



MATHS

BOOKS - CENGAGE MATHS (ENGLISH)

PARABOLA

Illustration 5 1

1. Find the equation of parabola

(i) having focus at $(0, -3)$ its directrix is $y = 3$.

(ii) having end points of latus rectum $(5, 10)$ and $(5, 10)$

and which opens towards right.

(iii) having vertex at origin and focus at $(0,2)$



Watch Video Solution

2. Find the equation of parabola

(i) having focus at $(0,-3)$ its directrix is $y = 3$.

(ii) having end points of latus rectum $(5,10)$ and $(5,10)$

and which opens towards right.

(iii) having vertex at origin and focus at $(0,2)$



Watch Video Solution

1. An arch is in the form of a parabola with its axis vertical. The arch is 12 m high and 6 m wide at the base. How wide is it 6 m from the vertex of the parabola ?



Watch Video Solution

2. An arch is in the form of a parabola with its axis vertical. The arch is 12 m high and 6 m wide at the base. How wide is it 6 m from the vertex of the parabola ?



Watch Video Solution

Illustration 5 3

1. A beam is supported at its ends by supports which are 12 metres apart. Since the load is concentrated at its centre, there is a deflection of 3 cm at the centre and the deflected beam is in the shape of a parabola. How far from the centre is the



Watch Video Solution

Illustration 5 4

1. Find the coordinates of a point the parabola $y^2 = 8x$ whose distance from the focus is 10.



Watch Video Solution

2. Find the coordinates of a point the parabola $y^2 = 8x$ whose distance from the focus is 10.



Watch Video Solution

Illustration 5 5

1. M is the foot of the perpendicular from a point P on a parabola $y^2 = 4ax$ to its directrix and SPM is an equilateral triangle, where S is the focus. Then find SP .



Watch Video Solution

Illustration 5 6

1. An equilateral triangle is inscribed in the parabola $y^2 = 4ax$, such that one vertex of this triangle coincides with the vertex of the parabola. Then find the side length of this triangle.



[Watch Video Solution](#)

Illustration 5 7

1. Find the equation of the chord of the parabola $y^2 = 8x$ having slope 2 if midpoint of the chord lies on the line $x=4$.



[Watch Video Solution](#)

2. Find the equation of the chord of the parabola $y^2 = 8x$ having slope 2 if midpoint of the chord lies on the line $x=4$.



[Watch Video Solution](#)

Illustration 5 8

1. Find the locus of midpoint of family of chords

$\lambda x + y = 5$ (λ is parameter) of the parabola $x^2 = 20y$



[Watch Video Solution](#)

Illustration 5 9

1. Find the position of points $P(1,3)$ w.r.t. parabolas

$$y^2 = 4x \text{ and } x^2 = 8y.$$



Watch Video Solution

2. Find the position of points $P(1,3)$ w.r.t. parabolas

$$y^2 = 4x \text{ and } x^2 = 8y.$$



Watch Video Solution

Illustration 5 10

1. The point $(a, 2a)$ is an interior point of the region bounded by the parabola $y^2 = 16x$ and the double ordinate through the focus. then find the values of a .



Watch Video Solution

Illustration 5 11

1. Find the locus of the middle points of the chords of the parabola $y^2 = 4ax$ which subtend a right angle at the vertex of the parabola.



Watch Video Solution

[Watch Video Solution](#)

Illustration 5 12

1. In the following figure, find the locus of centroid of triangle PAB, where AP perpendicular to PB.



[Watch Video Solution](#)

Illustration 5 13

1. A quadrilateral is inscribed in a parabola $y^2 = 4ax$ and three of its sides pass through fixed points on the axis. Show that the fourth side also passes through a fixed point on the axis of the parabola.



Watch Video Solution

Illustration 5 14

1. Find the equation of parabola

(i) having its vertex at $A(1,0)$ and focus at $S(3,0)$

(ii) having its focus at $S(2,5)$ and one of the extremities of latus rectum is $A(4,5)$



[Watch Video Solution](#)

2. Find the equation of parabola

(i) having its vertex at $A(1,0)$ and focus at $S(3,0)$

(ii) having its focus at $S(2,5)$ and one of the extremities of latus rectum is $A(4,5)$



[Watch Video Solution](#)

Illustration 5 15

1. $y^2 + 2y - x + 5 = 0$ represents a parabola. Find its vertex, equation of axis, equation of latus rectum,

coordinates of the focus, equation of the directrix, extremities of the latus rectum, and the length of the latus rectum.



Watch Video Solution

Illustration 5 16

1. The parametric equation of a parabola is $x = t^2 + 1, y = 2t + 1$. Then find the equation of the directrix.



Watch Video Solution

Illustration 5 17

1. Find the points on the parabola $y^2 - 2y - 4x = 0$ whose focal length is 6.



Watch Video Solution

Illustration 5 18

1. Find the value of P such that the vertex of $y = x^2 + 2px + 13$ is 4 units above the x-axis.



Watch Video Solution

Illustration 5 19

1. Find the equation of the parabola which has axis parallel to the y-axis and which passes through the points $(0, 2)$, $(-1, 0)$, and $(1, 6)$



[Watch Video Solution](#)

Illustration 5 20

1. Prove that the focal distance of the point (x, y) on the parabola $x^2 - 8x + 16y = 0$ is $|y + 5|$



[Watch Video Solution](#)

Illustration 5 21

1. If the focus of a parabola is $(2, 3)$ and its latus rectum is 8, then find the locus of the vertex of the parabola.



[Watch Video Solution](#)

Illustration 5 22

1. Prove that the locus of the center of the circle which touches the given circle externally and the given line is a parabola.



[Watch Video Solution](#)

Illustration 5 23

1. In triangle ABC, base BC is fixed. Then prove that the locus of vertex A such that $\tan B + \tan C = \text{Constant}$ is parabola.



[Watch Video Solution](#)

Illustration 5 24

1. Consider a square with vertices at $(1, 1)$, $(-1, 1)$, $(-1, -1)$, and $(1, -1)$. Set S be the region consisting of all points inside the square which are nearer to the origin than to any edge. Sketch the region S and find its area.



Watch Video Solution

Illustration 5 25

1. Find the value of λ if the equation $9x^2 + 4y^2 + 2\lambda xy + 4x - 2y + 3 = 0$ represents a parabola.



[Watch Video Solution](#)

Illustration 5 26

1. Does equation $(5x - 5)^2 + (5y + 10)^2 = (3x + 4y + 5)^2$ represents a parabola ?



[Watch Video Solution](#)

2. Does equation $(5x - 5)^2 + (5y + 10)^2 = (3x + 4y + 5)^2$ represents a parabola ?



[Watch Video Solution](#)

Illustration 5 27

1. Find the equation of the parabola having focus (1, 1) and vertex at (- 3, - 3)



[Watch Video Solution](#)

Illustration 5 28

1. Find the value of λ if the equation $(x - 1)^2 + (y - 2)^2 = \lambda(x + y + 3)^2$ represents a parabola. Also, find its focus, the equation of its directrix, the equation of its axis, the coordinates of its vertex, the equation of its latus rectum, the length of the latus rectum, and the extremities of the latus rectum.



Watch Video Solution

Illustration 5 29

1. Show that the curve whose parametric coordinates are $x = t^2 + t + 1, y = t^2 - t + 1$ represents a parabola.



Watch Video Solution

Illustration 5 30

1. If $(2, -8)$ is at an end of a focal chord of the parabola $y^2 = 32x$, then find the other end of the chord.



Watch Video Solution

Illustration 5 31

1. Let S is the focus of the parabola $y^2 = 4ax$ and X the foot of the directrix, PP' is a double ordinate of the curve and PX meets the curve again in Q . Prove that $P'Q$ passes through focus.



[Watch Video Solution](#)

Illustration 5 32

1. Length of the focal chord of the parabola $y^2 = 4ax$ at a distance p from the vertex is:



Watch Video Solution

Illustration 5 33

1. If AB is a focal chord of $x^2 - 2x + y - 2 = 0$ whose focus is S and $AS = l_1$, then find BS



Watch Video Solution

Illustration 5 34

1. Circles are drawn with diameter being any focal chord of the parabola $y^2 - 4x - y - 4 = 0$ with always touch a fixed line. Find its equation.



Watch Video Solution

Illustration 5 35

1. Find the equation of the tangent to the parabola $y^2 = 8x$ having slope 2 and also find the point of contact.



Watch Video Solution

Illustration 5 36

1. A tangent to the parabola $y^2 = 8x$ makes an angle of 45° with the straight line $y = 3x + 5$. Then find one of the points of contact.



Watch Video Solution

Illustration 5 37

1. Show that $x\cos\alpha + a\sin^2\alpha = p$ touches the parabola $y^2 = 4ax$ if $p\cos\alpha + a\sin^2\alpha = 0$ and that the point of contact is $\left(a\tan^2\alpha, -2a\tan\alpha\right)$.



[Watch Video Solution](#)

Illustration 5 38

1. The parabola $y^2 = 4x$ and the circle having its center at $(6, 5)$ intersect at right angle. Then find the possible points of intersection of these curves.



[Watch Video Solution](#)

Illustration 5 39

1. Find the equation of tangents of the parabola $y^2 = 12x$, which passes through the point $(2, 5)$.

 [Watch Video Solution](#)

Illustration 5 40

1. The tangents to the parabola $y^2 = 4ax$ at the vertex V and any point P meet at Q . If S is the focus, then prove that $SPSQ$, and SV are in GP.

 [Watch Video Solution](#)

Illustration 5 41

1. The equation of the common tangent to the parabolas $y^2 = 4ax$ and $x^2 = 4by$ is given by



Watch Video Solution

Illustration 5 42

1. If a tangent to the parabola $y^2 = 4ax$ meets the x-axis at T and intersects the tangents at vertex A at P , and rectangle $TAPQ$ is completed, then find the locus of point Q .



[Watch Video Solution](#)

Illustration 5 43

1. Two tangent are drawn from the point (- 2, - 1) to parabola $y^2 = 4x$ if α is the angle between these tangents, then find the value of $\tan\alpha$



[Watch Video Solution](#)

Illustration 5 44

1. If two tangents drawn from the point (α, β) to the parabola $y^2 = 4x$ are such that the slope of one tangent is double of the other, then prove that $\alpha = \frac{2}{9}\beta^2$.



Watch Video Solution

Illustration 5 45

1. If the tangent at the point $P(2, 4)$ to the parabola $y^2 = 8x$ meets the parabola $y^2 = 8x + 5$ at Q and R , then find the midpoint of chord QR .



Watch Video Solution

[Watch Video Solution](#)

Illustration 5 46

1. The locus of foot of the perpendiculars drawn from the vertex on a variable tangent to the parabola $y^2 = 4ax$ is

[Watch Video Solution](#)

Illustration 5 47

1. Find the equation of the tangent to the parabola

$y = x^2 - 2x + 3$ at point $(2, 3)$.



Watch Video Solution

Illustration 5 48

1. Find the equation of the tangent to the parabola

$x = y^2 + 3y + 2$ having slope 1.



Watch Video Solution

Illustration 5 49

1. Find the equation of tangents drawn to the parabola $y = x^2 - 3x + 2$ from the point $(1, -1)$.



Watch Video Solution

Illustration 5 50

1. Find the shortest distance between the line $y = x - 2$ and the parabola $y = x^2 + 3x + 2$.



Watch Video Solution

Illustration 5 51

1. If the lines L_1 and L_2 are tangents to $4x^2 - 4x - 24y + 49 = 0$ and are normals for $x^2 + y^2 = 72$, then find the slopes of L_1 and L_2 .



Watch Video Solution

Illustration 5 52

1. Tangents are drawn from the point $(-1, 2)$ on the parabola $y^2 = 4x$. Find the length that these tangents will intercept on the line $x = 2$.



Watch Video Solution

Illustration 5 53

1. Tangents are drawn to the parabola $y^2 = 4ax$ at the point where the line $lx + my + n = 0$ meets this parabola. Find the point of intersection of these tangents.



[Watch Video Solution](#)

Illustration 5 54

1. If the chord of contact of tangents from a point P to the parabola $y^2 = 4ax$ touches the parabola $x^2 = 4by$, then find the locus of P .



Watch Video Solution

Illustration 5 55

1. From a variable point on the tangent at the vertex of a parabola $y^2 = 4ax$, a perpendicular is drawn to its chord of contact. Show that these variable perpendicular lines pass through a fixed point on the axis of the parabola.



[Watch Video Solution](#)

Illustration 5 56

1. Find the points of contact Q and R of a tangent from the point $P(2, 3)$ on the parabola $y^2 = 4x$



[Watch Video Solution](#)

Illustration 5 57

1. Tangents are drawn from any point on the line $x + 4a = 0$ to the parabola $y^2 = 4ax$. Then find the angle subtended by the chord of contact at the vertex.



Watch Video Solution

Illustration 5 58

1. Two straight lines $(y - b) = m_1(x + a)$ and $(y - b) = m_2(x + a)$ are the tangents of $y^2 = 4ax$. Prove $m_1 m_2 = -1$.



Watch Video Solution

[Watch Video Solution](#)

Illustration 5 59

1. Mutually perpendicular tangents TA and TB are drawn to $y^2 = 4ax$. Then find the minimum length of AB .

[Watch Video Solution](#)

Illustration 5 60

1. Tangent PA and PB are drawn from the point P on the directrix of the parabola $(x - 2)^2 + (y - 3)^2 = \frac{(5x - 12y + 3)^2}{160}$. Find the least radius of the circumcircle of triangle PAB .



Watch Video Solution

Illustration 5 61

1. Tangents are drawn to the parabola $(x - 3)^2 + (y + 4)^2 = \frac{(3x - 4y - 6)^2}{25}$ at the extremities

of the chord $2x - 3y - 18 = 0$. Find the angle between the tangents.



Watch Video Solution

Illustration 5 62

1. Let $3x - y - 8 = 0$ be the equation of tangent to a parabola at the point $(7, 13)$. If the focus of the parabola is at $(-1, -1)$. Its directrix is



Watch Video Solution

2. Let $y=3x-8$ be the equation of the tangent at the point $(7, 13)$ lying on a parabola whose focus is at $(-1,-1)$. Find the equation of directrix and the length of the latus rectum of the parabola.



Watch Video Solution

Illustration 5 63

1. Find the locus of the point of intersection of tangents in the parabola $x^2 = 4ax$ which are inclined at an angle θ to each other. Which intercept constant length c on the tangent at the vertex. such

that the area of ABR is constant c , where A and B are the points of intersection of tangents with the y -axis and R is a point of intersection of tangents.



[Watch Video Solution](#)

Illustration 5 64

1. Find the equations of normal to the parabola $y^2 = 4ax$ at the ends of the latus rectum.



[Watch Video Solution](#)

Illustration 5 65

1. If $y = x + 2$ is normal to the parabola $y^2 = 4ax$, then find the value of a .



[Watch Video Solution](#)

Illustration 5 66

1. Find the equation of line which is normal to the parabola $x^2 = 4y$ and touches the parabola $y^2 = 12x$.



[Watch Video Solution](#)

2. Find the equation of line which is normal to the parabola $x^2 = 4y$ and touches the parabola $y^2 = 12x$.



Watch Video Solution

Illustration 5 67

1. Find the equation of normal to the parabola $y = x^2 - x - 1$ which has equal intercept on the axes. Also find the point where this normal meets the curve again.



Watch Video Solution

Illustration 5 68

1. Prove that the length of the intercept on the normal at the point $P(at^2, 2at)$ of the parabola $y^2 = 4ax$ made by the circle described on the line joining the focus and P as diameter is $a\sqrt{1+t^2}$.



Watch Video Solution

Illustration 5 69

1. A normal chord of the parabola $y^2 = 4ax$ subtends a right angle at the vertex if its slope is



[Watch Video Solution](#)

Illustration 5 70

1. How many normals can be drawn to parabola $y^2 = 4x$ from point $(15, 12)$? Find their equation. Also, find corresponding feet of normals on the parabola.



[Watch Video Solution](#)

2. How many normals can be drawn to parabola $y^2 = 4x$ from point $(15, 12)$? Find their equation. Also, find corresponding feet of normals on the parabola.



[Watch Video Solution](#)

Illustration 5 71

1. Three normals are drawn from the point $(7, 14)$ to the parabola $x^2 - 8x - 16y = 0$. Find the coordinates of the feet of the normals.



[Watch Video Solution](#)

Illustration 5 72

1. Find the minimum distance between the curves

$$y^2 = 4x \text{ and } x^2 + y^2 - 12x + 31 = 0$$



Watch Video Solution

Illustration 5 73

1. If normals drawn at three different point on the parabola $y^2 = 4ax$ pass through the point (h,k) , then show that $h > 2a$.



Watch Video Solution

Illustration 5 74

1. IF three distinct normals to the parabola $y^2 - 2y = 4x - 9$ meet at point (h,k) , then prove that $h > 4$.



[Watch Video Solution](#)

2. IF three distinct normals to the parabola $y^2 - 2y = 4x - 9$ meet at point (h,k) , then prove that $h > 4$.



[Watch Video Solution](#)

Illustration 5 75

1. In the parabola $y^2 = 4ax$, then tangent at P whose abscissa is equal to the latus rectum meets its axis at T , and normal P cuts the curve again at Q . Show that $PT:PQ = 4:5$.



Watch Video Solution

Illustration 5 76

1. Find the length of normal chord which subtends an angle of 90° at the vertex of the parabola $y^2 = 4x$.



[Watch Video Solution](#)

Illustration 5 77

1. Prove that the locus of the point of intersection of the normals at the ends of a system of parallel cords of a parabola is a straight line which is a normal to the curve.



[Watch Video Solution](#)

Illustration 5 78

1. Find the locus of the midpoint of normal chord of parabola $y^2 = 4ax$



Watch Video Solution

Illustration 5 79

1. If the angle between the normal to the parabola $y^2 = 4ax$ at point P and the focal chord passing through P is 60° , then find the slope of the tangent at point P.



Watch Video Solution

2. If the angle between the normal to the parabola $y^2 = 4ax$ at point P and the focal chord passing through P is 60° , then find the slope of the tangent at point P.



Watch Video Solution

Illustration 5 80

1. A parabola mirror is kept along $y^2 = 4x$ and two light rays parallel to its axis are reflected along one straight line. If one of the incident light rays is at 3

units distance from the axis, then find the distance of the other incident ray from the axis.



Watch Video Solution

Illustration 5 81

1. If two of the three feet of normals drawn from a point to the parabola $y^2 = 4x$ are $(1, 2)$ and $(1, -2)$, then find the third foot.



Watch Video Solution

Illustration 5 82

1. If the normals from any point to the parabola $y^2 = 4x$ cut the line $x = 2$ at points whose ordinates are in AP, then prove that the slopes of tangents at the co-normal points are in GP.



Watch Video Solution

Illustration 5 83

1. Find the locus of the point of intersection of two normals to a parabolas which are at right angles to one another.

[Watch Video Solution](#)

Illustration 5 84

1. $P(t_1)$ and $Q(t_2)$ are the point t_1 and t_2 on the parabola $y^2 = 4ax$. The normals at P and Q meet on the parabola. Show that the middle point PQ lies on the parabola $y^2 = 2a(x + 2a)$.

[Watch Video Solution](#)

Illustration 5 85

1. Normals are drawn at points A, B , and C on the parabola $y^2 = 4x$ which intersect at P . The locus of the point P if the slope of the line joining the feet of two of them is 2, is



Watch Video Solution

Solved Examples 5 1

1. Prove that for a suitable point P on the axis of the parabola, chord AB through the point P can be

drawn such that $\left[\left(\frac{1}{AP^2} \right) + \left(\frac{1}{BP^2} \right) \right]$ is same for all positions of the chord.



[Watch Video Solution](#)

Solved Examples 5 2

1. A parabola of latus rectum l touches a fixed equal parabola. The axes of two parabolas are parallel. Then find the locus of the vertex of the moving parabola.



[Watch Video Solution](#)

Solved Examples 5 3

1. about to only mathematics



Watch Video Solution

Solved Examples 5 4

1. Find the radius of the largest circle, which passes through the focus of the parabola $y^2 = 4(x + y)$ and is also contained in it.



Watch Video Solution

Solved Examples 5 5

1. The vertices A , B and C of a variable right triangle lie on a parabola $y^2 = 4x$. If the vertex B containing the right angle always remains at the point $(1, 2)$, then find the locus of the centroid of triangle ABC .



Watch Video Solution

Solved Examples 5 6

1. Tangents are drawn to the parabola at three distinct points. Prove that these tangent lines always make a triangle and that the locus of the

orthocentre of the triangle is the directrix of the parabola.



Watch Video Solution

Solved Examples 5 7

1. about to only mathematics



Watch Video Solution

Solved Examples 5 8

1. Two lines are drawn at right angles, one being a tangent to $y^2 = 4ax$ and the other $x^2 = 4by$. Then find the locus of their point of intersection.



[Watch Video Solution](#)

Solved Examples 5 9

1. about to only mathematics



[Watch Video Solution](#)

Solved Examples 5 10

1. If the normals at P, Q, R of the parabola $y^2 = 4ax$ meet in O and S be its focus, then prove that $.SP.SQ.SR = a.(SO)^2$.



Watch Video Solution

Solved Examples 5 11

1. The shortest distance between the parabolas

$2y^2 = 2x - 1$ and $2x^2 = 2y - 1$ is $2\sqrt{2}$ (b) $\frac{1}{2}\sqrt{2}$ (c) 4 (d)

$$\sqrt{\frac{36}{5}}$$



Watch Video Solution

Solved Examples 5 12

1. If two chords drawn from the point $A(4, 4)$ to the parabola $x^2 = 4y$ are bisected by the line $y = mx$, the interval in which m lies is $(-2\sqrt{2}, 2\sqrt{2})$
 $(-\infty, -\sqrt{2}) \cup (\sqrt{2}, \infty)$
 $(-\infty, -2\sqrt{2} - 2) \cup (2\sqrt{2} - 2, \infty)$ none of these



Watch Video Solution

Solved Examples 5 13

1. Tangent is drawn at any point (p, q) on the parabola $y^2 = 4ax$. Tangents are drawn from any point on this tangent to the circle $x^2 + y^2 = a^2$, such that the chords of contact pass through a fixed point (r, s) . Then p, q, r and s can hold the relation

$r^2q = 4p^2s$ (b) $rq^2 = 4ps^2$ $rq^2 = -4ps^2$ (d)
 $r^2q = -4p^2s$



Watch Video Solution

Solved Examples 5 14

1. about to only mathematics



[Watch Video Solution](#)

Concept Applications Exercise 5 1

1. Find the angle made by a double ordinate of length $2a$ at the vertex of the parabola $y^2 = ax$.



[Watch Video Solution](#)

2. If focal distance of a point P on the parabola $y^2 = 4ax$ whose abscissa is $5/10$, then find the value of a .



[Watch Video Solution](#)

3. Analyse the equation if it represents parabola or a part of parabola $x = \sqrt{-y}$



Watch Video Solution

4. Find the range of values of λ for which the point $(\lambda, -1)$ is exterior to both the parabolas $y^2 = |x|$.



Watch Video Solution

5. The locus of a point on the variable parabola $y^2 = 4ax$, whose distance from the focus is always equal to k , is equal to (a is parameter)



Watch Video Solution

6. Find the locus of the midpoint of chords of the parabola $y^2 = 4ax$ that pass through the point $(3a, a)$.



Watch Video Solution

7. If chord BC subtends right angle at the vertex A of the parabola $y^2 = 4x$ with $AB = \sqrt{5}$ then find the area of triangle ABC.



Watch Video Solution

8. PQ is a chord of the parabola $y^2 = 4x$ whose perpendicular bisector meets the axis at M and the ordinate of the midpoint PQ meets the axis at N. Then the length MN is equal to



Watch Video Solution

9. LOL' and MOM' are two chords of parabola $y^2 = 4ax$ with vertex A passing through a point O on its axis. Prove that the radical axis of the circles described on LL' and MM' as diameters passes through the vertex of the parabola.



[Watch Video Solution](#)

10. If focal distance of a point P on the parabola $y^2 = 4ax$ whose abscissa is 5, then find the value of a .



[Watch Video Solution](#)

11. If chord BC subtends right angle at the vertex A of the parabola $y^2 = 4x$ with $AB = \sqrt{5}$ then find the area of triangle ABC.



[Watch Video Solution](#)

Concept Applications Exercise 5 2

1. If the focus and vertex of a parabola are the points (0, 2) and (0, 4), respectively, then find the equation



[Watch Video Solution](#)

2. Find the equation of parabola whose focus is $(0,1)$ and the directrix is $x+2=0$. Also find the vertex of the parabola.



Watch Video Solution

3. Find the vertex, focus and directrix of the parabola $x^2 = 2(2x + y)$.



Watch Video Solution

4. The vertex of a parabola is $(2, 2)$ and the coordinates of its two extremities of latus rectum are

$(-2, 0)$ and $(6, 0)$. Then find the equation of the parabola.



Watch Video Solution

5. A parabola passes through the point the point $(1,2)$, $(2,1)$, $(3,4)$ and $(4,3)$. Find the equation of the axis of parabola.



Watch Video Solution

6. Find the length of the common chord of the parabola $y^2 = 4(x + 3)$ and the circle $x^2 + y^2 + 4x = 0$



Watch Video Solution

7. The equation of the latus rectum of a parabola is $x + y = 8$ and the equation of the tangent at the vertex is $x + y = 12$. Then find the length of the latus rectum.



Watch Video Solution

8. Find the length of the latus rectum of the parabola whose focus is at $(2, 3)$ and directrix is the

line $x - 4y + 3 = 0$.



Watch Video Solution

9. If (a, b) is the midpoint of a chord passing through the vertex of the parabola $y^2 = 4(x + 1)$, then prove that $2(a + 1) = b^2$



Watch Video Solution

10. about to only mathematics



Watch Video Solution

11. Plot the region in the first quadrant in which points are nearer to the origin than to the line $x = 3$.



Watch Video Solution

12. Prove that the locus of a point, which moves so that its distance from a fixed line is equal to the length of the tangent drawn from it to a given circle, is a parabola.



Watch Video Solution

13. Prove that the locus of the center of a circle, which intercepts a chord of given length $2a$ on the axis of x and passes through a given point on the axis of y distant b from the origin, is a parabola.



Watch Video Solution

14. Find the equation of the parabola whose focus is $S(-1, 1)$ and directrix is $4x + 3y - 24 = 0$.



Watch Video Solution

15. The axis of parabola is along the line $y=x$ and the distance of its vertex and focus from origin are $\sqrt{2}$ and $2\sqrt{2}$ respectively. If vertex and focus both lie in the first quadrant, then the equation of the parabola is :



Watch Video Solution

16. Find the equation of parabola whose focus is $(0,1)$ and the directrix is $x+2=0$. Also find the vertex of the parabola.



Watch Video Solution

17. Find the vertex, focus and directrix of the parabola $x^2 = 2(2x + y)$.



Watch Video Solution

Concept Applications Exercise 5 3

1. If t_1 and t_2 are the ends of a focal chord of the parabola $y^2 = 4ax$, then prove that the roots of the equation $t_1x^2 + ax + t_2 = 0$ are real.



Watch Video Solution

2. If the line passing through the focus S of the parabola $y = ax^2 + bx + c$ meets the parabola at P and Q and if $SP = 4$ and $SQ = 6$, then find the value of a .



Watch Video Solution

3. If a focal chord of $y^2 = 4ax$ makes an angle $\alpha \in [\pi/4, \pi/2]$ with the positive direction of the x -axis, then find the maximum length of this focal chord.



Watch Video Solution

4. If the length of focal chord of $y^2 = 4ax$ is l , then find the angle between the axis of the parabola and the focal chord.



Watch Video Solution

5. If length of focal chord PQ is l , and p is the perpendicular distance of PQ from the vertex of the parabola, then prove that $l \propto \frac{1}{p^2}$.



Watch Video Solution

6. Circles drawn on the diameter as focal distance of any point lying on the parabola $x^2 - 4x + 6y + 10 = 0$ will touch a fixed line whose equation is a. $y=1$ b. $y=-1$ c. $y=2$ d. $y=-2$



Watch Video Solution

7. A circle is drawn to pass through the extremities of the latus rectum of the parabola $y^2 = 8x$. It is given that this circle also touches the directrix of the parabola. Find the radius of this circle.



Watch Video Solution

Concept Applications Exercise 5 4

1. Find the point on the curve $y^2 = ax$ the tangent at which makes an angle of 45° with the x-axis.



Watch Video Solution

2. Find the equation of the straight lines touching both $x^2 + y^2 = 2a^2$ and $y^2 = 8ax$.



Watch Video Solution

3. Find the angle at which the parabolas $y^2 = 4x$ and $x^2 = 32y$ intersect.



Watch Video Solution

4. If the line $y = 3x + c$ touches the parabola $y^2 = 12x$ at point P , then find the equation of the tangent at point Q where PQ is a focal chord.



Watch Video Solution

5. If the line $x + y = a$ touches the parabola $y = x - x^2$, then find the value of a .



Watch Video Solution

6. Find the slopes of the tangents to the parabola $y^2 = 8x$ which are normal to the circle $x^2 + y^2 + 6x + 8y - 24 = 0$.



Watch Video Solution

7. Find the equation of the tangent to the parabola $9x^2 + 12x + 18y - 14 = 0$ which passes through the point $(0, 1)$.



Watch Video Solution

8. Find the locus of the point from which the two tangents drawn to the parabola $y^2 = 4ax$ are such that the slope of one is thrice that of the other.



Watch Video Solution

9. From an external point P , a pair of tangents is drawn to the parabola $y^2 = 4x$. If θ_1 and θ_2 are the inclinations of these tangents with the x-axis such that $\theta_1 + \theta_2 = \frac{\pi}{4}$, then find the locus of P .



Watch Video Solution

10. Show that the common tangents to the parabola $y^2 = 4x$ and the circle $x^2 + y^2 + 2x = 0$ form an equilateral triangle.



Watch Video Solution

11. TP and TQ are tangents to the parabola $y^2 = 4ax$ at P and Q , respectively. If the chord PQ passes through the fixed point $(-a, b)$, then find the locus of T .



Watch Video Solution

12. At any point P on the parabola $y^2 - 2y - 4x + 5 = 0$ a tangent is drawn which meets the directrix at Q . Find the locus of point R which divides QP externally in the ratio $\frac{1}{2} : 1$.



Watch Video Solution

13. If the distance of the point $(\alpha, 2)$ from its chord of contact w.r.t. the parabola $y^2 = 4x$ is 4, then find the value of α .



Watch Video Solution

Concept Applications Exercise 5 5

1. If the tangents at the points P and Q on the parabola $y^2 = 4ax$ meet at T , and S is its focus, prove that SP , ST , and SQ are in GP.



Watch Video Solution

2. If PQ is the focal chord of parabola $y = x^2 - 2x + 3$ such that $P \equiv (2, 3)$, then find slope of tangent at Q.



Watch Video Solution

3. If there exists at least one point on the circle $x^2 + y^2 = a^2$ from which two perpendicular tangents can be drawn to parabola $y^2 = 2x$, then find the values of a.



Watch Video Solution

4. Find the angle between the tangents drawn to $y^2 = 4x$, where it is intersected by the line $y = x - 1$.



Watch Video Solution

5. Find the angle between the tangents drawn from the origin to the parabolas $y^2 = 4a(x - a)$



Watch Video Solution

6. Find the locus of the point of intersection of the perpendicular tangents of the curve $y^2 + 4y - 6x - 2 = 0$.



[Watch Video Solution](#)

7. A tangent is drawn to the parabola $y^2 = 4ax$ at P such that it cuts the y -axis at Q . A line perpendicular to this tangent is drawn through Q which cuts the axis of the parabola at R . If the rectangle $PQRS$ is completed, then find the locus of S .



[Watch Video Solution](#)

8. Let $y=x+1$ is axis of parabola, $y+x-4=0$ is tangent of same parabola at its vertex and $y=2x+3$ is one of its

tangents. Then find the focus of the parabola.



Watch Video Solution

9. Let $y=x+1$ is axis of parabola, $y+x-4=0$ is tangent of same parabola at its vertex and $y=2x+3$ is one of its tangents. Then find the focus of the parabola.



Watch Video Solution

Concept Applications Exercise 5 6

1. Prove that the chord $y - x\sqrt{2} + 4a\sqrt{2} = 0$ is a normal chord of the parabola $y^2 = 4ax$. Also find the point on the parabola when the given chord is normal to the parabola.



Watch Video Solution

2. Find the equation of normal to parabola $y = x^2 - 3x - 4$

(a) at point (3,-4)

(b) having slope 5.



Watch Video Solution

3. If $y = 2x + 3$ is a tangent to the parabola $y^2 = 24x$, then find its distance from the parallel normal.



Watch Video Solution

4. For the parabola $y^2 = 16x$ prove that whatever be the value of θ , the line $y = (x - 11)\cos\theta - \cos 3\theta$ is always normal to the parabola



Watch Video Solution

5. Find the locus of the midpoints of the portion of the normal to the parabola $y^2 = 4ax$ intercepted

between the curve and the axis.



Watch Video Solution

6. If the parabolas $y^2 = 4ax$ and $y^2 = 4c(x - b)$ have a common normal other than the x-axis (a, b, c being distinct positive real numbers), then prove that $\frac{b}{a - c} > 2$.



Watch Video Solution

7. about to only mathematics



Watch Video Solution

8. Prove that for $\theta \in R$, the line $y = (x - 11)\cos\theta - \cos 3\theta$ is always normal to the parabola $y^2 = 16x$.



Watch Video Solution

Concept Applications Exercise 5 7

1. If the normal to the parabola $y^2 = 4ax$ at point t_1 cuts the parabola again at point t_2 , then prove that $t_2^2 \geq 8$.



Watch Video Solution

2. Find the angle at which normal at point $P(at^2, 2at)$ to the parabola meets the parabola again at point Q .



Watch Video Solution

3. If normal to parabola $y^2 = 4ax$ at point $P(at^2, 2at)$ intersects the parabola again at Q , such that sum of ordinates of the points P and Q is 3, then find the length of latus rectum in terms of t .



Watch Video Solution

4. If tangents are drawn to $y^2 = 4ax$ from any point P on the parabola $y^2 = a(x + b)$, then show that the normals drawn at their point of contact meet on a fixed line.



Watch Video Solution

5. If line $x - 2y - 1 = 0$ intersects parabola $y^2 = 4x$ at P and Q , then find the point of intersection of normals at P and Q .



Watch Video Solution

6. Find the locus of the point of intersection of the normals at the end of the focal chord of the parabola $y^2 = 4ax$.



Watch Video Solution

7. If incident ray from point $(-2,4)$ parallel to the axis of the parabola $y^2 = 4x$ strikes the parabola, then find the equation of the reflected ray.



Watch Video Solution

8. Let L_1, L_2 and L_3 be the three normals to the parabola $y^2 = 4ax$ from point P inclined at the angle θ_1, θ_2 and θ_3 with x-axis, respectively. Then find the locus of point P given that $\theta_1 + \theta_2 + \theta_3 = \alpha$ (constant).



Watch Video Solution

9. If line $x-2y-1=0$ intersects parabola $y^2 = 4x$ at P and Q, then find the point of intersection of normals at P and Q.



Watch Video Solution

Exercise Single Correct Answer Type

1. Which one of the following equation represent parametric equation to a parabolic curve? (a)

$$x = 3\cos t; y = 4\sin t \quad (b) x^2 - 2 = 2\cos t; y = 4\cos^2\left(\frac{t}{2}\right) \quad (c)$$

$$\sqrt{x} = \tan t; \sqrt{y} = \sec t \quad (d) x = \sqrt{1 - \sin t}; y = \frac{\sin t}{2} + \frac{\cos t}{2}$$

A. $x = 3\cos t, y = 4\sin t$

B. $x^2 - 2 = 2\cos t, y = 4\cos^2\frac{t}{2}$

C. $\sqrt{x} = \tan t, \sqrt{y} = \sec t$

D. $x = \sqrt{1 - \sin t}, y = \sin\frac{t}{2} + \cos\frac{t}{2}$

Answer: B



Watch Video Solution

2. A point $P(x, y)$ moves in the xy -plane such that

$x = a\cos^2\theta$ and $y = 2a\sin\theta$, where θ is a parameter.

The locus of the point P is a/an circle (b) aellipse

unbounded parabola (d) part of the parabola

A. circle

B. ellipse

C. unbounded parabola

D. part of the parabola

Answer: D

3. A line L passing through the focus of the parabola $y^2 = 4(x - 1)$ intersects the parabola at two distinct points. If m is the slope of the line L , then $-11m$ in \mathbb{R}

(d) none of these

A. $-1 < m < 1$

B. $m < -1$ or $m <$

C. $\min R$

D. none of these

Answer: D

[Watch Video Solution](#)

4. The circle $x^2 + y^2 + 2\lambda x = 0, \lambda \in R$, touches the parabola $y^2 = 4x$ externally. Then,

A. $\lambda > 0$

B. $\lambda < 0$

C. $\lambda > 1$

D. none of these

Answer: A

[Watch Video Solution](#)

5. A set of parallel chords of the parabola $y^2 = 4ax$ have their midpoint on any straight line through the vertex any straight line through the focus a straight line parallel to the axis another parabola

- A. any straight line through the vertex
- B. any straight line through the focus
- C. a straight line parallel to the axis
- D. another parabola

Answer: C



Watch Video Solution

6. If the points A (1,3) and B (5,5) lying on a parabola are equidistant from focus, then the slope of the directrix is

A. $\frac{1}{2}$

B. $-\frac{1}{2}$

C. 2

D. -2

Answer: A



Watch Video Solution

7. The radius of the circle whose centre is $(-4,0)$ and which cuts the parabola $y^2 = 8x$ at A and B such that the common chord AB subtends a right angle at the vertex of the parabola is equal to

A. $4\sqrt{13}$

B. $3\sqrt{5}$

C. $3\sqrt{2}$

D. $2\sqrt{5}$

Answer: A



Watch Video Solution

8. The circle $x^2 + y^2 = 5$ meets the parabola $y^2 = 4x$ at P and Q . Then the length PQ is equal to (a) 2 (b) $2\sqrt{2}$ (c) 4 (d) none of these

A. 2

B. $2\sqrt{2}$

C. 4

D. none of these

Answer: C



Watch Video Solution

9. If y_1, y_2 , and y_3 are the ordinates of the vertices of a triangle inscribed in the parabola $y^2 = 4ax$, then its area is

A. $\frac{1}{2a} \left| (y_1 - y_2)(y_2 - y_3)(y_3 - y_1) \right|$

B. $\frac{1}{4a} \left| (y_1 - y_2)(y_2 - y_3)(y_3 - y_1) \right|$

C. $\frac{1}{8a} \left| (y_1 - y_2)(y_2 - y_3)(y_3 - y_1) \right|$

D. none of these

Answer: C



Watch Video Solution

10. let P be the point $(1, 0)$ and Q be a point on the locus $y^2 = 8x$. The locus of the midpoint of PQ is

A. $y^2 + 4x + 2 = 0$

B. $y^2 - 4x + 2 = 0$

C. $x^2 - 4y + 2 = 0$

D. $x^2 + 4y + 2 = 0$

Answer: B



Watch Video Solution

11. An equilateral triangle SAB is inscribed in the parabola $y^2 = 4ax$ having its focus at S. If chord AB lies towards the left of S, then the side length of this triangle is

A. $2a(2 - \sqrt{3})$

B. $4a(2 - \sqrt{3})$

C. $a(2 - \sqrt{3})$

D. $8a(2 - \sqrt{3})$

Answer: B



Watch Video Solution

12. C is the centre of the circle with centre $(0, 1)$ and radius unity. $y = ax^2$ is a parabola. The set of the values of ' a ' for which they meet at a point other than the origin, is

A. $a > 0$

B. $a \in (0, 1/2)$

C. $(1/4, 1/2)$

D. $(1/2, \infty)$

Answer: D



Watch Video Solution

13. $P(x, y)$ is a variable point on the parabola $y^2 = 4ax$ and $Q(x + c, y + c)$ is another variable point, where c is a constant. The locus of the midpoint of PQ is a/n parabola (b) hyperbola hyperbola (d) circle

A. parabola

B. ellipse

C. hyperbola

D. circle

Answer: A



Watch Video Solution

14. AB is a chord of the parabola $y^2 = 4ax$ with its vertex at A. BC is drawn perpendicular to AB meeting the axis at C. The projection of BC on the axis of the parabola is

A. a

B. $2a$

C. $4a$

D. $8a$

Answer: C



Watch Video Solution

15. Set of value of α for which the point $(\alpha, 1)$ lies inside the circle $x^2 + y^2 - 4 = 0$ and parabola $y^2 = 4x$ is

A. $|\alpha| < \sqrt{3}$

B. $|\alpha| < 2$

C. $\frac{1}{4} < \alpha < \sqrt{3}$

D. none of these

Answer: C



Watch Video Solution

16. If X is the foot of the directrix on the a parabola. PP' is a double ordinate of the curve and PX meets the curve again in Q . Then prove that $P'Q$ passes through the focus of the parabola.

A. vertex

B. focus

C. midpoint of vertex and focus

D. none of these

Answer: B



Watch Video Solution

17. A water jet from a function reaches its maximum height of 4 m at a distance 0.5 m from the vertical passing through the point O of water outlet. The height of the jet above the horizontal OX at a distance of 0.75 m from the point O is 5 m (b) 6 m (c) 3 m (d) 7 m

A. 5 m

B. 6 m

C. 3 m

D. 7 m

Answer: C

[Watch Video Solution](#)

18. Area of the triangle formed by the vertex, focus and one end of latusrectum of the parabola $(x + 2)^2 = -12(y - 1)$ is

A. 36

B. 18

C. 9

D. 6

Answer: C

[Watch Video Solution](#)

19. The locus of the vertex of the family of parabolas

$$y = \frac{a^3 x^2}{3} + \frac{a^{2x}}{2} - 2a \text{ is } xy = \frac{105}{64} \quad (\text{b}) \quad xy = \frac{3}{4} \quad xy = \frac{35}{16}$$

$$(\text{d}) \quad xy = \frac{64}{105}$$

A. $xy=105/64$

B. $xy=3/4$

C. $xy=35/16$

D. $xy=64/105$

Answer: A



Watch Video Solution

20. Two parabola have the same focus. If their directrices are the x-axis and the y-axis respectively, then the slope of their common chord is :

A. ± 1

B. $4/3$

C. $3/4$

D. none of these

Answer: A



Watch Video Solution

21. The locus of the point $\left(\sqrt{3h}, \sqrt{\sqrt{3k} + 2}\right)$ if it lies on the line $x - y - 1 = 0$ is straight line (b) a circle a parabola (d) none of these

A. a straight line

B. a circle

C. a parabola

D. none of these

Answer: C



Watch Video Solution

22. A circle touches the x -axis and also touches the circle with center $(0, 3)$ and radius 2. The locus of the center

- A. a circle
- B. an ellipse
- C. a parabola
- D. a hyperbola

Answer: C



Watch Video Solution

23. If parabolas $y^2 = \lambda x$ and

$25[(x - 3)^2 + (y + 2)^2] = (3x - 4y - 2)^2$ are equal, then

the value of λ is 9 (b) 3 (c) 7 (d) 6

A. 9

B. 3

C. 7

D. 6

Answer: D



Watch Video Solution

24. The length of the latus rectum of the parabola

whose focus is a. $\left(\frac{u^2}{2g}\sin 2\alpha, -\frac{u^2}{2g}\cos 2\alpha\right)$ and directrix

is $y = \frac{u^2}{2g}$ is (a) $\frac{u^2}{g}\cos^2\alpha$ (b) $\frac{u^2}{g}\cos^2 2\alpha$ (c) $\frac{2u^2}{g}\cos^2 2\alpha$ (d) $\frac{2u^2}{g}\cos^2\alpha$

A. $\frac{u^2}{g}\cos^2\alpha$

B. $\frac{u^2}{g}\cos 2\alpha$

C. $\frac{2u^2}{g}\cos 2\alpha$

D. $\frac{2u^2}{g}\cos^2\alpha$

Answer: D



Watch Video Solution

25. The graph of the curve $x^2 + y^2 - 2xy - 8x - 8y + 32 = 0$ falls wholly in the (a) first quadrant (b) second quadrant third quadrant (d) none of these

- A. first quadrant
- B. second quadrant
- C. third quadrant
- D. none of these

Answer: A



Watch Video Solution

26. The vertex of the parabola whose parametric equation is $x = t^2 - t + 1, y = t^2 + t + 1; t \in R$, is (1, 1)

(b) $(2, 2)$ $\left(\frac{1}{2}, \frac{1}{2}\right)$ (d) $(3, 3)$

A. (1,1)

B. (2,2)

C. (1/2, 1/2)

D. (3,3)

Answer: A



Watch Video Solution

27. If the line $y - \sqrt{3}x + 3 = 0$ cut the parabola

$y^2 = x + 2$ at P and Q , then $APAQ$ is equal to [where

$$A = (\sqrt{3}, 0)] \quad \frac{2(\sqrt{3} + 2)}{3} \quad (b) \quad \frac{4\sqrt{3}}{2} \quad \frac{4(2 - \sqrt{2})}{3} \quad (d)$$

$$\frac{4(\sqrt{3} + 2)}{3}$$

$$A. \frac{2(\sqrt{3} + 2)}{3}$$

$$B. \frac{4\sqrt{3}}{2}$$

$$C. \left(4 \frac{2 - \sqrt{2}}{3} \right)$$

$$D. \left(4 \frac{\sqrt{3} + 2}{3} \right)$$

Answer: D



Watch Video Solution

28. A line is drawn from $A(-2, 0)$ to intersect the curve $y^2 = 4x$ at P and Q in the first quadrant such that $\frac{1}{AP} + \frac{1}{AQ} < \frac{1}{4}$. Then the slope of the line is always.

(a) $> \sqrt{3}$ (b) $< \frac{1}{\sqrt{3}}$ (c) $> \sqrt{2}$ (d) $> \frac{1}{\sqrt{3}}$

A. $> \sqrt{3}$

B. $< 1/\sqrt{3}$

C. $> \sqrt{2}$

D. $> 1/\sqrt{3}$

Answer: A



Watch Video Solution

29. The length of the chord of the parabola $y^2 = x$ which is bisected at the point $(2, 1)$ is $2\sqrt{3}$ (b) $4\sqrt{3}$ (c) $3\sqrt{2}$ (d) $2\sqrt{5}$

A. $2\sqrt{3}$

B. $4\sqrt{3}$

C. $3\sqrt{2}$

D. $2\sqrt{5}$

Answer: D



Watch Video Solution

30. If a line $y = 3x + 1$ cuts the parabola $x^2 - 4x - 4y + 20 = 0$ at A and B , then the tangent of the angle subtended by line segment AB at the origin is (a) $\frac{8\sqrt{3}}{205}$ (b) $\frac{8\sqrt{3}}{209}$ (c) $\frac{8\sqrt{3}}{215}$ (d) none of these

A. $8\sqrt{3}/205$

B. $8\sqrt{3}/209$

C. $8\sqrt{3}/215$

D. none of these

Answer: B



Watch Video Solution

31. If P be a point on the parabola $y^2 = 3(2x - 3)$ and M is the foot of perpendicular drawn from the point P on the directrix of the parabola, then find length of each sides of an equilateral triangle SMP (where S is the focus of the parabola).

A. 2

B. 4

C. 6

D. 8

Answer: C



32. A parabola $y = ax^2 + bx + c$ crosses the x-axis at $(\alpha, 0)(\beta, 0)$ both to the right of the origin. A circle also passes through these two points. The length of a tangent from the origin to the circle is: (a) $\sqrt{\frac{bc}{a}}$
(b) ac^2 (c) b/a (d) $\sqrt{\frac{c}{a}}$

A. $\sqrt{bc/a}$

B. ac^2

C. b/a

D. $\sqrt{c/a}$

Answer: D



Watch Video Solution

33. The number of common chords of the parabolas

$x = y^2 - 6y + 11$ and $y = x^2 - 6x + 11$ is 1 (b) 2 (c) 4 (d)

6

A. 1

B. 2

C. 4

D. 6

Answer: D



Watch Video Solution

34. Two parabola have the same focus. If their directrices are the x-axis and the y-axis respectively, then the slope of their common chord is :

A. -1

B. $-1/2$

C. $-\sqrt{3}/2$

D. none of these

Answer: A



Watch Video Solution

35. PSQ is a focal chord of a parabola whose focus is S and vertex is A. PA, QA, are produced to meet the directrix in R and T. Then $\angle RST$ is equal to

A. 30°

B. 90°

C. 60°

D. 45°

Answer: B



Watch Video Solution

36. If PSQ is a focal chord of the parabola $y^2 = 8x$ such that $SP = 6$, then the length of SQ is 6 (b) 4 (c) 3 (d) none of these

A. 6

B. 4

C. 3

D. none of these

Answer: C



Watch Video Solution

37. The triangle PQR of area A is inscribed in the parabola $y^2 = 4ax$ such that the vertex P lies at the vertex of the parabola and the base QR is a focal chord. The modulus of the difference of the ordinates of the points Q and R is $\frac{A}{2a}$ (b) $\frac{A}{a}$ (c) $\frac{2A}{a}$ (d) $\frac{4A}{a}$

A. $A/2a$

B. A/a

C. $2A/a$

D. $4A/a$

Answer: C



Watch Video Solution

38. If A_1B_1 and A_2B_2 are two focal chords of the parabola $y^2 = 4ax$, then the chords A_1A_2 and B_1B_2 intersect on directrix (b) axis tangent at vertex (d) none of these

A. directrix

B. axis

C. tangent at vertex

D. none of these

Answer: A



Watch Video Solution

39. If a and c are the lengths of segments of any focal chord of the parabola $y^2 = 2bx$, ($b > 0$), then the roots of the equation $ax^2 + bx + c = 0$ are (a) real and distinct (b) real and equal (c) imaginary (d) none of these

A. real and distinct

B. real and equal

C. imaginary

D. none of these

Answer: C



Watch Video Solution

40. If $y = mx + c$ touches the parabola

$y^2 = 4a(x + a)$, then (a) $c = \frac{a}{m}$ (b) $c = am + \frac{a}{m}$

$c = a + \frac{a}{m}$ (d) none of these

A. $c = \frac{1}{m}$

B. $c = am + \frac{a}{m}$

C. $c = a + \frac{a}{m}$

D. none of these

Answer: B



Watch Video Solution

41. The area of the triangle formed by the tangent and the normal to the parabola $y^2 = 4ax$, both drawn at the same end of the latus rectum, and the axis of the parabola is (a) $2\sqrt{2}a^2$ (b) $2a^2$ (c) $4a^2$ (d) none of these

A. $2\sqrt{2}a^2$

B. $2a^2$

C. $4a^2$

D. none of these

Answer: C



Watch Video Solution

42. Parabola $y^2 = 4a(x - c_1)$ and $x^2 = 4a(y - c_2)$

where c_1 and c_2 are variables, touch each other.

Locus of their point of contact is

A. $xy = 2a^2$

B. $xy = 4a^2$

C. $xy = a^2$

D. none of these

Answer: B



Watch Video Solution

43. Let $y = f(x)$ be a parabola, having its axis parallel to the y-axis, which is touched by the line $y = x$ at $x = 1$. Then, $2f(0) = 1 - f'(0)$ (b) $f(0) + f'(0) + f''(0) = 1$ $f'(1) = 1$ (d) $f'(0) = f'(1)$

A. $2f(0)=1-f'(0)$

B. $f(0)+f'(0)+f'(0)=1$

C. $f'(1)=1$

D. none of these

Answer: A



Watch Video Solution

44. If $y = 2x - 3$ is tangent to the parabola

$y^2 = 4a\left(x - \frac{1}{3}\right)$, then a is equal to $\frac{22}{3}$ (b) -1 (c) $\frac{14}{3}$

(d) $\frac{-14}{3}$

A. $\frac{22}{3}$

B. -1

C. $\frac{14}{3}$

D. $\frac{14}{3}$

Answer: D



Watch Video Solution

45. The locus of the center of a circle which cuts orthogonally the parabola $y^2 = 4x$ at (1,2) is a curve

A. (3,4)

B. (4,3)

C. (5,3)

D. (2,4)

Answer: A



Watch Video Solution

46. If the parabola $y = ax^2 - 6x + b$ passes through (0, 2) and has its tangent at $x = \frac{3}{2}$ parallel to the x-axis, then (a) $a = 2, b = -2$ (b) $a = 2, b = 2$
 $a = -2, b = 2$ (d) $a = -2, b = -2$

A. $a=2, b=-2$

B. $a=2, b=2$

C. $a=-2, b=2$

D. $a=-2, b=-2$

Answer: B



Watch Video Solution

47. Double ordinate AB of the parabola $y^2 = 4ax$

subtends an angle $\frac{\pi}{2}$ at the focus of the parabola.

Then the tangents drawn to the parabola at A and B

will intersect at (a) $(-4a, 0)$ (b) $(-2a, 0)$ (c) $(-3a, 0)$ (d)

none of these

A. $(-4a, 0)$

B. $(-2a, 0)$

C. $(-3a, 0)$

D. none of these

Answer: A



Watch Video Solution

48. find the equation of hyperbola where foci are $(0, 12)$ and $(0, -12)$ and the length of the latus rectum is 36



Watch Video Solution

49. A tangent is drawn to the parabola $y^2 = 4ax$ at the point P whose abscissa lies in the interval $(1, 4)$. The maximum possible area of the triangle formed by the tangent at P , the ordinates of the point P , and the x-axis is equal to 8 (b) 16 (c) 24 (d) 32

A. 8

B. 16

C. 24

D. 32

Answer: B



50. The straight lines joining any point P on the parabola $y^2 = 4ax$ to the vertex and perpendicular from the focus to the tangent at P intersect at R .

Then the equation of the locus of R is

(a) $x^2 + 2y^2 - ax = 0$ (b) $2x^2 + y^2 - 2ax = 0$ (c)

$2x^2 + 2y^2 - ay = 0$ (d) $2x^2 + y^2 - 2ay = 0$

A. $x^2 + 2y^2 - ax = 0$

B. $2x^2 + y^2 - ax = 0$

C. $2x^2 + 2y^2 - ay = 0$

D. $2x^2 + y^2 - ay = 0$

Answer: B



Watch Video Solution

51. Through the vertex O of the parabola $y^2 = 4ax$, two chords OP and OQ are drawn and the circles on OP and OQ as diameters intersect at R . If θ_1, θ_2 , and ϕ are the angles made with the axis by the tangents at P and Q on the parabola and by OR , then value of $\cot\theta_1 + \cot\theta_2$ is (a) $-2\tan\phi$ (b) $-2\tan(\pi - \phi)$ (c) 0 (d) $2\cot\phi$

A. $-2\tan\phi$

B. $-2\tan(\pi - \phi)$

C. 0

D. $2\cot\phi$

Answer: A



Watch Video Solution

52. AB is a double ordinate of the parabola $y^2 = 4ax$. Tangents drawn to the parabola at A and B meet the y -axis at A_1 and B_1 , respectively. If the area of trapezium V_1B_1B is equal to $12a^2$, then the angle

subtended by A_1B_1 at the focus of the parabola is equal to $2\tan^{-1}(3)$ (b) $\tan^{-1}(3)$ $2\tan^{-1}(2)$ (d) $\tan^{-1}(2)$

A. $2\tan^{-1}(3)$

B. $\tan^{-1}(3)$

C. $2\tan^{-1}(2)$

D. $\tan^{-1}(2)$

Answer: C



Watch Video Solution

53. If the locus of the middle of point of contact of tangent drawn to the parabola $y^2 = 8x$ and the foot

of perpendicular drawn from its focus to the tangents is a conic, then the length of latus rectum of this conic is $\frac{9}{4}$ (b) 9 (c) 18 (d) $\frac{9}{2}$

A. $9/4$

B. 9

C. 18

D. $9/2$

Answer: B



Watch Video Solution

54. If the bisector of angle APB , where PA and PB are the tangents to the parabola $y^2 = 4ax$, is equally inclined to the coordinate axes, then the point P lies on the tangent at vertex of the parabola directrix of the parabola circle with center at the origin and radius a the line of the latus rectum.

- A. tangent at vertex of the parabola
- B. directrix of the parabola
- C. circle with center at the origin and radius
- D. the line of latus rectum

Answer: D



55. From a point $A(t)$ on the parabola $y^2 = 4ax$, a focal chord and a tangent are drawn. Two circles are drawn in which one circle is drawn taking focal chord AB as diameter and other is drawn by taking the intercept of tangent between point A and point of the circles is

- A. the line joining focus and p
- B. the line joining focus and A
- C. tangent to the parabola at point A
- D. none of these

Answer: C



View Text Solution

56. The point of intersection of the tangents of the parabola $y^2 = 4x$ drawn at the endpoints of the chord $x + y = 2$ lies on

(a) $x - 2y = 0$ (b) $x + 2y = 0$ (c) $y - x = 0$ (d) $x + y = 0$

A. $x - 2y = 0$

B. $x + 2y = 0$

C. $y - x = 0$

D. $x + y = 0$

Answer: C



Watch Video Solution

57. The angle between tangents to the parabola $y^2 = 4ax$ at the points where it intersects with the line $x - y - a = 0$ is ($a > 0$)

A. $\pi/3$

B. $\pi/4$

C. $\pi/6$

D. $\pi/2$

Answer: D



Watch Video Solution

58. $y = x + 2$ is any tangent to the parabola $y^2 = 8x$

The point P on this tangent is such that the other tangent from it which is perpendicular to it is (a) $(2, 4)$ (b) $(-2, 0)$ (c) $(-1, 1)$ (d) $(2, 0)$

A. $(2,4)$

B. $(-2,0)$

C. $(-1,1)$

D. $(2,0)$

Answer: B



Watch Video Solution

59. If $y = m_1x + c$ and $y = m_2x + c$ are two tangents to the parabola $y^2 + 4a(x + c) = 0$, then $m_1 + m_2 = 0$

(b) $1 + m_1 + m_2 = 0$ $m_1m_2 - 1 = 0$ (d) $1 + m_1m_2 = 0$

A. $m_1 + m_2 = 0$

B. $1 + m_1 + m_2 = 0$

C. $m_1m_2 - 1 = 0$

D. $1 + m_1m_2 = 0$

Answer: D



Watch Video Solution

60. The angle between the tangents to the curve

$y = x^2 - 5x + 6$ at the point $(2, 0)$ and $(3, 0)$ is $\frac{\pi}{2}$ (b) $\frac{\pi}{3}$

(c) π (d) $\frac{\pi}{4}$

A. $\frac{\pi}{2}$

B. $\frac{\pi}{3}$

C. $\frac{\pi}{6}$

D. $\frac{\pi}{4}$

Answer: A



Watch Video Solution

61. Two mutually perpendicular tangents of the parabola $y^2 = 4ax$ meet the axis at P_1 and P_2 . If S is the focal of the parabola, Then $\frac{1}{SP_1} + \frac{1}{SP_2}$ is equal to

A. $\frac{1}{2a}$

B. $\frac{1}{a}$

C. $\frac{2}{a}$

D. $\frac{4}{a}$

Answer: B



Watch Video Solution

62. Radius of the circle that passes through the origin and touches the parabola $y^2 = 4ax$ at the point $(a, 2a)$ is $\frac{5}{\sqrt{2}}a$ (b) $2\sqrt{2}a$ $\sqrt{\frac{5}{2}}a$ (d) $\frac{3}{\sqrt{2}}a$

A. $\frac{5}{\sqrt{2}}a$

B. $2\sqrt{2}a$

C. $\sqrt{\frac{5}{2}}a$

D. $\frac{3}{\sqrt{2}}a$

Answer: A



Watch Video Solution

63. The mirror image of the parabola $y^2 = 4x$ in the tangent to the parabola at the point $(1, 2)$ is:

A. $(x - 1)^2 = 4(y + 1)$

B. $(x + 1)^2 = 4(y + 1)$

C. $(x + 1)^2 = 4(y - 1)$

D. $(x - 1)^2 = 4(y - 1)$

Answer: C

64. Consider the parabola $y^2 = 4x$. Let $A \equiv (4, -4)$ and $B \equiv (9, 6)$ be two fixed points on the parabola.

Let C be a moving point on the parabola between A and B such that the area of the triangle ABC is

maximum. Then the coordinates of C are (a) $\left(\frac{1}{4}, 1\right)$

(b) $(4, 4)$ (c) $\left(3, \frac{2}{\sqrt{3}}\right)$ (d) $(3, -2\sqrt{3})$

A. $(1/4, 1)$

B. $(4, 4)$

C. $(3, 2\sqrt{3})$

D. $(3, -2\sqrt{3})$

Answer: A



Watch Video Solution

65. A line of slope $\lambda (0 < \lambda < 1)$ touches the parabola $y + 3x^2 = 0$ at P . If S is the focus and M is the foot of the perpendicular of directrix from P , then $\tan \angle MPS$ equals (a) 2λ (b) $\frac{2\lambda}{-1 + \lambda^2}$ (c) $\frac{1 - \lambda^2}{1 + \lambda^2}$ (d) none of these

A. 2λ

B. $\frac{2\lambda}{-1 + \lambda^2}$

C. $\frac{1 - \lambda^2}{1 + \lambda^2}$

D. none of these

Answer: B



Watch Video Solution

66. The tangent at any point P on the parabola $y^2 = 4ax$ intersects the y -axis at Q . Then tangent to the circumcircle of triangle PQS (S is the focus) at Q is a line parallel to x -axis y -axis a line parallel to y -axis
(d) none of these

A. a line parallel to axis

B. y-axis

C. a line parallel to y-axis

D. none of these

Answer: B



Watch Video Solution

67. If $P(t^2, 2t)$, $t \in [0, 2]$, is an arbitrary point on the parabola $y^2 = 4x$, Q is the foot of perpendicular from focus S on the tangent at P , then the maximum area of PQS is (a) 1 (b) 2 (c) $\frac{5}{16}$ (d) 5

A. 1

B. 2

C. 5/16

D. 5

Answer: D



Watch Video Solution

68. The minimum area of circle which touches the parabolas $y = x^2 + 1$ and $y^2 = x - 1$ is $\frac{9\pi}{16}$ squnit (b)

$\frac{9\pi}{32}$ squnit $\frac{9\pi}{8}$ squnit (d) $\frac{9\pi}{4}$ squnit

A. $\frac{9\pi}{16}$ sq. unit

B. $\frac{9\pi}{32}$ sq. unit

C. $\frac{9\pi}{8}$ sq. unit

D. $\frac{9\pi}{4}$ sq. unit

Answer: B



Watch Video Solution

69. If the tangents and normals at the extremities of a focal chord of a parabola intersect at (x_1, y_1) and (x_2, y_2) , respectively, then (a) $x_1 = y_2$ (b) $x_1 = y_1$ (c) $y_1 = y_2$ (d) $x_2 = y_1$

A. $x_1 = y_2$

B. $x_1 = y_1$

C. $y_1 = y_2$

D. $x_2 = y_1$

Answer: C



Watch Video Solution

70. At what point on the parabola $y^2 = 4x$ the normal makes equal angle with the axes? (4, 4) (b) (9, 6) (d) (4, - 4) (d) (1, ± 2)

A. (4,4)

B. (9,6)

C. (4,-4)

D. (1, ± 2)

Answer: D



Watch Video Solution

71. The line $2x + y + \lambda = 0$ is a normal to the parabola

$$y^2 = -8x, \text{ is } \lambda =$$

A. 12

B. -12

C. 24

D. -24

Answer: C



Watch Video Solution

72. about to only mathematics

A. $(-2a, 0)$

B. $(a, 0)$

C. $(2a, 0)$

D. none of these

Answer: B



Watch Video Solution

73. The equation of the line that passes through (10, -1) and is perpendicular to $y = \frac{x^2}{4} - 2$ is
4x + y = 39 (b) 2x + y = 19 x + y = 9 (d) x + 2y = 8

A. $4x + y = 39$

B. $2x + y = 19$

C. $x + y = 9$

D. $x+2y=8$

Answer: D



Watch Video Solution

74. Tangent and normal drawn to a parabola at $A(at^2, 2at)$, $t \neq 0$ meet the x-axis at point B and D , respectively. If the rectangle $ABCD$ is completed, then the locus of C is

(a) $y = 2a$ (b) $y + 2a = c$ (c) $x = 2a$ (d) none of these

A. $y=2a$

B. $x = 2a - \frac{y^2}{4a}$

C. $x=2a$

D. none of these

Answer: B



Watch Video Solution

75. The radius of the circle touching the parabola

$y^2 = x$ at $(1, 1)$ and having the directrix of $y^2 = x$ as its

normal is $\frac{5\sqrt{5}}{8}$ (b) $\frac{10\sqrt{5}}{3}$ $\frac{5\sqrt{5}}{4}$ (d) none of these

A. $5\sqrt{5}/8$

B. $10\sqrt{5}/3$

C. $5\sqrt{5}/4$

D. none of these

Answer: C



Watch Video Solution

76. If two different tangents of $y^2 = 4x$ are the normals to $x^2 = 4by$, then $|b| > \frac{1}{2\sqrt{2}}$ (b) $|b| < \frac{1}{2\sqrt{2}}$

$|b| > \frac{1}{\sqrt{2}}$ (d) $|b| < \frac{1}{\sqrt{2}}$

A. $|b| > 1/2\sqrt{2}$

B. $|b| < 1/2\sqrt{2}$

C. $|b| < 1/\sqrt{2}$

D. $|b| < 1/\sqrt{2}$

Answer: B



Watch Video Solution

77. Maximum number of common normals of

$y^2 = 4ax$ and $x^2 = 4by$ is ____

A. 3

B. 4

C. 6

D. 5

Answer: D



Watch Video Solution

78. If line PQ , where equation is $y = 2x + k$, is a normal to the parabola whose vertex is $(-2, 3)$ and the axis parallel to the x -axis with latus rectum equal to 2, then the value of k is $\frac{58}{8}$ (b) $\frac{50}{8}$ (c) 1 (d) -1

A. $58/8$

B. $50/8$

C. 1

D. -1

Answer: C



Watch Video Solution

79.

$$\min \left[(x_1 - x_2)^2 + \left(5 + \sqrt{1 - x_1^2} - \sqrt{4x_2} \right)^2 \right], \forall x_1, x_2 \in R,$$

is (a) $4\sqrt{5} + 1$ (b) $3 - 2\sqrt{2}$ (c) $\sqrt{5} + 1$ (d) $\sqrt{5} - 1$

A. $4\sqrt{1}$

B. $3 - 2\sqrt{2}$

C. $\sqrt{5} + 1$

D. $\sqrt{5} - 1$

Answer: B



Watch Video Solution

80. If the normals to the parabola $y^2 = 4ax$ at three points $(ap^2, 2ap)$, and $(aq^2, 2aq)$ are concurrent, then the common root of equations $Px^2 + qx + r = 0$ and $a(b - c)x^2 + b(c - a)x + c(a - b) = 0$ is p (b) q (c) r (d) 1

A. p

B. q

C. r

D. 1

Answer: D



Watch Video Solution

81. Normals AO , ∇_1 and ∇_2 are drawn to the parabola $y^2 = 8x$ from the point $A(h, 0)$. If triangle OA_1A_2 is equilateral then the possible value of h is 26 (b) 24 (c) 28 (d) none of these

A. 26

B. 24

C. 28

D. none of these

Answer: C



Watch Video Solution

82. If the normals to the parabola $y^2 = 4ax$ at the ends of the latus rectum meet the parabola at Q and Q' , then QQ' is 10a (b) 4a (c) 20c (d) 12a

A. 10a

B. 4a

C. $20a$

D. $12a$

Answer: D



Watch Video Solution

83. From a point $(\sin\theta, \cos\theta)$, if three normals can be drawn to the parabola $y^2 = 4ax$ then the value of a is

A. $(1/2, 1)$

B. $[-1/2, 0)$

C. $[1/2, 1]$

D. $\left(-\frac{1}{2}, 0 \cup (0, 12)\right)$

Answer: D



Watch Video Solution

84. If the normals at $P(t_1)$ and $Q(t_2)$ on the parabola meet on the same parabola, then

A. $t_1 t_2 = -1$

B. $t_2 = -t_1 - \frac{2}{t_1}$

C. $t_1 t_2 = 1$

D. $t_1 t_2 = 2$

Answer: D



Watch Video Solution

85. If the normals to the parabola $y^2 = 4ax$ at P meets the curve again at Q and if PQ and the normal at Q make angle α and β , respectively, with the x-axis, then $\tan\alpha(\tan\alpha + \tan\beta)$ has the value equal to 0 (b) -2 (c) $-\frac{1}{2}$ (d) -1

A. 0

B. -2

C. $-1/2$

D. -1

Answer: B



Watch Video Solution

86. PQ is a normal chord of the parabola $y^2 = 4ax$ at P, A being the vertex of the parabola. Through P, a line is drawn parallel to AQ meeting the x-axis at R. Then the line length of AR is

(A) equal to the length of the latus rectum (B) equal to the focal distance of the point P (C) equal to twice the focal distance of the point P (D) equal to the distance of the point P from the directrix.

- A. equal to the length of the latus rectum
- B. equal to the focal distance of the point P
- C. equal to twice focal distance of the point P
- D. equal to the distance of the point P from the directrix

Answer: C



Watch Video Solution

87. P , Q , and R are the feet of the normals drawn to a parabola $(y - 3)^2 = 8(x - 2)$. A circle cuts the above parabola at points P , Q , R , and S . Then this circle

always passes through the point. (2, 3) (b) (3, 2) (c)
(0, 3) (d) (2, 0)

A. (2,3)

B. (3,2)

C. (0,3)

D. (2,0)

Answer: A



Watch Video Solution

88. Normals at two points (x_1, y_1) and (x_2, y_2) of the parabola $y^2 = 4x$ meet again on the parabola, where

$x_1 + x_2 = 4$. Then $|y_1 + y_2|$ is equal to $\sqrt{2}$ (b) $2\sqrt{2}$ (c) $4\sqrt{2}$ (d) none of these

A. $\sqrt{2}$

B. $2\sqrt{2}$

C. $4\sqrt{2}$

D. none of these

Answer: C



Watch Video Solution

89. The endpoints of two normal chords of a parabola are concyclic. Then the tangents at the feet

of the normals will intersect at

a. Tangent at vertex of the parabola

b. Axis of the parabola

c. Directrix of the parabola

d. None of these

A. tangent at vertex of the parabola

B. axis of the parabola

C. directrix of the parabola

D. none of these

Answer: B



Watch Video Solution

90. If normal at point P on the parabola $y^2 = 4ax$, ($a > 0$), meets it again at Q in such a way that OQ is of minimum length, where O is the vertex of parabola, then OPQ is a right angled triangle an obtuse angled triangle an acute angle triangle none of these

- A. a right-angled triangle
- B. an obtuse-angled triangle
- C. an acute-angled triangle
- D. none of these

Answer: A



91. The set of points on the axis of the parabola $(x - 1)^2 = 8(y + 2)$ from where three distinct normals can be drawn to the parabola is the set (h, k) of points satisfying

A. $h > 2$

B. $h > 1$

C. $k > 2$

D. none of these

Answer: C

92. Tangent and normal are drawn at the point $P \equiv (16, 16)$ of the parabola $y^2 = 16x$ which cut the axis of the parabola at the points A and B , respectively. If the center of the circle through P, A and B is C , then the angle between PC and the axis of x is

A. (a) $\tan^{-1}\left(\frac{1}{2}\right)$

B. (b) $\tan^{-1}2$

C. (c) $\tan^{-1}\left(\frac{3}{4}\right)$

D. (d) $\tan^{-1}\left(\frac{4}{3}\right)$

Answer: D



Watch Video Solution

93. In parabola $y^2=4x$, From the point $(15,12)$, three normals are drawn then centroid of triangle formed by three Co normal points is

A. $(16/3, 0)$

B. $(4, 0)$

C. $(26/3, 0)$

D. $(6, 0)$

Answer: C



Watch Video Solution

94. The line $x - y = 1$ intersects the parabola $y^2 = 4x$ at A and B . Normals at A and B intersect at C . If D is the point at which line CD is normal to the parabola, then the coordinates of D are (a) $(4, -4)$ (b) $(4, 4)$ (c) $(-4, -4)$ (d) none of these

A. $(4, -4)$

B. $(4, 4)$

C. $(-4, -4)$

D. none of these

Answer: B



Watch Video Solution

95. If normal are drawn from a point $P(h, k)$ to the parabola $y^2 = 4ax$, then the sum of the intercepts which the normals cut-off from the axis of the parabola is (a) $(h + c)$ (b) $3(h + a)$ (c) $2(h + a)$ (d) none of these

A. $(h+a)$

B. $3(h+a)$

C. $2(h+a)$

D. none of these

Answer: C



Watch Video Solution

96. The circle $x^2 + y^2 + 2\lambda x = 0, \lambda \in R$, touches the parabola $y^2 = 4x$ externally. Then,

A. $\lambda > 0$

B. $\lambda < 0$

C. $\lambda > 1$

D. none of these

Answer: A



Watch Video Solution

97. The radius of the circle whose centre is $(-4,0)$ and which cuts the parabola $y^2 = 8x$ at A and B such that the common chord AB subtends a right angle at the vertex of the parabola is equal to

A. $4\sqrt{13}$

B. $3\sqrt{5}$

C. $3\sqrt{2}$

D. $2\sqrt{5}$

Answer: A



Watch Video Solution

98. If normal at point P on the parabola $y^2 = 4ax$, ($a > 0$), meets it again at Q in such a way that OQ is of minimum length, where O is the vertex of parabola, then OPQ is a right angled triangle an obtuse angled triangle an acute angle triangle none of these

A. a right-angled triangle

B. an obtuse-angled triangle

C. an acute-angled triangle

D. none of these

Answer: A



Watch Video Solution

Exercise Multiple Correct Answer Type

1. If the focus of the parabola $x^2 - ky + 3 = 0$ is $(0,2)$,
then a values of k is (are) 4 (b) 6 (c) 3 (d) 2

A. 4

B. 6

C. 3

D. 2

Answer: B::D



Watch Video Solution

2. If the line $x - 1 = 0$ is the directrix of the parabola

$y^2 - kx + 8 = 0$, then one of the values of k is $\frac{1}{8}$ (b) 8

(c) 4 (d) $\frac{1}{4}$

A. -8

B. $1/8$

C. $1/4$

D. 4

Answer: A::D



Watch Video Solution

3. The extremities of latus rectum of a parabola are $(1, 1)$ and $(1, -1)$. Then the equation of the parabola can be $y^2 = 2x - 1$ (b) $y^2 = 1 - 2x$ $y^2 = 2x - 3$ (d) $y^2 = 2x - 4$

A. $y^2 + 2x - 1$

B. $y^2 = 1 - 2x$

C. $y^2 = 3 - 2x$

D. $y^2 = 2x - 4$

Answer: A::C



Watch Video Solution

4. The value(s) of a for which two curves $y = ax^2 + ax + \frac{1}{24}$ and $x = ay^2 + ay + \frac{1}{24}$ touch each other is/are

A. $\frac{2}{3}$

B. $\frac{1}{3}$

C. $\frac{3}{2}$

D. $\frac{1}{2}$

Answer: A::C



Watch Video Solution

5. In which of the following cases, a unique parabola will be obtained ?

A. (a) Focus and equation of tangent at vertex
are given.

B. (b) Focus and vertex are given

C. (c) Equation of directrix and vertex are given.

D. (d) Equation of directrix and equation of
tangent at vertex are given.

Answer: A::B::C



Watch Video Solution

6. A quadrilateral is inscribed in a parabola. Then the quadrilateral may be cyclic diagonals of the

quadrilateral may be equal all possible pairs of adjacent side may be perpendicular none of these

A. the quadrilateral may be cyclic

B. diagonals of the quadrilateral may be equal

C. all possible pairs of adjacent sides may be perpendicular

D. none of these

Answer: A::B



Watch Video Solution

7. The locus of the midpoint of the focal distance of a variable point moving on the parabola $y^2 = 4ax$ is a parabola whose (a) latus rectum is half the latus rectum of the original parabola (b) vertex is $\left(\frac{a}{2}, 0\right)$ (c) directrix is y-axis. (d) focus has coordinates $(a, 0)$

A. latus rectum is half the latus rectum of the original parabola

B. vertex is $(a/2, 0)$

C. directrix is y-axis

D. focus has coordinates $(a, 0)$

Answer: A::B::C::D



Watch Video Solution

8. A square has one vertex at the vertex of the parabola $y^2 = 4ax$ and the diagonal through the vertex lies along the axis of the parabola. If the ends of the other diagonal lie on the parabola, the coordinates of the vertices of the square are $(4a, 4a)$ (b) $(4a, -4a)$ (0, 0) (d) $(8a, 0)$

A. $(4a, 4a)$

B. $(4a, -4a)$

C. $(0, 0)$

D. $(8a, 0)$

Answer: A::B::C



Watch Video Solution

9. If two distinct chords of a parabola $y^2 = 4ax$, passing through $(a, 2a)$ are bisected by the line $x+y=1$,then length of latus rectum can be a) 2 b) 7 c) 4 d) 5

A. 2

B. 1

C. 4

D. 3

Answer: A::B::D



Watch Video Solution

10. about to only mathematics

A. (16,8)

B. (16,-8)

C. (9,6)

D. (9,-6)

Answer: A::B



Watch Video Solution

11. If the parabola $x^2 = ay$ makes an intercept of length $\sqrt{40}$ unit on the line $y - 2x = 1$ then a is equal to

A. -1

B. -2

C. 1

D. 2

Answer: B::C



Watch Video Solution

12. The equation of the directrix of the parabola with vertex at the origin and having the axis along the x-axis and a common tangent of slope 2 with the circle $x^2 + y^2 = 5$ is (are) $x = 10$ (b) $x = 20$ $x = -10$ (d) $x = -20$

A. $x=10$

B. $x=20$

C. $x=-10$

D. $x=-20$

Answer: A::C



Watch Video Solution

13. Tangent is drawn at any point (x_1, y_1) other than the vertex on the parabola $y^2 = 4ax$. If tangents are drawn from any point on this tangent to the circle $x^2 + y^2 = a^2$ such that all the chords of contact pass through a fixed point (x_2, y_2) , then (a) x_1, a, x_2 in

GP (b) $\frac{y_1}{2}, a, y_2$ are in GP

(c) $-4, \frac{y_1}{y_2}, \frac{x_1}{x_2}$ are in GP (d) $x_1x_2 + y_1y_2 = a^2$

A. x_1, a, x_2 are in GP

B. $\frac{y_1}{2}, a, y_2$ are in GP

C. $-4\frac{y_1}{y_2}, \frac{x_1}{x_2}$ are in GP

D. $x_1x_2 + y_1y_2 = a^2$

Answer: B::C::D



Watch Video Solution

14. The parabola $y^2 = 4x$ and the circle having its center at $(6, 5)$ intersect at right angle. Then find the possible points of intersection of these curves.

A. $(9,6)$

B. $(2, \sqrt{8})$

C. $(4,4)$

D. $(3, 2\sqrt{3})$

Answer: A::C



Watch Video Solution

15. Which of the following line can be tangent to the parabola $y^2 = 8x$?
 $x - y + 2 = 0$ (b) $9x - 3y + 2 = 0$
 $x + 2y + 8 = 0$ (d) $x + 3y + 12 = 0$

A. $x - y + 2 = 0$

B. $9x - 3y + 2 = 0$

C. $x + 2y + 8 = 0$

D. $x + 3y + 12 = 0$

Answer: A::B::C



Watch Video Solution

16. If the line $k^2(x - 1) + k(y - 2) + 1 = 0$ touches the parabola $y^2 - 4x - 4y + 8 = 0$, then k can be

A. -3

B. $-\sqrt{5}$

C. $\frac{7}{19}$

D. 1000

Answer: A::B::C::D



17. The equation of a circle of radius 1 touching the circles $x^2 + y^2 - 2|x| = 0$ is (a) $x^2 + y^2 + 2\sqrt{2}x + 1 = 0$
(b) $x^2 + y^2 - 2\sqrt{3}y + 2 = 0$ (c) $x^2 + y^2 + 2\sqrt{3}y + 2 = 0$
(d) $x^2 + y^2 - 2\sqrt{2} + 1 = 0$

A. $y = 4\sqrt{5}x + 20$

B. $y = 4\sqrt{3}x - 12$

C. $y=0$

D. $y = -4\sqrt{5}x - 20$

Answer: A::B::C





Watch Video Solution

18. about to only mathematics

A. $y=4(x-1)$

B. $y=0$

C. $y=-4(x-1)$

D. $y=-30x-50$

Answer: A::B



Watch Video Solution

19. The line $x + y + 2 = 0$ is a tangent to a parabola at point A, intersect the directrix at B and tangent at vertex at C respectively. The focus of parabola is $S(a, 0)$. Then

A. CS is perpendicular to AB

B. $AC \cdot BC = CS^2$

C. $AC \cdot BC = 8$

D. $AC=BC$

Answer: A::B::C



Watch Video Solution

20. Which of the following line can be normal to parabola $y^2 = 12x$?
 $x + y - 9 = 0$ (b) $2x - y - 32 = 0$
 $2x + y - 36 = 0$ (d) $3x - y - 72 = 0$

A. $x+y-9=0$

B. $2x-y-32=0$

C. $2x+y-36=0$

D. $3x-y-99=0$

Answer: A::C::D



Watch Video Solution

21. A normal drawn to the parabola $y^2 = 4ax$ meets the curve again at Q such that the angle subtended by PQ at the vertex is 90° . Then the coordinates of P can be $(8a, 4\sqrt{2}a)$ (b) $(8a, 4a)$ $(2a, -2\sqrt{2}a)$ (d) $(2a, 2\sqrt{2}a)$

A. $(8a, 4\sqrt{2}a)$

B. $(8a, 4a)$

C. $(2a, -2\sqrt{2}a)$

D. $(2a, 2\sqrt{2}a)$

Answer: C::D



Watch Video Solution

22. A circle is drawn having centre at $C(0, 2)$ and passing through focus (S) of the parabola $y^2 = 8x$, if radius (CS) intersects the parabola at point P, then

A. distance of point P from directrix is $(8 - 4\sqrt{2})$

B. distance of point C from point P is $(6\sqrt{2} - 8)$

C. angle subtended by intercept made by circle on directrix at its centre is $\frac{\pi}{2}$

D. point P is the midpoint of C and S

Answer: A::B::C



Watch Video Solution

23. From any point P on the parabola $y^2 = 4ax$, perpendicular PN is drawn on the meeting it at N. Normal at P meets the axis in G. For what value/values of t, the point N divides SG internally in the ratio 1 : 3, where S is the focus ? a. $\sqrt{\frac{3}{5}}$ b. $-\sqrt{\frac{5}{3}}$ c.

$-\sqrt{\frac{3}{5}}$ d. $\sqrt{\frac{5}{3}}$

A. $\sqrt{\frac{3}{5}}$

B. $\sqrt{-\frac{5}{3}}$

C. $\sqrt{-\frac{3}{5}}$

D. $\sqrt{\frac{5}{3}}$

Answer: B::D



Watch Video Solution

24. Let P be the point (1,0) and Q be a point on the locus $y^2 = 8x$. The locus of the midpoint of PQ is

A. P_1 lies on C_2 and Q_1 lies on C_1

B. $PQ \geq \min \{PP_1, QQ_1\}$

C. point P_0 on C_1 such that $P_0Q_0 \leq PQ$ for all

pairs of points (P,Q) is $\left(\frac{1}{3}, \frac{10}{9}\right)$

D. point Q_0 on C_2 such that $P_0Q_0 \leq PQ$ for all

pairs of points (P,Q) is $\left(\frac{10}{9}, \frac{1}{3}\right)$

Answer: A::B



Watch Video Solution

25. The value(s) of a for which two curves

$y = ax^2 + ax + \frac{1}{24}$ and $x = ay^2 + ay + \frac{1}{24}$ touch each

other is/are

A. $\frac{2}{3}$

B. $\frac{1}{3}$

C. $\frac{3}{2}$

D. $\frac{1}{2}$

Answer: A::C



Watch Video Solution

26. From any point P on the parabola $y^2 = 4ax$, perpendicular PN is drawn on the meeting it at N.

Normal at P meets the axis in G. For what value/values of t, the point N divides SG internally in

the ratio 1 : 3, where S is the focus ? a. $\sqrt{\frac{3}{5}}$ b. $-\sqrt{\frac{5}{3}}$ c.

$-\sqrt{\frac{3}{5}}$ d. $\sqrt{\frac{5}{3}}$

A. $\sqrt{\frac{3}{5}}$

B. $\sqrt{-\frac{5}{3}}$

C. $\sqrt{-\frac{3}{5}}$

D. $\sqrt{\frac{5}{3}}$

Answer: B::D



Watch Video Solution

Linked Comprehension Type

1. A tangent is drawn at any point $P(t)$ on the parabola $y^2 = 8x$ and on it is takes a point $Q(\alpha, \beta)$ from which a pair of tangent QA and OB are drawn to the circle $x^2 + y^2 = 8$. Using this information, answer the following questions :

The locus of the point of concurrency of the chord of contact AB of the circle $x^2 + y^2 = 8$ is

A. $y^2 - 2x = 0$

B. $y^2 - x^2 = 4$

C. $y^2 + 4x = 0$

D. $y^2 - 2x^2 = 4$

Answer: C



Watch Video Solution

2. A tangent is drawn at any point $P(t)$ on the parabola $y^2 = 8x$ and on it is takes a point $Q(\alpha, \beta)$ from which a pair of tangent QA and QB are drawn to the circle $x^2 + y^2 = 8$. Using this information, answer the following questions : The point from which perpendicular tangents can be drawn both the given circle and the parabola is

A. $(4, \pm \sqrt{3})$

B. $(-1, \sqrt{2})$

C. $(-\sqrt{2}, -\sqrt{2})$

D. $(-2, \pm 2\sqrt{3})$

Answer: D



Watch Video Solution

3. A tangent is drawn at any point $P(t)$ on the parabola $y^2 = 8x$ and on it is takes a point $Q(\alpha, \beta)$ from which a pair of tangent QA and OB are drawn to the circle $x^2 + y^2 = 8$. Using this information, answer the following questions :

The locus of the point of concurrency of the chord of contact AB of the circle $x^2 + y^2 = 8$ is

A. $x-2y+2=0$

B. $x+2y-4=0$

C. $x-2y-4=0$

D. $x+2y+4=0$

Answer: A



Watch Video Solution

4. Tangent to the parabola $y = x^2 + ax + 1$ at the point of intersection of the y-axis also touches the circle $x^2 + y^2 = r^2$. Also, no point of the parabola is

below the x-axis. The radius of circle when a attains its maximum value is

A. (a) $1/\sqrt{10}$

B. (b) $1/\sqrt{5}$

C. (c) 1

D. (d) $\sqrt{5}$

Answer: B



Watch Video Solution

5. Tangent to the parabola $y = x^2 + ax + 1$ at the point of intersection of the y-axis also touches the

circle $x^2 + y^2 = r^2$. Also, no point of the parabola is below the x-axis.

The slope of the tangents when the radius of the circle is maximum is

A. (a) -1

B. (b) 1

C. (c) 0

D. (d) 2

Answer: C



Watch Video Solution

6. Tangent to the parabola $y = x^2 + ax + 1$ at the point of intersection of the y-axis also touches the circle $x^2 + y^2 = r^2$. Also, no point of the parabola is below the x-axis.

The minimum area bounded by the tangent and the coordinate axes is (a) 1 (b) $1/3$ (c) $1/2$ (d) $1/4$

A. 1

B. $1/3$

C. $1/2$

D. $1/4$

Answer: D



7. The locus of the circumcenter of a variable triangle having sides the y -axis, $y=2$, and $lx+my=1$, where (l,m) lies on the parabola $y^2 = 4x$, is a curve C .

The coordinates of the vertex of this curve C is

A. $(-2, 3/2)$

B. $(-2, -3/2)$

C. $(2, 3/2)$

D. $(2, -3/2)$

Answer: A

[Watch Video Solution](#)

8. If the normal chord of the parabola $y^2 = 4x$ makes an angle 45° with the axis of the parabola, then its length, is

A. $1/4$

B. $1/12$

C. $1/8$

D. $1/16$

Answer: C

[Watch Video Solution](#)

9. The locus of the circumcenter of a variable triangle having sides the y -axis, $y=2$, and $lx+my=1$, where $(1,m)$ lies on the parabola $y^2 = 4x$, is a curve C.

The curve C is symmetric about the line

A. $x = 3/2$

B. $y = -3/2$

C. $x = -3/2$

D. $y = 3/2$

Answer: D



Watch Video Solution

10. $y=x$ is tangent to the parabola $y = ax^2 + c$.

If $a=2$, then the value of c is (a) 1 (b) $-\frac{1}{2}$ (c) $\frac{1}{2}$ (d) $\frac{1}{8}$

A. 1

B. $-\frac{1}{2}$

C. $\frac{1}{2}$

D. $\frac{1}{8}$

Answer: D



Watch Video Solution

11. $y=x$ is tangent to the parabola $y = ax^2 + c$.

If $(1,1)$ is the point of contact, then a is (a) $\frac{1}{4}$ (b) $\frac{1}{3}$ (c) $\frac{1}{2}$ (d) $\frac{1}{6}$

A. $1/4$

B. $1/3$

C. $1/2$

D. $1/6$

Answer: C



Watch Video Solution

12. $y=x$ is tangent to the parabola $y = ax^2 + c$.

If $c=2$, then the point of contact is (a) (3,3) (b) (2,2) (c) (6,6) (d) (4,4)

A. (3,3)

B. (2,2)

C. (6,6)

D. (4,4)

Answer: D



Watch Video Solution

13. find the area of triangle whose vertices are (3,8), (-4,2)and (5,1)



Watch Video Solution

14. If l and m are variable real number such that $5l^2 + 6m^2 - 4lm + 3l = 0$, then the variable line $lx+my=1$ always touches a fixed parabola, whose axes is parallel to the x-axis.

The directrix of the parabola is

A. $(1/6, -7/6)$

B. $(1/3, 4/3)$

C. $(3/2, -3/2)$

D. $(-3/4, 3/4)$

Answer: B



Watch Video Solution

15. If l and m are variable real number such that $5l^2 + 6m^2 - 4lm + 3l = 0$, then the variable line $lx + my = 1$ always touches a fixed parabola, whose axes is parallel to the x-axis.

The directrix of the parabola is

A. $6x + 7 = 0$

B. $4x+11=0$

C. $3x+11=0$

D. none of these

Answer: C



Watch Video Solution

16. Consider the parabola whose focus is at $(0,0)$ and tangent at vertex is $x - y + 1 = 0$

The length of latus rectum is (a) $4\sqrt{2}$ (b) $2\sqrt{2}$ (c) $8\sqrt{2}$
(d) $3\sqrt{2}$

A. $4\sqrt{2}$

B. $2\sqrt{2}$

C. $8\sqrt{2}$

D. $3\sqrt{2}$

Answer: B



Watch Video Solution

17. Consider the parabola whose focus is at $(0,0)$ and tangent at vertex is $x-y+1=0$

The length of the chord of parabola on the x-axis is

A. $4\sqrt{2}$

B. $2\sqrt{2}$

C. $8\sqrt{2}$

D. $3\sqrt{2}$

Answer: A



Watch Video Solution

18. Consider the parabola whose focus is at $(0,0)$ and tangent at vertex is $x-y+1=0$

Tangents drawn to the parabola at the extremities of the chord $3x+2y=0$ intersect at angle

A. (a) $\pi/6$

B. (b) $\pi/3$

C. (c) $\pi/2$

D. (d) none of these

Answer: C



Watch Video Solution

19. Two tangents on a parabola are $x-y=0$ and $x+y=0$.

$S(2,3)$ is the focus of the parabola.

The length of latus rectum of the parabola is

A. $4x-6y+5=0$

B. $4x-6y+3=0$

C. $4x-6y+1=0$

D. $4x-6y+3/2=0$

Answer: A



Watch Video Solution

20. Two tangents on a parabola are $x-y=0$ and $x+y=0$.

$S(2,3)$ is the focus of the parabola.

The length of latus rectum of the parabola is

A. (a) $6/\sqrt{3}$

B. (b) $10/\sqrt{13}$

C. (c) $2/\sqrt{13}$

D. (d) none of these

Answer: B



Watch Video Solution

21. Two tangents on a parabola are $x-y=0$ and $x+y=0$.

$S(2,3)$ is the focus of the parabola.

The length of latus rectum of the parabola is

A. $2\sqrt{13}/3$

B. $2\sqrt{13}$

C. $2\sqrt{13}/5$

D. none of these

Answer: C



Watch Video Solution

22. $y^2 = 4x$ and $y^2 = -8(x - a)$ intersect at points A and C. Points O(0, 0), A, B (a, 0), and C are concyclic.

The length of the common chord of the parabolas is

A. (a) $2\sqrt{6}$

B. (b) $4\sqrt{3}$

C. (c) $6\sqrt{5}$

D. (d) $8\sqrt{2}$

Answer: D



Watch Video Solution

23. $y^2 = 4x$ and $y^2 = -8(x - a)$ intersect at points A and C. Points O(0, 0), A, B (a, 0), and C are concyclic.

The area of cyclic quadrilateral OABC is

A. (a) $24\sqrt{3}$

B. (b) $48\sqrt{2}$

C. (c) $12\sqrt{6}$

D. (d) $18\sqrt{5}$

Answer: B



Watch Video Solution

24. $y^2 = 4x$ and $y^2 = -8(x - a)$ intersect at points A and C. Points O(0, 0), A, B (a, 0), and C are concyclic.

The area of cyclic quadrilateral OABC is

A. $96\sqrt{2}$

B. $48\sqrt{3}$

C. $54\sqrt{5}$

D. $36\sqrt{6}$

Answer: A



Watch Video Solution

25. The focus of the parabola $y = 2x^2 + x$ is

A. 96 sq. units

B. 64 sq. units

C. 72 sq. units

D. 48 sq. units

Answer: B



Watch Video Solution

26. The focus of the parabola $y = 2x^2 + x$ is

A. $6\sqrt{5}$

B. $3\sqrt{6}$

C. $\sqrt{10}$

D. $5\sqrt{3}$

Answer: C



Watch Video Solution

27. The focus of the parabola $y = 2x^2 + x$ is

A. 2:1

B. 3:2

C. 4:3

D. 3:1

Answer: D



Watch Video Solution

28. Consider the inequation $9^x - a3^x - a + 3 \leq 0$,

where a is real parameter.

The given inequality has at least one negative solution for $a \in$ (a) $(-\infty, 2)$ (b) $(3, \infty)$ (c) $(-2, \infty)$ (d) $(2, 3)$

A. (a) $(-\infty, 2)$

B. (b) $(3, \infty)$

C. (c) $(-2, \infty)$

D. (d) $(2, 3)$

Answer: D



Watch Video Solution

29. Consider the inequation $9^x - a3^x - a + 3 \leq 0$, where a is real parameter.

The given inequality has at least one negative solution for $a \in$ (a) $(-\infty, 2)$ (b) $(3, \infty)$ (c) $(-2, \infty)$ (d) $(2, 3)$

A. $(-\infty, -2)$

B. $(3, \infty)$

C. $(2, \infty)$

D. $[-2, \infty)$

Answer: C



30. Consider the inequation $9^x - a3^x - a + 3 \leq 0$, where a is real parameter.

The given inequality has at least one negative solution for $a \in$ (a) $(-\infty, 2)$ (b) $(3, \infty)$ (c) $(-2, \infty)$ (d) $(2, 3)$

A. $(-\infty, 3)$

B. $[2, \infty)$

C. $(3, \infty)$

D. $[-2, \infty)$

Answer: B



Watch Video Solution

31. Consider one sides AB of a square ABCD in order on line $y = 2x - 17$, and other two vertices C, D on $y = x^2$

The minimum intercept of line CD on the y-axis is

A. 3

B. 4

C. 2

D. 6

Answer: A



Watch Video Solution

32. Consider one sides AB of a square ABCD in order on line $y = 2x - 17$, and other two vertices C, D on $y = x^2$

The maximum possible area of square ABCD is

A. 1180

B. 1250

C. 1280

D. none

Answer: C



Watch Video Solution

33. Let PQ be a focal chord of the parabola $y^2 = 4ax$

The tangents to the parabola at P and Q meet at a point lying on the line $y = 2x + a, a > 0$. Length of chord PQ is

A. $7a$

B. $5a$

C. $2a$

D. $3a$

Answer: B



Watch Video Solution

34. Let PQ be a focal chord of the parabola $y^2 = 4ax$.

The tangents to the parabola at P and Q meet at point lying on the line

$$y = 2x + a, a < 0.$$

If chord PQ subtends an angle θ at the vertex of $y^2 = 4ax$, then $\tan\theta =$

A. $2\sqrt{7}/3$

B. $-2\sqrt{7}/3$

C. $2\sqrt{5}/3$

D. $-2\sqrt{5}/3$

Answer: D



Watch Video Solution

35. Let a, r, s, t be non-zero real numbers. Let $P(at^2, 2at)$, $Q, R(ar^2, 2ar)$ and $S(as^2, 2as)$ be distinct points on the parabola $y^2 = 4ax$. Suppose that PQ is the focal chord and lines QR and PK are parallel, where K is the point $(2a, 0)$. The value of r is

A. $-\frac{1}{t}$

B. $\frac{t^2 + 1}{t}$

C. $\frac{1}{t}$

D. $\frac{t^2 - 1}{t}$

Answer: D



Watch Video Solution

36. Let a, r, s, t be non-zero real numbers. Let $P(at^2, 2at)$, $Q(ar^2, 2ar)$ and $S(as^2, 2as)$ be distinct points on the parabola $y^2 = 4ax$. Suppose that PQ is the focal chord and lines QR and PK are parallel, where K the point $(2a, 0)$.

If $st=1$, then the tangent at P and the normal at S to the parabola meet at a point whose ordinate is

A. $\frac{(t^2 + 1)^2}{2t^3}$

B. $\frac{a(t^2 + 1)^2}{2t^3}$

C. $\frac{a(t^2 + 1)^2}{t^3}$

D. $\frac{a(t^2 + 2)^2}{t^3}$

Answer: B



Watch Video Solution

37. Tangent to the parabola $y = x^2 + ax + 1$ at the point of intersection of the y-axis also touches the circle $x^2 + y^2 = r^2$. Also, no point of the parabola is below the x-axis.

The radius of circle when a attains its maximum value is

A. $1/\sqrt{10}$

B. $1/\sqrt{5}$

C. 1

D. $\sqrt{5}$

Answer: B



Watch Video Solution

38. Tangent to the parabola $y = x^2 + ax + 1$ at the point of intersection of the y-axis also touches the circle $x^2 + y^2 = r^2$. Also, no point of the parabola is below the x-axis.

The slope of the tangents when the radius of the circle is maximum is

A. -1

B. 1

C. 0

D. 2

Answer: C



Watch Video Solution

39. Tangent to the parabola $y = x^2 + ax + 1$ at the point of intersection of the y-axis also touches the circle $x^2 + y^2 = r^2$. Also, no point of the parabola is below the x-axis.

The minimum area bounded by the tangent and the coordinate axes is

A. 1

B. $1/3$

C. $1/2$

D. $1/4$

Answer: D



Watch Video Solution

40. The locus of the circumcenter of a variable triangle having sides the y -axis, $y=2$, and $lx+my=1$, where $(1,m)$ lies on the parabola $y^2 = 4x$, is a curve C.

The coordinates of the vertex of this curve C is

A. $(-2, 3/2)$

B. $(-2, -3/2)$

C. $(2, 3/2)$

D. $(2, -3/2)$

Answer: A



Watch Video Solution

41. The locus of the circumcenter of a variable triangle having sides the y -axis, $y=2$, and $lx+my=1$, where $(1,m)$ lies on the parabola $y^2 = 4x$, is a curve C .

The length of the smallest chord of this C is

A. $1/4$

B. $1/12$

C. $1/8$

D. $1/16$

Answer: C



Watch Video Solution

42. The locus of the circumcenter of a variable triangle having sides the y -axis, $y=2$, and $lx+my=1$, where $(1,m)$ lies on the parabola $y^2 = 4x$, is a curve C.

The curve C is symmetric about the line

A. $x = 3/2$

B. $y = -3/2$

C. $x = -3/2$

D. $y = 3/2$

Answer: D



Watch Video Solution

43. $y=x$ is tangent to the parabola $y = ax^2 + c$.

If $(1,1)$ is the point of contact, then a is (a) $\frac{1}{4}$ (b) $\frac{1}{3}$ (c)

$\frac{1}{2}$ (d) $\frac{1}{6}$

A. $1/4$

B. $1/3$

C. $1/2$

D. $1/6$

Answer: C



Watch Video Solution

44. $y=x$ is tangent to the parabola $y = ax^2 + c$.

If $c=2$, then the point of contact is (a) (3,3) (b) (2,2) (c)

(6,6) (d) (4,4)

A. (3,3)

B. (2,2)

C. (6,6)

D. (4,4)

Answer: D



Watch Video Solution

45. Consider the parabola whose focus is at $(0,0)$ and tangent at vertex is $x-y+1=0$

Tangents drawn to the parabola at the extremities of the chord $3x+2y=0$ intersect at what angle ?

A. $\pi/6$

B. $\pi/3$

C. $\pi/2$

D. none of these

Answer: C



Watch Video Solution

Matrix Match Type

1. Consider the parabola

$$(x - 1)^2 + (y - 2)^2 = \frac{(12x - 5y + 3)^2}{169} \quad \text{and match the}$$

following lists :





[View Text Solution](#)

2. Consider the parabola $y^2 = 12x$ and match the following lists :



[View Text Solution](#)

3. Match the following lists :



[View Text Solution](#)

4. Match the following lists and then choose the correct code.

List I: Function	List II: Range
a. $f(x) = \log_3 (5 - 4x - x^2)$	p. Function not defined
b. $f(x) = \log_3 (x^2 - 4x - 5)$	q. $[0, \infty)$
c. $f(x) = \log_3 (x^2 - 4x + 5)$	r. $(-\infty, 2]$
d. $f(x) = \log_3 (4x - 5 - x^2)$	s. R

A. $\begin{matrix} a & b & c & d \\ p & r & q & q \end{matrix}$

B. $\begin{matrix} a & b & c & d \\ q & p & r & s \end{matrix}$

C. $\begin{matrix} a & b & c & d \\ s & p & q & r \end{matrix}$

D. $\begin{matrix} a & b & c & d \\ r & s & q & p \end{matrix}$

Answer: B



Watch Video Solution

5. about to only mathematics



[Watch Video Solution](#)

Numerical Value Type

1. If the length of the latus rectum rectum of the parabola $169\{(x - 1)^2 + (y - 3)^2\} = (5x - 12y + 17)^2$ is L then the value of $13L/4$ is _____.



[Watch Video Solution](#)

2. A circle is drawn through the point of intersection of the parabola $y = x^2 - 5x + 4$ and the x-axis such that origin lies outside it. The length of a tangent to the circle from the origin is _____ .



Watch Video Solution

3. The focal chord of $y^2 = 16x$ is tangent to $(x - 6)^2 + y^2 = 2$.

Then the possible value of the square of slope of this chord is _____ .



Watch Video Solution

4. Two tangent are drawn from the point $(-2, -1)$ to parabola $y^2 = 4x$ if α is the angle between these tangents, then find the value of $\tan\alpha$



Watch Video Solution

5. The equation of the line touching both the parabolas $y^2 = 4x$ and $x^2 = -32y$ is $ax + by + c = 0$. Then the value of $a + b + c$ is _____ .



Watch Video Solution

6. If the point $P(4, -2)$ is the one end of the focal chord PQ of the parabola $y^2 = x$, then the slope of the tangent at Q , is



Watch Video Solution

7. If the line $x+y=6$ is a normal to the parabola $y^2 = 8x$ at point (a,b) , then the value of $a+b$ is _____.



Watch Video Solution

8. The locus of the midpoints of the portion of the normal to the parabola $y^2 = 16x$ intercepted between the curve and the axis is another parabola whose latus rectum is _____ .



Watch Video Solution

9. Consider the locus of center of the circle which touches the circle $x^2 + y^2 = 4$ externally and the line $x=4$. The distance of the vertex of the locus from the origin is _____ .



Watch Video Solution

10. If on a given base BC[B(0,0) and C(2,0)], a triangle is described such that the sum of the base angles is 4, then the equation of the locus of the opposite vertex A is parabola whose directrix is $y=k$. The value of k is _____.



Watch Video Solution

11. PQ is any focal chord of the parabola $y^2 = 8x$. Then the length of PQ can never be less than _____.



Watch Video Solution

12. The length of focal chord to the parabola $y^2 = 12x$ drawn from the point (3,6) on is _____ .



Watch Video Solution

13. From the point (-1,2), tangent lines are to the parabola $y^2 = 4x$. If the area of the triangle formed by the chord of contact and the tangents is A, then the value of $A/\sqrt{2}$ is _____ .



Watch Video Solution

14. Line $y=2x-b$ cuts the parabola $y = x^2 - 4x$ at points A and B. Then the value of b for which $\angle AOB$ is a right is (where O is origin) _____ .



Watch Video Solution

15. A line through the origin intersects the parabola $5y = 2x^2 - 9x + 10$ at two points whose x-coordinates add up to 17.

Then the slope of the line is _____ .



Watch Video Solution

16. IF the circle $(x - 6)^2 + y^2 = r^2$ and the parabola $y^2 = 4x$ have maximum number of common chords , then the least integral value of r is



Watch Video Solution

17. The slope of line which belongs to family $(1 + l)x + (l - 1)y + 2(1 - l) = 0$ and makes shortest intercept on $x^2 = 4y - 4$



Watch Video Solution

18. If $3x+4y+k=0$ represents the equation of tangent at the vertex of the parabola $16x^2 - 24xy + 9y^2 + 14x + 2y + 7 = 0$, then the value of k is _____.



Watch Video Solution

19. Normals at (x_1, y_1) , (x_2, y_2) and (x_3, y_3) to the parabola $y^2 = 4x$ are concurrent at point P . If $y_1y_2 + y_2y_3 + y_3y_1 = x_1x_2x_3$, then locus of point P is part of parabola, length of whose latus rectum is _____.



Watch Video Solution

20. Foot of perpendicular from point P on the parabola $y^2 = 4ax$ to the axis is N. A straight line is drawn parallel to the axis which bisects PN and cuts the curve at Q. If NQ meets the tangent at the vertex A at a point T, then $\frac{PN}{AT} = \text{-----}$.



Watch Video Solution

21. about to only mathematics



Watch Video Solution

22. Normals are drawn from a point P with slopes m_1, m_2 and m_3 are drawn from the point p not from the parabola $y^2 = 4x$. For $m_1 m_2 = \alpha$, if the locus of the point P is a part of the parabola itself, then the value of α is (a) 1 (b)-2 (c) 2 (d) -1



Watch Video Solution

23. about to only mathematics



Watch Video Solution

24. about to only mathematics



Watch Video Solution

25. about to only mathematics



Watch Video Solution

26. If the normals of the parabola $y^2 = 4x$ drawn at the end points of its latus rectum are tangents to the circle $(x - 3)^2 + (y + 2)^2 = r^2$, then the value of r^2 is



Watch Video Solution

27. If the length of the latus rectum of the parabola $169\{(x - 1)^2 + (y - 3)^2\} = (5x - 12y + 17)^2$ is L then the value of $13\frac{L}{4}$ is _____.



Watch Video Solution

28. If the line $x+y=6$ is a normal to the parabola $y^2 = 8x$ at point (a,b) , then the value of $a+b$ is _____.



Watch Video Solution

29. Consider the locus of center of the circle which touches the circle $x^2 + y^2 = 4$ externally and the line $x=4$. The distance of the vertex of the locus from the origin is _____ .



Watch Video Solution

30. Line $y=2x-b$ cuts the parabola $y = x^2 - 4x$ at points A and B. Then the value of b for which $\angle AOB$ is a right is (where O is origin) _____ .



Watch Video Solution

31. A line through the origin intersects the parabola $5y = 2x^2 - 9x + 10$ at two points whose x-coordinates add up to 17.

Then the slope of the line is _____ .



Watch Video Solution

32. If $3x+4y+k=0$ represents the equation of tangent at the vertex of the parabola $16x^2 - 24xy + 9y^2 + 14x + 2y + 7 = 0$, then the value of k is _____ .



Watch Video Solution

Archives Single Correct Answer Type

1. If two tangents drawn from a point P to the parabola $y^2 = 4x$ are at right angles, then the locus of P is (1) $2x + 1 = 0$ (2) $x = -1$ (3) $2x - 1 = 0$ (4) $x = 1$

A. $2x - 1 = 0$

B. $x = 1$

C. $2x + 1 = 0$

D. $x = -1$

Answer: D



Watch Video Solution

2. Statement 1: An equation of a common tangent to the parabola $y^2 = 16\sqrt{3}x$ and the ellipse $2x^2 + y^2 = 4$ is $y = 2x + 2\sqrt{3}$. Statement 2: If the line $y = mx + \frac{4\sqrt{3}}{m}$, ($m \neq 0$) is a common tangent to the parabola $y^2 = 16\sqrt{3}x$ and the ellipse $2x^2 + y^2 = 4$, then m satisfies $m^4 + 2m^2 = 24$.

(1) Statement 1 is false, statement 2 is true (2) Statement 1 is true, statement 2 is true; statement 2 is a correct explanation for statement 1 (3) Statement 1 is true, statement 2 is true; statement 2 is not a correct explanation for statement 1 (4) Statement 1 is true, statement 2 is false

A. Statement 1 is true , statement 2 is true ,
statement 2 is a correct explanation for
statement 1.

B. Statement 1 is true , statement 2 is true ,
statement 2 is not correct explanation for
statement 1.

C. Statement 1 is true , statement 2 is false.

D. Statement 1 is false , statement 2 is true.

Answer: B



Watch Video Solution

3. The slope of the line touching both the parabolas $y^2 = 4x$ and $x^2 = -32y$ is (a) $1/2$ (b) $3/2$ (c) $1/8$ (d) $2/3$

A. $1/2$

B. $3/2$

C. $1/8$

D. $2/3$

Answer: A



Watch Video Solution

4. Let O be the vertex and Q be any point on the parabola $x^2 = 8y$. IF the point P divides the line segment OQ internally in the ratio 1:3 , then the locus of P is

A. $x^2 = y$

B. $y^2 = x$

C. $y^2 = 2x$

D. $x^2 = 2y$

Answer: D



Watch Video Solution

5. Let P be the point on the parabola, $y^2 = 8x$ which is at a minimum distance from the centre C of the circle, $x^2 + (y + 6)^2 = 1$. Then the equation of the circle, passing through C and having its centre at P is

: (1) $x^2 + y^2 - 4x + 8y + 12 = 0$ (2)

$x^2 + y^2 - x + 4y - 12 = 0$ (3) $x^2 + y^2 - \frac{x}{4} + 2y - 24 = 0$

(4) $x^2 + y^2 - 4x + 9y + 18 = 0$

A. $x^2 + y^2 - x + 4y - 12 = 0$

B. $x^2 + y^2 - \frac{x}{4} + 2y - 24 = 0$

C. $x^3 + y^2 - 4x + 9y - 18 = 0$

D. $x^2 + y^2 - 4x + 8y - 12 = 0$

Answer: D



Watch Video Solution

6. The radius of a circle, having minimum area, which touches the curve $y = 4 - x^2$ and the lines $y = |x|$ is :

A. (a) $4(\sqrt{2} + 1)$

B. (b) $2(\sqrt{2} + 1)$

C. (c) $2(\sqrt{2} - 1)$

D. (d) $4(\sqrt{2} - 1)$

Answer: D

[Watch Video Solution](#)

7. If the tangent at $(1,7)$ to curve $x^2 = y - 6$ touches the circle $x^2 + y^2 + 16x + 12y + c = 0$ then the value of c is

- A. 95
- B. 195
- C. 185
- D. 85

Answer: A

[Watch Video Solution](#)

8. Tangent and normal are drawn at the point $P \equiv (16, 16)$ of the parabola $y^2 = 16x$ which cut the axis of the parabola at the points A and B , respectively. If the center of the circle through P, A and B is C , then the angle between PC and the axis of x is

A. $4/3$

B. $1/2$

C. 2

D. 3

Answer: C



Watch Video Solution

Jee Advanced Single Correct Answer Type

1. Let (x,y) be any point on the parabola $y^2 = 4x$. Let P be the point that divides the line segment from $(0,0)$ and (x,y) in the ratio 1:3. Then the locus of P is :

A. $x^2 = y$

B. $y^2 = 2x$

C. $y^2 = x$

D. $x^2 = 2y$

Answer: C



Watch Video Solution

2. about to only mathematics

A. 3

B. 6

C. 9

D. 15

Answer: D



Watch Video Solution

Multiple Correct Answer Type

1. about to only mathematics

A. vertex is $(2a/3, 0)$

B. directrix is $x=0$

C. latus rectum is $2a/3$

D. focus is $(a,0)$

Answer: A::D



Watch Video Solution

2. Let A and B be two distinct points on the parabola $y^2 = 4x$. If the axis of the parabola touches a circle of radius r having AB as its diameter, then find the slope of the line joining A and B .

A. $-1/r$

B. $1/r$

C. $2/r$

D. $-2/r$

Answer: C::D



Watch Video Solution

3. Let L be a normal to the parabola $y^2 = 4x$. If L passes through the point $(9, 6)$, then L is given by (a) $y - x + 3 = 0$ (b) $y + 3x - 33 = 0$ (c) $y + x - 15 = 0$ (d) $y - 2x + 12 = 0$

A. $y - x + 3 = 0$

B. $y + 3x - 33 = 0$

C. $y + x - 15 = 0$

D. $y - 2x + 12 = 0$

Answer: A::C::D



Watch Video Solution

4. Let P and Q be distinct points on the parabola $y^2 = 2x$ such that a circle with PQ as diameter passes through the vertex O of the parabola. If P lies in the first quadrant and the area of the triangle $\triangle OPQ$ is $3\sqrt{2}$, then which of the following is (are) the coordinates of P ? (a) $(4, 2\sqrt{2})$ (b) $(9, 3\sqrt{2})$ (c) $(1, \sqrt{2})$ (d) $(4, 1\sqrt{2})$

A. $(4, 2\sqrt{2})$

B. $(9, 3\sqrt{2})$

C. $\left(\frac{1}{4}, \frac{1}{\sqrt{2}}\right)$

D. $(1, \sqrt{2})$

Answer: A::D



Watch Video Solution

5. Let P be the point on parabola $y^2 = 4x$ which is at the shortest distance from the center S of the circle $x^2 + y^2 - 4x - 16y + 64 = 0$ let Q be the point on the circle dividing the line segment SP internally. Then

A. (a) $SP = 2\sqrt{5}$

B. (b) $SQ:QP = (\sqrt{5} + 1):2$

C. (c) the x-intercept of the normal to the parabola at P is 6

D. (d) the slope of the tangent to the circle at Q

is $\frac{1}{2}$

Answer: A::C::D



Watch Video Solution

6. The circle $C_1 : x^2 + y^2 = 3$, with center at O, intersects the parabola $x^2 = 2y$ at the point P in the first quadrant. Let the tangent to the circle C_1 at P touches other two circles C_2 and C_3 at R_2 and R_3 , respectively. Suppose C_2 and C_3 have equal radii $2\sqrt{3}$ and centers Q_2 and Q_3 , respectively. If Q_2 and Q_3 lie on the y-axis, then

A. $Q_2Q_3 = 12$

B. $R_2R_3 = 4\sqrt{6}$

C. area of the triangle OR_2R_3 is $6\sqrt{2}$

D. area of the triangle PQ_2Q_3 is $4\sqrt{2}$

Answer: A::B::C



Watch Video Solution

7. If a chord, which is not a tangent, of the parabola $y^2 = 16x$ has the equation $2x+y=p$, and midpoint (h,k) , then which of the following is (are) possible value(s) of p, h and k ?

A. $p=5, h=4, k=-3$

B. $p=-1, h=1, k=-3$

C. $p=-2, h=2, k=-4$

D. $p=2, h=3, k=-4$

Answer: D



Watch Video Solution

Single Correct Answer Type

1. The equation $x^2 - 2xy + y^2 + 3x + 2 = 0$ represents

(a) a parabola (b) an ellipse (c) a hyperbola (d) a

circle

- A. A parabola
- B. An ellipse
- C. A hyperbola
- D. A circle

Answer: A



Watch Video Solution

2. The length of the latus rectum of

$3x^2 - 4y + 6x - 3 = 0$ is (a) 3 (b) 2 (c) $\frac{4}{3}$ (d) $\frac{3}{4}$

A. 3

B. 2

C. $\frac{4}{3}$

D. $\frac{3}{4}$

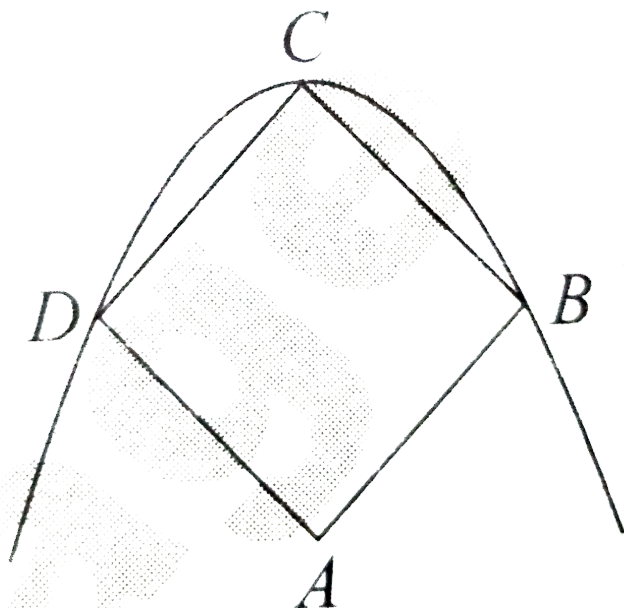
Answer: C



Watch Video Solution

3. In the adjacent figure a parabola is drawn to pass through the vertices B, C and D of the square ABCD. If

$A(2, 1)$, $C(2, 3)$, then focus of this parabola is



A. $\left(1, \frac{11}{4}\right)$

B. $\left(2, \frac{11}{4}\right)$

C. $\left(3, \frac{13}{4}\right)$

D. $\left(2, \frac{13}{4}\right)$

Answer: B



Watch Video Solution

4. Length of the latus rectum of the parabola

$\sqrt{x} + \sqrt{y} = \sqrt{a}$ is (a) $a\sqrt{2}$ (b) $\frac{a}{\sqrt{2}}$ (c) a (d) $2a$

A. $a\sqrt{2}$

B. $\frac{a}{\sqrt{2}}$

C. a

D. $2a$

Answer: A



Watch Video Solution

5. Consider the parabola $x^2 + 4y = 0$. Let $P(a, b)$ be any fixed point inside the parabola and let S be the focus of the parabola. Then the minimum value at $SQ + PQ$ as point Q moves on the parabola is (a) $|1 - a|$ (b) $|ab| + 1$ (c) $\sqrt{a^2 + b^2}$ (d) $1 - b$

A. $|1 - a|$

B. $|ab| + 1$

C. $\sqrt{a^2 + b^2}$

D. $1 - b$

Answer: D



Watch Video Solution

6. If the points $(2,3)$ and $(3,2)$ on a parabola are equidistant from the focus, then the slope of its tangent at vertex is (a) 1 (b) -1 (c) 0 (d) ∞

A. 1

B. -1

C. 0

D. ∞

Answer: B



Watch Video Solution

7. Let $A(x_1, y_1)$ and $B(x_2, y_2)$ be two points on the parabola $y^2 = 4ax$. If the circle with chord AB as a diameter touches the parabola, then $|y_1 - y_2|$ is equal to

A. $4a$

B. $8a$

C. $6\sqrt{2}a$

D. not a constant

Answer: B



Watch Video Solution

8. $y = \sqrt{3}x + \lambda$ is drawn through focus S of the parabola $y^2 = 8x + 16$. If two intersection points of the given line and the parabola are A and B such that perpendicular bisector of AB intersects the x-axis at P then length of PS is

A. $8/7$

B. $7/17$

C. $8\sqrt{3}$

D. $16/3$

Answer: D



Watch Video Solution

9. If the point $(2a, a)$ lies inside the parabola $x^2 - 2x - 4y + 3 = 0$, then a lies in the interval (a)

$\left[\frac{1}{2}, \frac{3}{2}\right]$ (b) $\left(\frac{1}{2}, \frac{3}{2}\right)$ (c) $(1, 3)$ (d) $\left(-\frac{3}{2}, -\frac{1}{2}\right)$

A. $\left[\frac{1}{2}, \frac{3}{2}\right]$

B. $\left(\frac{1}{2}, \frac{3}{2}\right)$

C. $(1, 3)$

D. $\left(\frac{-3}{2}, \frac{-1}{2}\right)$

Answer: B



Watch Video Solution

10. If AFB is a focal chord of the parabola $y^2 = 4ax$ such that $AF = 4$ and $FB = 5$ then the latus-rectum of the parabola is equal to (a) 80 (b) $\frac{9}{80}$ (c) 9 (d) $\frac{80}{9}$

A. 80

B. $\frac{9}{80}$

C. 9

D. $\frac{80}{9}$

Answer: D



Watch Video Solution

11. Length of the focal chord of the parabola $(y + 3)^2 = -8(x - 1)$ which lies at a distance 2 units from the vertex of the parabola is (a) 8 (b) $6\sqrt{2}$ (c) 9 (d) $5\sqrt{3}$

A. 8

B. $6\sqrt{2}$

C. 9

D. $5\sqrt{3}$

Answer: A



Watch Video Solution

12. Let $A(0, 2)$, B and C be points on parabola $y^2 + x + 4$ such that $\angle CBA = \frac{\pi}{2}$. Then the range of ordinate of C is (a) $(-\infty, 0) \cup (4, \infty)$ (b) $(-\infty, 0] \cup [4, \infty)$ (c) $[0, 4]$ (d) $(-\infty, 0) \cup [4, \infty)$

A. $(-\infty, 0) \cup (4, \infty)$

B. $(-\infty, 0] \cup [4, \infty)$

C. $[0, 4]$

D. $(-\infty, 0) \cup [4, \infty)$

Answer: B



Watch Video Solution

13. $lx + my = 1$ is the equation of the chord PQ of $y^2 = 4x$ whose focus is S. If PS and QS meet the parabola again at R and T respectively, then slope of RT is (a) $-1/m$ (b) $1/m$ (c) $2/m$ (d) none of the above

A. $-\frac{1}{m}$

B. $\frac{l}{m}$

C. $\frac{2}{m}$

D. none of these

Answer: A



Watch Video Solution

14. A line from $(-1, 0)$ intersects the parabola $x^2 = 4y$ at A and B. Then the locus of centroid of ΔOAB is (where O is origin) (a) $3x^2 - 2x = 4y$ (b) $3y^2 - 2y = 4x$ (c) $3x^2 + 2x = 4y$ (d) none of these

A. $3x^2 - 2x = 4y$

B. $3y^2 - 2y = 4x$

C. $3x^2 + 2x = 4y$

D. none of these

Answer: C



Watch Video Solution

15. All the three vertices of an equilateral triangle lie on the parabola $y = x^2$, and one of its sides has a slope of 2. Then the sum of the x-coordinates of the three vertices is

A. $\frac{5}{9}$

B. $\frac{9}{13}$

C. $\frac{6}{11}$

D. None of these

Answer: C



Watch Video Solution

16. Find the equations of the chords of the parabola $y^2 = 4ax$ which pass through the point $(-6a, 0)$ and which subtends an angle of 45° at the vertex.

A. $\pm \frac{2}{7}$

B. $\pm \frac{3}{8}$

C. $\pm \frac{7}{2}$

D. $\pm \frac{5}{6}$

Answer: A



Watch Video Solution

17. Two equal circles of largest radii have following property:

(i) They intersect each other orthogonally,

(ii) They touch both the curves $4(y + 2) = x^2$ and $4(2 - y) = x^2$ in the region $x \in [-2\sqrt{2}, 2\sqrt{2}]$. Then radius of this circle is

A. $\sqrt{2}$

B. $\sqrt{3}$

C. $\frac{1}{\sqrt{3}}$

D. $\frac{3}{2}$

Answer: A



Watch Video Solution

18. Let P and Q are points on the parabola $y^2 = 4ax$ with vertex O, such that OP is perpendicular to OQ and have lengths r_1 and r_2 respectively, then the

value of $\frac{r_1^{4/3} r_2^{4/3}}{r_1^{2/3} + r_2^{2/3}}$ is :

A. $16a^2$

B. a^2

C. $4a$

D. None of these

Answer: A



Watch Video Solution

19. A line $ax + by + c = 0$ through the point $A(-2, 0)$

intersects the curve $y^2 = 4a$ in P and Q such that

$\frac{1}{AP} + \frac{1}{AQ} = \frac{1}{4}$ (P, Q are in 1st quadrant). The value of $\sqrt{a^2 + b^2 + c^2}$ is

A. 2

B. 4

C. 6

D. 8

Answer: B



Watch Video Solution

20. Suppose a parabola $y = x^2 - ax - 1$ intersects the coordinate axes at three points A, B and C, respectively. The circumcircle of $\triangle ABC$ intersects the y-axis again at the point $D(0, t)$. Then the value of t is

A. $1/2$

B. 1

C. $3/2$

D. 2

Answer: B



Watch Video Solution

21. The line $x - b + \lambda y = 0$ cuts the parabola $y^2 = 4ax (a > 0)$ at $P(t_1)$ and $Q(t_2)$. If $b \in [2a, 4a]$ then range of $t_1 t_2$ where $\lambda \in R$ is

A. $[-4, -2]$

B. $[2, 4]$

C. $[4, 16]$

D. $[-16, -4]$

Answer: A



Watch Video Solution

22. If the parabola $y = (a - b)x^2 + (b - c)x + (c - a)$ touches x -axis then the line $ax + by + c = 0$ (a) always passes through a fixed point (b) represents

the family of parallel lines (c) is always perpendicular to x-axis (d) always has negative slope

- A. always passes through a fixed point
- B. represents the family of parallel lines
- C. is always perpendicular to x-axis
- D. always has negative slope

Answer: A



Watch Video Solution

23. A normal to parabola, whose inclination is 30° ,

cuts it again at an angle of (a) $\tan^{-1}\left(\frac{\sqrt{3}}{2}\right)$ (b)

$\tan^{-1}\left(\frac{2}{\sqrt{3}}\right)$ (c) $\tan^{-1}(2\sqrt{3})$ (d) $\tan^{-1}\left(\frac{1}{2\sqrt{3}}\right)$

A. $\tan^{-1}\left(\frac{\sqrt{3}}{2}\right)$

B. $\tan^{-1}\left(\frac{2}{\sqrt{3}}\right)$

C. $\tan^{-1}(2\sqrt{3})$

D. $\tan^{-1}\left(\frac{1}{2\sqrt{3}}\right)$

Answer: D



Watch Video Solution

24. If $(-2, 5)$ and $(3, 7)$ are the points of intersection of the tangent and normal at a point on a parabola with the axis of the parabola, then the focal distance of that point is

A. $\frac{\sqrt{29}}{2}$

B. $\frac{5}{2}$

C. $\sqrt{29}$

D. $\frac{2}{5}$

Answer: A



Watch Video Solution

25. The angle of intersection between the curves

$x^2 = 4(y + 1)$ and $x^2 = -4(y + 1)$ is (a) $\frac{\pi}{6}$ (b) $\frac{\pi}{4}$ (c) 0

(d) $\frac{\pi}{2}$

A. $\frac{\pi}{6}$

B. $\frac{\pi}{4}$

C. 0

D. $\frac{\pi}{2}$

Answer: C



Watch Video Solution

26. The parabolas $y^2 = 4ax$ and $x^2 = 4by$ intersect orthogonally at point $P(x_1, y_1)$ where $x_1, y_1 \neq 0$ provided (A) $b = a^2$ (B) $b = a^3$ (C) $b^3 = a^2$ (D) none of these

A. $b = a^2$

B. $b = a^3$

C. $b^3 = a^2$

D. None of these

Answer: D



Watch Video Solution

27. Sum of slopes of common tangent to

$y = \frac{x^2}{4} - 3x + 10$ and $y = 2 - \frac{x^2}{4}$ is (a) -6 (b) -3 (c) $\frac{1}{2}$ (d)

none of these

A. -6

B. -3

C. $\frac{1}{2}$

D. none of these

Answer: B



Watch Video Solution

28. The slope of normal to the parabola $y = \frac{x^2}{4} - 2$ drawn through the point (10, -1) is (a) -2 (b) $-\sqrt{3}$ (c) $-\frac{1}{2}$ (d) $-\frac{5}{3}$

A. -2

B. $-\sqrt{3}$

C. $-1/2$

D. $-5/3$

Answer: C



Watch Video Solution

29. The tangent and normal at the point $P(4, 4)$ to the parabola, $y^2 = 4x$ intersect the x-axis at the points Q and R, respectively. Then the circumcentre of the ΔPQR is (a) (2, 0) (b) (2, 1) (c) (1, 0) (d) (1, 2)

A. (2, 0)

B. (2, 1)

C. (1, 0)

D. (1, 2)

Answer: C



Watch Video Solution

30. The point on the parabola $y^2 = 8x$ at which the normal is inclined at 60° to the x-axis has the coordinates as (a) $(6, -4\sqrt{3})$ (b) $(6, 4\sqrt{3})$ (c) $(-6, -4\sqrt{3})$ (d) $(-6, 4\sqrt{3})$

A. $(6, -4\sqrt{3})$

B. $(6, 4\sqrt{3})$

C. $(-6, -4\sqrt{3})$

D. $(-6, 4\sqrt{3})$

Answer: A



Watch Video Solution

31. If two distinct chords of a parabola $y^2 = 4ax$, passing through $(a, 2a)$ are bisected by the line $x+y=1$, then length of latus rectum can be a) 2 b) 7 c) 4 d) 5

A. 9

B. 3

C. 4

D. 5

Answer: B



Watch Video Solution

32. From an external point P , a pair of tangents is drawn to the parabola $y^2 = 4x$. If θ_1 and θ_2 are the inclinations of these tangents with the x-axis such that $\theta_1 + \theta_2 = \frac{\pi}{4}$, then find the locus of P .

A. $x - y + 1 = 0$

B. $x + y - 1 = 0$

C. $x - y - 1 = 0$

D. $x + y + 1 = 0$

Answer: C



Watch Video Solution

33. A variable parabola $y^2 = 4ax$, a (where $a \neq -\frac{1}{4}$)

being the parameter, meets the curve

$y^2 + x - y - 2 = 0$ at two points. The locus of the point

of intersection of tangents at these points is

A. $x - 2y - 4 = 0$

B. $x - 4y + 2 = 0$

C. $x - 4y - 1 = 0$

D. $2x - y + 1 = 0$

Answer: B



Watch Video Solution

34. If X is the foot of the directrix on the a parabola. PP' is a double ordinate of the curve and PX meets the curve again in Q . Then prove that $P'Q$ passes through the focus of the parabola.

A. line

B. circle

C. parabola

D. none of these

Answer: A



Watch Video Solution

35. Let PQ be the latus rectum of the parabola $y^2 = 4x$ with vertex A. Minimum length of the projection of PQ on a tangent drawn in portion of Parabola PAQ is

A. $2\sqrt{2}$

B. $2a\sqrt{2}$

C. 2

D. $3a\sqrt{2}$

Answer: B



Watch Video Solution

36. Through the vertex O of the parabola $y^2 = 4ax$, a perpendicular is drawn to any tangent meeting it at P and the parabola at Q. Then OP, $2a$ and OQ are in

A. A.P.

B. G.P.

C. H.P.

D. none of these

Answer: B



Watch Video Solution

37. Tangents PQ and PR are drawn to the parabola $y^2 = 20(x + 5)$ and $y^2 = 60(x + 15)$, respectively such that $\angle RPQ = \frac{\pi}{2}$. Then the locus of point P is

A. $x + 10 = 0$

B. $x + 30 = 0$

C. $x + 40 = 0$

D. $x + 20 = 0$

Answer: D



Watch Video Solution

38. The locus of centroid of triangle formed by a tangent to the parabola $y^2 = 36x$ with coordinate axes is (a) $y^2 = -9x$ (b) $y^2 + 3x = 0$ (c) $y^2 = 3x$ (d) $y^2 = 9x$

A. $y^2 = -9x$

B. $y^2 + 3x = 0$

C. $y^2 = 3x$

D. $y^2 = 9x$

Answer: B



Watch Video Solution

39. PC is the normal at P to the parabola $y^2 = 4ax$, C being on the axis. CP is produced outwards to Q so that $PQ = CP$; show that the locus of Q is a parabola.

A. $(a, 0)$

B. $(-a, 0)$

C. $(-2a, 0)$

D. $(2a, 0)$

Answer: D



Watch Video Solution

40. If three parabols touch all the lines $x = 0, y = 0$ and $x + y = 2$, then maximum area of the triangle formed by joining their foci is

A. $\sqrt{3}$

B. $\sqrt{6}$

C. $\frac{3\sqrt{3}}{4}$

D. $\frac{3\sqrt{3}}{2}$

Answer: D



Watch Video Solution

41. If $2x + 3y = \alpha$, $x - y = \beta$ and $kx + 15y = r$ are 3 concurrent normal of parabola $y^2 = \lambda x$ then value of k is (a) 3 (b) 4 (c) 5 (d) 7

A. 3

B. 4

C. 5

D. 7

Answer: C



Watch Video Solution

42. Let $(2, 3)$ be the focus of a parabola and $x + y = 0$ and $x - y = 0$ be its two tangents. Then equation of its directrix will be (a) $2x - 3y = 0$ (b) $3x + 4y = 0$ (c) $x + y = 5$ (d) $12x - 5y + 1 = 0$

A. $2x - 3y = 0$

B. $3x + 4y = 0$

C. $x + y = 5$

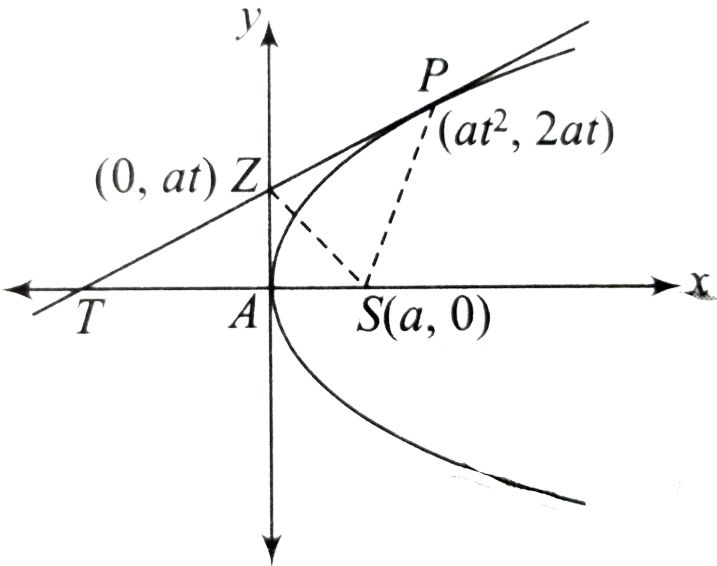
D. $12x - 5y + 1 = 0$

Answer: A



Watch Video Solution

43. In the following figure, $AS = 4$ and $SP = 9$. The value of SZ is



- A. 6
- B. 5.5
- C. 6.5
- D. none of these

Answer: A



Watch Video Solution

44. TP and TQ are any two tangents to a parabola and the tangent at a third point R cuts them in P' and Q' , prove that $\frac{TP'}{TP} + \frac{TQ'}{TQ} = 1$.

A. 1

B. 2

C. 3

D. none of these

Answer: A



Watch Video Solution

45. The distance of two points P and Q on the parabola $y^2 = 4ax$ from the focus S are 3 and 12 respectively. The distance of the point of intersection of the tangents at P and Q from the focus S is

A. 8

B. 6

C. 9

D. 12

Answer: B



Watch Video Solution

46. A parabola having directrix $x + y + 2 = 0$ touches a line $2x + y - 5 = 0$ at $(2,1)$. Then the semi-latus rectum of the parabola, is

A. 8

B. $\frac{9}{\sqrt{2}}$

C. $\frac{10}{\sqrt{2}}$

D. $\frac{11}{\sqrt{2}}$

Answer: B



Watch Video Solution

Multiple Correct Answers Type

1. A family of curve S is given by $S \equiv x^2 + 2xy + y^2 - 4x(1 - \lambda) - 4y(1 + \lambda) + 4$, then $S = 0$ represents (a) pair of straight line $\forall \lambda \in R$ (b) straight line for exactly one value of λ (c) parabola $\forall \lambda \in R - \{0\}$ (d) ellipse for three values of λ

A. pair of straight line $\forall \lambda \in R$

B. straight line for exactly one value of λ

C. parabola $\forall \lambda \in R - \{0\}$

D. ellipse for three values of λ

Answer: B::C



Watch Video Solution

2. The curves $x^2 + y^2 + 6x - 24y + 72 = 0$ and $x^2 - y^2 + 6x + 16y - 46 = 0$ intersect in four points P, Q, R and S lying on a parabola. Let A be the focus of the parabola, then

A. $AP + AQ + AR + AS = 20$

B. $AP + AQ + AR + AS = 40$

C. vertex of the parabola is at $(-3, 1)$

D. coordinates of A are $(-3, 1)$

Answer: B::C



Watch Video Solution

3. If the parabols $y^2 = 4kx (k > 0)$ and $y^2 = 4(x - 1)$ do not have a common normal other than the axis of parabola, then $k \in$

A. $(0, 1)$

B. $(2, \infty)$

C. $(3, \infty)$

D. $(0, \infty)$

Answer: A::B::C



Watch Video Solution

4. Find the length of normal chord which subtends an angle of 90° at the vertex of the parabola $y^2 = 4x$.

A. $PQ = 2a\sqrt{6}$

B. $PR = 6a\sqrt{3}$

C. area of $\Delta PQR = 18\sqrt{2}a^2$

D. $PQ = 3a\sqrt{2}$

Answer: A::B::C



Watch Video Solution

5. Let $y^2 - 5y + 3x + k = 0$ be a parabola, then

A. its latus rectum is least when $k = 1$

B. its latus rectum is independent of k

C. the line $y = 2x + 1$ will touch the parabola if

$$k = \frac{73}{16}$$

D. $y = \frac{5}{2}$ is the only normal to the parabola

whose slope is zero

Answer: B::C::D



Watch Video Solution

6. Let A, B and C be three distinct points on $y^2 = 8x$ such that normals at these points are concurrent at

P. The slope of AB is 2 and abscissa of centroid of

ΔABC is $\frac{4}{3}$. Which of the following is (are) correct?

(a) Area of $\triangle ABC$ is 8 sq. units (b) Coordinates of $P \equiv (6, 0)$ (c) Angle between normals are $45^\circ, 45^\circ, 90^\circ$ (d) Angle between normals are $30^\circ, 30^\circ, 60^\circ$

A. Area of $\triangle ABC$ is 8 sq. units

B. Coordinates of $P \equiv (6, 0)$

C. Angle between normals are $45^\circ, 45^\circ, 90^\circ$

D. Angle between normals are $30^\circ, 30^\circ, 60^\circ$

Answer: A::B::C



Watch Video Solution

7. If PQ and Rs are normal chords of the parabola $y^2 = 8x$ and the points P,Q,R,S are concyclic, then

- A. tangents at P and R meet on X-axis
- B. tangents at P and R meet on Y-axis
- C. PR is parallel to Y-axis
- D. PR is parallel to X-axis

Answer: A::C



Watch Video Solution

8. find the angle of intersection of the curve $xy=6$ and

$$x^2y = 12$$



Watch Video Solution

9. Find the equation of the tangent and normal to

the parabola $y^2 = 4ax$ at the point $(at^2, 2at)$.



Watch Video Solution

10. If a parabola touches the lines $y = x$ and $y = -x$

at $P(3, 3)$ and $Q(2, -2)$ respectively, then (a) focus is

($30/13$, $-6/13$) (b) equation of directrix is $x + 5y = 0$
(c) equation of line through origin and focus is $x + 5y = 0$
(d) equation of line through origin and parallel to axis is $x - 5y = 0$

A. focus is $\left(\frac{30}{13}, \frac{-6}{13}\right)$

B. equation of directrix is $x + 5y = 0$

C. equation of line through origin and focus is

$$x + 5y = 0$$

D. equation of line through origin and parallel to

axis is $x - 5y = 0$

Answer: A::B::C::D



Comprehension Type

1. A parabola is drawn through two given points $A(1, 0)$ and $B(-1, 0)$ such that its directrix always touches the circle $x^2 + y^2 = 4$. Then, The locus of

focus of the parabola is (a) $\frac{x^2}{4} + \frac{y^2}{3} = 1$ (b) $\frac{x^2}{4} + \frac{y^2}{5} = 1$ (c) $\frac{x^2}{3} + \frac{y^2}{4} = 1$ (d) $\frac{x^2}{5} + \frac{y^2}{4} = 1$

A. $\frac{x^2}{4} + \frac{y^2}{3} = 1$

B. $\frac{x^2}{4} + \frac{y^2}{5} = 1$

C. $\frac{x^2}{3} + \frac{y^2}{4} = 1$

D. $\frac{x^2}{5} + \frac{y^2}{4} = 1$

Answer: A



Watch Video Solution

2. A parabola is drawn through two given points $A(1, 0)$ and $B(-1, 0)$ such that its directrix always touches the circle $x^2 + y^2 = 4$. Then, the maximum possible length of semi latus rectum is

A. $2 + \sqrt{3}$

B. $3 + \sqrt{3}$

C. $4 + \sqrt{3}$

D. $1 + \sqrt{3}$

Answer: A



Watch Video Solution

Matching Column Type

1. AB is a chord of $y^2 = 4x$ such that normals at A and B intersect at $C(9, 6)$ and the tangent at A and B at point T , find $(CT)^2/13$



Watch Video Solution