



MATHS

BOOKS - NCERT MATHS (ENGLISH)

ARITHMETIC PROGRESSIONS



1. In an AP, if d = -4, n = 7 and a_n = 4, then a is

equal to

A. 6

B. 7

C. 20

D. 28

Answer: D

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2. In an AP, if a=3.5, d=0 and n=101,

then a_n will be

A. 0

B. 3.5

 $C.\,103.5$

 $D.\,104.5$

Answer: B

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3. The list of number -10, -6, -2, 2, ... is

A. an AP with d = -16

B. an AP with d = 4

C. an AP with d = -4

D. not an AP

Answer: B

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4. The 11th term of an AP -5, $\frac{-5}{2}$, 0, $\frac{5}{2}$, ...

A. -20

C. -30

D. 30

Answer: B



5. The first four terms of an A.P. whose first term is -2 and the common difference is -2 are

A. -2, 0, 2, 4

B. -2, 4, -8, 16

$$C.-2, -4, -6, -8$$

 $\mathsf{D.}-2, -4, -8, -16$

Answer: C



6. The 21st term of an AP whose first two terms

are -3 and 4, is

A. 17

B. 137

C. 143

D. -143

Answer: B



7. If the 2nd term of an AP is 13 and 5th term is

25, what is its 7th term?

A. 30

B. 33

C. 37

D. 38

Answer: B



8. Which term of an AP: 21, 42, 63, 84, ... is 210?

A. 9th

B. 10th

C. 11th

D. 12th

Answer: B

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9. If the common difference of an AP is 5, then what is $a_{18} - a_{13}$?

A. 5

B.20

C. 25

D. 30

Answer: C

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10. What is the common difference of an AP in

which $a_{18} - a_{14} = 32$?

A. 8

B. -8

C. -4

D. 4

Answer: A

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11. Two APs have the same common difference. The first term of one of these is -1 and that of the other is -8. The difference between their 4th terms is B. -8

C. 7

D. -9

Answer: C

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12. If 7 times the 7th term of an AP is equal to 11 times its 11th term, then its 18th term will be

B. 11

C. 18

D. 0

Answer: D

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13. The 4th term from the end of an AP -11, -8,

-5, ..., 49 is

B.40

C. 43

D. 58

Answer: B

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14. The famous mathematician associated with finding the sum of the first 100 natural numbers is

A. Pythagoras

- **B.** Newton
- C. Gauss
- D. Euclid

Answer: C



15. If the first term of an AP is -5 and the common difference is 2, then the sum of the first 6 terms is

A. 0

B. 5

C. 6

D. 15

Answer: A

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16. The sum of first 16 terms of the AP 10, 6, 2, ...

A. -320

B. 320

C. -352

D. -400

Answer: A

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17. In an AP, if a=1, $a_n=20$ and $S_n=399$,

then n is equal to

A. 19

B. 21

C. 38

D. 42

Answer: C

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18. The sum of first five multiples of 3 is

B. 55

C. 65

D. 75

Answer: A

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Very Short Answer Type Questions

1. Which of the following form of an AP ? Justify Your answer.

(i) $-1, -1, -1, -1, \ldots$

(ii) $0, 2, 0, 2, \ldots$

(iii) $1, 1, 2, 2, 3, 3, \ldots$

(iv) $11, 22, 33, \ldots$

(v) $2,\,2^2,\,2^3,\,2^4$

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2. Justify whether it is true to say that
$$-1, \frac{-3}{2}, -2, \frac{5}{2}, \ldots$$
 Forms an AP as $a_2 - a_1 = a_3 - a_2.$

3. For the AP -3, -7, -11, ... can we find directly $a_{30} - a_{20}$ without actually finding a_{30} and a_{20} ? Give reason for your answer.

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4. Two A.P have the same common difference. The first term of one A.P is 2 and that of the other is 7. The difference between the 10th terms is the same as the difference between their 21st terms, which is the same as the difference between any corresponding terms.

Why?



6. The taxi fare after each km, when the fare is Rs. 15 for the first km and Rs 8 for each

additional km, does not form an AP as the total fare (in Rs.) after each km is 15, 8, 8, 8, Is the statement true? Give reasons.



7. In which of the following situations, do the lists of numbers involved form an AP? Give reasons for your answers.

(i) The fee charged from a student every month by a school for the whole session, when

the monthly fee is Rs. 400.

(ii) The fee charged every month by a school from classes I to XII, When the monthly fee for class I is Rs. 250 and it increases by Rs. 50 for the next higher class. (iii) The amount of money in the account of Varun at the end of every year when Rs. 1000 is deposited at simple interest of 10~% per annum.

(iv) The number of bacteria in a certain food item after each second, when they double in every second. **8.** Justify whether it is true to say that the following are the nth terms of an AP.

(i) 2n-3 (ii) $3n^2+5$ (iii) $1+n+n^2$

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Short Answer Type Questions

1. Match the AP's given in column A with suitable common differences given in column

Β.

Column A		Column B		
(A ₁)	2, -2, -6, -10,		(B ₁)	$\frac{2}{3}$
(A ₂)	$a = -18, n = 10, a_n = 0$	(B ₂)	-5	
(A ₃)	$a = 0, a_{10} = 6$	(B ₃)	4	
(A_4)	$a_2 = 13, a_4 = 3$	(B ₄)	-4	
		(B ₅)	2	
		$(B_6) \frac{1}{2}$		
		(B ₇)	5	

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2. Verify that each of the following is an AP and

then write its next three terms.

(i) $0, \frac{1}{4}, \frac{1}{2}, \frac{3}{4}, \dots$ (ii) $5, \frac{14}{3}, \frac{13}{3}, 4, \dots$ (iii) $\sqrt{3}, 2\sqrt{3}, 3\sqrt{3}, \dots$ (iv) $a + b, (a + 1) + b, (a + 1) + (b + 1), \dots$

(v) $a, 2a+1, 3a+2, 4a+3, \ldots$

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3. Write the first three terms of the AP's, when

a and d are as given below

(i)
$$a=rac{1}{2}, d=-rac{1}{6}$$

(ii)
$$a = -5, d = -3$$

4. Find a, b and c such that the following

numbers are in AP, a, 7, b, 23 and c.

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5. Determine the AP whose fifth term is 19 and the difference of the eighth term from the thirteenth term is 20.

6. The 26th, 11th and the last terms of an AP are, 0, 3 and $-\frac{1}{5}$, respectively. Find the

common difference and the number of terms.



7. The sum of the 5th and the 7th terms of an

AP is 52 and the 10th term is 46. Find the AP.



8. Find the 20th term of the AP whose 7th term is 24 less than the 11th term, first term being 12.



9. If the 9th term of an AP is zero, then prove

that its 29th term is twice its 19th term.



10. Find whether 55 is a term of the AP 7, 10, 13,

... or not. If yes, find which term it is.



are three consecutive terms of an AP.

12. Split 207 into three parts such that these are in A.P. and the product of the two smaller parts is 4623.



13. The angles of a triangle are in A.P. The greatest angle is twice the least. Find all the

angles



14. If the nth terms of the two AP's 9, 7, 5, ... and 24, 21, 18, ... are the same, then find the value of n. Also, that term.

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15. If sum of the 3rd and the 8th terms of an AP is 7 and the sum of the 7th and 14th terms

is -3, then find the 10th term.

16. Find the 12th term from the end of the AP

$$-2, -4, -6, \ldots, -100.$$



17. Which term of the AP 53, 48, 43, ... is the first

negative term?

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18. How many numbers lie between 10 and 300, which divided by 4 leave a remainder 3?



20. The first term of an AP is -5 and the last term is 45. If the sum of the terms of the AP is 120, then find the number of terms and the common difference.





21. Find the sum
(i)

$$1 + (-2) + (-5) + (-8) + \dots + (-236)$$

(ii)
 $\left(4 - \frac{1}{n}\right) + \left(4 - \frac{2}{n}\right) + \left(4 - \frac{3}{n}\right) + \dots$

upto n terms.

(iii) $\frac{a-b}{a+b} + \frac{3a-2b}{a+b} + \frac{5a-3b}{a+b} + \dots$ to 11

terms.

22. Which term of the AP -2, -7, -12, ... will be -77? Find the sum of this AP upto the term -77.



23. If $a_n = 3 - 4n$, then show that

 a_1, a_2, a_3, \ldots form an AP. Also, find S_{20} .

24. In an AP, If $S_n = n(4n+1)$, then find the

AP.



25. In an AP, If $S_n=3n^2+5n$ and $a_k=164,$

then find the value of k.



26. If S_n denotes the sum of first n terms of an

AP, then prove that $S_{12} = 3(S_8 - S_4)$.

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27. Find the sum of first 17 terms of an AP whose 4th and 9th terms are -15 and -30, respectively.

28. If sum of first 6 terms of an AP is 36 and that of the first 16 terms is 256 , then find the sum of first 10 terms.



29. Find the sum of all the 11 terms of an AP

whose middle most term is 30.



30. Find the sum of last ten terms of the AP 8,

10, 12, ..., 126.

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31. Find the sum of first seven numbers which

are multiples of 2 as well as of 9.



33. The sum of the first n terms of an AP whose first term is 8 and the common difference is 20 is equal to the sum of first 2n terms of another AP whose first term is -30 and the common difference is 8. Find n.



34. Kanika was given her pocket money on Jan 1st, 2008. She puts Rs. 1 on day 1, Rs. 2 on day 2, Rs. 3 on day 3 and continued doing so till the end of the month, from this money into her piggy bank she also spent Rs. 204 of her pocket money, and found that at the end of the month she still had Rs. 100 with her. How much was her pocket money for the month?



35. Yasmeen saves Rs. 32 during the first month, Rs. 36 in the second month and Rs. 40 in the third month. If she continues to save in this manner, in how many months will she save Rs. 2000?

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Long Answer Type Questions

1. The sum of the first five terms of an AP and the sum of the first seven terms of the same

AP is 167. If the sum first ten terms of this AP is

235, find the sum of its first twenty terms.



2. Find the

(i) sum of those integers between 1 and 500which are multiples of 2 as well as of 5.(ii) sum of those integers from 1 to 500 which

are multiples of 2 as well as of 5.

(iii) sum of those integers from 1 to 500 which

are multiples of 2 or 5.





3. The eighth term of an AP is half its second term and the eleventh term exceeds one-third of its fourth term by 1. Find the 15th term.

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4. An AP consists of 37 terms. The sum of the three middle most terms is 225 and the sum of the last three terms is 429. Find the AP.

5. Find the sum of the integers between 100

and 200 that are

(i) divisible by 9.

(ii) not divisible by 9.

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6. The ratio of the 11th term to the 18th term of an AP is 2:3. Find the ratio of the 5th term to the 21st term and also the ratio of the sum

of the first five terms to the sum of the first 21

terms.





9. Jaspal Singh repays his total loan of Rs. 118000 by paying every month starting with the first installment of Rs. 1000. If he increases the installment by Rs. 100 every month, what amount will be paid by him in the 30th installment? What amount of loan does

he still have to pay after the 30th installment?



10. The students of a school decided to beautify the school on the annual day by fixing colourful flags on the straight passage of the school. They have 27 flags to be fixed at intervals of every 2 m. The flags are stored at the position of the middle most flag. Ruchi was given the responsibility of placing the flags.

Ruchi kept her books where the flags were stored. She could carry only one flag at a time. How much distance she did cover in completing this job and returning back to collect her books ? What is the maximum distance she travelled carrying a flag ?