}{dx} - 2y = 0$
C. $rac{d^2y}{dx^2} + \left(rac{dy}{dx}
ight)^2 + y = 0$

D.
$$\displaystyle rac{d^2y}{dx^2} - 7 \displaystyle rac{dy}{dx} + 2y = 0$$

Answer: A



6. Differential equation of the family of circles touching the line y=2 at

$$-2(vvv)\Big)=0(www)$$

(xxx) (yyy) None of these

A.
$$x^2 + (y-2)^2 + rac{dy}{dx}(y-2) = 0$$

B. $x^2 + (y-2)\left(2 - 2xrac{dx}{dy} - y
ight) = 0$
C. $x^2 + (y-2)^2 + \left(rac{dx}{dy} + y - 2
ight)(y-2) = 0$

D. None of these

Answer: D



7. The order and degree of the differential equation of all tangent lines to

the parabola $y=x^2$ is

A. 1,2

B. 2,3

C. 2,1

D. 1,1

Answer: A



8. The differential equation for the family of curve $x^2 + y^2 - 2ay = 0$,

where a is an arbitrary constant, is

A.
$$2(x^2-y^2)y'=xy$$

B. $2(x^2+y^2)y'=xy$
C. $(x^2-y^2)y'=2xy$
D. $(x^2+y^2)y'=2xy$

Answer: C

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9. The differential equation whose general solution is given by $y = (c_1 \cos(x + c_2) - (c_3 e^{(-x+c4)} + (c_5 \sin x), \text{ where } c_1, c_2, c_3, c_4, c_5)$ are arbitrary constants, is (a) $(b)(c)(d) \frac{(e)(f)d^{(g)4(h)}(i)y}{j}((k)d(l)x^{(m)4(n)}(o))(p)(q) - (r)\frac{(s)(t)d^{(u)}}{x}$ (gg) (hh) $(ii)(jj)(kk) \frac{(ll)(mm)d^{(nn)3(oo)}(pp)y}{qq}((rr)d(ss)x^{(tt)3(uu)}(vv))(ww)(\times 1)$ $+ (mmm)\frac{(nnn)dy}{ooo}((ppp)dx)(qqq)(rrr) + y = 0(sss)$ (ttt) (uuu) $(vvv)(www)(\times x)\frac{(yyy)(zzz)d^{(aaaa)5(bbbb)}(cccc)}{ddd}((eee)d(ffff)x^{(gggg)5(t)})$ (mmmm) (nnnn)

$$(0000)(pppp)(qqqq)\frac{(rrrr)(ssss)d^{(tttt)3(uuuu)}(vvvv)y}{www}((xxxx)d(yyy)x^{(zzz)} - (eeeee)\frac{(fffff)(ggggg)d^{(hhhhh)2(iiiii)}(jjjjj)y}{kkkkk}((lllll)d(mmmm)x^{(nn)} = 0(yyyyy)$$
(zzzz)

A.
$$\frac{d^4y}{dx^4} - \frac{d^2y}{dx^2} + y = 0$$

B. $\frac{d^3y}{dx^3} + \frac{d^2y}{dx^2} + \frac{dy}{dx} + y = 0$
C. $\frac{d^5y}{dx^5} + y = 0$
D. $\frac{d^3y}{dx^3} - \frac{d^2y}{dx^2} + \frac{dy}{dx} - y = 0$

Answer: B

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10. If $y = \frac{x}{|In|cx|}$ (where c is an arbitrary constant) is the general solution of the differential equation $\frac{dy}{dx} = \frac{y}{x} + \phi\left(\frac{x}{y}\right)$ then function $\phi\left(\frac{x}{y}\right)$ is:

A.
$$x^2 / y^2$$

B. $-x^2 / y^2$
C. y^2 / x^2
D. $-y^2 / x^2$

Answer: D

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11. The differential equation of the curve $\frac{x}{c-1} + \frac{y}{c+1} = 1$ is (a) [Math Processing Error] (cc) (dd) $(ee)(ff)\left((gg)(hh)(ii)\frac{(jj)dy}{kk}((ll)dx)(mm)(\cap) + 1(oo)\right)\left((pp)(qq)y - x\right)$ (fff) (ggg) $(hhh)(iii)\left((jjj)(kkk)(lll)\frac{(mmm)dy}{nnn}((ooo)dx)(ppp)(qqq) + 1(rrr)\right)\left((ss)$ $= 2(bbbb)\frac{(cccc)dy}{ddd}((eeee)dx)(ffff)(gggg)(hhhh)$ (iiii)

A.
$$\displaystyle rac{dy}{dx} - 1 igg(y + x rac{dy}{dx}igg) = 2 rac{dy}{dx}$$

B.
$$\left(\frac{dy}{dx}+1\right)\left(y-x\frac{dy}{dx}\right)=\frac{dy}{dx}$$

C. $\left(\frac{dy}{dx}+1\right)\left(y-x\frac{dy}{dx}\right)=2\frac{dy}{dx}$
D. y^2/x^2

Answer: C

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12. If
$$y = y(x)$$
 and $\left(\frac{2+\sin x}{y+1}\right)\frac{dy}{dx} = -\cos x$, $y(0) = 1$, then $y\left(\frac{\pi}{2}\right)$ equals (A) $\frac{1}{3}$ (B) $\frac{2}{3}$ (C) $-\frac{1}{3}$ (D) 1

A. 1/3

B. 2/3

C. - 1/3

D. 1

Answer: A

13. The equation of the curves through the point (1, 0) and whose slope is

$$\frac{y-1}{x^2+x}$$
 is (a) $(b)(c)((d)(e)y-1(f))((g)(h)x+1(i))+2x=0(j)$ (k)
(l) $(m)(n)2x((o)(p)y-1(q))+x+1=0(r)$ (s) (t)
 $(u)(v)x((w)(x)y-1(y))((z)(aa)x+1(bb))+2=0(cc)$ (dd) (ee)None

of these

A.
$$(y-1)(x+1)+2x=0$$

B.
$$2x(y-1)+x+1=0$$

C.
$$x(y-1)(x+1)+2=0$$

D. None of these

Answer: A

14. The solution of the equation $\frac{dy}{dx} = \left(x\frac{2\log x + 1}{\sin y + y\cos y}\right)$ is (a) $(b)(c)y\sin y = (d)x^{(e)2(f)}(g)\log x + (h)\frac{(i)(j)x^{(k)2(l)}(m)}{n}2(o)(p) + c(q)$

(r) (s)
$$(t)(u)y\cos y = (v)x^{(w)2(x)}(y)(\log x + 1) + c(z)$$
 (aa) (bb)
 $(cc)(dd)y\cos y = (ee)x^{(ff)2(gg)}(hh)\log x + (ii)\frac{(jj)(kk)x^{(ll)2(mm)}(nn)}{oo}$
(ss) (tt) $(uu)(\vee)y\sin y = (ww)x^{(xx)2(yy)}(zz)\log x + c(aaa)$ (bbb)
A. $y\sin y = x^2\log x + \frac{x^2}{2} + c$
B. $y\cos y = x^2(\log x + 1) + c$
C. $y\cos y = x^2\log x + \frac{x^2}{2} + c$
D. $y\sin y = x^2\log x + c$

Answer: D

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15. The solution of the equation $ig(x^2y+x^2ig)dx+y^2(x-1)dy=0$ is

$$\begin{array}{l}(b)(c)(d)x^{\,(e\,)\,2\,(f\,)}\,(g)+(h)y^{\,(i\,)\,2\,(j\,)}\,(k)+2((l)(m)x-y(n))+21n(o)\frac{(p)(d)}{2}(p)(d)x^{\,(e\,)\,2\,(f\,)}\,(g)+(h)y^{\,(i\,)\,2\,(f\,)}\,(k)+2((l)(m)x-y(n))+21n(o)\frac{(p)(d)}{2}(p)(d)x^{\,(e\,)\,2\,(f\,)}\,(g)+(h)y^{\,(i\,)\,2\,(f\,)}\,(k)+2((l)(m)x-y(n))+21n(o)\frac{(p)(d)}{2}(p)(d)x^{\,(e\,)\,2\,(f\,)}\,(g)+(h)y^{\,(i\,)\,2\,(f\,)}\,(k)+2((l)(m)x-y(n))+21n(o)\frac{(p)(d)}{2}(p)(d)x^{\,(e\,)\,2\,(f\,)}\,(g)+(h)y^{\,(e\,)\,2\,(g)}\,(g)+(h)y^{\,(e\,)\,2\,(g)}$$

$$(cc)(dd)(ee)x^{(ff)\,2\,(gg)}\,(hh)+(ii)y^{(jj)\,2\,(kk)}\,(ll)+2((mm)(\,\cap\,)x-y(\infty)$$

(bbb) (ccc)

$$(ddd)(eee)(fff)x^{(ggg)2(hhh)}(iii) + (jjj)y^{(kkk)2(lll)}(mmm) + 2((nnn)(content)) = 0(bbbb)$$

(cccc) (dddd) None of these

A.
$$x^2 + y^2 + 2(x - y) + 2\ln \frac{(x - 1)(y + 1)}{c} = 0$$

B. $x^2 + y^2 + 2(x - y) + \ln \frac{(x - 1)(y + 1)}{c} = 0$
C. $x^2 + y^2 + 2(x - y) - 2\ln \frac{(x - 1)(y + 1)}{c} = 0$

D. None of these

Answer: A

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16. Solve the following differential equations

$$rac{dy}{dx} = \sin x \cdot \sin y$$
A. $e^{\cos x} rac{ an y}{2} = c$

B. $e^{\cos x} \tan y = c$

 $\mathsf{C.}\cos x \tan y = c$

D. $\cos x \sin y = c$

Answer: A

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17. The solution of
$$\frac{dv}{dt} + \frac{k}{m}v = -g$$
 is (a)
 $(b)(c)v = c(d)e^{(e)(f)(g)\frac{k}{h}g(i)(j)t(k)}(l) - (m)\frac{(n)mg}{o}k(p)(q)(r)$ (s)

(b) [Math Processing Error] (kk) (c) $(d)(e)v(f)e^{(g)(h)(i)\frac{k}{j}m(k)(l)t(m)}(n) = c - (o)\frac{(p)mg}{a}k(r)(s)(t)$ (u)

(d) [Math Processing Error] (mm)

A.
$$v = ce^{-rac{k}{m}t} - rac{mg}{k}$$

B. $v = c - rac{mg}{k}e^{-rac{k}{m}t}$
C. $ve^{-rac{k}{m}t} = c - rac{mg}{k}$
D. $ve^{rac{k}{m}t} = c - rac{mg}{k}$

Answer: A



18. The general solution of the differential equation

$$\frac{dy}{dx} + \frac{\sin(x+y)}{2} = \frac{\sin(x-y)}{2} \qquad \text{is} \qquad \text{(a)}$$

$$(b)(c)\log\tan\left((d)(e)(f)\frac{y}{g}2(h)(i)(j)\right) = c - 2\sin x(k) \quad \text{(I)} \quad \text{(m)} \quad [Math]$$
Processing Error] (ee) (ff) [Math Processing Error] (uu) (vv)

$$(ww)(\times)\log\tan\left((yy)(zz)(aaa)\frac{y}{bbb}4(ccc)(ddd) + (eee)\frac{\pi}{fff}4(ggg)(hhh)\right)$$
(rrr)

A.
$$\log \tan\left(\frac{y}{2}\right) = c - 2\sin x$$

B. $\log \tan\left(\frac{y}{2}\right) = c - 2\sin\left(\frac{x}{2}\right)$
C. $\log \tan\left(\frac{y}{2} + \frac{\pi}{4}\right) = c - 2\sin x$
D. $\log \tan\left(\frac{y}{4} + \frac{\pi}{4}\right) = c - 2\sin\left(\frac{x}{2}\right)$

Answer: B

19. if
$$y + x \frac{dy}{dx} = x \frac{\phi(xy)}{\phi'(xy)}$$
 then $\phi(xy)$ is equation to
A. $ke^{x^2/2}$
B. $ke^{y^2/2}$
C. $ke^{xy/2}$
D. ke^{xy}

Answer: A

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20. The solution of differential equation
$$x^2 = 1$$

 $+\left(\frac{x}{y}\right)^{-1}\frac{dy}{dx} + \frac{\left(\frac{x}{y}\right)^{-2}\left(\frac{dy}{dx}\right)^2}{2!} + \frac{\left(\frac{x}{y}\right)^{-3}\left(\frac{dy}{dx}\right)^3}{3!} + \dots is$
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21. The solution of the differential equation

$$\frac{x + \frac{x^3}{3!} + \frac{x^5}{5!} +}{1 + \frac{x^2}{2!} + \frac{x^4}{4!} +} = \frac{dx - dy}{dx + dy} is$$
(a)
(b)(c)2y(d)e^{(e)(f)2x(g)}(h) = C(i)e^{(j)(k)2x(l)}(m) + 1(n) (o) (p)
(q)(r)2y(s)e^{(t)(u)2x(v)}(w) = C(x)e^{(y)(z)2x(aa)}(bb) - 1(cc) (dd) (ee)
(ff)(gg)y(hh)e^{(ii)(jj)2x(kk)}(ll) = C(mm)e^{(nn)(\infty)2x(pp)}(qq) + 2(rr)
(ss) (d) None of these

A.
$$2ye^{2x} = Ce^{2x} + 1$$

B.
$$2ye^{2x} = Ce^{2x} - 1$$

$$\mathsf{C}. y e^{2x} = C e^{2x} + 2$$

D. None of these

Answer: B



22. The solution of the differential equation

$$x = 1 + xy \frac{dy}{dx} + \frac{x^2 y^2}{2!} \left(\frac{dy}{d}\right)^2 + \frac{x^3 y^3}{3!} \left(\frac{dy}{dx}\right)^3 + is$$
(a)
(b)(c)y = 1n((d)x(e)) + c(f)
(g)
(b)
(h)(i)(j)y^{(k)2(l)}(m) = (n)(o)((p)(q)1nx(r))^{(s)2(t)}(u) + c(v) (w) (c)
(d)(e)y = log x + xy(f) (g) (d) (h)(i)xy = (j)x^{(k)y(l)}(m) + c(n) (o)

A.
$$y = \ln(x) + C$$

$$\mathsf{B}.\,y^2=\left(\ln \ x\right)^2+c$$

$$\mathsf{C}.\, y = \log x + xy$$

D.
$$xy = x^y + c$$

Answer: B

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23. A curve passing through (2,3) and satisfying the differential equation

$$\int_0^x ty(t)dt = x^2y(x), (x > 0) \qquad \text{is} \qquad (a)$$

(b)(c)(d) $x^{(e)2(f)}(g) + (h)y^{(i)2(j)}(k) = 13(l) \qquad (m) \qquad (b)$

$$\begin{split} &(n)(o)(p)y^{(q)\,2\,(r)}\,(s)\,=\,(t)\frac{9}{u}2(v)(w)x(x) & \text{(y)} & \text{(c)} \\ &(d)(e)(f)\frac{(g)(h)x^{\,(i)\,2\,(j)}\,(k)}{l}8(m)(n)\,+\,(o)\frac{(p)(q)y^{\,(r)\,2\,(s)}\,(t)}{u}((v)18)(w)(x) & \text{(c)} \end{split}$$

(z) (d) [Math Processing Error] (dd)

A.
$$x^2 + y^2 = 13$$

B. $y^2 = \frac{9}{2}x$
C. $\frac{x^2}{8} + \frac{y^2}{18} = 1$
D. $xy = 6$

Answer: D

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24. The solution of the differential equation $\frac{d^2y}{dx^2} = \sin 3x + e^x + x^2$ when $y_1(0) = 1$ and y(0) is (a) $(b)(c)(d)\frac{(e) - \sin 3x}{f}9(g)(h) + (i)e^{(j)x(k)}(l) + (m)\frac{(n)(o)x^{(p)4(q)}(r)}{s}(l)}{s}(dd)$ (bb) (cc) [Math Processing Error] (ddd) (eee)

$$(fff)(ggg)(hhh)rac{(iii)-\cos 3x}{jjj} 3(kkk)(lll)+(mmm)e^{(\,nnn\,)\,x\,(\,\infty\,o\,)}\left(ppp
ight)+$$

(ffff) (d) None of these

A.
$$y = \frac{-\sin 3x}{9} + e^x + \frac{x^4}{12} + \frac{1}{3}x - 1$$

B. $y = \frac{-\sin 3x}{9} + e^x + \frac{x^4}{12} + \frac{1}{3}x$
C. $y = \frac{-\cos 3x}{3} + e^x + \frac{x^4}{12} + \frac{1}{3}x + 1$

D. None of these

Answer: A

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25. The solution of the differential equation $y'y^{'''} = 3(y^{''})^2$ is

A.
$$x=A_1y^2+A_2y+A_3$$

$$\mathsf{B.}\, x = A_1 y + A_2$$

$$\mathsf{C.}\, x = A_1 y^2 + A_2 y$$

D. None of these

Answer: A



26. The solution of the differential equation
$$y^{-8}y^{=0}$$
, where
 $y(0) = \frac{1}{8}, y'(0) = 0, y^{0} = 1$, is (a)
 $(b)(c)y = (d)\frac{1}{e}8(f)(g)\left((h)(i)(j)\frac{(k)(l)e^{(m)(n)8x(o)}(p)}{q}8(r)(s) + x - (t))\right)$
(z) (aa) [Math Processing Error] (zz) (aaa)
 $(bbb)(c)y = (ddd)\frac{1}{eee}8(fff)(ggg)\left((hhh)(iii)(jjj)\frac{(kkk)(lll)e^{(mmm)(n)x}}{qqq}\right)$

(zzz) (d) None of these

A.
$$y = rac{1}{8} \left(rac{e^{8x}}{8} + x - rac{7}{9}
ight)$$

B. $y = rac{1}{8} \left(rac{e^{8x}}{8} + x + rac{7}{8}
ight)$
C. $y = rac{1}{8} \left(rac{e^{8x}}{8} - x + rac{7}{8}
ight)$

D. None of these

Answer: C

27. The slope of the tangent at (x, y) to a curve passing through $\left(1, \frac{\pi}{4}\right)$ is given by $\frac{y}{x} - \cos^2\left(\frac{y}{x}\right)$, then the equation of the curve is (a) $(b)(c)y = (d)(e)\tan^{(f)(g)-1(h)}(i)\left((j)(k)\log\left((l)(m)(n)\frac{e}{o}x(p)(q)(r)\right)(s)$ (u) (v) [Math Processing Error] (pp) (qq) [Math Processing Error] (kkk) (d)

none of these

A.
$$y = \tan^{-1} \log\left(\frac{e}{x}\right)$$

B. $y = x \tan^{-1} \log\left(\frac{x}{e}\right)$
C. $y = x \tan^{-1} \log\left(\frac{e}{x}\right)$

D. None of these

Answer: C

28.
$$x \frac{dy}{dx} = y(\log y - \log x + 1)$$

A.
$$\frac{\log x}{y} = cy$$

B. $\frac{\log y}{x} = cy$
C. $\frac{\log y}{x} = cx$

D. None of these

Answer: C

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29. The solution of differential equation $xy' = x\left(rac{y^2}{x^2} + rac{f\left(rac{y^2}{x^2}
ight)}{f'\left(rac{y^2}{x^2}
ight)}
ight)$ is (a)

$$(d)(e)(f)x^{(g)2(h)}(i)f\bigg((j)(k)(l)\frac{(m)(n)y^{(o)2(p)}(q)}{r}\Big((s)(t)x^{(u)2(v)}(w)\Big)(s^{$$

(bb) (d) [Math Processing Error] (bbb)

A.
$$fig(y^2 \, / \, x^2ig) = c x^2$$

B.
$$x^2 fig(y^2 / x^2ig) = c^2 y^2$$

C. $x^2 fig(y^2 / x^2ig) = c$
D. $fig(y^2 / x^2ig) = cy / x$

Answer: A

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30. The solution of
$$ig(x^2+xyig)dy=ig(x^2+y^2ig)dx$$
 is (a)

$$(b)(c)\log x = \log((d)(e)x - y(f)) + (g)rac{y}{h}x(i)(j) + c(k)$$
 (I) (m)

$$(n)(o){\log x} = 2\log((p)(q)x - y(r)) + (s)rac{y}{t}x(u)(v) + c(w)$$
 (x) (y)

[Math Processing Error] (jj) (kk) None of these

A.
$$\log x = \log(x-y) + \frac{y}{x} + c$$

B. $\log x = 2\log(x-y) + \frac{y}{x} + c$
C. $\log x = \log(x-y) + \frac{x}{y} + c$

D. None of these

Answer: B

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31. The solution of
$$(y + x + 5)dy = (y - x + 1)dx$$
 is (a) [Math
Processing Error] (jj) (kk)
 $(ll)(mm)\log((nn)(\infty)(pp)(qq)((rr)(ss)y + 3(tt))^{(uu)2(vv)}(ww) + (xx)(qx)) + (ggg)(hhh)\tan^{(iii)(jjj)-1(kkk)}(lll)(mmm)\frac{(nnn)y - 3}{ooo}((ppp)y - 2)(qq)$
(ttt) (uuu) [Math Processing Error] (dddd) (eeeee) [Math Processing
Error] (nnnnn)

$$\begin{aligned} \mathsf{A}.\log\Bigl((y+3)^2+(x+2)^2\Bigr) &+ \frac{\tan^{-1}(y+3)}{y+2} + C \\ \mathsf{B}.\log\Bigl((y+3)^2+(x-2)^2\Bigr) &+ \frac{\tan^{-1}(y-3)}{x-2} = C \\ \mathsf{C}.\log\Bigl((y+3)^2+(x+2)^2\Bigr) &+ 2\frac{\tan^{-1}(y+3)}{x+2} = C \\ \mathsf{D}.\log\Bigl((y+3)^2+(x+2)^2\Bigr) &- 2\frac{\tan^{-1}(y+3)}{x+2} = C \end{aligned}$$

Answer: A

32. The slope of the tangent at
$$(x, y)$$
 to a curve passing through a point
 $(2, 1)$ is $\frac{x^2 + y^2}{2xy}$, then the equation of the curve is (a)
 $(b)(c)2\Big((d)(e)(f)x^{(g)2(h)}(i) - (j)y^{(k)2(l)}(m)(n)\Big) = 3x(o)$ (p) (b)
[Math Processing Error] (ee) (c)
 $(d)(e)x\Big((f)(g)(h)x^{(i)2(j)}(k) - (l)y^{(m)2(n)}(o)(p)\Big) = 6(q)$ (r) (d)
 $(s)(t)x\Big((u)(v)(w)x^{(x)2(y)}(z) + (aa)y^{(bb)2(cc)}(dd)(ee)\Big) = 10(ff)$
(gg)

A.
$$2(x^2 - y^2) = 3x$$

B. $2(x^2 - y^2) = 6y$
C. $x(x^2 - y^2) = 6$
D. $x(x^2 + y^2) = 10$

Answer: A

33. Solution f the differential equation $ydx - xdy + x\sqrt{xy}dy = 0$ is

A.
$$rac{x^2+y^2}{2}+ an^{-1}\sqrt{rac{y}{x}}=c$$

B. $rac{x^2+y^2}{2}+2 an^{-1}\sqrt{rac{x}{y}}=C$
C. $rac{x^2+y^2}{2}+2 an^{-1}\sqrt{rac{x}{y}}=c$

D. None of these

Answer: D

34. The solution of
$$x^2 rac{dy}{dx} - xy = 1 + rac{\cos y}{x}$$
 is

A.
$$an\left(rac{y}{2x}
ight) = c - rac{1}{2x^2}$$

B. $rac{ an y}{x} = c + rac{1}{x}$
C. $\cos\left(rac{y}{x}
ight) = 1 + rac{c}{x}$
D. $x^2 = (c + x^2) rac{ an y}{x}$

Answer: A





Answer: D



A.
$$\ln \left| rac{x}{y}
ight| + rac{xy}{x-y} = c$$

B. $rac{xy}{x-y} = c e^{x/y}$
C. $\ln |xy| + rac{x^4y^4}{4} = C$

D. None of these

Answer: A

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37. The solution of differential equation

$$(2y + xy^3)dx + (x + x^2y^2)dy = 0$$
 is (a)
 $(b)(c)(d)x^{(e)2(f)}(g)y + (h)\frac{(i)(j)x^{(k)3(l)}(m)(n)y^{(o)3(p)}(q)}{r}3(s)(t) = c(a)$
(v) (b)
 $(w)(x)x(y)y^{(z)2(aa)}(bb) + (cc)\frac{(dd)(ee)x^{(ff)3(gg)}(hh)(ii)y^{(jj)3(kk)}(ll)}{mm}3(a)$
(qq) (c)
 $(d)(e)(f)x^{(g)2(h)}(i)y + (j)\frac{(k)(l)x^{(m)4(n)}(o)(p)y^{(q)4(r)}(s)}{t}4(u)(v) = c(a)$

(x) (d) None of these

A.
$$x^2y + rac{x^3y^3}{3} = c$$

B. $xy^2 + rac{x^3y^3}{3} = c$
C. $x^2y + rac{x^4y^4}{4} = c$

D. None of these

Answer: A

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38. The solution of
$$ye^{-rac{x}{y}}dx-\left(xe^{\left(-rac{x}{y}
ight)}+y^3
ight)dy=0$$
 is (a)

$$(b)(c)(d)e^{\,(\,e\,)\,(\,f\,)\,-\,(\,g\,)rac{x}{h}y(\,i\,)\,(\,j\,)\,(\,k\,)}\,(l)\,+\,(m)y^{\,(\,n\,)\,2\,(\,o\,)}\,(p)\,=\,C(q)$$
 (r) (b)

[Math Processing Error] (ee) (c) $(d)(e)2(f)e^{(g)(h) - (i)\frac{x}{j}y(k)(l)(m)}(n) + (o)y^{(p)2(q)}(r) = C(s)$ (t) (d)

[Math Processing Error] (kk)

A.
$$e^{-x/y}+y^2=C$$

B. $xe^{-x/y}+y=C$
C. $2e^{-x/y}+y^2=C$

D.
$$e^{-x/y} + 2y^2 = C$$

Answer: C

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39. The curve satisfying the equation $\frac{dy}{dx} = \frac{y(x+y^3)}{x(y^3-x)}$ and passing through the point (4, -2) is (a) $(b)(c)(d)y^{(e)2(f)}(g) = -2x(h)$ (i) (b) (j)(k)y = -2x(l) (m) (c) $(d)(e)(f)y^{(g)3(h)}(i) = -2x(j)$ (k) (d) None of these

A.
$$y^2 = -2x$$

 $\mathsf{B}.\,y=\,-\,2x$

$$\mathsf{C}.\,y^3=\,-\,2x$$

D. None of these

Answer: C

40. The solution of differential equation

$$egin{aligned} &rac{x+yrac{dy}{dx}}{y-xrac{dy}{dx}} = xigg(rac{\cos^2ig(x^2+y^2ig)}{y^3}ig) ext{ is } \ & ext{A.} ext{tan}ig(x^2+y^2ig) = rac{x^2}{y^2} + c \ & ext{B.} ext{cot}ig(x^2+y^2ig) = rac{x^2}{y^2} + c \ & ext{C.} ext{tan}ig(x^2+y^2ig) = rac{y^2}{x^2} + c \ & ext{D.} ext{cot}ig(x^2+y^2ig) = rac{y^2}{x^2} + c \end{aligned}$$

Answer: A

.

41. The solution of the differential equation
$$\frac{dy}{dx} = \frac{3x^2y^4 + 2xy}{x^2 - 2x^3y^3}$$
 is (a)
 $(b)(c)(d)\frac{(e)(f)y^{(g)2(h)}(i)}{j}x(k)(l) - (m)x^{(n)3(o)}(p)(q)y^{(r)2(s)}(t) = c(u)$
(v) (w) [Math Processing Error] (ww) (xx)
 $(yy)(zz)(aaa)\frac{(bbb)(c)x^{(ddd)2(eee)}(fff)}{ggg}y(hhh)(iii) + (jjj)x^{(kkk)3(lll)}(m)$
(sss)

(d)

(0000)

A.
$$rac{y^2}{x} - x^3y^2 = c$$

B. $rac{x^2}{y^2} + x^3y^3 = c$
C. $rac{x^2}{y} + x^3y^2 = c$
D. $rac{x^2}{3y} - 2x^3y^2 = c$

Answer: C

42. The solution of the differential equation

$$\left\{1 + x\sqrt{\left(x^2 + y^2\right)}\right\}dx + \left\{\sqrt{\left(x^2 + y^2\right)} - 1\right\}ydy = 0 \text{ is equal to (a)}$$

$$(b)(c)(d)x^{(e)2(f)}(g) + (h)\frac{(i)(j)y^{(k)2(l)}(m)}{n}2(o)(p) + (q)\frac{1}{r}3(s)(t)(u)(v)$$

$$(qq) (rr) [Math Processing Error] (dddd) (eeee) [Math Processing Error]$$

$$(qqqqq)$$

A.
$$x^2 + rac{y^2}{2} + rac{1}{3} ig(x^2 + y^2ig)^{3/2} = c$$

B. $x - rac{y^3}{3} + rac{1}{2} ig(x^2 + y^2ig)^{1/2} = c$
C. $x - rac{y^2}{2} + rac{1}{3} ig(x^2 + y^2ig)^{3/2} = c$

D. None of these

Answer: C

43. The solution of the differential equation

$$yig(2x^4+yig)rac{dy}{dx}=ig(1-4xy^2ig)x^2$$
 is given by

A.
$$3(x^2y)^2 + y^3 - x^3 = c$$

B. $xy^2 + \frac{y^3}{3} - \frac{x^3}{3} + c = 0$
C. $\frac{2}{5}yx^5 + \frac{y^3}{3} = \frac{x^3}{3} - \frac{4xy^3}{3} + c$

D. None of these

Answer: A

44. The solution of the differential equation $(x \cot y + \log \cos x)dy + (\log \sin y - y \tan x)dx = 0$ is

A.
$$(\sin x)^y (\cos y)^x = c$$

$$\mathsf{B.} (\sin y)^x (\cos x)^y = c$$

- $\mathsf{C}.\left(\sin x\right)^x(\cos y)^y=c$
- D. None of these

Answer: B

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45. If $\frac{dy}{dx} = (e^y - x)^{-1}$, where y(0) = 0, then y is expressed explicitly

as

A.
$$rac{1}{2} {
m log}_e ig(1+x^2ig)$$

B.
$$\log_e \left(1+x^2
ight)$$

C. $\log_e \left(x+\sqrt{1+x^2}
ight)=c$

D. None of these

Answer: C

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46. The general solution of the differential equation, $y' + y\varphi'(x) = 0$, where $\varphi(x)$ is a known function, is (a) $(b)(c)y = c(d)e^{(e)(f) - \varphi((g)x(h))(i)}(j) + \varphi((k)x(l)) - 1(m)$ (n) (o) $(p)(q)y = c(r)e^{(s)(t) + \varphi((u)x(v))(w)}(x) + \varphi((y)x(z)) - 1(aa)$ (bb) (cc) $(dd)(ee)y = c(ff)e^{(gg)(hh) - \varphi((ii)x(jj))(kk)}(ll) - \varphi((mm)x(\cap)) + 1(o)$ (pp) (d) $(qq)(rr)y = c(ss)e^{(tt)(\cup) - \varphi((vv)x(wv))(xx)}(yy) + \varphi((zz)x(aaa)) + 1(bi)$ (ccc)

A.
$$y = c e^{-\phi(x)} + \phi(x) - 1$$

B.
$$y = ce^{+\phi(x)} + \phi(x) - 1$$

C. $y = ce^{-\phi(x)} - \phi(x) + 1$
D. $y = ce^{-\phi(x)} + \phi(x) + 1$

Answer: A

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47. The integrating factor of the differential equation $\frac{dy}{dx}(x(\log)_e x) + y = 2(\log)_e x$ is given by

A. x

 $\mathsf{B.}\,e^x$

 $\mathsf{C}.\log_e x$

 $\mathsf{D}.\log_e(\log_e x)$

Answer: C

48. The solution of the differential equation

$$x(x^2+1)\left(\frac{dy}{dx}\right) = y(1-x^2) + x^3 \log x$$
 is (a) [Math Processing Error]
(gg) (hh)
 $(ii)(jj)(kk)\frac{(ll)y((mm)(\cap)(\infty)x^{(pp)2(qq)}(rr) - 1(ss))}{tt}x(\cup)(\vee) = (wr) + c(mmm)$

(nnn) (000) [Math Processing Error] (uuuu) (vvvv) None of these

A.
$$y(x^2+1)/x = rac{1}{4}x^2\log x + rac{1}{2}x^2 + c$$

B. $y^2(x^2-1)/x = rac{1}{2}x^2\log x - rac{1}{4}x^2 + c$
C. $y(x^2+1)x = rac{1}{2}x^2\log x - rac{1}{4}x^2 + c$

D. None of these

Answer: C

49. Integrating factor of differential equation $\cos x \frac{dy}{dx} + y \sin x = 1$ is (a) $(b)(c)\cos x(d)$ (e) (b) $(f)(g)\tan x(h)$ (i) (c) $(d)(e)\sec x(f)$ (g) (d) $(h)(i)\sin x(j)$ (k)

A. $\cos x$

 $B.\tan x$

 $\mathsf{C}.\sec x$

D. $\sin x$

Answer: C

50. Solution of the equation
$$\cos^2 x \frac{dy}{dx} - (\tan 2x)y = \cos^4 x$$
, where
 $|x| < \frac{\pi}{4}$ and $y\left(\frac{\pi}{6}\right) = \frac{3\sqrt{3}}{8}$ is
A. $y = \tan 2x \cos^2 x$
B. $y = \cot 2x \cos^2 x$

C.
$$y=rac{1}{2} an 2x\cos^2 x$$

D. $y=rac{1}{2} an 2x\cos^2 x$

Answer: C



51. If integrating factor of
$$xig(1-x^2ig)dy+ig(2x^2y-y-ax^3ig)dx=0$$
 is $e^{\int pdx},$ then P is equal to

A.
$$rac{2x^2-ax^2}{x(1-x^2)}$$

B. $2x^3-1$
C. $rac{2x^2-a}{ax^3}$
D. $rac{2x^2-1}{x(1-x^2)}$

Answer: D

52. A function
$$y = f(x)$$
 satisfies
 $(x+1)f'(x) - 2(x^2+x)f(x) = \frac{e^x \cdot 2}{(x+1)}, \forall x \succ 1.$ If $f(0) = 5$, then
 $f(x)$ is (a)
 $(b)(c)\left((d)(e)(f)\frac{(g)3x+5}{h}((i)x+1)(j)(k)(l)\right)(m)e^n(o)(p)x^{((g)2(r))(s)}$
(w) (b) [Math Processing Error] (ss) (c)
 $(d)(e)\left((f)(g)(h)\frac{(i)6x+5}{j}((k)x+1)(l)(m)(n)\right)(o)e^p(q)(r)x^{((s)2(t))(s)}$

(y) (d) [Math Processing Error] (uu)

A.
$$\left(\frac{3x+5}{x+1}\right)e^{x^2}$$
B.
$$\left(\frac{6x+5}{x+1}\right)e^{x^2}$$
C.
$$\left(\frac{6x+5}{(x+1)^2}\right)e^{x^2}$$
D.
$$\left(\frac{5-6x}{x+1}\right)e^{x^2}$$

Answer: B

53. The general solution of the equation
$$rac{dy}{dx}=1+xy$$
 is

A.
$$y=ce^{-x^2/2}$$

B. $y=ce^{x^2/2}$
C. $y=(x+c), e^{-x^2/2}$

D. None of these

Answer: D

54. The solution of the differential equation $rac{ig(x+2y^3ig)dy}{dx}=y$ is

A.
$$\displaystyle rac{x}{y^2} = y + c$$

B. $\displaystyle rac{x}{y} = y^2 + c$
C. $\displaystyle rac{x^2}{y} = y^2 + c$
D. $\displaystyle rac{y}{z} = x^2 + c$

Answer: B

x

55. The solution of the differential equation

$$x^2 \frac{dy}{dx} \cos\left(\frac{1}{x}\right) - y \sin\left(\frac{1}{x}\right) = -1$$
, where $y - -1 \operatorname{as} x - \infty$ is
A. $y = \sin\left(\frac{1}{x}\right) - \cos\left(\frac{1}{x}\right)$
B. $y = \frac{x+1}{x \sin\left(\frac{1}{x}\right)}$
C. $y = \cos\left(\frac{1}{x}\right) + \sin\left(\frac{1}{x}\right)$
D. $y = \frac{x+1}{x \cos(1/x)}$

Answer: A

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56. The solution of
$$rac{dy}{dx}=rac{x^2+y^2+1}{2xy}$$
 satisfying $y(1)=1$ is given by

A. a system of parabolas

B. a system of circles

C.
$$y^2=x(1+x)-1$$

D.
$$\left(x-2
ight)^{2}+\left(y-3
ight)^{2}=5$$

Answer: C

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57. The solution of the differential equation
$$\frac{dy}{dx} = \frac{1}{xy[x^2 \sin y^2 + 1]}$$
 is
(a)
(b)(c)(d) $x^{(e)2(f)}(g)\left(\cos(h)y^{(i)2(j)}(k) - \sin(l)y^{(m)2(n)}(o) - 2C(p)e^q(r)\right)$
(z) (aa) [Math Processing Error] (zz) (aaa)
(bbb)(c)(ddd) $x^{(eee)2(fff)}(ggg)\left(\cos(hhh)y^{(iii)2(jjj)}(kkk) - \sin(lll)y^{(mmr)}\right)$

(zzz) (aaaa) None of these

A.
$$x^2 \Big(\cos y^2 - \sin y^2 - 2Ce^{-y^2}\Big) = 2$$

B. $y^2 \Big(\cos x^2 - \sin y^2 - 2Ce^{-y^2}\Big) = 4C$

C. None of these

D. a system of circles

Answer: A



58. The equation of a curve passing through $\left(2, \frac{7}{2}\right)$ and having gradient $1 - \frac{1}{x^2}$ at (x, y) is (a) $(b)(c)y = (d)x^{(e)2(f)}(g) + x + 1(h)$ (i) (b) $(j)(k)xy = (l)x^{(m)2(n)}(o) + x + 1(p)$ (q) (c) (d)(e)xy = x + 1(f) (g)

(d) None of these

A.
$$y=x^2+x+1$$

B. $xy=x^2+x+1$
C. $xy=x+1$

D. None of these

Answer: B

59. Which of the following is not the differential equation of family of curves whose tangent form an angle of $\frac{\pi}{4}$ with the hyperbola $xy=c^2$?

A.
$$rac{dy}{dx}=rac{x-y}{x+y}$$

B. $rac{dy}{dx}=rac{x}{x-y}$
C. $rac{dy}{dx}=rac{x+y}{y-x}$

D. None of these

Answer: B

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60. Tangent to a curve intercepts the y-axis at a point P. A line perpendicular to this tangent through P passes through another point differential equation of the curve (1,0). The is (a) $(b)(c)y(d)rac{(e)dy}{f}((g)dx)(h)(i)-x(j)(k)igg((l)(m)(n)rac{(o)dy}{p}((q)dx)(r)(s)(t))$ Processing Error] (eee) (b) [Math (c) (y) $(d)(e)y(f)rac{(g)dx}{b}((i)dy)(j)(k)+x=1(l)$ (m) (d) None of these

A.
$$y rac{dy}{dx} - x \left(rac{dy}{dx}
ight)^2 = 1$$

B. $rac{xd^2y}{dx^2} + \left(rac{dy}{dx}
ight)^2 = 0$
C. $y rac{dy}{dx} + x = 1$

D. None of these

Answer: A

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61. Orthogonal trajectories of family of the curve $x^{\frac{2}{3}} + \frac{y^2}{3} = a^{\left(\frac{2}{3}\right)}$, where *a* is any arbitrary constant, is (a) $(b)(c)(d)x^{(e)(f)(g)\frac{2}{h}3(i)(j)(k)}(l) - (m)y^{(n)(o)(p)\frac{2}{q}3(r)(s)(t)}(u) = c(v)$ (w) (b) [Math Processing Error] (ss) (c) $(d)(e)(f)x^{(g)(h)(i)\frac{4}{j}3(k)(l)(m)}(n) + (o)y^{(p)(q)(r)\frac{4}{s}3(t)(u)(v)}(w) = c(x)$ (y) (d) [Math Processing Error] (uu)

A. $x^{2/3} - y^{2/3} = c$ B. $x^{4/3} - u^{4/3} = c$

C.
$$x^{4/3} + y^{4/3} = c$$

D.
$$x^{rac{1}{3}}-y^{1/3}=c$$

Answer: B

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62. The curve in the first quadrant for which the normal at any point (x, y) and the line joining the origin to that point form an isosceles triangle with the x-axis as base is (a) an ellipse (b) a rectangular hyperbola (c) a circle (d) None of these

A. an ellipse

B. a rectangular hyperbola

C. a circle

D. None of these

Answer: B



63. The equation of the curve which is such that the portion of the axis of x cut off between the origin and tangent at any point is proportional to the ordinate of that point is (a) $(b)(c)x = y(a - b\log x)(d)$ (e) (f) $(g)(h)\log x = b(i)y^{(j)2(k)}(l) + a(m)$ (n) (o)

 $(p)(q)(r)x^{\,(\,s\,)\,2\,(\,t\,)}\,(u)=y(a-b\log y)(v)$ (w) (d) None of these

A.
$$x = y(a - b\log y)$$

 $\mathsf{B.}\log_x = by^2 + a$

$$\mathsf{C}.\,x^2 = y(a - b\log y)$$

D. None of these

Answer: A

64. The family of curves represented by $\frac{dy}{dx} = \frac{x^2 + x + 1}{y^2 + y + 1}$ and the family represented by $\frac{dy}{dx} + \frac{y^2 + y + 1}{x^2 + x + 1} = 0$

A. Touch each other

B. Are orthogonal

C. Are one and the same

D. None of these

Answer: B

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65. A normal at P(x, y) on a curve meets the x-axis at Q and N is the foot of the ordinate at P. If $NQ = \frac{x(1+y^2)}{1+x^2}$, then the equation of curve given that it passes through the point (3, 1) is

A.
$$x^2-y^2=8$$

 $\mathsf{B}.\,x^2+2y^2=11$

$$\mathsf{C}.\,x^2-5y^2=4$$

D. None of these

Answer: C

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66. A curve is such that the mid-point of the portion of the tangent intercepted between the point where the tangent is drawn and the point where the tangent meets the y-axis lies on the line y = x. If the curve (1, 0).passes through then the curve is (a) $(b)(c)2y=(d)x^{\,(\,e\,)\,2\,(\,f\,)}\,(g)-x(h)$ (i) (b) $(j)(k)y = (l)x^{\,(\,m\,)\,2\,(\,n\,)}\,(o) - x(p)$ (q) (c) $(d)(e)y = x - (f)x^{(g)2(h)}(i)(j)$ (k) (d) $(l)(m)y=2ig((n)(o)x-(p)x^{\,(\,q\,)\,2\,(\,r\,)}\,(s)(t)ig)(u)$ (V)

A. $2y = x^2 - x$

 $\mathsf{B}.\, y = x^2 - x$

 $\mathsf{C}.\, y = x - x^2$

D.
$$y=2ig(x-x^2ig)$$

Answer: C



67. The normal to a curve at P(x, y) meet the x-axis at G. If the distance of G from the origin is twice the abscissa of P, then the curve is a (a) parabola (b) circle (c) hyperbola (d) ellipse

A. parabola

B. circle

C. hyperbola

D. ellipse

Answer: C

68. The x-intercept of the tangent to a curve is equal to the ordinate of the point of contact. The equation of the curve through the point (1,1) is

A.
$$ye^{x/y} = e$$

B. $xe^{x/y} = e$
C. $xe^{y/x} = e$
D. $ye^{y/x} = e$

Answer: A



69. The equation of a curve passing through (1,0) for which the product of the abscissa of a point P and the intercept made by a normal at P on the x-axis equal twice the square of the radius vector of the point P is (a) $(b)(c)(d)x^{(e)2(f)}(g) + (h)y^{(i)2(j)}(k) = (l)x^{(m)4(n)}(o)(p)$ (q) (b) $(r)(s)(t)x^{(u)2(v)}(w) + (x)y^{(y)2(z)}(aa) = 2(bb)x^{(cc)4(dd)}(ee)(ff)$ (gg) (c) $(d)(e)(f)x^{(g)2(h)}(i) + (j)y^{(k)2(l)}(m) = 4(n)x^{(o)4(p)}(q)(r)$ (s) (d) None of these

A. $x^2+y^2=x^4$ B. $x^2+y^2=2x^4$ C. $x^2+y^2=4x^4$

D. None of these

Answer: A

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70. The curve with the property that the projection of the ordinate on the normal is constant and has a length equal to a is (a) $(b)(c)a1n\left((d)(e)\sqrt{(f)(g)(h)y^{(i)2(j)}(k) - (l)a^{(m)2(n)}(o)(p)}(q) + y(r)\right)$ (t)
(u) $(v)(w)x + \sqrt{(x)(y)(z)a^{(aa)2(bb)}(cc) - (dd)y^{(ee)2(ff)}(ag)(hh)}(ii) = c(i)$

$$(zz)(aaa)ay = (bbb)(c)\tan^{(ddd)(eee)-1(fff)}(ggg)((hhh)(iii)x + c(jjj))(k$$

A.
$$a \ln \left(\sqrt{y^2-a^2}\right) = x+c$$

B. $x+\sqrt{a^2-y^2} = c$
C. $(y-a)^2 = cx$

D.
$$ay = \tan^{-1}(x + c)$$

Answer: A

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71. Spherical rain drop evaporates at a rate proportional to its surface area. The differential equation corresponding to the rate of change of the radius of the rain drop if the constant of proportionality is K > 0 is (a)

$$(b)(c)(d)rac{(e)dy}{f}((g)dt)(h)(i)+K=0(j)$$
 (k) (b)

$$(l)(m)(n)rac{(o)dr}{p}((q)dt)(r)(s)-K=0(t)$$
 (u) (c)
 $(d)(e)(f)rac{(g)dr}{h}((i)dt)(j)(k)=Kr(l)$ (m) (d) None of these

A.
$$rac{dr}{dt}+K=0$$

B. $rac{dr}{dt}-K=0$

C.
$$rac{dr}{dt}=Kr$$

D. None of these

Answer: A

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72. Water is drained from a vertical cylindrical tank by opening a value at the base of the tank. It is known that the rate at which the water level drops is proportional to the square root of water depth y, where the constant of proprortionality k > 0 depends on the acceliration due to gravity and the geomety of the hole. If is measured in minutes and $k = \frac{1}{15}$ then the time of drain the tank, If the water is 4 m deep to start with is

A. 30 min

B. 45 min

C. 60 min

D. 80 min

Answer: C



73. The population of a country increases at a rate proportional to the number of inhabitants. f is the population which doubles in 30 years, then the population will triple in approximately. (a) 30 years (b) 45 years (c) 48 years (d) 54 years

A. 30 years

B. 45 years

C. 48 years

D. 54 years

Answer: C

74. An object falling from rest in air is subject not only to the gravitational force but also to air resistance. Assume that the air resistance is proportional to the velocity with constant of proportionality as k > 0, and acts in a direction opposite to motion $\left(g = 9.8 \frac{m}{s^2}\right)$. Then velocity cannot exceed. (a)9.8m/k m/s (b) 98/km m/s (c) k/g m/s (d) None of these

A. 9.8/km/s

B. 98/k m/s

C.
$$\frac{k}{9.8}m/x$$

D. None of these

Answer: A

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MULTIPLE CORRECT ANSWERS TYPE

1. Which one of the following function(s) is/are homogeneous? $(a)f(x,y) = \frac{x-y}{x^2+y^2} \quad \text{(b)} \quad f(x,y) = x^{\frac{1}{3}}y^{-\frac{2}{3}}\tan^{-1}\left(\frac{x}{y}\right) \quad \text{(c)}$ $f(x,y) = x\left(\ln\sqrt{x^2+y^2} - \ln y\right) + ye^{\frac{x}{y}} \text{ (d) none of these}$

$$\begin{array}{l} \mathsf{A.}\ f(x,y) = \frac{x-y}{x^2+y^2} \\ \mathsf{B.}\ f(x,y) = x^{\frac{1}{3}}y^{-\frac{2}{3}}\frac{\tan^{-1}x}{y} \\ \mathsf{C.}\ f(x,y) = x\Big(\ \ln \ \sqrt{x}^2+y^2\Big) - \ \ln \ y+ye^{x/y} \\ \mathsf{D.}\ f(x,y) = x\Big[\ \ln \ (2x^2+y^2)x - \ \ln \ (x+y)\Big] + y^2\frac{\tan(x+2y)}{3x-y} \end{array}$$

Answer: A::B::C

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2. For the differential equation whose solution is $(x - h)^2 + (y - k)^2 = a^2$ (a is a constant), its (a) order is 2 (b) order is 3 (c) degree is 2 (d) degree is 3

A. order is 2

B. order is 3

C. degree is 2

D. degree is 3

Answer: A::C

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3. The equation of the curve satisfying the differential equation

 $y igg(rac{dy}{dx} igg)^2 + (x-y) rac{dy}{dx} - x = 0$ can be a (a) circle (b) Straight line (c)

Parabola (d) Ellipse

A. Circle

B. Straight line

C. Parabola

D. Ellipse

Answer: A::B

4. Which of the following equation(s) is/are linear?

A.
$$\frac{dy}{dx} + \frac{y}{x} = \log x$$

B. $y\frac{dy}{dx} + 4x = 0$

C.
$$\left(2x+y^3
ight)rac{dy}{dx}=3y$$

D. None of these

Answer: A::C



5. The solution of
$$\frac{dy}{dx} = \frac{ax+h}{by+k}$$
 represent a parabola when (a)
 $(b)(c)a = 0, b \neq 0(d)$ (e) (b) $(f)(g)a \neq 0, b \neq 0(h)$ (i) (c)
 $(d)(e)b = 0, a \neq 0(f)$ (g) (d) $(h)(i)a = 0, b \in R(j)$ (k)

A. a=0, b
eq 0

 $\mathsf{B}.\,a\neq 0, b\neq 0$

C. $b = 0, a \neq 0$

D. $a = 0, b \in R$

Answer: A::C

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6. The equation of the curve satisfying the differential equation $y_2(x^2 + 1) = 2xy_1$ passing through the point (0,1) and having slope of tangent at x = 0 as 3 (where y_2 and y_1 represent 2nd and 1st order derivative), then (a) (b)(c)y = f((d)x(e))(f) (g) is a strictly increasing function (h) (i)(j)y = f((k)x(l))(m) (n) is a non-monotonic function (o) (p)(q)y = f((r)x(s))(t) (u) has a three distinct real roots (v) (w)(x)y = f((y)x(z))(aa) (bb) has only one negative root.

A. y = f(x) is a strictly increasing function

B. y = f(x) is a non-monoatomic function

C. y = f(x) has three distinct real root

D. y = f(x) has only one negative root

Answer: A::D



7. Identify the statement(s) which is/are true.

A.
$$f(x, y) = e^{y/x} = e^{\frac{y}{x}} + \frac{\tan y}{x}$$
 is a homogeneous of degree zero.
B. $x \ln \frac{y}{x} dx + \frac{y^2}{x} \frac{\sin^{-1} y}{x} dx = 0$ is a homogenous differential

equation.

C. $f(x,y)=x^2+\sin x\cos y$ is a non-homogenous

D. $ig(x^2+y^2ig)dx-ig(xy^2-y^3ig)dy=0$ is a homogenous differential

equationn.

Answer: A::B::C

8. The graph of the function y = f(x) passing through the point (0,1) and satisfying the differential equation $\frac{dy}{dx} + y \cos x = \cos x$ is such that (a) it is a constant function. (b) it is periodic (c) it is neither an even nor an odd function. (d) it is continuous and differentiable for all $(e)(f)x\dot{g}(h)$

A. It is constant function

B. It is periodic

C. it is neither an even nor an odd function.

D. it is continuous and differentiable for all x

Answer: A::B::D



9. If f(x), g(x) be twice differentiable functions on [0,2] satisfying f''(x) = g''(x), f'(1) = 2g'(1) = 4 and f(2) = 3g(2) = 9, then

f(x)-g(x) at x = 4 equals (A) 0 (B) 10 (C) 8 (D) 2

A.
$$f(4) - g(4) = 10$$

B. $|f(x) - g(x)| < 2 \Rightarrow -2 < x < 0$
C. $f(2) = g(2) \Rightarrow x = -1$
D. $f(x) - g(x) = 2x$ has real root

Answer: A::B::C

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10. The solution of the differential equation $(x^2y^2 - 1)dy + 2xy^3dx = 0$ is (a) $(b)(c)1 + (d)x^{(e)2(f)}(g)(h)y^{(i)2(j)}(k) = cx(l)$ (m) (b) $(n)(o)1 + (p)x^{(q)2(r)}(s)(t)y^{(u)2(v)}(w) = cy(x)$ (y) (c) (d)(e)y = 0(f)(g) (d) $(h)(i)y = -(j)\frac{1}{k}((l)(m)x^{(n)2(o)}(p))(q)(r)(s)$ (t)

A.
$$1+x^2y^2=cx$$

B. $1+x^2y^2=cy$
C. $y=0$

D.
$$y=~-~rac{1}{x^2}$$

Answer: B

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11.
$$y = ae^{-\frac{1}{x}} + b$$
 is a solution of $\frac{dy}{dx} = \frac{y}{x^2}$, then (a) $(b)(c)a \in R(d)$ (e)
(b) 0 (c) $(d)(e)b = 1(f)$ (g) (d) $(h)a(i)$ (j) takes finite number of values

A. $x\in R-\{0\}$

 $\mathsf{B}.\,b=0$

 $\mathsf{C}.\,b=1$

D. a takes finite number of values

Answer: A::B

12. For the equation of the curve whose subnormal is constant then,

A. its eccentricity is 1

B. its eccentricity is $\sqrt{2}$

C. its axis is the x-axis

D. its axis is the y-axis

Answer: B

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13. The solution of
$$rac{xdd+ydy}{xdy-ydx}=\sqrt{rac{1-x^2-y^2}{x^2+y^2}}$$
 is (a) [Math Processing

Error] (dd) (ee) [Math Processing Error] (hhh) (iii)

$$egin{aligned} (jjj)(kkk) &\sqrt{(lll)(mmm) \Big(igcap) x^{(ooo)\,2\,(ppp)}\,(qqq) + (rrr) y^{(sss)\,2\,(ttt)}\,(uuu)} \ &= \Big(an \Big\{si(imes x) n^{(yyy)\,(zzz)\,-1\,(aaaa)}\,(bbbb) \Big((cccc)(dddd)(eeee) rac{y}{ffff} x(eee) \Big\} \Big\} \ &= (ext{kkk}) \ (ext{lll}) \end{aligned}$$

$$(mmmm) \left(\bigcap n\right) y$$

+ $x \tan\left((oooo)(pppp)c + (qqqq)(rrrr)\sin^{(ssss)(tt)-1(uuuu)}(vvvv)\sqrt{(www}(jjjjj))\right)$
(kkkk)

A.
$$\sqrt{x^2 + y^2} = \sin\{(\tan^{-1}y/x) + C\}$$

B. $\sqrt{x^2 + y^2} = \cos\{(\tan^{-1}y/x) + C\}$
C. $\sqrt{x^2 + y^2} = (\tan(\sin^{-1}y/x) + C)$
D. $y = x \tan(c + \sin^{-1}\sqrt{x^2 + y})$

Answer: A::D

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14. Find the curves for which the length of normal is equal to the radius vector.

A. circles

B. rectangular hyperbola
C. ellipses

D. straight lines

Answer: A::B

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15. In which of the following differential equation degree is not defined? (a) [Math Processing Error] (uu) (vv) [Math Processing Error] (pppp) (qqqq) [Math Processing Error] (ddddd) (eeeee) $(fffff)(ggggg)x - 2y = \log\left((hhhhh)(iiiii)(jjjjj)\frac{(kkkk)dy}{lllll}((mmmr))\right)$

A.
$$\displaystyle rac{d^2y}{dx^2}+3igg(rac{dy}{dx}igg)^2=xrac{\log(d^2y)}{dx^2}$$

B. $\displaystyle rac{d^2y}{ig(dx^2ig)^2}+igg(rac{dy}{dx}ig)^2=xrac{\sin(d^2y)}{dx^2}$
C. $\displaystyle x=rac{\sin(dy)}{dx}-2y, |x|<1$
D. $\displaystyle x-2y=rac{\log(dy)}{dx}$

Answer: A::B



16. If y = f(x) is the solution of equation $y dx + dy = -e^x y^2$ dy, f(0)=1

and area bounded by the curve $y=f(x), y=e^x$ and x=1 is A, then

A. curve y=f(x) is passing through (-2, e).

B. Curve y = f(x) is passing through (1, 1/e)

C. curve y = f(x) is passing through (1,1/3)

D.
$$A=e+rac{2}{\sqrt{e}}-3$$

Answer: A::D



17. A particle falls in a medium whose resistance is proportional to the square of the velocity of the particles. If the differential equation of the

free fall is $\displaystyle rac{dv}{dt} = g - k v^2$ (k is constant) then

A.
$$v = 2\sqrt{rac{g}{k}} rac{e^{2t\sqrt{g/t}} + 1}{e^{2r\sqrt{g/k}} - 1}$$

B. $v = \sqrt{rac{g}{k}} rac{e^{2t\sqrt{gk}} - 1}{e^{2t\sqrt{gk}} + 1}$
C. $v o 0$ as $t o \infty$
D. $v o \sqrt{rac{g}{k}}$ as $t o \infty$

Answer: B::D

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Linked Comprehension types

1. For certain curves y= f(x) satisfying $\frac{d^2y}{dx^2} = 6x - 4$, f(x) has local minimum value 5 when x=1.9. Number of critical point for y=f(x) for x â, [0,2] (a) 0 (b)1. c).2 d) 3 10. Global minimum value y = f(x) for x â, [0,2] is (a)5 (b)7 (c)8 d) 9 11 Global maximum value of y = f(x) for x â, [0,2] is (a) 5 (b) 7 (c) 8 (d) 9

| A. 0 | |
|------|--|
| B. 1 | |
| C. 2 | |

Answer: C

D. 3

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2. For certain curve y = f(x) satisfying $\frac{d^2y}{dx^2} = 6x - 4, f(x)$ has local minimum value 5 when x = 1

The number of critical point for y=f(x) for $x\in [0,2]$ is

A. 5 B. 7

C. 8

D. 9

Answer: A



3. For certain curve y=f(x) satisfying $\displaystyle rac{d^2y}{dx^2}=6x-4,\,f(x)$ has local

minimum value 5 when x=1

Global maximum value of y=f(x) for $x\in [0,2]$ is

A. 5

B. 7

C. 8

D. 9

Answer: B

4. The differential equation y = px + f(p),(i) where $p = \frac{dy}{dx}$, is known as Clairout's equation. To solve equation i) differentiate it with respect to x, which gives either $\frac{dp}{dx} = 0 \Rightarrow p = c$(ii) or $x + f^i(p) = 0$(iii) Which of the following is true about solutions of differential equation $y = xy' + \sqrt{1 + y'^2}$?

A. the general solution of equation is family of parabolas

B. the general solution of equation is family of circles

C. the singular solution of equation is circle

D. the singular solution of equation is ellipse

Answer: C

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5. The differential equation y = px + f(p),(i)

where $p = \frac{dy}{dx}$, is known as Clairout's equation. To solve equation i) differentiate it with respect to x, which gives either

$$rac{dp}{dx}=0 \Rightarrow p=c$$
.....(ii)
or $x+f^i(p)=0$(iii)

The number of solution of the equation $f(x)=\ -1$ and the singular

solution of the equation
$$y=xrac{dy}{dx}+\left(rac{dy}{dx}
ight)^2$$
 is

| A. 1 | |
|------|--|
| B. 2 | |
| C. 4 | |
| D. 0 | |

Answer: B

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6. The differential equation y = px + f(p),(i)

where $p = \frac{dy}{dx}$, is known as Clairout's equation. To solve equation i) differentiate it with respect to x, which gives either

$$rac{dp}{dx}=0 \Rightarrow p=c$$
.....(ii)

or $x+f^i(p)=0$(iii)

The singular solution of the differential equation $y = mx + m - m^3$, where $m = \frac{dy}{dx}$, passes through the point.

A. (0,0)

B. (0,1)

C. (1,0)

D. (-1,0)

Answer: D

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7. Let f(x) be a non-positive continuous function and $F(x) = \int_0^x f(t)dt \, \forall x \ge 0$ and $f(x) \ge cF(x)$ where c < 0 and let $g: [0, \infty) \to R$ be a function such that $\frac{dg(x)}{dx} < g(x) \, \forall x > 0$ and g(0) = 0

The total number of root(s) of the equation f(x)=g(x) is/ are

| A. ∞ | |
|-------------|--|
| B. 1 | |
| C. 2 | |
| D. 0 | |

Answer: B

Watch Video Solution

8. Let
$$f(x)$$
 be a non-positive continuous function and $F(x) = \int_0^x f(t)dt \, \forall x \ge 0$ and $f(x) \ge cF(x)$ where $c < 0$ and let $g: [0, \infty) \to R$ be a function such that $\frac{dg(x)}{dx} < g(x) \, \forall x > 0$ and $g(0) = 0$

The number of solution(s) of the equation

$$\left|x^2+x-6
ight|=f(x)+g(x)$$
 is/are

A. 2

B. 1

C. 0

D. 3

Answer: C

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9. Let
$$f(x)$$
 be a non-positive continuous function and $F(x) = \int_0^x f(t)dt \, \forall x \ge 0$ and $f(x) \ge cF(x)$ where $c < 0$ and let $g: [0,\infty) \to R$ be a function such that $\frac{dg(x)}{dx} < g(x) \, \forall x > 0$ and $g(0) = 0$

The solution set of inequation $g(x)igl(\cos^{-1}x-\sin^{-1}igr)\le 0$

A.
$$\begin{bmatrix} -1, \frac{1}{\sqrt{2}} \\ B. \begin{bmatrix} \frac{1}{\sqrt{2}}, 1 \end{bmatrix}$$

C.
$$\begin{bmatrix} 0, \frac{1}{\sqrt{2}} \end{bmatrix}$$

D.
$$\begin{bmatrix} 0, \frac{1}{\sqrt{2}} \end{bmatrix}$$

Answer: A



10. A curve C with negative slope through the point (0, 1) lies in the first quadrant. The tangent at any point P on it meets the x-axis at Q such that PQ = 1. Then the curve in parametric for is

A.
$$x = \cos heta + \log_e an(heta/2), y = \sin heta$$

 $\texttt{B.} \, x = \, -\cos\theta + \log_e \tan(\theta/2), y = \sin\theta$

C. $x=\ -\cos heta-\log_e an heta/2, y=\sin heta$

D. None of these

Answer: C

11. A curve 'C' with negative slope through the point(0,1) lies in the I Quadrant. The tangent at any point 'P' on it meets the x-axis at 'Q'. Such that PQ = 1. Then

The area bounded by 'C' and the co-ordinate axes is

A. 1

 $\mathsf{B.}\log_e 2$

C. $\pi / 4$

D. $\pi/2$

Answer: C

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12. A curve C with negative slope through the point (0, 1) lies in the first quadrant. The tangent at any point P on it meets the x-axis at Q such that PQ = 1. Then the curve in parametric for is

A. Circles

B. Parabolas

C. Ellipses

D. Hyperbolas

Answer: A

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13. Let
$$y=f(x)$$
 satisfies the equation $f(x)=ig(e^{-x}+e^xig)\cos x-2x-\int_0^x(x-t)f'(t)dt$ y satisfies the

differential equation

A.
$$\frac{dy}{dx} + y = e^x(\cos x - \sin x) - e^{-x}(\cos x + \sin x)$$

B. $\frac{dy}{dx} - y = e^x(\cos x - \sin x) + e^{-x}(\cos x + \sin x)$
C. $\frac{dy}{dx} + y = e^x(\cos x + \sin x) - e^{-x}(\cos x - \sin x)$
D. $\frac{dy}{dx} - y = e^x(\cos x - \sin x) + e^{-x}(\cos x - \sin x)$

Answer: A



14. Let y = f(x) satisfies the equation

$$f(x)=ig(e^{-x}+e^xig){\cos x}-2x+\int_0^x(x-t)f'(t)dt$$

The value of $f(0)+f^{\,\prime}\left(0
ight)$ equal (a) -1 (b) 0 (c) 1 (d) none of these

A. - 1

B. 0

C. 1

D. 1

Answer: B

15. Let y = f(x) satisfies the equation

$$f(x) = ig(e^{-x} + e^x ig) \cos x - 2x + \int_0^x (x-t) f'(t) dt$$

y satisfies the differential equation

$$A. e^{-x}(\cos x - \sin x) + \frac{e^x}{5}(3\cos x + \sin x) + \frac{2}{5}e^{-x}$$

$$B. e^{-x}(\cos x + \sin x) + \frac{e^x}{5}(3\cos x - \sin x) - \frac{2}{5}e^{-x}$$

$$C. e^{-x}(\cos x - \sin x) + \frac{e^x}{5}(3\cos x - \sin x) + \frac{2}{5}e^{-x}$$

$$D. e^{-x}(\cos x + \sin x) + \frac{e^x}{5}(3\cos x - \sin x) - \frac{2}{5}e^{-x}$$

Answer: C

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16. A certain radioactive material is known to decay at a rate proportional to the amount present. If initially there is 50 kg of the material present and after two hours it is observed that the material has lost 10% of its original mass, find () and expression for the mass of the material remaining at any time t, (ii) the mass of the material after four hours and

(iii) the time at which the material has decayed to one half of its initial mass.

A.
$$N = 50 e^{(1/2)(\ln 9)t}$$

B. $50e^{(1/4)(\ln 9)t}$

C. $N = 50e^{-(\ln 0.9)t}$

D. None of these

Answer: A

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17. A certain radioactive material is known to decay at a rate proportional to the amount present. Initially there is 50 kg of the material present and after 2h it is observed that the material has lost 10 percent of its original mass. Based on these data answer the following questions.

The time at which the material has decayed to one half of its initial mass

A. $50^{-0.5}$ ln 9

B. $50e^{-2 \ln 9}$

C. $50e^{-2 \ln 0.9}$

D. None of these

Answer: C



18. A certain radioactive material is known to decay at a rate proportional to the amount present. If initially there is 50 kg of the material present and after two hours it is observed that the material has lost 10% of its original mass, find () and expression for the mass of the material remaining at any time t, (ii) the mass of the material after four hours and (iii) the time at which the material has decayed to one half of its initial mass.

A.
$$\frac{\ln \ 0.25}{\ln \ 0.9}h$$

B.
$$\frac{\ln \ 0.5}{\ln \ 0.81}h$$

C. $\frac{\ln \ 0.25}{\ln \ 0.81}h$

D. None of these

Answer: C

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19. Consider a tank which initially holds V_0 liter of brine that contains a lb of salt. Another brine solution, containing b lb of salt per liter is poured into the tank at the rate of eL/\min . The problem is to find the amount of salt in the tank at any time t.

Let Q denote the amount of salt in the tank at any time. The time rate of change of Q, $\frac{dQ}{dt}$, equals the rate at which salt enters the tank at the rate at which salt leaves the tank. Salt enters the tank at the rate of be lb/min. To determine the rate at which salt leaves the tank, we first calculate the volume of brine in the tank at any time t, which is the initial volume V_0 plus the volume of brine added et minus the volume of brine removed ft.

Thus, the volume of brine at any time is

$$V_0 + et - ft$$

The concentration of salt in the tank at any time is $Q/(V_0 + et - ft)$, from which it follows that salt leaves the tank at the rate of $f\left(\frac{Q}{V_0 + et - ft}\right)$ lb/min. Thus, $\frac{dQ}{dt} = be - f\left(\frac{Q}{V_0 + et - ft}\right)Q = be$

A tank initially holds 100 L of a brine solution containing 20 lb of salt. At t=0, fresh water is poured into the tank at the rate of 5 L/min, while the well-stirred mixture leaves the tank at the same rate. Then the amount of salt in the tank after 20 min.

A. 20/e

B. 10/e

 $\mathsf{C.}\,40\,/\,e^2$

D. 5/e L

Answer: A

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20. A 50 L tank initailly contains 10 L of fresh water, At t=0, a brine solution containing 1 lb of salt per gallon is poured into the tank at the rate of 4 L/min, while the well-stirred mixture leaves the tank at the rate of 2 L/min. Then the amount of time required for overflow to occur in

A. 30 min

B. 20 min

C. 10 min

D. 40 min

Answer: B

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21. In the above question, the amount of salt in the tank at the moment

of overflow is

B. 50 lb

C. 30 lb

D. None of these

Answer: D

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Numerical value type

1. If y = y(x) and it follows the relation $4xe^{xy} = y + 5\sin^2 x$, then y'(0) is equal to_____

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2. If
$$x rac{dy}{xt} = x^2 + y - 2, \, y(1) = 1, ext{ then } y(2) ext{ equal}$$

3. If the dependent variable y is changed to z by the substitution method

y=tanz then the differential equation $d^2 \frac{y}{dx^2} = 1 + 2 \frac{1+y}{1+y^2} \left(\frac{dy}{dx}\right)^2$ is changed to $d^2 \frac{z}{dx^2} = \cos^2 z + k \left(\frac{dz}{dx}\right)^2$ then find the value off k

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4. Let y = y(t) be a solution to the differential equation $y' + 2ty = t^2$, then $16(\lim_{t \to \infty} \frac{y}{t}$ is_____ Watch Video Solution 5. If the solution of the differential equation $\frac{dy}{dx} = \frac{1}{x \cos y + \sin 2y}$ is $x = ce^{\sin y} - k(1 + \sin y)$, then the value of k is_____ **6.** If the independent variable x is changed to y, then the differential

equation
$$x \frac{d^2 y}{dx^2} + \left(\frac{dy}{dx}\right)^3 - \frac{dy}{dx} = 0$$
 is changed to $x \frac{d^2 x}{dy^2} + \left(\frac{dx}{dy}\right)^2 = k$ where k equals____

7. Let y_1 and y_2 be two different solutions of the equation

 $rac{dy}{dx}+P(x).\ y=Q(x).$ Then $lpha y_1+eta y_2$ will be solution of the given equation if $lpha+eta=\ldots\ldots\ldots$

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8. Tangent is drawn at the point (x_i, y_i) on the curve y = f(x), which intersects the x-axis at $(x_{i+1}, 0)$. Now, again a tangent is drawn at (x_{i+1}, y_{i+1}) on the curve which intersect the x-axis at $(x_{i+2}, 0)$ and the process is repeated n times, i.e. i = 1, 2, 3; n. If $x_1, x_2, x_3, ; x_n$ from an arithmetic progression with common difference equal to $(\log)_2 e$ and



and the origin is $e,\,\,{
m then}$ the value of $5e^2$ is___

11. If the solution of the differential equation $\frac{dy}{dx} - y = 1 - e^{-x}$ and $y(0) = y_0$ has a finite value, when $x \stackrel{\rightarrow}{\infty}$, then the value of $\left| \frac{2}{y_0} \right|$ is______

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12. Let f be a function defined on the interval $[0, 2\pi]$ such that $\int_0^x (f'(t) - \sin 2t) dt = \int_x^0 f(t) \tan t dt$ and f(0) = 1. Then the maximum value of f(x) is.....

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13. Let
$$y(x)$$
 be a function satisfying $d^2y/dx^2 - dy/dx + e^{2x} = 0, y(0) = 2$ and $y'(0) = 1$. If maximum

value of y(x) is y(lpha), Then Integral part of (2lpha) is



14. Let f be a real-valued differentiable function on R (the set of all real numbers) such that f(1) = 1. If the $y - \in tercept$ of the tangent at any point P(x, y) on the curve y = f(x) is equal to the cube of the abscissa of P, then the value of f(-3) is equal to _____

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15. Let
$$y'(x)+y(x)g'(x)=g(x)g'(x),y(0),x\in R,$$
 where $f'(x)$

denotes $\frac{dy(x)}{dx}$, and g(x) is a given non-constant differentiable function on R with g(0) = g(2) = 0. Then the value of y(2) is_____

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16. Let $f\colon [1,\infty]$ be a differentiable function such that f(1)=2. If $6{\int_1^x f(t)dt}=3xf(x)-x^3$ for all $x\ge 1,$ then the value of f(2) is

17. Let $f \colon R \to R$ be a differentiable function with f(0) = 0. If y = f(x)

satisfies the differential equation

 $rac{dy}{dx}=(2+5y)(5y-2)$, then the value of $\lim_{x
ightarrow\infty}~f(x)$ is

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Archives

1. The differential equaiotn which represents the family of curves $y = C_1 e^{C_2 x}$, where C_1 and C_2 are arbitrary constants, is

A.
$$y' = y^2$$

B. $y'' = y'y$
C. $yy'' = y'$
D. $yy'' = (y')^2$

Answer: D

2. Solution of the following equation

 $\cos x \, \mathrm{d}y$ =y(sinx-y)dx, $0 < x < rac{\pi}{2}$ is

A.
$$an x = (\sec x + c)y$$

 $\mathsf{B.} \sec x = (\tan x + c)y$

 $\mathsf{C}.\,y\sec x=\tan x+c$

 $\mathsf{D}.\,y\tan x = \sec x + c$

Answer: B

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3. Let I be the purchase value of an equipment and V(t) be the value after it has been used for t years. The value V(t) depreciates at a rate given by differential equation $\left(dV\frac{t}{dt} = -k(T-t)\right)$, where k > 0 is a constant and T is the total life in years of the equipment. Then the scrap value V(T) of the equipment is :

(1)
$$T^{2} - \frac{1}{k}$$

(2) $I - \frac{kT^{2}}{2}$
(3) $I - \frac{k(T-t)^{2}}{2}$
(4) e^{-kT}
A. e^{-kT}
B. $T^{2} - \frac{I}{k}$
C. $I - \frac{kT^{2}}{2}$
D. $I - \frac{k(T-t)^{2}}{2}$

Answer: C

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4. If
$$rac{dy}{dx} = y+3 ext{ and } y(0) = 2$$
, then y(ln 2) is equal to

 $\mathsf{A.}-2$

B. 7

C. 5

D. 13

Answer: B

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5. A spherical balloon is filled with 4500p cubic meters of helium gas. If a leak in the balloon causes the gas to escape at the rate of 72π cubic meters per minute, then the rate (in meters per minute) at which the radius of the balloon decreases 49 minutes after the leakage began is (1) $\frac{9}{7}$ (2) $\frac{7}{9}$ (3) $\frac{2}{9}$ (4) $\frac{9}{2}$

A.
$$\frac{9}{7}$$

B. 7/9

C.2/9

D. None of these

Answer: C



6. The population p(t) at time t of a certain mouse species satisfies the differential equation $\frac{dp(t)}{dt} = 0.5p(t) - 450$. If p(0) = 850, then the time at which the population becomes zero is

A. 2 ln 18

B. ln 9

C.
$$\frac{1}{2}$$
 ln 18

D. ln 18

Answer: A

7. At present, a firm is manufacturing 2000 items. It is estimated that the rate of change of production P w.r.t. additional number of workers x is given by $\frac{dP}{dx} = 100 - 12\sqrt{x}$. If the firm employs 25 more workers, then the new level of production of items is (1) 3000 (2) 3500 (3) 4500 (4) 2500

A. 3000

B. 3500

C. 4500

D. 2500

Answer: C

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8. Let the population of rabbits surviving at a time t be governed by the differential equation $\frac{dp(t)}{dt} = \frac{1}{2}p(t) - 200$. If p(0) = 100, then p(t) equals (1) $400 - 300e^{t/2}$ (2) $300 - 200e^{-t/2}$ (3) $600 - 500e^{t/2}$ (4) $40 - 300e^{-t/2}$

A. $400 - 300e^{t/2}$

- B. $200 200e^{-t/2}$
- C. $600 500e^{t/2}$
- D. $40 300e^{-t/2}$

Answer: A

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9. Let y(x) be the solution the differential equation $(x \log x) \frac{dy}{dx} + y = 2x \log x, (x \ge 1)$. Then $y \in$ is equal to

A. e

B. 0

C. 2

D. 2e

Answer: C

10. If a curve y=f(x) passes through the point (1, -1) and satisfies the differential equation , y(1+xy)dx=xdy , then $f\left(-rac{1}{2}
ight)$ is equal

to:

A.
$$-\frac{4}{5}$$

B. $\frac{2}{5}$
C. $\frac{4}{5}$
D. $-\frac{2}{5}$

Answer: C

11. If
$$(2 + \sin x) \frac{dy}{dx} + (y + 1) \cos x = 0$$
 and $y(0) = 1$, then $y\left(\frac{\pi}{2}\right)$ is equal to

A.
$$\frac{4}{3}$$

B. $\frac{1}{3}$
C. $-\frac{2}{3}$
D. $-\frac{1}{3}$

Answer: B

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12. Let y=g(x) be the solution of the differential equation $rac{\sin(dy)}{dr}+y\cos x=4x, x\in(0,\pi)$ If y(pi/2)=0, theny(pi/6)` is equal to

A.
$$-\frac{4}{9}\pi^2$$

B. $\frac{4}{9\sqrt{3}}\pi^2$
C. $-\frac{8}{9\sqrt{3}}\pi^2$
D. $-\frac{8}{9}\pi^2$

Answer: D

Jee advanced

1. A curve passes through the point $\left(1, \frac{\pi}{6}\right)$. Let the slope of the curve at each point (x, y) be $\frac{y}{x} + \sec\left(\frac{y}{x}\right), x > 0$. Then the equation of the curve is (a) $(b)(c)\sin\left((d)(e)(f)\frac{y}{g}x(h)(i)(j)\right) = \log x + (k)\frac{1}{l}2(m)(n)(o)$ (p) (q) $(r)(s)\cos \sec\left((t)(u)(v)\frac{y}{w}x(x)(y)(z)\right) = \log x + 2(aa)$ (bb) (cc) $(dd)(ee)\sec\left((ff)(gg)(hh)\frac{(ii)2y}{ii}x(kk)(ll)(mm)\right) = \log x + 2(nn)$

(oo) (pp) [Math Processing Error] (fff)

A.
$$\sin\left(\frac{y}{x}\right) = \log x + \frac{1}{2}$$

B. $\csc\left(\frac{y}{x}\right) = \log x + 2$
C. $\frac{\sec(2y)}{x} = \log x + 2$
D. $\frac{\cos(2y)}{x} = \log x + \frac{1}{2}$

Answer: A
2. The function y = f(x) is the solution of the differential equation $\frac{dy}{dx} + \frac{xy}{x^2 - 1} = \frac{x^4 + 2x}{\sqrt{1 - x^2}} \text{ in } (-1, 1) \text{ satisfying } f(0) = 0. \text{ Then}$ $\int_{\frac{\sqrt{3}}{2}}^{\frac{\sqrt{3}}{2}} f(x)dx \text{ is (a) } (b)(c)(d)\frac{\pi}{e}3(f)(g) - (h)\frac{(i)\sqrt{(j)3(k)}(l)}{m}2(n)(o)(p)$ (q) (b) $(r)(s)(t)\frac{\pi}{u}3(v)(w) - (x)\frac{(y)\sqrt{(z)3(aa)}(bb)}{cc}4(dd)(ee)(ff)$ (gg) (c) $(d)(e)(f)\frac{\pi}{g}6(h)(i) - (j)\frac{(k)\sqrt{(l)3(m)}(n)}{o}4(p)(q)(r)$ (s) (d) $(t)(u)(v)\frac{\pi}{w}6(x)(y) - (z)\frac{(aa)\sqrt{(bb)3(cc)}(dd)}{ee}2(ff)(gg)(hh)$ (ii)

A.
$$\frac{\pi}{3} - \frac{\sqrt{3}}{2}$$

B. $\frac{\pi}{3} - \frac{\sqrt{3}}{4}$
C. $\frac{\pi}{6} - \frac{\sqrt{3}}{4}$
D. $\frac{\pi}{6} - \frac{\sqrt{3}}{2}$

Answer: B

3. If
$$y = y(x)$$
 satisfies the differential equation
 $8\sqrt{x}\left(\sqrt{9+\sqrt{x}}\right)dy = \left(\sqrt{4+\sqrt{9+\sqrt{x}}}\right)^{-1}dx, x > 0 and y(0) = \sqrt{7},$ then $y(256) =$ 16 (b) 80 (c) 3 (d) 9



Answer: A

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Multiple Correct Answerts type

1. If y(x) satisfies the differential equation $y'-y \tan x = 2x secx$ and y(0)=0 , then (a)

$$(b)(c)y\left((d)(e)(f)\frac{\pi}{g}4(h)(i)(j)\right) = (k)\frac{(l)(m)\pi^{(n)\,2(o)}(p)}{q}\left((r)8\sqrt{(s)2(t)}(r)\right)$$
(y) (b) [Math Processing Error] (xx) (c)

$$(d)(e)y\left((f)(g)(h)\frac{\pi}{i}3(j)(k)(l)\right) = (m)\frac{(n)(o)\pi^{(p)\,2(q)}(r)}{s}9(t)(u)(v)$$

(w) (d) [Math Processing Error] (ddd)

A.
$$y\left(\frac{\pi}{4}\right) = \frac{\pi^2}{8\sqrt{2}}$$

B. $y'\left(\frac{\pi}{4}\right) = \frac{\pi^2}{18}$
C. $y\left(\frac{\pi}{3}\right) = \frac{\pi^2}{9}$
D. $y'\left(\frac{\pi}{3}\right) = \frac{4\pi}{3} + \frac{2\pi^2}{3\sqrt{3}}$

Answer: A::D

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2. Consider the family of all circles whose centers lie on the straight line y = x. If this family of circles is represented by the differential equation $Py^+Qy'+1=0$, where P, Q are functions of x, y and $y'\left(herey'=\frac{dy}{dx}, y^=\frac{d^2y}{dx^2}\right)$, then which of the following statements is

(are) true? (a)
$$(b)(c)P = y + x(d)$$
 (e) (b) $(f)(g)P = y - x(h)$ (i) (c)
 $(d)(e)P + Q = 1 - x + y + y + (f)(g)((h)(i)y^{(j)'(k)}(l)(m))^{(n)2(o)}(p)$
(r) (s)
 $(t)(u)P - Q = x + y - y - (v)(w)((x)(y)y^{(z)'(aa)}(bb)(cc))^{(dd)2(ee)}(f)$
(hh)
A. $P = y + x$
B. $P = y - x$
C. $P + Q = 1 - x + y + y' + (y')^2$

D.
$$P-Q=x+y-y'-\left(y'
ight)^2$$

Answer: B::C

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3. Let y(x) be a solution of the differential equation $(1+e^x)y'+ye^x=1$. If y(0)=2, then which of the following statements is (are) true? (a) (b)(c)y((d)(e)-4(f))=0(g) (h) (b) (i)(j)y((k)(l)-2(m))=0(n) (o) (c) (d)(e)y((f)x(g))(h) (i) has a critical point in the interval (j)(k)((l)(m) - 1, 0(n))(o) (p) (q) (r)(s)y((t)x(u))(v) (w) has no critical point in the interval (x)(y)((z)(aa) - 1, 0(bb))(cc) (dd)

A.
$$y(-4) = 0$$

B. y(-2) = 0

C. y(x) has a critical point in the interval (-1, 0)

D. y(x) has no critical point in the interval (-1, 0)

Answer: A::C

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4. A solution curve of the differential equation $(x^2 + xy + 4x + 2y + 4) \frac{dy}{dx} - y^2 = 0, x > 0$, passes through the

point (1,3) Then, the solution curve

A. intersects y = x + 2 exactly at one point

B. intersects y = x + 2 exactly at two points

C. intersects $y = (x + 2)^2$

D. does NOT intersect $y = (x + 3)^2$

Answer: A::D

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5. Let $f: R \to R$ and $g: R \to R$ be two non-constant differentiable functions. If $f'(x) = \left(e^{(f(x) - g(x))}\right)g'(x)$ for all $x \in R$, and f(1) = g(2) = 1, then which of the following statement(s) is (are) TRUE? $f(2) < 1 - (\log)_e 2$ (b) $f(2) > 1 - (\log)_e 2$ (c) $g(1) > 1 - (\log)_e 2$ (d) $g(1) < 1 - (\log)_e 2$

A. $f(2) < 1 - \log_e 2$

B. $f(2) > 1 - \log_e(2)$

 $\mathsf{C}.\,g(1) < 1 - \log_e 2$

D. $g(1) < 1 - \log_e 2$

Answer: B::C

Single Correct Answer Type

1. The order of the differential equation whose general solution is $y=c_1\cos 2x+c_2\cos^2 x+c_3\sin^2 x+c_4$ is

A. 2

B. 4

C. 3

D. None of these

Answer: A



2. Order of the differential equation whose general solution is $y = \frac{ax}{bx + c}$, where a, b, c are arbitrary constants is

A. 1

B. 2

C. 3

D. None of these

Answer: B

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3. If p and q are order and degree of differential equation $y^2 \bigg(\frac{d^2y}{dx^2}\bigg)^2 + 3x \bigg(\frac{dy}{dx}\bigg)^{\frac{1}{3}} + x^2y^2 = \sin x, then$

A. p > qB. $rac{p}{q} = rac{1}{2}$ C. p = q

 $\mathsf{D}.\, p < q$

Answer: D

4. If m and n are the order and degree of the differential equation

$$(y'')^{5}+4. \ rac{(y'')^{3}}{y'''}+y'''=\sin x, then$$

A. m = 3, n = 5

B. m = 3, n = 1

C. m = 3, n = 3

D. m = 3, n = 2

Answer: D

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5. If the differenential equation $rac{dx}{3y+f}+rac{dy}{px+g}=0$ represents a

family of circle, then p=

B. f

C. 4

D. 3

Answer: D

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6. The general solution of
$$\frac{dy}{dx} = 1 - x^2 - y^2 + x^2 y^2$$
 is
A. $2\sin^{-1}y = x\sqrt{1-y^2} + c$
B. $\sin^{-1}y = \frac{1}{2}\sin^{-1}x + c$
C. $\cos^{-1}y = x\cos^{-1}x + c$
D. $\frac{1}{2}\log\left(\frac{1+y}{1-y}\right) = x - \frac{x^3}{3} + c$

Answer: D

7. The solution of the differential equation $e^{-x}(y+1)dy + (\cos^2 x - \sin 2x)y(dx) = 0$ subjected to the condition that y = 1 when x = 0 is

A.
$$(y+1)+e^x\cos^2x=2$$

$$\mathsf{B}.\, y + \log y = e^x \cos^2 x$$

C.
$$\log(y+1) + e^x \cos^2 x = 1$$

D.
$$y+\log y+e^x\cos^2x=2$$

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Answer: D

8. The solutio of the differential equation $(x^{2} - yx^{2})\frac{dy}{dx} + y^{2} + xy^{2} = 0$ is A. $\log\left(\frac{x}{y}\right) = \frac{1}{x} + \frac{1}{y} + c$ B. $\log\left(\frac{y}{x}\right) = \frac{1}{x} + \frac{1}{y} + c$

$$\mathsf{C.}\log(xy) = rac{1}{x} + rac{1}{y} + c$$
 $\mathsf{D.}\log(xy) + rac{1}{x} + rac{1}{y} = c$

Answer: A

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9. The family of curves passing through (0, 0) and satisfying the differential equation $\frac{y_2}{y_1} = 1$ (where, $y_n = \frac{d^n y}{dx^n}$) is (A) y = k (B) y = kx (C) $y = k(e^x + 1)$ (C) $y = k(e^x - 1)$ A. y = kB. y = kxC. $y = k(e^x + 1)$ D. $y = k(e^x - 1)$

Answer: D

10. The solution of the differential equation $y^2 dx + (x^2 - xy + y^2) dy = 0$ is A. $\tan^{-1}\left(\frac{x}{y}\right) + In \quad y + C = 0$ B. $2\tan^{-1}\left(\frac{x}{y}\right) + In \quad x + C = 0$ C. $In\left(y + \sqrt{x^2 + y^2}\right) + In \quad y + C = 0$ D. $In\left(x + \sqrt{x^2 + y^2} + C = 0\right)$

Answer: A

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11. The solution of differential equation $ig(1-xy+x^2y^2ig)dx=x^2dy$ is

A. tan xy = $\log |cx|$

B. tan (y/x) = tan log |cx|

C. xy = tan $\log |cx|$

D. None of these

Answer: C





13. If
$$rac{dy}{dx} - y \log_e 2 = 2^{\sin x} (\cos x - 1) \log_e 2$$
, then y =

A. $2^{\sin x} + c2^x$

B. $2^{\cos x} + c2^{x}$

 $\mathsf{C.}\, 2^{\sin x} + c 2^{-x}$

D. $2^{\cos x} + c2^{-x}$

Answer: A

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14. If $ye^y dx = ig(y^3 + 2xe^yig) dy, y(0) = 1$, then the value of x when y = 0 is

A. -1

B. 0

C. 1

D. 2

Answer: B



15. If $y_1(x)$ is a solution of the differential equation $rac{dy}{dx}-f(x)y=0$, then a solution of the differential equation $rac{dy}{dx}+f(x)y=r(x)$ is

D. None of these

Answer: A



16. The general solution of
$$x \left(rac{dy}{dx}
ight) + (\log x) y = x^{-rac{1}{2} \log x}$$
 is

A.
$$y = x^{1 - \frac{1}{2}\log x} + cx^{-\frac{1}{2}\log x}$$

B. $y. x^{\frac{1}{2}\log x} = x^{\frac{1}{2}\log x} + c$
C. $y = e^{\frac{(\log x)^2}{2}}(x + c)$
D. $y = e^{\frac{1}{2}(\log x)^2} \left(x^{1 - \frac{1}{2}(\log x)} - x^{-\frac{1}{2}\log x}\right) + c$

Answer: A



- 17. Find the general solution of the differential equation $(1 + \tan y)(dx dy) + 2xdy = 0$
 - A. $x(\sin y + \cos y) = \sin y + ce^y$

 $\mathsf{B.} x(\sin y + \cos y) = \sin y + c e^{-y}$

 $\mathsf{C}.\,y(\sin x + \cos x) = \sin x + c e^x$

D. None of these

Answer: B

18. Solution of differential equation $x^2y - x^3 rac{dy}{dx} = y^4 \cos x$ is

A.
$$x^2y^{-3}=2\sin x+c$$

B. $x^2y^{-3} = 3\cos x + c$

C.
$$x^3y^{-3} = 3\sin x + c$$

D. $x^2y^3 = 3\sin x + cx^2y$

Answer: C

19. Suppose a solutions of the differential equation
$$(xy^3 + x^2y^7)\frac{dy}{dx} = 1$$
 satisfies the initial conditions $y\left(\frac{1}{4}\right) = 1$. Then the value of $\frac{dy}{dx}$ when $y = -1$ is
A. $-\frac{3}{20}$

B.
$$-\frac{20}{3}$$

C. $-\frac{5}{16}$
D. $-\frac{16}{5}$

Answer: D



20. The general solution of the differential equation $\frac{dy}{dx} = y \tan x - y^2 \sec x \text{ is}$

A. $an x = (c + \sec x) y$

 $\mathsf{B.} \sec y = (c + \tan y)x$

 $\mathsf{C.} \sec x = (c + \tan x)y$

D. None of these

Answer: C

21. The solution of differential equation $x^2(xdy + ydx) = (xy - 1)^2 dx$ is (where c is an arbitrary constant)

A.
$$xy-1=cx$$

B. $xy-1=cx^2$
C. $\displaystyle rac{1}{xy-1}=\displaystyle rac{1}{x}+c$

D. None of these

Answer: C



22. Solution of the differential
$$\left(x+2y^3
ight)=rac{dx}{dy}y$$
 is

A.
$$x=y^2ig(c+y^2ig)$$

B. $x=yig(c-y^2ig)$
C. $x=2yig(c-y^2ig)$

D.
$$x=yig(c+y^2ig)$$

Answer: D

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Answer: C

24. Solution of the differential y' = $\frac{3yx^2}{x^3+2y^4}$ is

A.
$$x^3y^{-1} = rac{2}{3}y^3 + c$$

B. $x^2y^{-1} = rac{2}{3}y^3 + c$
C. $xy^{-1} = rac{2}{3}y^3 + c$

D. None of these

Answer: A

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25. For $y>0\,\,{
m and}\,\,x\in R,\,ydx+y^2dy=xdy$ where y = f(x). If f(1)=1, then

the value of f(-3) is

A. 1

B. 2

C. 3

Answer: C

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26. An equation of the curve satisfying $xdy - ydx = \sqrt{x^2 - y^2}dx$ and y(1) = 0 is

A.
$$y=x^2 \log |\sin x|$$

B. $y=x \sin (\log |x|)$
C. $y^2=x(x-1)^2$
D. $y=2x^2(x-1)$

Answer: B

27. The solution

$$(y(1 + x^{-1}) + \sin y)dx + (x + \log x + x \cos y)dy = 0$$
 is
A. $(1 + y^{-1} \sin y) + x^{-1} \log x = c$
B. $(y + \sin y) + xy \log x = C$
C. $xy + y \log x + x \sin y = C$
D. None of these

of

Answer: C

28. The solution of
$$(1+x)rac{dy}{dx}+1=e^{x-y}$$
 is

A.
$$e^{y}(x+1) = c$$

$$\mathsf{B.}\,e^y(x+1)=e^x+c$$

$$\mathsf{C}.\,e^y(x+1)=ce^x$$

D.
$$(x + 1) = e^x + c$$

Answer: B

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29. The solution of differential equation

$$x \sec\left(\frac{y}{x}\right)(ydx + xdy) = y \csc\left(\frac{y}{x}\right)(xdy - ydx)$$
 is
A. $xy = c \csc\left(\frac{y}{x}\right)$
B. $xy^2 \sin\frac{y}{x} = c$
C. $xy \csc\frac{y}{x} = c$
D. $xy = c \sin\left(\frac{x}{y}\right)$

Answer: C

30. The general solution of the differential equation

$$\sqrt{1-x^2y^2}dx = ydx + xdy$$
 is
A. $\sin(xy) = x + c$
B. $\sin^{-1}(xy) + x = c$
C. $\sin(x+c) = xy$
D. $\sin(xy) + x = c$

Answer: C

31.
$$(1+xy)ydx+(1-xy)xdy=0$$

A.
$$\frac{x}{y} + \frac{1}{xy} = k$$

B. $\log\left(\frac{x}{y}\right) = \frac{1}{xy} + k$
C. $\frac{x}{y} + \frac{1}{xy} = k$
D. $\log\left(\frac{x}{y}\right) = xy + k$

Answer: C



32. Solution of the differential equation
$$\displaystyle rac{dy}{dx} = \displaystyle rac{y^3}{e^{2x}+y^2}$$
 , is

A.
$$e^{-2x}y^2+2In|y|=c$$

B.
$$e^{2x}y^2=2In|y|=c$$

$$\mathsf{C}.\, e^x + In|y| = c$$

D. None of these

Answer: A



33. A popular grows at the rate of 10% of the population per year. How

long does it take for the population to doble ?

A. 2 log 10 years

B. 20 log 2 years

C. 10 log 2 years

D. 5 log 2 years

Answer: C

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34. A tangent drawn to the curve y = f(x) at P(x, y) cuts the x and y axes at A and B, respectively, such that AP : PB = 1 : 3. If f(1) = 1 then the curve passes through $\left(k, \frac{1}{8}\right)$ where k is

A. 1

B. 2

C. 3

D. 4

Answer: B



35. A curve 'C' with negative slope through the point(0,1) lies in the I Quadrant. The tangent at any point 'P' on it meets the x-axis at 'Q'. Such that PQ = 1. Then

The curve in parametric form is

A. $x = \cos heta + In \tan(heta/2), y = \sin heta$

 $\texttt{B.} \, x = \, -\cos\theta + In \tan(\theta/2), \, y = \sin\theta$

C. $x = -\cos heta - In an(heta/2), y = \sin heta$

D. None of these

Answer: C

36. Tangent to a curve intercepts the y-axis at a point P. A line perpendicular to this tangent through P passes through another point equation of (1,0). The differential the curve is (a) $(b)(c)y(d)rac{(e)dy}{f}((g)dx)(h)(i)-x(j)(k)igg((l)(m)(n)rac{(o)dy}{n}((q)dx)(r)(s)(t))$ (b) [Math Processing Error] (eee) (y) (c) $(d)(e)y(f)rac{(g)dx}{h}((i)dy)(j)(k)+x=1(l)$ (m) (d) None of these

A.
$$y. \ \frac{dy}{dx} - x\left(\frac{dy}{dx}\right)^2 = 1$$

B. $x \frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^2 = 1$
C. $y. \ \frac{dx}{dy} + x = 1$

D. None of these

Answer: A

37. The orthogonal trajectories of the family of curves an $a^{n-1}y = x^n$ are

given by (A) $x^n+n^2y=cons an t$ (B) $ny^2+x^2=cons an t$ (C)

 $n^2x+y^n=cons an t$ (D) y=x

A. $x^n + n^2 y$ = const B. $ny^2 + x^2$ = const C. $n^2 x + y^n$ = const D. $n^2 x - y^n$ = const

Answer: B

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Multiple Correct Answer Type

1. The differential equation for the family of curves $y = c \sin x$ can be given by

A.
$$\left(rac{dy}{dx}
ight)^2 = y^2 \cot^2 x$$

B. $\left(rac{dy}{dx}
ight)^2 - \left(\sec x rac{dy}{dx}
ight)^2 + y^2 = 0$

C.
$$\left(rac{dy}{dx}
ight)^2 = an^2 x$$

D. $rac{dy}{dx} = y \cot x$

Answer: A::B::D

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2. If the solution of the equation $\frac{d^2x}{dt^2} + 4\frac{dx}{dt} + 3x = 0$ given that for t = 0, x = 0 and $\frac{dx}{dt} = 12$ is in the form $x = Ae^{-3t} + Be^{-t}$, then A. A + B = 0B. A + B = 12C. |AB| = 36D. |AB| = 49

Answer: A::C

3. The solution of
$$\left(rac{dy}{dx}
ight)^2 - 2\left(x+rac{1}{4x}
ight)rac{dy}{dx} + 1 = 0$$

A.
$$y=x^2+c$$

B. $y=rac{1}{2}In(x)+c, x>0$
C. $y=rac{x}{2}+c$
D. $y=rac{x^2}{2}+c$

Answer: A::B

4.
$$\left(rac{dy}{dx}
ight)^2 + 2y \cot x rac{dy}{dx} = y^2$$
 has the solution

A.
$$y + \frac{c}{1 + \cos x} = 0$$

B. $y = \frac{c}{1 - \cos x}$
C. $x = 2\sin^{-1}\sqrt{\frac{c}{2y}}$
D. $x = 2\cos^{-1}\left(\frac{c}{2y}\right)$

Answer: A::B



5. Let $\frac{dy}{dx} + y = f(x)$ where y is a continuous function of x with y(0) = 1 and $f(x) = \begin{cases} e^{-x} & \text{if } o \le x \le 2\\ e^{-2} & \text{if } x > 2 \end{cases}$ Which of the following hold(s) good ? A. $y(1) = 2e^{-1}$

B.
$$y'(1) = -e^{-1}$$

C.
$$y(3) = -2e^{-3}$$

D.
$$y'(3) = -2e^{-3}$$

Answer: A::B::D

Which of the following hold(s) good?

A. f(x) has a minimum value 1 - e

B. f(x) has a maximum value 1 - e^{-1}

C.
$$f''ig(rac{\pi}{2}ig)=e$$

D. f'(0) = 1

Answer: A::B::C

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7. y = f(x) which has differential equation $y(2xy + e^x)dx - e^xdy = 0$ passing through the point (0,1). Then which of the following is/are true about the function?

function

satisfies

A. $x=1+\sqrt{2}$ is point of local maxima

B. $x=1-\sqrt{2}$ is point of local minima

$$\mathsf{C}.\lim_{x\,\to\,\infty}f(x)=\,-\,\infty$$

D.
$$\lim_{x o -\infty} f(x) = 0$$

Answer: A::B::C::D

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8. Suppose a curve whose sub tangent is n times the abscissa of the point of contact and passes through the point (2, 3). Then

A. for n = 1, equation of the curve is 2y = 3x

B. for n = 1, equation of the curve is $2y^2 = 9x$

C. for n = 2, equation of the curve is 2y = 3x

D. for n = 2, equation of the curve is $2y^2 = 9x$

Answer: A::D
9. Let C be a curve such that the normal at any point P on it meets x-axis and y-axis at A and B respectively. If BP : PA = 1 : 2 (internally) and the curve passes through the point (0, 4), then which of the following alternative(s) is/are correct?

A. The curves passes through $(\sqrt{10}, -6)$.

B. The equation of tangent at $\left(4, 4\sqrt{3}
ight)$ is $2\mathrm{x} + \sqrt{3}y = 20$.

C. The differential equation for the curve is yy' + 2x = 0.

D. The curve represents a hyperbola.

Answer: A::D

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10. The normal at a general point (a, b) on curve makes an angle θ with xaxis which satisfies $b(a^2 \tan \theta - \cot \theta) = a(b^2 + 1)$. The equation of curve can be

A.
$$y=e^{x^2/2}+c$$

B. $\log ky^2=x^2$
C. $y=ke^{x^2/2}$
D. $x^2-y^2=k$

Answer: B::C::D



Comprehension Type

1. Tangent is drawn at the point (x_i, y_i) on the curve y = f(x), which intersects the x-axis at $(x_{i+1}, 0)$. Now, again a tangent is drawn at (x_{i+1}, y_{i+1}) on the curve which intersect the x-axis at $(x_{i+2}, 0)$ and the process is repeated n times, i.e. i = 1, 2, 3; n. If $x_1, x_2, x_3, ; x_n$ from an arithmetic progression with common difference equal to $(\log)_2 e$ and curve passes through (0, 2). Now if curve passes through the point (-2, k), then the value of k is____ A. (1, 4)

B. (5, 1/16)

C. (2, 1/2)

D. None of these

Answer: B

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2. Tangent is drawn at the point (x_i, y_i) on the curve y = f(x), which intersects the x-axis at $(x_{i+1}, 0)$. Now again tangent is drawn at (x_{i+1}, y_{i+1}) on the curve which intersects the x-axis at $(x_{i+2}, 0)$ and the process is repeated n times i.e. i = 1, 2, 3,....,n.

If $x_1, x_2, x_3, ..., x_n$ form a geometric progression with common ratio equal to 2 and the curve passes through (1, 2), then the curve is

A. circle

B. hyperbola

| C. ellipse | |
|--------------------------------------|--|
| D. parabola | |
| Answer: B | |
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| Matrix Match Type | |
| 1. Match the following lists: | |
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| | |
| 2. Match the following lists: | |
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3. Match the differential equation in List I with its solution in List II and

then choose the correct code.



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4. if the differential equation of a curve, passing through $\left(0, -\frac{\pi}{4}\right)$ and (t, 0) is $\cos y \left(\frac{dy}{dx} + e^{-x}\right) + \sin y \left(e^{-x} - \frac{dy}{dx}\right) = e^{e^{-x}}$ then find the value of $t \cdot e^{e^{-1}}$

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5. Let f be a continuous function satisfying the equation $\int_0^x f(t)dt + \int_0^x tf(x-t)dt = e^{-x} - 1$, then find the value of $e^9f(9)$ is

equal to.....

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