MATHS

BOOKS - CENGAGE MATHS (ENGLISH)

THREE DIMENSIONAL GEOMETRY

Others

1. Find the angle between the line whose direction cosines are given by $l+m+n=0 and l^2+m^2-n^2-0.$

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2. A line makes angles $\alpha, \beta, \gamma and \delta$ with the diagonals of a cube. Show that $\cos^2\alpha+\cos^2\beta+\cos^2\gamma+\cos^2\delta=4/3.$

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3. ABC is a triangle and A=(2,3,5),B=(-1,3,2) and C= $(\lambda, 5, \mu)$. If the median through A is equally inclined to the axes, then find the value of λ and μ

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4. A line OP through origin O is inclined at $30^0 and 45^0 \rightarrow OX and OY$, respectivley. Then find the angle at which it is inclined to OZ.

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5. If $\alpha, \beta, and \gamma$ are the an gles which a directed line makes with the positive directions of the co-ordinates axes, then find the value of $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma$.

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6. If the sum of the squares of the distance of a point from the three coordinate axes is 36, then find its distance from the origin.

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7. If $A(3, 2, -4), B(5, 4, -6) and C(9, 8, -10)$ are three collinear points, then find the ratio in which point C divides AB.

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8. Find the ratio in which the $y-z$ plane divides the join of the points $(-2, 4, 7) and (3, -5, 8)$.

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9. A line passes through the points $(6, -7, -1) and (2, -3, 1)$. Find te direction cosines off the line if the line makes an acute angle with the positive direction of the x-axis.

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10. Find the angle between the lines whose direction cosines are connected by the relations $l+m+n=0 and 2lm+2nl-mn=0.$

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11. Find the point where line which passes through point $(1, 2, 3)$ and is parallel to line $\vec{r}=\hat{i}+\hat{j}+2\hat{k}+\lambda\left(\hat{i}-2\hat{j}+3\hat{k}\right)$ meets the xy-plane.

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12. Find the equation of the line passing through the points $(1, 2, 3) and (-1, 0, 4).$

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13. Find the equation of the line passing through the point $(-1, 2, 3)$ and perpendicular to the lines $\frac{x}{2} = \frac{y-1}{-3} = \frac{z+2}{-2} and \frac{x+3}{-1} = \frac{y+3}{2} = \frac{z-1}{3}$.

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14. The line joining the points $(-2, 1, -8) and (a, b, c)$ is parallel to the line whose direction ratios are $6, 2, and 3$. Find the values of a, b and c

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15. A parallelepiped is formed by planes drawn through the points $P(6, 8, 10) and (3, 4, 8)$ parallel to the coordinate planes. Find the length of edges and diagonal of the parallelepiped.

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16. Find the angle between any two diagonals of a cube.

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17. Direction ratios of two lines are $a, b, c and 1/bc, 1/ca, 1/ab$. Then the lines are _____.

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18. Find the equation of the line passing through the intersection of $\frac{x-1}{2}=\frac{y-2}{3}=\frac{z-3}{4} and \frac{x-4}{5}=\frac{y-1}{2}=z$. and also through the point $(2, 1, -2)$.

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19. The straight line $\frac{x-3}{3}=\frac{y-2}{1}=\frac{z-1}{0}$ is (a)Parallel to x-axis (b)Parallel to the y-axis (c)Parallel to the z-axis (d)Perpendicular to the z-axis

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20. Find the equation of a plane containing the lines $\frac{x-5}{4}=\frac{y-7}{4}=\frac{z+3}{-5}$ and $\frac{x-8}{7}=\frac{y-4}{1}=\frac{z-5}{3}$.

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21. Find the equation of the plane passing through the points $(1, 0, -1) and (3, 2, 2)$ and parallel to the line $x-1=\frac{1-y}{2}=\frac{z-2}{3}$.

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22. Find the equation of the sphere described on the joint of points $A and B$ having position vectors $2\hat{i}+6\hat{j}-7\hat{k} and -2\hat{i}+4\hat{j}-3\hat{k},$

respectively, as the diameter. Find the center and the radius of the sphere.

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23. Find the radius of the circular section in which the sphere $\left|\vec{r}\right| = 5$ is cut by the plane $\vec{r}\cdot\left(\hat{i}+\hat{j}+\hat{k}\right) = 3\sqrt{3.}$

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24. Find the equation of a sphere which passes through $(1, 0, 0)(0, 1, 0)and(0, 0, 1),$ and has radius as small as possible.

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25. Find the locus of a point which moves such that the sum of the squares of its distance from the points $A(1, 2, 3), B(2, -3, 5)$ and $C(0, 7, 4)$ is 120.

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26. Find the equation of the sphere which has centre at the origin and touches the line $2(x+1) = 2 - y = z + 3$.

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27. Find the equation of the sphere which passes through $(1, 0, 0), (0, 1, 0)$ and $(0, 0, 1)$ and whose centre lies on the plane $3x - y + z = 2$.

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28. Find the equation of a sphere whose centre is $(3, 1, 2)$ radius is 5.

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29. Find the equation of the sphere passing through $(0, 0, 0), (1, 0, 0), (0, 1, 0)$ and $(0, 0, 1)$.

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30. Find the image of the line $\frac{x-1}{9} = \frac{y-2}{-1} = \frac{z+3}{-3}$ in the plane $3x - 3y + 10z - 26 = 0.$

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31. Find the equations of the bisectors of the angles between the planes $2x - y + 2z + 3 = 0 and 3x - 2y + 6z + 8 = 0$ and specify the plane which bisects the acute angle and the plane which bisects the obtuse angle.

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32. If the x-coordinate of a point P on the join of $Q(2, 2, 1) and R(5, 1, -2) is 4$, then find its $z-$ coordinate.

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33. A sphere of constant radius k passes through the origin and meets the axes at A, B and C. Prove that the centroid of triangle ABC lies on the sphere $9\left(x^2+y^2+z^2\right)=4k^2$.

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34. A variable plane passes through a fixed point (a, b, c) and cuts the coordinate axes at points $A, B, and C$. Show that eh locus of the centre of the sphere $OABC is \frac{a}{x}+\frac{b}{y}+\frac{c}{z}=2.$

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35. Show that the plane $2x - 2y + z + 12 = 0$ touches the sphere $x^2 + y^2 + z^2 - 2x - 4y + 2z - 3 = 0.$

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36. If O is the origin, OP = 3, with direction ratios -1, 2 and -2, then find the coordinates of P.

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37. If $P(x, y, z)$ is a point on the line segment joining Q(2,2,4) and R(3,5,6) such that the projection of $\overrightarrow{OP}$ on the axes are $\frac{13}{9}, \frac{19}{5}, \frac{26}{5}$ respectively, then P divides QR in the ratio:

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38. If $\vec{r}$ is a vector of magnitude 21 and has direction ratios 2, -3 and 6, then find $\vec{r}$.

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39. Find the distance of the point $P(a, b, c)$ from the x-axis.

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40. A line makes angles $\alpha, \beta and \gamma$ with the coordinate axes. If $\alpha + \beta = 90^0$, then find γ.

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41. If a line makes angles $\alpha, \beta and \gamma$ with threew-dimensional coordinate axes, respectively, then find the value of $\cos 2\alpha + \cos 2\beta + \cos 2\gamma$.

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42. Find the distance between the parallel planes $x + 2y - 2z + 1 = 0 and 2x + 4y - 4z + 5 = 0.$

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43. A ray of light passing through the point $A(1, 2, 3)$, strikews the plane $xy + z = 12 at B$ and on reflection passes through point $C(3, 5, 9)$. Find the coordinate so point B.

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44. The plane $ax + by = 0$ is rotated through an angle α about its line of intersection with the plane $z = 0.$ Show that he equation to the plane in the new position is $ax + by \pm z\sqrt{a^2 + b^2} \tan\alpha = 0$

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45. Find the equation of a plane containing the line of intersection of the planes $x + y + z - 6 = 0 and 2x + 3y + 4z + 5 = 0$ passing through $(1, 1, 1)$.

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46. Find the locus of a point, the sum of squares of whose distance from the planes $x - z = 0, x - 2y + z = 0$ and $x + y + z = 0$ is 36

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47. Find the length and the foot of the perpendicular from the point $(7,\ 14,\ 5)$ to the plane $2x + 4y - z = 2.$ Also, the find image of the point P in the plane.

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48. Find the angle between the lines $\overrightarrow{r} = \hat{i} + 2\dot{\hat{j}} - \hat{k} + \lambda\left(\hat{i} - \hat{j} + \hat{k}\right)$

and the plane $\overrightarrow{r} = 2\hat{i} - \dot{\hat{j}} + \hat{k} = 4$.

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49. Find the equation of the projection of the line $\dfrac{x-1}{2} = \dfrac{y+1}{-1} = \dfrac{z-3}{4}$ on the plane $x + 2y + z = 9$.

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50. Find the equation the plane which contain the line of intersection of the planes $\overrightarrow{r}\hat{i} + 2\dot{\hat{j}} + 3\hat{k} - 4 = 0 and \overrightarrow{r}2\hat{i} + \dot{\hat{j}} - \hat{k} + 5 = 0$ and which is perpendicular to the plane $\overrightarrow{r}\left(5\hat{i} + 3\hat{j} - 6\hat{k}\right) + 8 = 0$.

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51. Find the vector equation of the line passing through (1, 2, 3) and parallel to the planes $\rightarrow r\dot{\hat{i}} - \hat{j} + 2\hat{k} = 5 \, and \, \rightarrow r3\dot{\hat{i}} + \hat{j} + \hat{k} = 6.$

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52. Find the distance of the point $P(3, 8, 2)$ from the line $\frac{1}{2}(x-1) = \frac{1}{4}(y-3) = \frac{1}{3}(z-2)$ measured parallel to the plane $3x + 2y - 2z + 15 = 0.$

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53. Find the distance of the point $(1, 0, -3)$ from the plane $x - y - z = 9$ measured parallel to the line $\frac{x-2}{2} = \frac{y+2}{2} = \frac{z-6}{-6}.$

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54. Show that $ax + by + r = 0, by + cz + p = 0 andcz + ax + q = 0$ are perpendicular to $x - y, y - zandz - x$ planes, respectively.

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55. Reduce the equation of line $x - y + 2z = 5adn3x + y + z = 6$ in symmetrical form. Or Find the line of intersection of planes $x - y + 2z = 5and3x + y + z = 6$.

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56. Find the angle between the lines $x - 3y - 4 = 0, 4y - z + 5 = 0andx + 3y - 11 = 0, 2y = z + 6 = 0$.

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57. If the line $x = y = z$ intersect the line $\sin A\dot{x} + \sin B\dot{y} + \sin C\dot{z} = 2d^2, \sin 2A\dot{x} + \sin 2B\dot{y} + \sin 2C\dot{z} = d^2,$ then find the value of $\frac{\sin A}{2}\frac{\sin B}{2}\frac{\sin C}{2} where A, B, C$ are the angles of a triangle.

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58. The point of intersecting of the line passing through $(0, 0, 1)$ and intersecting the lines $x + 2y + z = 1, \ -x + y - 2z = 2$ and $x + y = 2, x + z = 2$ with xy-plane is

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59. A horizontal plane $4x - 3y + 7z = 0$ is given. Find a line of greatest slope passes through the point $(2, 1, 1)$ in the plane $2x + y - 5z = 0.$

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60. Find the equation of the plane passing through the points $(-1, 1, 1)$ and $(1, -1, 1)$ and perpendicular to the plane $x + 2y + 2z = 5.$

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61. Find ten equation of the plane passing through the point $(0, 7, -7)$ and containing the line $\frac{x+1}{-3} = \frac{y-3}{2} = \frac{z+2}{1}$.

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62. If a plane meets the equations axes at $A, BandC$ such that the centroid of the triangle is $(1, 2, 4)$, then find the equation of the plane.

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63. Find the equation of the plane which is parallel to the lines $\vec{r} = \hat{i} + \hat{j} + \lambda\left(2\hat{i} + \hat{j} + 4\hat{k}\right) and \frac{x+1}{-3} = \frac{y-3}{2} = \frac{z+2}{1}$ and is passing through the point $(0, 1, -1)$.

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64. Show that the plane whose vector equation is $\vec{r}\hat{i} + 2\dot{\hat{j}} = \hat{k} = 3$ contains the line whose vector equation is $\vec{r}\hat{i}\dot{+}\hat{j} + \lambda\left(2\hat{i} + \hat{j} + 4\hat{k}\right).$

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65. Find the vector equation of the following planes in Cartesian form: $\vec{r} = \hat{i} - \hat{j} + \lambda\left(\hat{i} + \hat{j} + \hat{k}\right) + \mu\left(\hat{i} - 2\hat{j} + 3\hat{k}\right).$

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66. Show that the line of intersection of the planes $\vec{r}\hat{i}+2\dot{\hat{j}}+3\hat{k}=0and\vec{r}=\left(3\hat{i}+2\hat{j}+\hat{k}\right)=0$ is equally inclined to $iandk\cdot$ Also find the angle it makes with $j\cdot$

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67. Find the equation of the plane passing through $A(2, 2, -1)$, $B(3, 4, 2)$ and $C(7, 0, 6)$.

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68. Find the equation of the plane such that image of point $(1, 2, 3)$ in it is$(-1, 0, 1)\cdot$

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69. The foot of the perpendicular drawn from the origin to a plane is $(1, 2, -3)$. Find the equation of the plane. or If O is the origin and the coordinates of P is $(1, 2, -3)$, then find the equation of the plane passing through P and perpendicular to OP.

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70. Find the angel between the planes $2x + y - 2z + 3 = 0 and \vec{r} \cdot 6\hat{i} + 3\hat{j} + 2\hat{k} = 5.$

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71. Find the equation of the plane passing through $(3, 4, -1)$, which is parallel to the plane $\vec{r} \cdot 2\hat{i} - 3\hat{j} + 5\hat{k} + 7 = 0.$

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72. Find the distance of the point $(-1, -5, -10)$ from the point of intersection of the line $\frac{x-2}{3} = \frac{y+1}{4} = \frac{z-2}{12}$ and plane $x - y + z = 5$.

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73. Find the equation of the plane passing through the point $(-1, 3, 2)$ and perpendicular to each of the planes $x + 2y + 3z = 5 and 3x + 3y + z = 0$.

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74. Find the angle between the line $\frac{x-1}{3} = \frac{y-1}{2} = \frac{z-1}{4}$ and the plane $2x + y - 3z + 4 = 0$.

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75. Find the distance between the line $\frac{x+1}{-3} = \frac{y-3}{2} = \frac{z-2}{1}$ and the plane $x + y + z + 3 = 0.$

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76. The extremities of a diameter of a sphere lie on the positive y- and positive z-axes at distance 2 and 4, respectively. Show that the sphere passes through the origin and find the radius of the sphere.

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77. A plane passes through a fixed point $(a, b, c)\cdot$ Show that the locus of the foot of the perpendicular to it from the origin is the sphere $x^2 + y^2 + z^2 - ax - by - cz = 0.$

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78. Find the radius of the circular section of the sphere $\left|\vec{r}\right| = 5$ by the plane $\vec{r}\,\hat{i} + 2\hat{j} - \hat{k} = 4\sqrt{3}.$

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79. A point $P(x, y, z)$ is such that $3PA = 2PB,$ where $A and B$ are the point $(1, 3, 4) and (1, -2, -1),$ irrespectivley. Find the equation to the locus of the point P and verify that the locus is a sphere.

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80. Find the shortest distance between lines $\vec{r} = \left(\hat{i} + 2\hat{j} + \hat{k}\right) + \lambda\left(\hat{i} - \hat{j} + \hat{k}\right) and \vec{r} = 2\hat{i} - \hat{j} - \hat{k} + \mu\left(2\hat{i} + \hat{j} + 2\hat{k}\right.$

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81. Find the shortest distance between the lines $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4} and \frac{x-2}{3} = \frac{y-4}{4} = \frac{z-5}{5}$.

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82. Determine whether the following pair of lines intersect or not. (1) $\vec{r} = \hat{i} - 5\hat{j} + \lambda(2\hat{i} + \hat{k}); \vec{r} = 2\hat{i} - \hat{j} + \mu(\hat{i} + \hat{j} - \hat{k})$ (2) $\vec{r} = \hat{i} + \hat{j} - \hat{k} + \lambda(3\hat{i} - \hat{j}); \vec{r} = 4\hat{i} - \hat{k} + \mu(2\hat{i} + 3\hat{k})$

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83. Find the equation of plane which is at a distance $\frac{4}{\sqrt{14}}$ from the origin and is normal to vector $2\hat{i} + \hat{j} - 3\hat{k}$.

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84. Find the unit vector perpendicular to the plane $\vec{r} \cdot 2\hat{i} + \hat{j} + 2\hat{k} = 5$.

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85. If the straight lines $x = -1 + s, y = 3 - \lambda s, z = 1 + \lambda s and x = \frac{t}{2}, y = 1 + t, z = 2 - t,$ with paramerters $s and t,$ respectivley, are coplanar, then find λ.

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86. Find the equation of a line which passes through the point $(1, 1, 1)$ and intersects the lines $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4} and \frac{x+2}{1} = \frac{y-3}{2} = \frac{z+1}{4}$.

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87. Find the vector equation of a line passing through $3\hat{i} - 5\hat{j} + 7\hat{k}$ and perpendicular to the plane $3x - 4y + 5z = 8$.

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88. Find the equation of the plane passing through the point $(2, 3, 1)$ having $(5, 3, 2)$ as the direction ratio is of the normal to the plane.

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89. Find the equation of the plane through the points $(2, 3, 1)$ and $(4, -5, 3)$ and parallel to the x-axis.

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90. Find the equation of the image of the plane $x - 2y + 2z - 3 = 0$ in plane $x + y + z - 1 = 0$.

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91. Find the equation of a plane which passes through the point $(1, 2, 3)$ and which is equally inclined to the planes

$x - 2y + 2z - 3 = 0$ and $8x - 4y + z - 7 = 0.$

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92. Find the equation of a plane which is parallel to the plane $x - 2y + 2z = 5$ and whose distance from the point $(1, 2, 3)$ is 1.

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93. Find the direction ratios of orthogonal projection of line $\frac{x-1}{1} = \frac{y+1}{-2} = \frac{z-2}{3}$ in the plane $x - y + 2z - 3 = 0$. Also find the direction ratios of the image of the line in the plane.

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94. Find the equation of the plane which passes through the point $(1, 2, 3)$ and which is at the minimum distance from the point $(-1, 0, 2)$.

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95. Find the angle between the lines $\overrightarrow{r} = \hat{i} + 2\dot{\hat{j}} - \hat{k} + \lambda\left(\hat{i} - \hat{j} + \hat{k}\right)$ and the plane $\overrightarrow{r} = 2\hat{i} - \dot{\hat{j}} + \hat{k} = 4.$

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96. Find the equation of the plane passing through the line $\frac{x-1}{5} = \frac{y+2}{6} = \frac{z-3}{4}$ and point $(4, 3, 7)$.

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97. Find the equation of the plane perpendicular to the line $\frac{x-1}{2} = \frac{y-3}{-1} = \frac{z-4}{2}$ and passing through the origin.

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98. Find the equation of the plane passing through the straight line $\frac{x-1}{2} = \frac{y+2}{-3} = \frac{z}{5}$ and perpendicular to the plane $x - y + z + 2 = 0$.

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99. Find the equation of the line drawn through the point $(1, 0, 2)$ to meet at right angles to the line $\frac{x+1}{3} = \frac{y-2}{-2} = \frac{z+1}{-1}$.

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100. If $\vec{r} = \left(\hat{i} + 2\hat{j} + 3\hat{k}\right) + \lambda\left(\hat{i} - \hat{j} + \hat{k}\right)$ and $\vec{r} = \left(\hat{i} + 2\hat{j} + 3\hat{k}\right) + \mu\left(\hat{i} + \hat{j} - \hat{k}\right)$ are two lines, then the equation of acute angle bisector of two lines is

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101. Find the coordinates of a point on the $\frac{x-1}{2} = \frac{y+1}{-3} = z$ atg a distance $4\sqrt{14}$ from the point $(1, -1, 0)$.

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102. Line L_1 is parallel to vector $\vec{\alpha} = -3\hat{i} + 2\hat{j} + 4\hat{k}$ and passes through a point $A(7, 6, 2)$ and line L_2 is parallel vector $\vec{\beta} = 2\hat{i} + \hat{j} + 3\hat{k}$ and point $B(5, 3, 4)$. Now a line L_3 parallel to a vector $\vec{r} = 2\hat{i} - 2\hat{j} - \hat{k}$ intersects the lines $L_1 and L_2$ at points $C and D$, respectively, then find $\left|\vec{C} D\right|$.

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103. Find the values p so that line $\frac{1-x}{3} = \frac{7y-14}{2p} = \frac{z-3}{2} and \frac{7-7x}{3p} = \frac{y-5}{1} = \frac{6-z}{5}$ are at right angles.

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104. Find the angel between the following pair of lines: $\overrightarrow{r} = 2\hat{i} - 5\hat{j} + \hat{k} + \lambda\left(3\hat{i} + 2\hat{j} + 6\hat{k}\right) and \overrightarrow{r} = 7\hat{i} - 6\hat{k} + \mu\left(\hat{i} + 2\hat{j} + 2\hat{k}\right)$
$\frac{x}{2} = \frac{y}{2} = \frac{z}{1} and \frac{x-5}{4} = \frac{y-2}{1} = \frac{z-3}{8}$

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105. Fid the condition if lines $x = ay + b, z = cy + d and x = a'y + b', z = c'y + d'$ are perpendicular.

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106. Find the acute angle between the lines $\frac{x-1}{l} = \frac{y+1}{m} = \frac{1}{n} and = \frac{x+1}{m} = \frac{y-3}{n} = \frac{z-1}{l} where l > m > n,$ are the roots of the cubic equation $x^3 + x^2 - 4x = 4.$

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107. Find the length of the perpendicular drawn from point $(2, 3, 4)$ to line $\frac{4-x}{2} = \frac{y}{6} = \frac{1-z}{3}$.

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108. Find the coordinates of the foot of the perpendicular drawn from point $A(1, 0, 3)$ to the join of points $B(4, 7, 1) and C(3, 5, 3)\cdot$

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109. Find the vector equation of the line passing through $(1, 2, 3)$ and parallel to the planes $\overrightarrow{r}\hat{i} - \dot{\hat{j}} + 2\hat{k} and \overrightarrow{r}3\hat{i} + \dot{\hat{j}} + \hat{k} = 6.$

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110. Find the value of m for which thestraight line $3x - 2y + z + 3 = 0 = 4x + 3y + 4z + 1$ is parallel to the plane $2x - y + mz - 2 = 0.$

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111. Show that the lines $\frac{x-a+d}{\alpha-\delta}=\frac{y-a}{\alpha}=\frac{z-a-d}{\alpha+\delta}$ and $\frac{x-b+c}{\beta-\gamma}=\frac{y-b}{\beta}=\frac{z-b-c}{\beta+\gamma}$ are coplanar.

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112. Find the equation of line $x+y-z-3=0=2x+3y+z+4$ in symmetric form. Find the direction ratio of the line.

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113. Find the vector equation of line passing through the point $(1, 2, -4)$ and perpendicular to the two lines: $\frac{x-8}{3}=\frac{y+19}{-16}=\frac{z-10}{7} and \frac{x-15}{3}=\frac{y-29}{8}=\frac{z-5}{-5}$

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114. Find the vector equation of line passing through $A(3, 4-7) and B(1, -1, 6)\cdot$ Also find its Cartesian equations.

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115. Find Cartesian and vector equation of the line which passes through the point $(-2, 4, -5)$ and parallel to the line given by $\frac{x+3}{3}=\frac{y-4}{5}=\frac{z+8}{6}.$

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116. Find the equation of a line which passes through the point $(2, 3, 4)$ and which has equal intercepts on the axes.

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117. Find the points where line $\frac{x-1}{2}=\frac{y+2}{-1}=\frac{z}{1}$ intersects $xy, yz and zx$ planes.

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118. A mirror and source of light are situated at the origin O and a point on OX respectively. A ray of light from the source strikes the mirror and is reflected. If the DRs of the normal to the plane of mirror are $1, -1, 1$, then DCs for the reflacted ray are :

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119. The Cartesian equation of a line is $\frac{x-3}{2}=\frac{y+1}{-2}=\frac{z-3}{5}$. Find the vector equation of the line.

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120. The Cartesian equations of a line are $6x-2=3y+1=2z-2$. Find its direction ratios and also find a vector equation of the line.

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121. A line passes through the point with position vector $2\hat{i} - 3\hat{j} + 4\hat{k}$ and is in the direction of $3\hat{i} + 4\hat{j} - 5\hat{k}\cdot$ Find the equations of the line in vector and Cartesian forms.

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122. Find the plane of the intersection of $x^2 + y^2 + z^2 + 2x + 2y + 2 = 0$ and $4x^2 + 4y^2 + 4z^2 + 4x + 4y + 4z - 1 = 0.$

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123. Let $l_1 and l_2$ be the two skew lines. If P, Q are two distinct points on $l_1 nd R, S$ are two distinct points on $l_2,$ then prove that PR cannot be parallel to $QS\cdot$

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124. If the lines $\frac{x-1}{-3}=\frac{y-2}{2k}=\frac{z-3}{-2}$ and $\frac{x-1}{3k}=\frac{y-5}{1}=\frac{z-6}{-5}$ are at right angle, then find the value of k.

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125. Find the angle between the lines $2x=3y=-z$ and $6x=-y=-4z$

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126. Find the length of the perpendicular drawn from the point $(5, 4, -1)$ to the line $\overrightarrow{r}=\hat{i}+\lambda\left(2\hat{i}+9\hat{j}+5\hat{k}\right)$, wher λ is a parameter.

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127. The equations of motion of a rocket are $x = 2t, y = -4tandz = 4t$, where time$t$ is given in seconds, and the coordinates of a moving points in kilometers. What is the path of the rocket? At what distance will be the rocket from the starting point $O(0, 0, 0)$ in $10s$?

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128. Find the shortest distance between the lines $\vec{r} = (1-\lambda)\hat{i} + (\lambda - 2)\hat{j} + (3 - 2\lambda)\hat{k}$ and $\vec{r} = (\mu + 1)\hat{i} + (2\mu + 1)\hat{k}$.

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129. Find the image of the point $(1, 2, 3)$ in the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$.

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130. If the lines $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-1}{4}$ and $\frac{x-3}{1} = \frac{y-k}{2} = \frac{z}{1}$ intersect, then find the value of k.

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131. Find the shortest distance between the z-axis and the line, $x + y + 2z - 3 = 0, 2x + 3y + 4z - 4 = 0.$

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132. The lines which intersect the skew lines $y = mx, z = c; y = -mx, z = -c$ and the x-axis lie on the surface: (a.) $cz = mxy$ (b.) $xy = cmz$ (c.) $cy = mxz$ (d.) none of these

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133. Distance of the point $P\left(\vec{p}\right)$ from the line $\vec{r}=\vec{a}+\lambda\vec{b}$ is a. $\left|\left(\vec{a}-\vec{p}\right)+\frac{\left(\left(\vec{p}-\vec{a}\right)\dot{\vec{b}}\right)\vec{b}}{\left|\vec{b}\right|^2}\right|$ b. $\left|\left(\vec{b}-\vec{p}\right)+\frac{\left(\left(\vec{p}-\vec{a}\right)\dot{\vec{b}}\right)\vec{b}}{\left|\vec{b}\right|^2}\right|$ c. $\left|\left(\vec{a}-\vec{p}\right)+\frac{\left(\left(\vec{p}-\vec{b}\right)\dot{\vec{b}}\right)\vec{b}}{\left|\vec{b}\right|^2}\right|$ d. none of these

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134. The direction ratios of a normal to the plane through $(1, 0, 0) and (0, 1, 0)$, which makes and angle of $\frac{\pi}{4}$ with the plane $x+y=3$, are a. $\langle 1, \sqrt{2}, 1\rangle$ b. $\langle 1, 1, \sqrt{2}\rangle$ c. $\langle 1, 1, 2\rangle$ d. $\langle\sqrt{2}, 1, 1\rangle$

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135. The centre of the circle given by $\overrightarrow{r}\hat{i}+2\hat{j}+2\hat{k}=15 and \left|\overrightarrow{r}-\left(\hat{j}+2\hat{k}\right)\right|=4$ is a. $(0, 1, 2)$ b. $(1, 3, 4)$ c. $(-1, 3, 4)$ d. none of these

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136. Two systems of rectangular axes have the same origin. If a plane cuts them at distance $a, b, c$and a', b', c' from the origin, then a. $\frac{1}{a^2}+\frac{1}{b^2}+\frac{1}{c^2}+\frac{1}{a'^2}+\frac{1}{b'^2}+\frac{1}{c'^2}=0$ b. $\frac{1}{a^2}-\frac{1}{b^2}-\frac{1}{c^2}+\frac{1}{a'^2}-\frac{1}{b'^2}-\frac{1}{c'^2}=0$ c. $\frac{1}{a^2}+\frac{1}{b^2}+\frac{1}{c^2}-\frac{1}{a'^2}-\frac{1}{b'^2}-\frac{1}{c'^2}=0$ d. $\frac{1}{a^2}+\frac{1}{b^2}+\frac{1}{c^2}+\frac{1}{a'^2}+\frac{1}{b'^2}+\frac{1}{c'^2}=0$

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137. Find the equation of a plane which passes through the point (3, 2, 0) and contains the line $\frac{x-3}{1}=\frac{y-6}{5}=\frac{z-4}{4}$

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138. The lines $\frac{x-2}{1}=\frac{y-3}{1}=\frac{z-4}{-k} and \frac{x-1}{k}=\frac{y-4}{2}=\frac{z-5}{1}$ are coplanar if a. $k=1 \text{ or } -1$ b. $k=0 \text{ or } -3$ c. $k=3 \text{ or } -3$ d. $k=0 \text{ or } -1$

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139. The point of intersection of the lines $\frac{x-5}{3}=\frac{y-7}{-1}$ and $\frac{x+3}{-36}=\frac{y-3}{2}=\frac{z-6}{4}$ is

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140. A tetrahedron has vertices of $O(0,0,0), A(1,2,1), B(2,1,3)$ and $C(-1,1,2)$. Then, the angle between the faces OAB and ABC will be

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141. The radius of the circle in which the sphere $x^2 = y^2 + z^2 + 2z - 2y - 4z - 19 = 0$ is cut by the plane $x + 2y + 2z + 7 = 0$ is

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142. A sphere of constant radius $2k$ passes through the origin and meets the axes in $A, B, and C.$ The locus of a centroid of the tetrahedron $OABC$ is a. $x^2 + y^2 + z^2 = 4k^2$ b. $x^2 + y^2 + z^2 = k^2$ c. $2(x^2 + y^2 + z)^2 = k^2$ d. none of these

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143. A plane passes through a fixed point (a,b,c). The locus of the foot of the perpendicular to it from the origin is a sphere of radius

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144. Equation of the plane containing the straight line $\frac{x}{2} = \frac{y}{3} = \frac{z}{4}$ and perpendicular to the plane containing the straight lines $\frac{x}{3} = \frac{y}{4} = \frac{z}{2}$ and $\frac{x}{4} = \frac{y}{2} = \frac{z}{3}$ is

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145. The equation of the plane through the intersection of the planes $x + 2y + 3z - 4 = 0$ and $4x + 3y + 2z + 1 = 0$ and passing through the origin is (a) $17x + 14y + 11z = 0$ (b) $7x + 4y + z = 0$ (c) $x + 14 + 11z = 0$ (d) $17x + y + z = 0$

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146. The plane $4x + 7y + 4z + 81 = 0$ is rotated through a right angle about its line of intersection with the plane $5x + 3y + 10z = 25.$ The equation of the plane in its new position is a. $x - 4y + 6z = 106$ b. $x - 8y + 13z = 103$ c. $x - 4y + 6z = 110$ d. $x - 8y + 13z = 105$

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147. The vector equation of the plane passing through the origin and the line of intersection of the planes $\vec{r}\dot{\vec{a}} = \lambda and \vec{r}\dot{\vec{b}} = \mu$ is (a) $\vec{r}\lambda\dot{\vec{a}} - \mu\vec{b} = 0$ (b) $\vec{r}\lambda\dot{\vec{b}} - \mu\vec{a} = 0$ (c) $\vec{r}\lambda\dot{\vec{a}} + \mu\vec{b} = 0$ (d) $\vec{r}\lambda\dot{\vec{b}} + \mu\vec{a} = 0$

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148. The lines $\vec{r} = \vec{a} + \lambda\left(\vec{b} \times \vec{c}\right) and \vec{r} = \vec{b} + \mu\left(\vec{c} \times \vec{a}\right)$ will intersect if a. $\vec{a} \times \vec{c} = \vec{b} \times \vec{c}$ b. $\vec{a}\dot{\vec{c}} = \vec{b}\dot{\vec{c}}$ c. $b \times \vec{a} = \vec{c} \times \vec{a}$ d. none of these

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149. The projection of the line $\frac{x+1}{-1} = \frac{y}{2} = \frac{z-1}{3}$ on the plane $x - 2y + z = 6$ is the line of intersection of this plane with the plane

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150. The direction cosines of a line satisfy the relations $\lambda(l+m)=n$ and $mn+nl+lm=0$. The value of λ for which the two lines are perpendicular to each other, is

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151. The intercepts made on the axes by the plane which bisects the line joining the point $(1, 2, 3)$ and $(-3, 4, 5)$ at right angles are :

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152. The pair of lines whose direction cosines are given by the equations $3l+m+5n=0 and 6mn-2nl+5lm=0$ are a. parallel b. perpendicular c. inclined at $\cos^{-1}\left(\frac{1}{6}\right)$ d. none of these

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153. If the distance of the point $P(1, -2, 1)$ from the plane $x+2y-2z=\alpha, where\alpha>0, is5,$ then the foot of the perpendicular from P to the plane is a. $\left(\frac{8}{3}, \frac{4}{3}, -\frac{7}{3}\right)$ b. $\left(\frac{4}{3}, -\frac{4}{3}, \frac{1}{3}\right)$ c. $\left(\frac{1}{3}, \frac{2}{3}, \frac{10}{3}\right)$ d. $\left(\frac{2}{3}, -\frac{1}{3}, -\frac{5}{3}\right)$

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154. A line with positive direction cosines passes through the point $P(2, -1, 2)$ and makes equal angles with the coordinate axes. The line meets the plane $2x+y+z=9$ at point Q. The length of the line segment PQ equals

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155. The value of k such that $\frac{x-4}{1}=\frac{y-2}{1}=\frac{z-k}{2}$ lies in the plane $2x-4y+z=7$ is a. 7 b. -7 c. no real value d. 4

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156. The equation of the plane passing through lines $\frac{x-4}{1}=\frac{y-3}{1}=\frac{z-2}{2} and \frac{x-3}{2}=\frac{y-2}{-4}=\frac{z}{5}$ is a. $11x-y-3z=35$ b. $11x+y-3z=35$ c. $11x-y+3z=35$ d. none of these

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157. The line through $\hat{i}+3\hat{j}+2\hat{k}$ and $\perp$ to the line $\vec{r}=\left(\hat{i}+2\hat{j}-\hat{k}\right)+\lambda\left(2\hat{i}+\hat{j}+\hat{k}\right) and \vec{r}=\left(2\hat{i}+6\hat{j}+\hat{k}\right)+\mu\left(\hat{i}+2\hat{j}$ is a. $\vec{r}=\left(\hat{i}+2\hat{j}-\hat{k}\right)+\lambda\left(-\hat{i}+5\hat{j}-3\hat{k}\right)$ b. $\vec{r}=\hat{i}+3\hat{j}+2\hat{k}+\lambda\left(\hat{i}-5\hat{j}+3\hat{k}\right)$ c. $\vec{r}=\hat{i}+3\hat{j}+2\hat{k}+\lambda\left(\hat{i}+5\hat{j}+3\hat{k}\right)$ d. $\vec{r}=\hat{i}+3\hat{j}+2\hat{k}+\lambda\left(-\hat{i}-5\hat{j}-3\hat{k}\right)$

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158. The equation of the plane through the line of intersection of the planes $ax + by + cz + d = 0$ and $a'x + b'y + c'z + d' = 0$ parallel to the line $y = 0$ and $z = 0$ is

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159. The three planes $4y + 6z = 5, 2x + 3y + 5z = 5$ and $6x + 5y + 9z = 10$ (a) meet in a point (b) have a line in common (c) form a triangular prism (d) none of these

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160. Given $\overrightarrow{\alpha} = 3\hat{i} + \hat{j} + 2\hat{k}$ and $\overrightarrow{\beta} = \hat{i} - 2\hat{j} - 4\hat{k}$ are the position vectors of the points A and B Then the distance of the point $\hat{i} + \hat{j} + \hat{k}$ from the plane passing through B and perpendicular to AB is (a) 5 (b) 10 (c)15 (d) 20

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161. Find the following are equations for the plane passing through the points $P(1, 1, -1), Q(3, 0, 2) and R(-2, 1, 0)$?

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162. The shortest distance between the lines $\frac{x-3}{3}=\frac{y-8}{-1}=\frac{z-3}{1}$ and $\frac{x+3}{-3}=\frac{y+7}{2}=\frac{z-6}{4}$ is

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163. $L_1 and L_2$ and two lines whose vector equations are $L_1 : \vec{r}=\lambda\left(\left(\cos\theta+\sqrt{3}\right)\hat{i}+\left(\sqrt{2}\sin\theta\right)\hat{j}+\left(\cos\theta-\sqrt{3}\right)\hat{k}\right)$ $L_2 : \vec{r}=\mu\left(a\hat{i}+b\hat{j}+c\hat{k}\right)$, where $\lambda and \mu$ are scalars and α is the acute angel between $L_1 and L_2$. If the angel α is independent of θ, then the value of α is a. $\frac{\pi}{6}$ b. $\frac{\pi}{4}$ c. $\frac{\pi}{3}$ d. $\frac{\pi}{2}$

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164. Value of λ such that the line $\frac{x-1}{2}=\frac{y-1}{3}=\frac{z-1}{\lambda}$ is $\perp$ to normal to the plane $\vec{r}.\left(2\vec{i}+3\vec{j}+4\vec{k}\right)=0$ is a. $-\frac{13}{4}$ b. $-\frac{17}{4}$ c. 4 d. none of these

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165. Equation of the plane passing through the points $(2, 2, 1) and (9, 3, 6), and \perp$ to the plane $2x+6y+6z=9$ is a. $3x+4y+5z=9$ b. $3x+4y-5z=9$ c. $3x+4y-5z=9$ d. none of these

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166. The equation of a plane which passes through the point of intersection of lines $\frac{x-1}{3}=\frac{y-2}{1}=\frac{z-3}{2}$, and $\frac{x-3}{1}=\frac{y-1}{2}=\frac{z-2}{3}$ and at greatest distance from point (0,0,0) is

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167. If the foot of the perpendicular from the origin to plane is $P(a, b, c)$, the equation of the plane is a. $\frac{x}{a}=\frac{y}{b}=\frac{z}{c}=3$ b. $ax+by+cz=3$ c. $ax+by+cz=a^2+b^2+c^2$ d. $ax+by+cz=a+b+c$

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168. Equation of a line in the plane $\pi=2x-y+z-4=0$ which is perpendicular to the line l whose equation is $\frac{x-2}{1}=\frac{y-2}{-1}=\frac{z-3}{-2}$ and which passes through the point of intersection of l and π is (A) $\frac{x-2}{1}=\frac{y-1}{5}=\frac{z-1}{-1}$ (B) $\frac{x-1}{3}=\frac{y-3}{5}=\frac{z-5}{-1}$ (C) $\frac{x+2}{2}=\frac{y+1}{-1}=\frac{z+1}{1}$ (D) $\frac{x-2}{2}=\frac{y-1}{-1}=\frac{z-1}{1}$

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169. The intercept made by the plane $\vec{r}.\vec{n}=q$ on the x-axis is a. $\frac{q}{\hat{i}.\vec{n}}$ b. $\frac{\hat{i}.\vec{n}}{q}$ c. $\frac{\hat{i}.\vec{n}}{q}$ d. $\frac{q}{\left|\vec{n}\right|}$

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170. The coordinates o the foot of the perpendicular drawn from the origin to the line joining the point $(-9, 4, 5) and (10, 0, -1)$ will be a. $(-3, 2, 1)$ b. $(1, 2, 2)$ c. $4, 5, 3$ d. none of these

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171. The point on the line $\frac{x-2}{1}=\frac{y+3}{-2}=\frac{z+5}{-2}$ at a distance of 6 from the point $(2, -3, -5)$ is a. $(3, -5, -3)$ b. $(4, -7, -9)$ c. $(0, 2, -1)$ d. none of these

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172. Let $A(1, 1, 1), B(2, 3, 5) and C(-1, 0, 2)$ be three points, then equation of a plane parallel to the plane ABC which is at distance 2 is a. $2x - 3y + z + 2\sqrt{14} = 0$ b. $2x - 3y + z - \sqrt{14} = 0$ c. $2x - 3y + z + 2 = 0$ d. $2x - 3y + z - 2 = 0$

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173. Let $A\left(\vec{a}\right) and B\left(\vec{b}\right)$ be points on two skew lines $\vec{r} = \vec{a} + \lambda \vec{p}\, and\, \vec{r} = \vec{b} + u \vec{q}$ and the shortest distance between the skew lines is $1, where\, \vec{p}\, and\, \vec{q}$ are unit vectors forming adjacent sides of a parallelogram enclosing an area of 1/2 units. If angle between AB and the line of shortest distance is 60^0, then $AB =$ a. $\frac{1}{2}$ b. 2 c. 1 d. $\lambda R = \{10\}$

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174. Consider three planes $P_1 : x - y + z = 1$, $P_2 : x + y - z = -1$ and $P_3 : x - 3y + 3z = 2$ Let L_1, L_2 and L_3 be the lines of intersection of the planes P_2 and P_3, P_3 and P_1 and P_1 and P_2 respectively.Statement 1: At least two of the lines L_1, L_2 and L_3 are non-parallel . Statement 2:The three planes do not have a common point

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175. Consider the planes $3x - 6y - 2z - 15 = 0$ and $2x + y - 2z - 5 = 0$ Statement 1:The parametric equations of the line intersection of the given planes are $x = 3 + 14t, y = 2t, z = 15t$. Statement 2: The vector $14\hat{i} + 2\hat{j} + 15\hat{k}$ is parallel to the line of intersection of the given planes.

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176. The length of projection of the line segment joining the points $(1, 0, -1)$ and $(-1, 2, 2)$ on the plane $x + 3y - 5z = 6$ is equal to a. 2 b. $\sqrt{\frac{271}{53}}$ c. $\sqrt{\frac{472}{31}}$ d. $\sqrt{\frac{474}{35}}$

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177. If $P_1 : \vec{r} . \vec{n}_1 - d_1 = 0$ $P_2 : \vec{r} . \vec{n}_2 - d_2 = 0$ and $P_3 : \vec{r} . \vec{n}_3 - d_3 = 0$ are three planes and $\vec{n}_1, \vec{n}_2$ and $\vec{n}_3$ are three non-coplanar vectors, then three lines $P_1 = 0, P_2 = 0; P_2 = 0, P_3 = 0$; $P_3 = 0$ $P_1 = 0$ are

a. parallel lines

b. coplanar lines

c. coincident lines

d. concurrent lines

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178. Perpendiculars are drawn from points on the line $\frac{x+2}{2} = \frac{y+1}{-1} = \frac{z}{3}$ to the plane $x + y + z = 3$ The feet of perpendiculars lie on the line (a) $\frac{x}{5} = \frac{y-1}{8} = \frac{z-2}{-13}$ (b) $\frac{x}{2} = \frac{y-1}{3} = \frac{z-2}{-5}$ (c) $\frac{x}{4} = \frac{y-1}{3} = \frac{z-2}{-7}$ (d) $\frac{x}{2} = \frac{y-1}{-7} = \frac{z-2}{5}$

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179. The point P is the intersection of the straight line joining the points $Q(2, 3, 5)$ and $R(1, -1, 4)$ with the plane $5x - 4y - z = 1$. If S is the foot of the perpendicular drawn from the point $T(2, 1, 4)$ to QR, then the length of the line segment PS is (A) $\frac{1}{\sqrt{2}}$ (B) $\sqrt{2}$ (C) 2 (D) $2\sqrt{2}$

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180. A line l passing through the origin is perpendicular to the lines $l_1 : (3 + t)\hat{i} + (-1 + 2t)\hat{j} + (4 + 2t)\hat{k}, \infty < t < \infty, l_2 : (3 + s)\hat{i} + (3 + 2$ then the coordinates of the point on l_2 at a distance of $\sqrt{17}$ from the point of intersection of $l \& l_1$ is/are:

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181. Two lines $L_1 : x = 5, \frac{y}{3 - \alpha} = \frac{z}{-2}$ and $L_2 : x = \alpha, \frac{y}{-1} = \frac{z}{2 - \alpha}$ are coplanar. Then α can take value (s) a. 1 b. 2 c. 3 d. 4

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182. The projection of point $P\left(\vec{p}\right)$ on the plane $\vec{r}\dot{\vec{n}}=q$ is $\left(\vec{s}\right)$, then

a. $\vec{s}=\dfrac{\left(q-\vec{p}\dot{\vec{n}}\right)\vec{n}}{\left|\vec{n}\right|^2}$ b. $\vec{s}=p+\dfrac{\left(q-\vec{p}\dot{\vec{n}}\right)\vec{n}}{\left|\vec{n}\right|^2}$ c. $\vec{s}=p-\dfrac{\left(\vec{p}\dot{\vec{n}}\right)\vec{n}}{\left|\vec{n}\right|^2}$ d. $\vec{s}=p-\dfrac{\left(q-\vec{p}\dot{\vec{n}}\right)\vec{n}}{\left|\vec{n}\right|^2}$

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183. The angle between i and line of the intersection of the plane $\vec{r}.\left(\hat{i}+2\hat{j}+3\hat{k}\right)=0$ and $\vec{r}.\left(3\hat{i}+3\hat{j}+\hat{k}\right)=0$ is a. $\cos^{-1}\left(\frac{1}{3}\right)$ b. $\cos^{-1}\left(\frac{1}{\sqrt{3}}\right)$ c. $\cos^{-1}\left(\frac{2}{\sqrt{3}}\right)$ d. none of these

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184. From the point $P(a,b,c)$, let perpendiculars $PLandPM$ be drawn to $YOZandZOX$ planes, respectively. Then the equation of the plane

OLM is a. $\frac{x}{a}+\frac{y}{b}+\frac{z}{c}=0$ b. $\frac{x}{a}+\frac{y}{b}-\frac{z}{c}=0$ c. $\frac{x}{a}-\frac{y}{b}-\frac{z}{c}=0$ d. $\frac{x}{a}-\frac{y}{b}+\frac{z}{c}=0$

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185. The plane $\vec{r}\dot{\vec{n}}=q$ will contain the line $\vec{r}=\vec{a}+\lambda\vec{b}$, if a. $b.\,n\neq 0, a.\,n\neq q$ b. $b.\,n=, a.\,n\neq q$ c. $b.\,n=0, a.\,n=q$ d. $b.\,n\neq 0, a.\,n=q$

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186. Consider triangle AOB in the $x-y$ plane, where $A\equiv(1,0,0), B\equiv(0,2,0) and O\equiv(0,0,0)$. The new position of O, when triangle is rotated about side AB by 90^0 can be a. $\left(\frac{4}{5},\frac{3}{5},\frac{2}{\sqrt{5}}\right)$ b. $\left(\frac{-3}{5},\frac{\sqrt{2}}{5},\frac{2}{\sqrt{5}}\right)$ c. $\left(\frac{4}{5},\frac{2}{5},\frac{2}{\sqrt{5}}\right)$ d. $\left(\frac{4}{5},\frac{2}{5},\frac{1}{\sqrt{5}}\right)$

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187. Let $\vec{a} = \hat{i} + \hat{j}$ and $\vec{b} = 2\hat{i} - \hat{k}$, then the point of intersection of the lines $\vec{r} \times \vec{a} = \vec{b} \times \vec{a}$ and $\vec{r} \times \vec{b} = \vec{a} \times \vec{b}$ is a. $(3, -1, 1)$ b. $(3, 1, -1)$ c. $(-3, 1, 1)$ d. $(-3, -1, -1)$

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188. The line $\frac{x+6}{5} = \frac{y+10}{3} = \frac{z+14}{8}$ is the hypotenuse of an isosceles right-angled triangle whose opposite vertex is $(7, 2, 4)$. Then which of the following in not the side of the triangle?

a. $\frac{x-7}{2} = \frac{y-2}{-3} = \frac{z-4}{6}$

b. $\frac{x-7}{3} = \frac{y-2}{6} = \frac{z-4}{2}$

c. $\frac{x-7}{3} = \frac{y-2}{5} = \frac{z-4}{-1}$

d. none of these

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189. The equation of the plane which passes through the line of intersection of planes $\vec{r}.\vec{n}_1 = , q_1, \vec{r}.\vec{n}_2 = q_2$ and the is parallel to the line of intersection of planers $\overrightarrow{r}.\overrightarrow{n}_3 = q_3 and \overrightarrow{r}.\overrightarrow{n}_4 - q_4$ is

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190. The coordinates of the point P on the line $\overrightarrow{r} = \left(\hat{i} + \hat{j} + \hat{k}\right) + \lambda\left(-\hat{i} + \hat{j} - \hat{k}\right)$ which is nearest to the origin is a. $\left(\frac{2}{4}, \frac{4}{3}, \frac{2}{3}\right)$ b. $\left(-\frac{2}{3}, -\frac{4}{3}, \frac{2}{3}\right)$ c. $\left(\frac{2}{3}, -\frac{4}{3}, \frac{2}{3}\right)$ d. none of these

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191. The ratio in which the line segment joining the points whose position vectors are $2\hat{i} - 4\hat{j} - 7\hat{k} and - 3\hat{i} + 5\hat{j} - 8\hat{k}$ is divided by the plane whose equation is $\hat{r}\hat{i} - 2\dot{\hat{j}} + 3\hat{k} = 13$ is a. $13:12$ internally b. $12:25$ externally c. $13:25$ internally d. $37:25$ internally

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192. The number of planes that are equidistant from four non-coplanar points is

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193. In a three-dimensional coordinate system, P, Q , and $R$are images of a point $A(a, b, c)$ in the $x-y$, $y-z$ and $z-x$ planes, respectively. If G is the centroid of triangle PQR, then area of triangle AOG is (O is the origin) (A) 0 (B) $a^2+b^2+c^2$ (C) $\frac{2}{3}\left(a^2+b^2+c^2\right)$ (D) none of these

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194. A plane passing through $(1, 1, 1)$ cuts positive direction of coordinates axes at $A, BandC,$ then the volume of tetrahedron $OABC$ satisfies a. $V \leq \frac{9}{2}$ b. $V \geq \frac{9}{2}$ c. $V=\frac{9}{2}$ d. none of these

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195. If lines $x = y = zandx = \frac{y}{2} = \frac{z}{3}$ and third line passing through $(1, 1, 1)$ form a triangle of area $\sqrt{6}$ units, then the point of intersection of third line with the second line will be a. $(1, 2, 3)$ b. $2, 4, 6$ c. $\frac{4}{3}, \frac{6}{3}, \frac{12}{3}$ d. none of these

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196. The point of intersection of the line passing through $(0, 0, 1)$ and intersecting the lines $x + 2y + z = 1, \ -x + y - 2z = 2$ and $x + y = 2, x + z = 2$ with xy plane is a. $\left(\frac{5}{3}, \ -\frac{1}{3}, 0\right)$ b. $(1, 1, 0)$ c. $\left(\frac{2}{3}, \frac{1}{3}, 0\right)$ d. $\left(-\frac{5}{3}, \frac{1}{3}, 0\right)$

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197. Shortest distance between the lines $\frac{x-1}{1} = \frac{y-1}{1} = \frac{z-1}{1} and \frac{x-2}{1} = \frac{y-3}{1} = \frac{z-4}{1}$ is equal to a. $\sqrt{14}$ b. $\sqrt{7}$ c. $\sqrt{2}$ d. none of these

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198. Distance of point $P\left(\overrightarrow{p}\right)$ from the plane $\overrightarrow{r}\dot{\overrightarrow{n}}=0$ is a. $\left|\overrightarrow{p}\dot{\overrightarrow{n}}\right|$ b. $\frac{\left|\overrightarrow{p}\times\overrightarrow{n}\right|}{\left|\overrightarrow{n}\right|}$ c. $\frac{\left|\overrightarrow{p}\dot{\overrightarrow{n}}\right|}{\left|\overrightarrow{n}\right|}$ d. none of these

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199. The reflection of the point $\overrightarrow{a}$ in the plane $\overrightarrow{r}\dot{\overrightarrow{n}}=q$ is a. $\overrightarrow{a}+\frac{\left(\overrightarrow{q}-\overrightarrow{a}\dot{\overrightarrow{n}}\right)}{\left|\overrightarrow{n}\right|}$ b. $\overrightarrow{a}+2\left(\frac{\left(\overrightarrow{q}-\overrightarrow{a}\dot{\overrightarrow{n}}\right)}{\left|\overrightarrow{n}\right|}\right)\overrightarrow{n}$ c. $\overrightarrow{a}+\frac{2\left(\overrightarrow{q}+\overrightarrow{a}\dot{\overrightarrow{n}}\right)}{\left|\overrightarrow{n}\right|^2}\overrightarrow{n}$ d. none of these

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200. Line $\overrightarrow{r}=\overrightarrow{a}+\lambda\overrightarrow{b}$ will not meet the plane $\overrightarrow{r}\dot{\overrightarrow{n}}=q$, if a. $\overrightarrow{b}\dot{\overrightarrow{n}}=0, \overrightarrow{a}\dot{\overrightarrow{n}}=q$ b. $\overrightarrow{b}\dot{\overrightarrow{n}}\neq 0, \overrightarrow{a}\dot{\overrightarrow{n}}\neq q$ c. $\overrightarrow{b}\dot{\overrightarrow{n}}=0, \overrightarrow{a}\dot{\overrightarrow{n}}\neq q$ d.

$\vec{b}\dot{\vec{n}} \neq 0, \vec{a}\dot{\vec{n}} = q$

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201. If a line makes an angle of $\frac{\pi}{4}$ with the positive direction of each of x-axis and y-axis, then the angel that the line makes with the positive direction of the z-axis is a. $\frac{\pi}{3}$ b. $\frac{\pi}{4}$ c. $\frac{\pi}{2}$ d. $\frac{\pi}{6}$

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202. A parallelepiped S has base points $A, B, CandD$ and upper face points $A', B', C', andD'$. The parallelepiped is compressed by upper face $A'B'C'D'$ to form a new parallepiped T having upper face points $A'', B'', C''$and D'' . The volume of parallelepiped T is 90 percent of the volume of parallelepiped S. Prove that the locus of A is a plane.

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203. Find the equation of the plane containing the lines 2x-y+z-3=0,3x+y+z=5 and a t a distance of $\frac{1}{\sqrt{6}}$ from the point (2,1,-1).

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204. A plane which prependicular totwo planes $2x-2y+z=0$and $x-y+2z=4$ passes through the point $(1, -2, 1)$ is:

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205. Let $P(3, 2, 6)$ be a point in space and Q be a point on line $\overrightarrow{r}=\left(\hat{i}-\hat{j}+2\hat{k}\right)+\mu\left(-3\hat{i}+\hat{j}+5\hat{k}\right)$. Then the value of μ for which the vector $\overrightarrow{P}Q$ is parallel to the plane $x-4y+3z=1$ is a. 1/4 b. -1/4 c. 1/8 d. -1/8

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206. If the lines $\frac{x-1}{2}=\frac{y+1}{3}=\frac{z-1}{4}$ and $\frac{x-3}{1}=\frac{y-k}{2}=\frac{z}{1}$ intersect, then k is equal to (1) -1 (2) $\frac{2}{9}$ (3) $\frac{9}{2}$ (4) 0

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207. Consider a set of point R in which is at a distance of 2 units from the line $\frac{x}{1}=\frac{y-1}{-1}=\frac{z+2}{2}$ between the planes $x-y+2z=3=0$ and $x-y+2z-2=0$. (a) The volume of the bounded figure by points R and the planes is $\left(\frac{10}{3}\sqrt{3}\right)\pi$ cube units (b) The area of the curved surface formed by the set of points R is $\left(\frac{20}{\sqrt{6}}\right)\pi$ sq. units The volume of the bounded figure by the set of points R and the planes is $\left(\frac{20}{\sqrt{6}}\right)\pi$ cubic units. (d) The area of the curved surface formed by the set of points R is $\left(\frac{10}{\sqrt{3}}\right)\pi$ sq. units

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208. Let L be the line of intersection of the planes $2x + 3y + z = 1$ and $x + 3y + 2z = 2$. If L makes an angles α with the positive x-axis, then cos α equals

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209. Statement 1: A plane passes through the point $A(2, 1, -3)$. If distance of this plane from origin is maximum, then its equation is $2x + y - 3z = 14.$ Statement 2: If the plane passing through the point $A\left(\vec{a}\right)$ is at maximum distance from origin, then normal to the plane is vector $\vec{a}$.

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210. Consider the following linear equations: $ax + by + cz = 0$ $bx + cy + az = 0$ $cx + ay + bz = 0$ Match the expression/statements in column I with expression/statements in Column II. Column I, Column II $a + b + c \neq 0 and a^2 + b^2 + c^2 = ab + bc + ca$, p. the equations represent planes meeting only at a single point $a+b+c=0 and a^2+b^2+c^2 \neq ab+bc+ca$, q. the equations represent the line $x=y=z$ $a+b+c \neq 0 and a^2+b^2+c^2 \neq ab+bc+ca$, r. the equations represent identical planes $a+b+c \neq 0 and a^2+b^2+c^2 \neq ab+bc+ca$, s. the equations represent the whole of the three dimensional space

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211. If the distance between the plane $Ax-2y+z=d.$ and the plane containing the lies $\frac{x-1}{2}=\frac{y-2}{3}=\frac{z-3}{4}$ and $\frac{x-2}{3}=\frac{4-3}{4}=\frac{z-4}{5}$ is $\sqrt{6}$, then $|d|$ is

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212. Prove that the volume of tetrahedron bounded by the planes $\vec{r}\dot{}m\hat{j}+n\hat{k}=0, \vec{r}\dot{}n\hat{k}+l\hat{i}=0, \vec{r}\dot{}l\hat{i}+m\hat{j}=0, \vec{r}\dot{}l\hat{i}+m\hat{j}+n\hat{k}=\pi s\frac{2p}{3ln}$

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213. If a variable plane forms a tetrahedron of constant volume $64k^3$ with the co-ordinate planes, then the locus of the centroid of the tetrahedron is:

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214. $OA, OBandOC, withO$ as the origin, are three mutually perpendicular lines whose direction cosines are $l_r m_r andn_r(r=1, 2and3)\cdot$ If the projection of $OAandOB$ on the plane $z=0$ make angles $\varphi_1 and\varphi_2,$ respectively, with the x-axis, prove that $\tan(\varphi_1-\varphi_2)=\pm n_3/n_1n_2\cdot$

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215. Prove that for all values of λ and μ, the planes $\frac{2x}{a}+\frac{y}{b}+\frac{2z}{c}-1+\lambda\left(\frac{x}{a}-\frac{2y}{b}-\frac{z}{c}-2\right)=0$ and $\frac{4x}{a}-\frac{3y}{b}-5+\mu\left(\frac{5y}{b}+\frac{4z}{c}+3\right)=0$ intersect on the same line.

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216. If P is any point on the plane $lx+my+nz=pandQ$ is a point on the line OP such that $OP.\,OQ=p^2$, then find the locus of the point Q.

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217. find the equation of the plane with intercepts 2,3 and 4 on the x, y and z-axis respectively.

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218. A variable plane $lx + my + nz = p(where l, m, n$ are direction cosines of normal) intersects the coordinate axes at points $A, B and C$, respectively. Show that the foot of the normal on the plane from the origin is the orthocenter of triangle ABC and hence find the coordinate of the circumcentre of triangle ABC.

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219. P is a point and $PM and PN$ are the perpendicular form $P \rightarrow z - x and x - y$ planes. If OP makes angles $\theta, \alpha, \beta and \gamma$ with the plane OMN and the $x - y, y - z and z - x$ planes, respectively, then prove that $\cos ec^2\theta = \cos ec^2\alpha + \cos ec^2\beta + \cos ec^2\gamma$.

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220. Let a plane $ax + by + cz + 1 = 0, where a, b, c$ are parameters, make an angle 60^0 with the line $x = y = z, 45^0$ with the line $x = y - z = 0$ and θ with the plane $x = 0$. The distance of the plane from point $(2, 1, 1)$ is 3 units. Find the value of θ and the equation of the plane.

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221. Let $x - y\sin\alpha - z\sin\beta = 0, x\sin\alpha + z\sin\gamma - y = 0$ and $x\sin\beta + y\sin\gamma - z = 0$ be the equations of the planes such that $\alpha + \beta + \gamma = \pi/2$ (where α, β and $\gamma \neq 0$). Then show that there is a common line of intersection of the three given planes.

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222. The position vectors of the four angular points of a tetrahedron OABC are $(0, 0, 0)$; $(0, 0, 2)$, $(0, 4, 0)$ and $(6, 0, 0)$ respectively. A point P inside the tetrahedron is at the same distance r from the four plane faces of the tetrahedron. Find the value of r

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223. Find the distance of the point $(-2, 3, -4)$ from the line $\frac{x+2}{3} = \frac{2y+3}{4} = \frac{3z+4}{5}$ measured parallel to the plane $4x + 12y - 3z + 1 = 0$.

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224. The plane $4x + 7y + 4z + 81 = 0$ is rotated through a right angle about its line of intersection with the plane $5x + 3y + 10z = 25$. The equation of the plane in its new position is a. $x - 4y + 6z = 106$ b. $x - 8y + 13z = 103$ c. $x - 4y + 6z = 110$ d. $x - 8y + 13z = 105$

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225. If (a, b, c) is a point on the plane $3x + 2y + z = 7$, then find the least value of $2(a^2 + b^2 + c^2)$, using vector method.

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226. Let the equation of the plane containing the line $x - y - z - 4 = 0 = x + y + 2z - 4$ and is parallel to the line of intersection of the planes $2x + 3y + z = 1$ and $x + 3y + 2z = 2$ be $x + Ay + Bz + C = 0$ Compute the value of $|A + B + C|$.

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227. Let $a_1, a_2, a_3.........$ be in $A.P.$ and $h_1, h_2, h_3.....$,in $H.P.$ If $a_1 = 2 = h_1,$ and $a_{30} = 25 = h_{30}$ then $a_7 h_{24} + a_{14} + a_{17} =$

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228. If the angle between the plane $x - 3y + 2z = 1$ and the line $\frac{x-1}{2} = \frac{y-1}{1} = \frac{z-1}{-3} is, \theta$ then the find the value of $\cos ec\theta$.

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229. The length of projection of the line segment joining the points $(1, 0, -1) and (-1, 2, 2)$ on the plane $x + 3y - 5z = 6$ is equal to a. 2 b. $\sqrt{\frac{271}{53}}$ c. $\sqrt{\frac{472}{31}}$ d. $\sqrt{\frac{474}{35}}$

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230. Find the equation of a plane passing through (1, 1, 1) and parallel to the lines L_1 and L_2 direction ratios (1, 0,-1) and (1,-1, 0) respectively. Find the volume of the tetrahedron formed by origin and the points where this plane intersects the coordinate axes.

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231. Find the equation of the plane passing through the points $(2, 1, 0), (5, 0, 1)$ and $(4, 1, 1)$ If P is the point $(2, 1, 6)$ then find point Q such that PQ is perpendicular to the above plane and the mid point of PQ lies on it.

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232. For the line $\frac{x-1}{1}=\frac{y-2}{2}=\frac{z-3}{3}$, which one of the following is incorrect?

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233. The value of m for which straight lein $3x-2y+z+3=0=4x-3y+4z+1$ is parallel to the plane $2x-y+mz-2=0$ is a. -2 b. 8 c. -18 d. 11

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234. Let the equations of a line and plane be $\frac{x+3}{2}=\frac{y-4}{3}=\frac{z+5}{2} and 4x-2y-z=1,$ respectively, then a. the line is parallel to the plane b. the line is perpendicular to the plane c. the line lies in the plane d. none of these

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235. The length of the perpendicular form the origin to the plane passing through the point a and containing the line $\vec{r} = \vec{b} + \lambda\vec{c}$ is a. $\dfrac{\left[\vec{a}\,\vec{b}\,\vec{c}\right]}{\left|\vec{a}\times\vec{b}+\vec{b}\times\vec{c}+\vec{c}\times\vec{a}\right|}$ b. $\dfrac{\left[\vec{a}\,\vec{b}\,\vec{c}\right]}{\left|\vec{a}\times\vec{b}+\vec{b}\times\vec{c}\right|}$ c. $\dfrac{\left[\vec{a}\,\vec{b}\,\vec{c}\right]}{\left|\vec{b}\times\vec{c}+\vec{c}\times\vec{a}\right|}$ d. $\dfrac{\left[\vec{a}\,\vec{b}\,\vec{c}\right]}{\left|\vec{c}\times\vec{a}+\vec{a}\times\vec{b}\right|}$

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236. In a three-dimensional xyz space , the equation $x^2 - 5x + 6 = 0$ represents a. Points b. planes c. curves d. pair of straight lines

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237. The line $\dfrac{x-2}{3} = \dfrac{y+1}{2} = \dfrac{z-1}{-1}$ intersects the curve $xy = c^2, z = 0$ if c is equal to a. ± 1 b. $\pm\dfrac{1}{3}$ c. $\pm\sqrt{5}$ d. none of these

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238. A unit vector parallel to the intersection of the planes $\vec{r}.\left(\hat{i}-\hat{j}+\hat{k}\right)=5\,and\,\vec{r}.\left(2\hat{i}+\hat{j}-3\hat{k}\right)=4$ a. $\frac{2\hat{i}+5\hat{j}-3\hat{k}}{\sqrt{38}}$ b. $\frac{-2\hat{i}+5\hat{j}-3\hat{k}}{\sqrt{38}}$ c. $\frac{2\hat{i}+5\hat{j}-3\hat{k}}{\sqrt{38}}$ d. $\frac{-2\hat{i}-5\hat{j}-3\hat{k}}{\sqrt{38}}$

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239. Let L_1 be the line $\vec{r}_1=2\hat{i}+\hat{j}-\hat{k}+\lambda\left(\hat{i}+2\hat{k}\right)$ and let L_2 be the line $\vec{r}_2=3\hat{i}+\hat{j}+\mu\left(\hat{i}+\hat{j}-\hat{k}\right)$. Let π be the plane which contains the line L_1 and is parallel to L_2. The distance of the plane π from the origin is a. $\sqrt{6}$ b. $1/7$ c. $\sqrt{2/7}$ d. none of these

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240. The distance of point $A(-2,3,1)$ from the line PQ through $P(-3,5,2)$, which makes equal angles with the axes is a. $2/\sqrt{3}$ b.

$\sqrt{14/3}$ c. $16/\sqrt{3}$ d. $5/\sqrt{3}$

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241. The Cartesian equation of the plane $\overrightarrow{r} = (1 + \lambda - \mu)\hat{i} + (2 - \lambda)\hat{j} + (3 - 2\lambda + 2\mu)\hat{k}$ is a. $2x + y = 5$ b. $2x - y = 5$ c. $2x + z = 5$ d. $2x - z = 5$

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242. Find the angle between the lines $\overrightarrow{r} = 3\hat{i} + 2\hat{j} - 4\hat{k} + \lambda\left(\hat{i} + 2\hat{j} + 2\hat{k}\right) and \overrightarrow{r} = \left(5\hat{j} - 2\hat{k}\right) + \mu\left(3\hat{i} + 2\hat{j} +\right.$

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243. The distance between the line $\overrightarrow{r} = \left(2\hat{i} - 2\hat{j} + 3\hat{k}\right) + \lambda\left(\hat{i} - \hat{j} + 4\hat{k}\right)$ and plane $\overrightarrow{r} \cdot \hat{i} + 5\hat{j} + \hat{k} = 5.$

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244. Let L be the line of intersection of the planes $2x + 3y + z = 1$ and $x + 3y + 2z = 2$. If L makes an angles α with the positive x-axis, then cos α equals

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245. Statement 1: there exists a unique sphere which passes through the three non-collinear points and which has the least radius. Statement 2: The centre of such a sphere lies on the plane determined by the given three points.

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246. Statement 1: There exist two points on the $\frac{x-1}{1} = \frac{y}{-1} = \frac{z+2}{2}$ which are at a distance of 2 units from point $(1, 2, -4)\cdot$ Statement 2: Perpendicular distance of point $(1, 2, -4)$ form the line $\frac{x-1}{1} = \frac{y}{-1} = \frac{z+2}{2}$ is 1 unit.

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247. Statement 1: The shortest distance between the lines $\frac{x}{-3} = \frac{y-1}{1} = \frac{z+1}{-1} and \frac{x-2}{1} = \frac{y-3}{2} = \left(\frac{z+(13/7)}{-1}\right)$ is zero.

Statement 2: The given lines are perpendicular.

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248. Find the number of sphere of radius r touching the coordinate axes.

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249. Find the distance of the z-axis from the image of the point $M(2-3, 3)$ in the plane $x-2y-z+1=0$.

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250. A line with direction cosines proportional to $1, -5, and -2$ meets lines $x = y + 5 = z + 11 and x + 5 = 3y = 2z$. The coordinates of each of the points of the intersection are given by a. $(2, -3, 1)$ b. $(1, 2, 3)$ c. $(0, 5/3, 5/2)$ d. $(3, -2, 2)$

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251. If the planes $\vec{r}\hat{i} + \hat{j} + \hat{k} = q_1, \vec{r}\hat{i} + 2a\hat{j} + \hat{k} = q_2 and \vec{r} a\hat{i} + a^2\hat{j} + \hat{k} = q_3$ intersect in a line, then the value of a is a. 1 b. $1/2$ c. 2 d. 0

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252. The equation of a line passing through the point $\vec{a}$ parallel to the plane $\vec{r}.\vec{n} = q$ and perpendicular to the line $\vec{r} = \vec{b} + t\vec{c}$ is a. $\vec{r} = \vec{a} + \lambda(\vec{n} \times \vec{c})$ b. $(\vec{r} - \vec{a}) \times (\vec{n} \times \vec{c})$ c. $\vec{r} = \vec{b} + \lambda(\vec{n} \times \vec{c})$ d. none of these

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253. A straight line L on the xy-plane bisects the angle between $OXandOY\cdot$ What are the direction cosines of $L?$ a. $\langle(1/\sqrt{2}),(1/\sqrt{2}),0\rangle$ b. $\langle(1/2),(\sqrt{3}/2),0\rangle$ c. $\langle 0,0,1\rangle$ d. $\left\langle\begin{matrix}2/3\\2/3\\1/3\end{matrix}\right\rangle$

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254. Statement 1: Vector $\vec{c}=5\hat{i}+7\hat{j}+2\hat{k}$ is along the bisector of angel between $\vec{a}=\hat{i}+2\hat{j}+2\hat{k}and\vec{b}=-8\hat{i}+\hat{j}-4\hat{k}\cdot$ Statement 2: $\vec{c}$ is equally inclined to $\vec{a}\,and\,\vec{b}\cdot$ Which of the following statements is/are correct ?

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255. The equation of the line $x+y+z-1=0,\ 4x+y-2z+2=0$ written in the symmetrical form is

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256. The equation of two straight lines are $\frac{x-1}{2}=\frac{y+3}{1}=\frac{z-2}{-3} and \frac{x-2}{1}=\frac{y-1}{3}=\frac{z+3}{2}$. Statement 1: the given lines are coplanar. Statement 2: The equations $2r-s=1, r+3s=4 and 3r+2s=5$ are consistent.

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257. Statement 1: Lines $\vec{r}=\hat{i}+\hat{j}-\hat{k}+\lambda\left(3\hat{i}-\hat{j}\right) and \vec{r}=4\hat{i}-\hat{k}+\mu\left(2\hat{i}+\ +3\hat{k}\right)$ intersect. Statement 2: $\vec{b}\times\vec{d}=0$, then lines $\vec{r}=\vec{a}+\lambda\vec{b} and \vec{r}=\vec{c}+\lambda\vec{d}$ do not intersect.

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258. Statement 1: Line $\frac{x-1}{1}=\frac{y-0}{2}=\frac{z2}{-1}$ lies in the plane $2x-3y-4z-10=0$. Statement 2: if line $\vec{r}=\vec{a}+\lambda\vec{b}$ lies in the plane $\vec{r}\dot{\vec{c}} = n(where n$ is scalar$\Big)$, $then \vec{b}\dot{\vec{c}} = 0$.

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259. What is the equation of the plane which passes through the z-axis and is perpendicular to the line $\dfrac{x-a}{\cos\theta} = \dfrac{y+2}{\sin\theta} = \dfrac{z-3}{0}$? (A) $x + y\tan\theta = 0$ (B) $y + x\tan\theta = 0$ (C) $x\cos\theta - y\sin\theta = 0$ (D) $x\sin\theta - y\cos\theta = 0$

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260. Statement 1: let $A\left(\vec{i} + \vec{j} + \vec{k}\right) and B\left(\vec{i} - \vec{j} + \vec{k}\right)$ be two points. Then point $P\left(2\vec{i} + 3\vec{j} + \vec{k}\right)$ lies exterior to the sphere with AB as its diameter. Statement 2: If $A and B$ are any two points and P is a point in space such that $\vec{P}A\dot{\vec{P}}B > 0$, then point P lies exterior to the sphere with AB as its diameter.

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261. Statement 1: Let θ be the angle between the line $\frac{x-2}{2} = \frac{y-1}{-3} = \frac{z+2}{-2}$ and the plane $x+y-z=5$. Then $\theta = \sin^{-1}(1/\sqrt{51})$. Statement 2: The angle between a straight line and a plane is the complement of the angle between the line and the normal to the plane. Which of the following statements is/are correct ?

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262. If the volume of tetrahedron $ABCD$ is 1 cubic units, where $A(0, 1, 2), B(-1, 2, 1) and C(1, 2, 1)$, then the locus of point D is a. $x+y-z=3$ b. $y+z=6$ c. $y+z=0$ d. $y+z=-3$

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263. A rod of length 2 units whose one ends is $(1, 0, -1)$ and other end touches the plane $x-2y+2z+4=0$, then which statement is false

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264. The equation of the plane which is equally inclined to the lines $\frac{x-1}{2} = \frac{y}{-2} = \frac{z+2}{-1} and = \frac{x+3}{8} = \frac{y-4}{1} = \frac{z}{-4}$ and passing through the origin is/are a. $14x - 5y - 7z = 0$ b. $2x + 7y - z = 0$ c. $3x - 4y - z = 0$ d. $x + 2y - 5z = 0$

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265. Which of the following lines lie on the plane $x + 2y - z + 4 = 0$? a. $\frac{x-1}{1} = \frac{y}{-1} = \frac{z-5}{1}$ b. $x - y + z = 2x + y - z = 0$ c. $\hat{r} = 2\hat{i} - \hat{j} + 4\hat{k} + \lambda\left(3\hat{i} + \hat{j} + 5\hat{k}\right)$ d. none of these

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266. The equations of the plane which passes through $(0, 0, 0)$ and which is equally inclined to the planes $x - y + z - 3 = 0 and x + y = z + 4 = 0$ is/are a. $y = 0$ b. $x = 0$ c. $x + y = 0$ d. $x + z = 0$

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267. The x-y plane is rotated about its line of intersection with the y-z plane by 45^0 , then the equation of the new plane is/are a. $z + x = 0$ b. $z - y = 0$ c. $x + y + z = 0$ d. $z - x = 0$

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268. Consider the planes $3x - 6y + 2z + 5 = 0 and 4x - 12 + 3z = 3.$ The plane $67x - 162y + 47z + 44 = 0$ bisects the angel between the given planes which a. contains origin b. is acute c. is obtuse d. none of these

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269. A variable plane $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ at a unit distance from origin cuts the coordinate axes at A, B and C. Centroid (x, y, z) satisfies the equation $\frac{1}{x^2} + \frac{1}{y^2} + \frac{1}{z^2} = K$. The value of K is (A) 9 (B) 3 (C) $\frac{1}{9}$ (D) $\frac{1}{3}$

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270. Let $P=0$ be the equation of a plane passing through the line of intersection of the planes $2x-y=0 and 3z-y=0$ and perpendicular to the plane $4x+5y-3z=8$. Then the points which lie on the plane $P=0$ is/are a. $(0, 9, 17)$ b. $(1/7, 21/9)$ c. $(1, 3, -4)$ d. $(1/2, 1, 1/3)$

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271. The equation of the line $x+y+z-1=0, 4x+y-2z+2=0$ written in the symmetrical form is

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272. A point P moves on a plane $\frac{x}{a}+\frac{y}{b}+\frac{z}{c}=1.$ A plane through P and perpendicular to OP meets the coordinate axes at $A, B and C\cdot$ If the planes through $A, B and C$ parallel to the planes $x=0, y=0 and z=0,$ respectively, intersect at $Q,$ find the locus of $Q\cdot$

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273. If the planes $x - cy - bz = 0, cx = y + az = 0 and bx + ay - z = 0$ pass through a straight line, then find the value of $a^2 + b^2 + c^2 + 2ab \cdot$

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274. Find the equation of the plane through the points $(1, 0, -1), (3, 2, 2)$ and parallel to the line $\frac{x-1}{1} = \frac{y-1}{-2} = \frac{z-2}{3}$.

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275. A variable plane passes through a fixed point (α, β, γ) and meets the axes at $A, B, and C\cdot$ show that the locus of the point of intersection of the planes through $A, B and C$ parallel to the coordinate planes is $\alpha x^{-1} + \beta y^{-1} + \gamma z^{-1} = 1.$

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276. Show that the straight lines whose direction cosines are given by the equations $al + bm + cn = 0$ and $ul^2 + vm^2 + wn^2 = 0$ are parallel or perpendicular as $\frac{a^2}{u} + \frac{b^2}{v} + \frac{c^2}{w} = 0$ or $a^2(v+w) + b^2(w+u) + c^2(u+v) = 0$

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277. The perpendicular distance of a corner of uni cube from a diagonal not passing through it is

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278. If the direction cosines of a variable line in two adjacent points be l, M, n and $l + \delta l, m + \delta m + n + \delta n$ the small angle $\delta\theta$as between the two positions is given by

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279. the image of the point $(-1, 3, 4)$ in the plane $x-2y=0$ a. $\left(-\frac{17}{3}, \frac{19}{3}, 4\right)$ b.(15,11,4) c.$\left(-\frac{17}{3}, \frac{19}{3}, 1\right)$ d.$\left(\frac{9}{5}, -\frac{13}{5}, 4\right)$

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280. The ratio in which the plane $\vec{r}\cdot\left(\vec{i}-2\vec{j}+3\vec{k}\right)$=17 divides the line joining the points $-2\vec{i}+4\vec{j}+7\vec{k}$ and $3\vec{i}-5\vec{j}+8\vec{k}$ is a. $1:5$ b. $1:10$ c. $3:5$ d. $3:10$

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281. Let L be the line of intersection of the planes $2x+3y+z=1$ and $x+3y+2z=2$. If L makes an angles α with the positive x-axis, then cos α equals a.$\frac{1}{\sqrt{3}}$ b. $\frac{1}{2}$ c. 1 d.$\frac{1}{\sqrt{2}}$

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282. The distance between the line $\overrightarrow{r} = 2\hat{i} - 2\hat{j} + 3\hat{k} + \lambda\left(\hat{i} - \hat{j} + 4\hat{k}\right)$ and the plane $\overrightarrow{r}\,\hat{i} + 5\dot{\hat{j}} + \hat{k} = 5$ is a. $\frac{10}{3\sqrt{3}}$ b. $\frac{10}{9}$ c. $\frac{10}{3}$ d. $\frac{3}{10}$

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283. If angle θ bertween the line $\frac{x+1}{1} = \frac{y-1}{2} = \frac{z-2}{2}$ and the plane $2x - y + \sqrt{\lambda}z + 4 = 0$ is such that $\sin\theta = 1/3$, the value of λ is

a. $-\frac{3}{5}$

b. $\frac{5}{3}$

c. $-\frac{4}{3}$

d. $\frac{3}{4}$

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284. The length of the perpendicular drawn from $(1, 2, 3)$ to the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$ is a. 4 b. 5 c. 6 d. 7

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285. A plane makes intercepts $OA, OBandOC$ whose measurements are a, b and c on the $OX, OYandOZ$ axes. The area of triangle ABC is a. $\frac{1}{2}(ab+bc+ca)$ b. $\frac{1}{2}abc(a+b+c)$ c. $\frac{1}{2}\left(a^2b^2+b^2c^2+c^2a^2\right)^{1/2}$ d. $\frac{1}{2}(a+b+c)^2$

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286. The intersection of the spheres $x^2+y^2+z^2+7x-2y-z=13andx^2+y^2+z^2-3x+3y+4z=8$ is the same as the intersection of one of the spheres and the plane a. $x-y-z=1$ b. $x-2y-z=1$ c. $x-y-2z=1$ d. $2x-y-z=1$

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287. The shortest distance from the plane $12x+4y+3z=327$ to the sphere $x^2+y^2+z^2+4x-2y-6z=155$ is a. 39 b. 26 c. $41-\frac{4}{13}$ d. 13

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288. A line makes an angel θ with each of the x-and z-axes. If the angel β, which it makes with the y-axis, is such that $\sin^2\beta = 3\sin^2\theta$,then $\cos^2\theta$ equals a. $\frac{2}{3}$ b. $\frac{1}{5}$ c. $\frac{3}{5}$ d. $\frac{2}{5}$

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289. Find the equation of a straight line in the plane $\vec{r}\cdot\vec{n} = d$ which is parallel to $\vec{r} = \vec{a} + \lambda\vec{b}$ and passes through the foot of the perpendicular drawn from point $P\left(\vec{a}\right) \to \vec{r}\dot{\vec{n}} = d\left(where\vec{n}\dot{\vec{b}} = 0\right)$. a. $\vec{r} = \vec{a} + \left(\frac{d - \vec{a}\cdot\vec{n}}{n^2}\right)n + \lambda\vec{b}$ b. $\vec{r} = \vec{a} + \left(\frac{d - \vec{a}\cdot\vec{n}}{n}\right)n + \lambda\vec{b}$ c. $\vec{r} = \vec{a} + \left(\frac{\vec{a}\cdot\vec{n} - d}{n^2}\right)n + \lambda\vec{b}$ d. $\vec{r} = \vec{a} + \left(\frac{\vec{a}\cdot\vec{n} - d}{n}\right)n + \lambda\vec{b}$

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290. What is the nature of the intersection of the set of planes $x + ay + (b + c)z + d = 0, x + by + (c + a)z + d = 0 and x + cy + (a + b$

(a). they meet at a point (b). they form a triangular prism (c). they pass through a line (d). they are at equal distance from the origin

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291. Let P_1 denote the equation of a plane to which the vector $\left(\hat{i} + \hat{j}\right)$ is normal and which contais the line whose equation is $\overrightarrow{r} = \hat{i} + \hat{j} + \hat{k} + \lambda\left(\hat{i} - \hat{j} - \hat{k}\right) and P_2$ denote the equation of the plane containing the line L and a point with position vector $\hat{j}$. Which of the following holds good? a. The equation of P_1 is x+y=2. b. The equation of P_2 is $\overrightarrow{r}.(i - 2j + k) = 2$ c. The acute angle between P_1 and P_2 is $\cot^{-1}\sqrt{3}$ d. The angle between plane P_2 and the line L is $\tan^{-1}\sqrt{3}$

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292. Let PM be the perpendicular from the point $P(1, 2, 3)$ to the $x-y$ plane. If $\overrightarrow{O}P$ makes an angle θ with the positive direction of the $z-$ axis and$\overrightarrow{O}M$ makes an angle ϕ with the positive direction of $x-$ axis, $whereO$ is the origin and $\theta and \phi$ are acute angels, then a. $\cos\theta\cos\phi = 1/\sqrt{14}$ b. $\sin\theta\sin\phi = 2/\sqrt{14}$ c. $\tan\phi = 2$ d. $\tan\theta = \sqrt{5}/3$

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293. If the plane $\frac{x}{2} + \frac{y}{3} + \frac{z}{6} = 1$ cuts the axes of coordinates at points, $A, B, andC$, then find the area of the triangle ABC. a. $18sq$. unit b. $36sq$. unit c. $3\sqrt{14}sq$. unit d. $2\sqrt{14}sq$. unit

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294. For what value (s) of a will the two points $(1, a, 1)$ and $(-3, 0, a)$ lie on opposite sides of the plane $3x + 4y - 12z + 13 = 0$?

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