



MATHS

BOOKS - DEEPTI MATHS (TELUGU ENGLISH)

DE MOIVRE'S THEOREM

SOLVED EXAMPLES

1. If A, B, C are angles of a triangle such that $x = cisA, y = cisB, z = cisC$, then find the value of xyz .

A. -1

B. 0

C. 1

D. 2



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2. The equation whose roots are the n th powers of the roots of the equation $x^2 - 2x \cos \theta + 1 = 0$ is

A. $x^2 - 2x \cos n\theta + 1 = 0$

B. $x^2 + 2x \cos n\theta + 1 = 0$

C. $x^2 - 2x \cos n\theta - 1 = 0$

D. $x^2 + 2x \cos n\theta - 1 = 0$



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3. $[\sqrt{2}(\cos 56^\circ 15' + i \sin 56^\circ 15')]^8$

A. 1

B. i

C. 16

D. $16i$



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4. The value of

$$1 + \sum_{k=0}^{14} \left\{ (\cos) \frac{(2k+1)\pi}{15} + (i \sin) \frac{(2k+1)\pi}{15} \right\} \text{ is}$$

A. 0

B. -1

C. 1

D. i



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5. If ω is a complex cube root of unity, then $\sin \left[(\omega^{10} + \omega^{23})\pi - \frac{\pi}{4} \right]$

A. $1/\sqrt{2}$

B. $\frac{1}{2}$

C. 1

D. $\sqrt{3}/2$



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6. If $(\omega \neq 1)$ is a cube root of unity, then

$$\{(1, 1 + i + \omega^2), (\omega^2, 1 - i), (\omega, -1 + \omega - i, -1)\}$$

A. -1

B. -2

C. 0

D. 2



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7. The number of real roots of the equation $z^3 + iz - 1 = 0$ is

A. 0

B. 1

C. 2

D. 3



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8. If $x^2 - 2x \cos \theta + 1 = 0$, then $x^{2n} - 2x^n \cos n\theta + 1$

A. -1

B. 0

C. 1

D. 2



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9. If $z = \sqrt{\frac{1-i}{1+i}}$ then $\text{Arg } z =$

A. $\frac{\pi}{4}$

B. $\frac{\pi}{2}$

C. $\frac{3\pi}{2}$

D. $\frac{3\pi}{4}$



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10. If the roots of $(z - 1)^n = i(z + 1)^n$ are plotted on the argand plane, they are

A. on $x=0$

B. Concyctic

C. on a parabola

D. on $y=0$



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EXERCISE 1

1. $(\cos 3\alpha + i \sin 3\alpha)^5 (\cos 4\alpha - i \sin 4\alpha)^6$

A. $\cos 9\alpha - i \sin 9\alpha$

B. $\cos 9\alpha + i \sin 9\alpha$

C. $\cos 8\alpha - i \sin 8\alpha$

D. $\cos 8\alpha + i \sin 8\alpha$



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$$2. \frac{(\cos \theta + i \sin \theta)^5 (\cos 3\theta - i \sin 3\theta)^6}{(\cos 2\theta + i \sin 2\theta)^3 (\cos 4\theta - i \sin 4\theta)^5}$$

A. 1

B. $\text{cis} \theta$

C. i

D. -1



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$$3. \frac{(\cos 2\theta + i \sin 2\theta)^3 (\cos 3\theta - i \sin 3\theta)^4}{(\cos 3\theta + i \sin 3\theta)^2 (\cos 4\theta + i \sin 4\theta)^{-3}}$$

A. 1

B. $\text{cis} \theta$

C. i

D. -1



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4.
$$\frac{(\cos \alpha + i \sin \alpha)^5}{(\sin \beta + i \cos \beta)^3} =$$

A. $\sin(5\alpha + 3\beta) + i \cos(5\alpha + 3\beta)$

B. $-\sin(5\alpha + 3\beta) + i \cos(5\alpha + 3\beta)$

C. $\sin(3\alpha + 5\beta) + i \cos(3\alpha + 5\beta)$

D. $-\sin(3\alpha + 5\beta) + i \cos(3\alpha + 5\beta)$

Answer: B



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5.
$$\frac{1 - \cos \theta + i \sin \theta}{1 + \cos \theta - i \sin \theta}$$

A. $i \tan \frac{\theta}{2}$

B. $-i \tan \frac{\theta}{2}$

C. $\tan \frac{\theta}{2}$

D. $-\tan \frac{\theta}{2}$



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6. $\left(\frac{1 + \cos \theta + i \sin \theta}{1 + \cos \theta - i \sin \theta} \right)^n$

A. $cis n\theta$

B. $-cis n\theta$

C. $cis \theta$

D. $-cis \theta$



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7. $(\sin x + i \cos x)^n$

A. $\text{cisn}\left(\frac{\pi}{2} + x\right)$

B. $\text{cisn}\left(\frac{\pi}{2} - x\right)$

C. $\text{cisn}\left(\frac{\pi}{3} + x\right)$

D. $\text{cisn}\left(\frac{\pi}{3} - x\right)$



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8. $(1 + \sin \theta + i \cos \theta)^n$

A. $2^n \cdot \cos^n \left[\frac{\pi}{3} - \frac{\theta}{2} \right] \cdot \text{cis} \left[n \frac{\pi}{3} - \frac{\theta}{2} \right]$

B. $2^n \cdot \cos^n \left[\frac{\pi}{4} - \frac{\theta}{2} \right] \cdot \text{cis} \left[n \frac{\pi}{4} - \frac{\theta}{2} \right]$

C. $2^n \cdot \cos^n \left[\frac{\pi}{5} - \frac{\theta}{2} \right] \cdot \text{cis} \left[n \left(\frac{\pi}{5} - \frac{\theta}{2} \right) \right]$

D. none

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9. $(1 + \cos \theta - i \sin \theta)^n$

A. $2^n \cos^n \left(\frac{\theta}{2} \right) cis \frac{n\theta}{2}$

B. $2^n \cos^n \left(\frac{\theta}{2} \right) cis \left(-\frac{n\theta}{2} \right)$

C. $2^n \sin^n \left(\frac{\theta}{2} \right) cis \frac{n\theta}{2}$

D. $2^n \sin^n \left(\frac{\theta}{2} \right) - cis \frac{n\theta}{9}$

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10. $(1 - \cos \theta + i \sin \theta)^6$

A. $2^6 \sin^6 \frac{\theta}{2} (\cos 3\theta + i \sin 3\theta)$

B. $2^6 \sin^6 \frac{\theta}{2} (-\cos 3\theta + i \sin 3\theta)$

C. $2^6 \sin^6 \frac{\theta}{2} (\cot 3\theta + i \sin 3\theta)$

D. $2^6 \sin^6 \frac{\theta}{2} (-\cot 3\theta + i \sin 3\theta)$

Answer: B

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11. $(1 + i)^4$

A. 4

B. -4

C. 0

D. i

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12. $(1 + i\sqrt{3})^9 =$

A. -2^6

B. -2^8

C. -2^9

D. -2^{12}

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13. $(1 - i)^5$

A. $2^{5/2} \sin\left(\frac{-5\pi}{4}\right)$

B. $2^{5/2} \operatorname{cis}\left(\frac{-5\pi}{4}\right)$

C. $2^{5/2} \cot\left(\frac{-5\pi}{4}\right)$

D. $2^{5/2} \tan\left(\frac{-5\pi}{4}\right)$

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14. $\frac{\cos 75^\circ + i\sin 75^\circ}{\cos 30^\circ + i\sin 30^\circ}$

A. $\frac{1}{\sqrt{2}}(1 + i)$

B. $\frac{1}{\sqrt{2}}(1 - i)$

C. $\frac{1}{\sqrt{3}}(1 + i)$

D. $\frac{1}{\sqrt{3}}(1 - i)$



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15. $\left(\frac{1}{2} + \frac{\sqrt{3}}{2}i\right)^6$

A. 0

B. 1

C. -1

D. 2



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16. If $\left(\frac{1 + \cos \theta + i \sin \theta}{\sin \theta + i + i \cos \theta} \right)^4 = \cos n\theta + i \sin n\theta$ then $n =$

A. 4

B. 8

C. 6

D. 2



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17. $\left(\frac{1 + \cos \frac{\pi}{8} - i \sin \frac{\pi}{8}}{1 + \cos \frac{\pi}{8} + i \sin \frac{\pi}{8}} \right)^8$

A. 1

B. -1

C. 2

D. $1/2$



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18. $\left[\frac{1 + \sin(\pi/8) + i \cos(\pi/8)}{1 + \sin(\pi/8) - i \cos \pi/8} \right]^{-8/3}$

A. $1 + i$

B. $1-i$

C. 1

D. -1



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19. $\left(\frac{\sin \pi/8 + i \cos \pi/8}{\sin \pi/8 - i \cos \pi/8} \right)^8$

A. -1

B. 0

C. 1

D. 2i



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20. $\left(\frac{1 + \sin \theta + i \cos \theta}{1 + \sin \theta - i \cos \theta} \right)^n$

A. $\cos\left(\frac{n\pi}{2} - n\theta\right) + i \sin\left(\frac{n\pi}{2} - n\theta\right)$

B. $\cos\left(\frac{n\pi}{2} - n\theta\right) + i \sin\left(\frac{n\pi}{2} + n\theta\right)$

C. $\cos\left(\frac{n\pi}{2} + n\theta\right) + i \sin\left(\frac{n\pi}{2} - n\theta\right)$

D. none



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21. If n is a positive integer, show that

$$(1 + i)^n + (1 - i)^n = 2^{\frac{n+2}{2}} \cos\left(\frac{n\pi}{4}\right).$$

A. $2^{(n/2) + 1} \cdot \cos \frac{n\pi}{3}$

B. $2^{(n/2) + 1} \cdot \cos \frac{n\pi}{4}$

C. $2^{(n/2) + 1} \cdot \cos \frac{n\pi}{5}$

D. $2^{(n/2) + 1} \cdot \cos \frac{n\pi}{5}$



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22. $(1 + i)^5 + (1 - i)^5$

A. -8

B. 81

C. 8

D. 32



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23. $(\sqrt{3} + i)^7 + (\sqrt{3} - i)^7$

A. $128\sqrt{3}$

B. $256\sqrt{3}$

C. $-128\sqrt{3}$

D. $-256\sqrt{3}$



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24. If n is a positive integer and $(1 + i)^{2n} + (1 - i)^{2n} = k \cos(n\pi/2)$

then the value of k is

A. 2^n

B. 2^{n-1}

C. 2^{n+1}

D. none

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25. If n is a positive integer, then $(\sqrt{3} + i)^n + (\sqrt{3} - i)^n$

A. $2^{(n+1)} \cos\left(\frac{n\pi}{2}\right)$

B. $2^{(n+1)} \cos\left(\frac{n\pi}{3}\right)$

C. $2^{(n+1)} \cos\left(\frac{n\pi}{5}\right)$

D. $2^{(n+1)} \cos\left(\frac{n\pi}{6}\right)$

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26. If n is a positive integer and $(1 + i\sqrt{3})^n + (1 - i\sqrt{3})^n = 2^{n+1} \cos \theta$, then the value of θ is

A. $n\pi/3$

B. $n\pi/2$

C. $n\pi/4$

D. none



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27. If n is an integer which leaves remainder one when divided by three, then $(1 + \sqrt{3}i)^n + (1 - \sqrt{3}i)^n$

A. -2^{n+1}

B. 2^{n+1}

C. $-(-2)^n$

D. -2^n



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28. $\left(\frac{-1 + i\sqrt{3}}{2}\right)^{3n} + \left(\frac{-1 - i\sqrt{3}}{2}\right)^{3n}$

A. 0

B. 1

C. 2

D. 3



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29. $(1 + \cos \theta + i \sin \theta)^n + (1 + \cos \theta - i \sin \theta)^n$

A. $2^{n+1} \cos^n(\theta/2) \cdot \cos(n\theta/2)$

B. $2^n \cdot \cos^n(\theta/2) \cdot \sin(n\theta/2)$

C. $2^{n+1} \sin^n(\theta/2) \cdot \cos(n\theta/2)$

D. none

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30. $(\cos \theta + i \sin \theta)^{10} + (\cos \theta - i \sin \theta)^{10}$

A. $\cos 10\theta$

B. $i \sin 10\theta$

C. $2 \cos 10\theta$

D. $2i \sin 10\theta$

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31. If n is a positive integer, then $(a + ib)^{m/n} + (a - ib)^{m/n}$

A. $2(a^2 + b^2)^{m/2n} \cos \left[\frac{m}{n} \tan^{-1} \frac{b}{a} \right]$

B. $2(a^2 + b^2)^{m/2n} \sin \left[\frac{m}{n} \tan^{-1} \frac{b}{a} \right]$

C. $2(a^2 + b^2)^{m/2n} \cot \left[\frac{m}{n} \tan^{-1} \frac{b}{a} \right]$

D. none



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32.

$$[(\cos \alpha - \cos \beta) + i(\sin \alpha - \sin \beta)]^n + [(\cos \alpha - \cos \beta) - i(\sin \alpha - \sin \beta)]^n$$

A. $2^{n+1} \cdot \sin^n \left(\frac{\alpha - \beta}{2} \right) \cos \left[n \left(\frac{\pi}{2} + \frac{\alpha + \beta}{2} \right) \right]$

B. $2^{n-1} \cdot \sin^n \left(\frac{\alpha - \beta}{2} \right) \cos \left[n \left(\frac{\pi}{2} + \frac{\alpha + \beta}{2} \right) \right]$

C. $2^{n+1} \cdot \sin^n \left(\frac{\alpha + \beta}{2} \right) \cos \left[n \left(\frac{\pi}{2} + \frac{\alpha - \beta}{2} \right) \right]$

D. $2^{n-1} \cdot \sin^n \left(\frac{\alpha + \beta}{2} \right) \cos \left[n \left(\frac{\pi}{2} + \frac{\alpha - \beta}{2} \right) \right]$



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33. If $(\sqrt{3} + i)^{100} = 2^{99}(a + ib)$ then $b =$

A. 1

B. $\sqrt{3}$

C. $\sqrt{2}$

D. 2



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34. A value of n such that $\left(\frac{\sqrt{3}}{2} + \frac{i}{2}\right)^n = 1$ is

A. 12

B. 3

C. 2

D. 1

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35. If n is a multiple of 3, then $\left(\frac{-1 + i\sqrt{3}}{2}\right)^n + \left(\frac{-1 - i\sqrt{3}}{2}\right)^n$

A. 1

B. 2

C. 3

D. 4

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36. $4 + 5\left(-\frac{1}{2} + \frac{i\sqrt{3}}{2}\right)^{334} + 3\left(-\frac{1}{2} + \frac{i\sqrt{3}}{2}\right)^{365}$

A. $1 - i\sqrt{3}$

B. $-1 + i\sqrt{3}$

C. $i\sqrt{3}$

D. $-i\sqrt{3}$

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37. $\left(\frac{-1 + i\sqrt{3}}{2}\right)^6 + \left(\frac{-1 - i\sqrt{3}}{2}\right)^6$

A. 2

B. -2

C. 1

D. 0

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38. If n is an integer and $z = -1 + i\sqrt{3}$, then $z^{2n} + 2^n \cdot z^n + 2^{2n}$

A. 0

B. 2

C. 3

D. 4



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39. If $\theta = \pi/6$ then the 10th term of the series

$1 + (\cos \theta + i \sin \theta) + (\cos \theta + i \sin \theta)^2 + \dots$ is

A. i

B. -1

C. 1

D. $-i$



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40. If $x = cis\theta$, then find the value of $\left[x^6 + \frac{1}{x^6} \right]$.

A. $2 \cos 6\theta$

B. $2 \sin 6\theta$

C. $-2 \cos 6\theta$

D. $-2 \sin 6\theta$



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41. If $x + \frac{1}{x} = 2 \cos \theta$ then $x^{10} + \frac{1}{x^{10}}$

A. $2^{10} \cos 10\theta$

B. $2 \cos 10\theta$

C. $2^{10} \cos^{10} \theta$

D. $2 \cos^{10} \theta$

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42. If $z^2 + z + 1 = 0$ where z is a complex number, then the value of

$$\left(z + \frac{1}{z}\right)^2 + \left(z^2 + \frac{1}{z^2}\right)^2 + \left(z^3 + \frac{1}{z^2}\right)^2 + \dots + \left(z^6 + \frac{1}{z^6}\right)^2$$

A. 6

B. 12

C. 18

D. 54

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43. If $z = \cos \theta + i \sin \theta$, then $\frac{z^{2n} - 1}{z^{2n} + 1}$

- A. $\cos n\theta$
- B. $\sin n\theta$
- C. $-i \sin \theta$
- D. $i \tan n\theta$



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44. If $x = \cos \alpha + i \sin \alpha$, $y = \cos \beta + i \sin \beta$, then $\frac{x}{y} + \frac{y}{x}$

- A. $2 \sin(\alpha + \beta)$
- B. $2 \sin(\alpha - \beta)$
- C. $2 \cos(\alpha + \beta)$
- D. $2 \cos(\alpha - \beta)$



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45. If $x = \cos \alpha + i \sin \alpha$, $y = \cos \beta + i \sin \beta$, then $\frac{x}{y} - \frac{y}{x}$

A. $2i \sin(\alpha + \beta)$

B. $2i \sin(\alpha - \beta)$

C. $2i \cos(\alpha + \beta)$

D. $2i \cos(\alpha - \beta)$



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46. If $x = \cos \alpha + i \sin \alpha$, $y = \cos \beta + i \sin \beta$, then $\frac{x - y}{x + y}$

A. $i \cdot \cos\left(\frac{\alpha - \beta}{2}\right)$

B. $i \cdot \sin\left(\frac{\alpha - \beta}{2}\right)$

C. $i \cdot \cot\left(\frac{\alpha - \beta}{2}\right)$

D. $i \cdot \tan\left(\frac{\alpha - \beta}{2}\right)$



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47. If $x = \cos \alpha + i \sin \alpha$, $y = \cos \beta + i \sin \beta$, then $x^m \cdot y^n + \frac{1}{x^m \cdot y^n}$

A. $2 \cos(m\alpha + n\beta)$

B. $2 \cos(m\alpha - n\beta)$

C. $2 \sin(m\alpha + n\beta)$

D. $2 \sin(m\alpha - n\beta)$



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48. If $p = \cos 2\alpha + i \sin 2\alpha$, $q = \cos 2\beta + i \sin 2\beta$ then $\sqrt{p/q} - \sqrt{q/p}$

A. $2i \sin(\alpha - \beta)$

B. $2 \sin(\alpha - \beta)$

C. $2i \cos(\alpha - \beta)$

D. $2 \cos(\alpha - \beta)$

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49. If $x + \frac{1}{x} = 2 \cos \alpha$, $y + \frac{1}{y} = 2 \cos \beta$, then $xy + \frac{1}{xy} =$

A. $\cos(\alpha \pm \beta)$

B. $2 \cos(\alpha \pm \beta)$

C. $2i \sin(\alpha \pm \beta)$

D. $\sin(\alpha \pm \beta)$

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50. If α and β are the roots of the equation $x^2 - x + 1 = 0$ then $\alpha^{2009} + \beta^{2009}$

A. -2

B. -1

C. 1

D. 2



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51. If α and β are the roots of $x^2 - 2x + 4 = 0$ then $\alpha^n + \beta^n$

A. $2^n \cos(n\pi/2)$

B. $2^{n+1} \cos(n\pi/3)$

C. $2^{n-1} \sin(n\pi/3)$

D. none



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52. If α and β are the roots of $x^2 - 2x + 4 = 0$ then $\alpha^n - \beta^n$

A. $2^{n+1} \cdot i \cos(n\pi/3)$

B. $2^{n+1} \cdot i \sin(n\pi/3)$

C. $2^{n-1} \cdot i \cos(n\pi/3)$

D. $2^{n-1} \cdot i \sin(n\pi/3)$



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53. If α, β are roots of the equation $x^2 - 4x + 8 = 0$ then for any

$n \in N, \alpha^{2n} + \beta^{2n}$

A. $2^{2n+1} \cos \frac{n\pi}{2}$

B. $2^{3n} \cos \frac{n\pi}{2}$

C. $2^{3n+1} \cos \frac{n\pi}{2}$

D. $2^{3n} \cos \frac{n\pi}{4}$



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54. If α and β are the roots of $x^2 - 2x + 4 = 0$, then the value of $\alpha^6 + \beta^6$ is :

A. 32

B. 64

C. 128

D. 256



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55. If x satisfies the equation $x^2 - 2x \cos \theta + 1 = 0$, then the value of $x^n + 1/x^n$ is

A. $2^n \cos n\theta$

B. $2^n \cos^n \theta$

C. $2 \cos n\theta$

D. $2 \cos^n \theta$



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56. If $a = \cos 4\pi/3 + i \sin 4\pi/3$ then $(1 + a)^{3n}$

A. -1

B. 0

C. 1

D. $(-1)^n$



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57. If $\cos \alpha + \cos \beta = 0 = \sin \alpha + \sin \beta$ then $\cos 2\alpha + \cos 2\beta$

A. $-2 \sin(\alpha + \beta)$

B. $-2 \cos(\alpha + \beta)$

C. $2 \sin(\alpha + \beta)$

D. $2 \cos(\alpha + \beta)$



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58.

If

$\cos \alpha + \cos \beta + \cos \gamma = 0 = \sin \alpha + \sin \beta + \sin \gamma$ then $\cos 3\alpha + \cos 3\beta +$

A. $\cos(\alpha + \beta + \gamma)$

B. $2 \cos(\alpha + \beta + \gamma)$

C. $3 \cos(\alpha + \beta + \gamma)$

D. none

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59.

If

$\cos \alpha + \cos \beta + \cos \gamma = 0 = \sin \alpha + \sin \beta + \sin \gamma$ then $\sin 3\alpha + \sin 3\beta + \sin 3\gamma =$

A. $3 \sin(\alpha + \beta + \gamma)$

B. $2 \sin(\alpha + \beta + \gamma)$

C. $\sin(\alpha + \beta + \gamma)$

D. none

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60. If $\cos \alpha + \cos \beta + \cos \gamma = 0 = \sin \alpha + \sin \beta + \sin \gamma$ then
 $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma =$

A. 2

B. 1

C. $1/2$

D. 0



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61. If $\cos \alpha + \cos \beta + \cos \gamma = 0 = \sin \alpha + \sin \beta + \sin \gamma$ then
 $\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma =$

A. 0

B. $1/2$

C. $3/2$

D. 2



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62. If $\cos \alpha + \cos \beta + \cos \gamma = 0 = \sin \alpha + \sin \beta + \sin \gamma$ then
 $\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma =$

A. 0

B. $1/2$

C. $3/2$

D. 2



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63. If $\cos \alpha + \cos \beta + \cos \gamma = 0 = \sin \alpha + \sin \beta + \sin \gamma$ then
 $\cos(2\alpha - \beta - \gamma) + \cos(2\beta - \gamma - \alpha) + \cos(2\gamma - \alpha - \beta) =$

A. 0

B. 1

C. 2

D. 3



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64. If $\cos \alpha + \cos \beta + \cos \gamma = 0 = \sin \alpha + \sin \beta + \sin \gamma$ then

$$\sin(2\alpha - \beta - \gamma) + \sin(2\beta - \gamma - \alpha) + \sin(2\gamma - \alpha - \beta) =$$

A. 0

B. 1

C. 2

D. 3



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65. If $\cos \alpha + \cos \beta + \cos \gamma = 0 = \sin \alpha + \sin \beta + \sin \gamma$ then

$$\cos(\alpha + \beta) + \cos(\beta + \gamma) + \cos(\gamma + \alpha) =$$

A. 0

B. 1

C. $\cos 2(\alpha + \beta + \gamma)$

D. $3 \cos(\alpha + \beta + \gamma)$



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66. If $a = cis \alpha$, $b = cis \beta$, $c = cis \gamma$, and $\frac{a}{b} + \frac{b}{c} + \frac{c}{a} - 1 = 0$ then

$$\cos(\alpha - \beta) + \cos(\beta - \gamma) + \cos(\gamma - \alpha) =$$

A. 0

B. 1

C. -1

D. 2



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67. Let A and B denote the statements

$$A: \cos \alpha + \cos \beta + \cos \gamma = 0 \quad B: \sin \alpha + \sin \beta + \sin \gamma = 0$$

If $\cos(\beta - \gamma) + \cos(\gamma - \alpha) + \cos(\alpha + \beta) = -\frac{3}{2}$, then :

- A. A is false and B is true
- B. both A and B are true
- C. both A and B are false
- D. A is true and B is false



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68. The value of $(i)^i$ is

A. ω

B. $-\omega^2$

C. $\pi/3$

D. none



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69. $\log(\log i)$

A. $\log \pi / 2$

B. $i\pi / 2$

C. $i\pi / 2 + \log \pi / 2$

D. none



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70. $\sqrt{i} + \sqrt{-i} =$

A. $i\sqrt{2}$

B. $1 / (i\sqrt{2})$

C. 0

D. $-\sqrt{1}$



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71. One value of $(1 + i)^{1/2}$ is $2^{1/4}e^{i\pi/8}$. The other value is

A. $\sqrt{2}e^{-i\pi/8}$

B. $\sqrt{2}e^{i5\pi/8}$

C. $\sqrt{2}e^{i5\pi/8}$

D. $\sqrt{2}e^{i9\pi/8}$





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72. The modulus of $\sqrt{2}i - \sqrt{-2i}$ is

A. 2

B. $\sqrt{2}$

C. 0

D. $2\sqrt{2}$



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73. $\left(\cos \frac{\pi}{6} + i \sin \frac{\pi}{6}\right)^{1/2} + \left(\cos \frac{\pi}{6} - i \sin \frac{\pi}{6}\right)^{11/2}$

A. -1

B. 1

C. 0

D. 2



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74. If n is a multiple of 3 then $\omega^n + \omega^{2n} =$

A. 0

B. 1

C. -1

D. 2



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75. $(1 + \omega - \omega^2)(1 - \omega + \omega^2)$

A. 0

B. 1

C. 2

D. 4



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76. $(2 + \omega^2 + \omega^4)^5$

A. 0

B. 1

C. 2

D. 4



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77. $(3 + 5\omega + 3\omega^2)^6$

A. 42

B. 48

C. 52

D. 64



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78. $(1 - \omega)(1 - \omega^2)(1 - \omega^4)(1 - \omega^5)(1 - \omega^7)(1 - \omega^8)$

A. 25

B. 36

C. 27

D. 30



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79. $(1 + \omega)(1 + \omega^2)(1 + \omega^4)(1 + \omega^5) \dots \dots \dots 2n$ factors =

A. 0

B. 1

C. -1

D. none



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80. $(1 + \omega)(1 + \omega^2)(1 + \omega^3)(1 + \omega^4)(1 + \omega^5) \dots \dots (1 + \omega^{3n})$

A. 2^{3n}

B. 2^{2n}

C. 2^n

D. none



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81. $(1 - \omega + \omega^2)^7 + (1 + \omega - \omega^2)^7$

A. 2^5

B. 2^7

C. 2^9

D. 2^{10}



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82. $(1 - \omega + \omega^2)^6 + (1 - \omega^2 + \omega)^6$

A. 0

B. 6

C. 64

D. 128

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83. If ω is a complex cube root of unity, then

$$225 + (3\omega + 8\omega^2)^2 + (3\omega^2 + 8\omega)^2$$

A. 72

B. 192

C. 200

D. 248

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84. If ω is a complex cube root of unity, then $(x + 1)(x + \omega)(x - \omega - 1)$

A. $x^3 - 1$

B. $x^3 + 1$

C. $x^3 + 2$

D. $x^3 - 2$



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85. $(a - b)(a\omega - b\omega^2)(a\omega^2 - b\omega)$

A. $a^2 - b^2$

B. $a^2 + b^2$

C. $a^3 - b^3$

D. $a^3 + b^3$



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86. $(a + 2b)^2 + (a\omega + 2b\omega^2)^2 + (a\omega^2 + 2b\omega)^2$

A. $8ab$

B. $9ab$

C. $11ab$

D. $12ab$



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87. If $1, \omega, \omega^2$ are the cube roots of unity, then $(a + b)^3 + (a\omega + b\omega^2)^3 + (a\omega^2 + b\omega)^3 =$

A. $a^2 + b^2$

B. $3(a^3 + b^3)$

C. $a^3 - b^3$

D. $a^3 + b^3 + 3ab$



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88. If $x = a + b$, $y = a\omega + b\omega^2$, $z = a\omega^2 + b\omega$ then xyz

A. $a^2 + b^2$

B. $a^2 - b^2$

C. $a^3 + b^3$

D. $a^3 - b^3$



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89. If a , b are real and

$x = a + b$, $y = a\omega^2 + b\omega$, $z = a\omega + b\omega^2$ then $x^2 + y^2 + z^2$

A. $6ab$

B. $12ab$

C. $8a^2b^2$

D. $4a^2b^2$

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90. $(1 - \omega + \omega^2)(1 - \omega^2 + \omega^4)(1 - \omega^4 + \omega^8)(1 - \omega^8 + \omega^{16})$

A. 4

B. 8

C. 12

D. 16

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91. If $1, \omega, \omega^2$ are the cube roots of unity, then prove that

$$(x + y + z)(x + y\omega + z\omega^2)(x + y\omega^2 + z\omega) = x^3 + y^3 + z^3 - 3xyz$$

A. $x^3 + y^3 + z^3 + 3xyz$

B. $x^3 - y^3 - z^3 - 3xyz$

C. $x^2 + y^3 + z^3$

D. none



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92. $(1 - \omega + \omega^2)(1 - \omega^2 + \omega^4)(1 - \omega^4 + \omega^8) \dots$ to $2n$ factors

A. 2

B. 2^{2n}

C. $2n$

D. none



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93. If ω is a complex cube root of unity then

$$\omega \left(\frac{1}{3} + \frac{2}{9} + \frac{4}{27} + \dots \cdot \infty \right) + \omega \left(\frac{1}{2} + \frac{3}{8} + \frac{9}{32} + \dots \cdot \infty \right) =$$

A. 1

B. -1

C. ω

D. i



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94.
$$\frac{a + b\omega + c\omega^2}{c + a\omega + b\omega^2}$$

A. ω

B. ω^2

C. $a^2 + b^2$

D. 0



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95. $\frac{1}{1+2\omega} - \frac{1}{1+\omega} + \frac{1}{2+\omega}$

A. ω

B. ω^2

C. $a^2 + b^2$

D. 0



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96. If ω is a complex cube root of unity, then $\sin\left[(\omega^{10} + \omega^{23})\pi - \frac{\pi}{4}\right]$

A. $\frac{1}{\sqrt{2}}$

B. $\frac{1}{2}$

C. 1

D. $\frac{\sqrt{3}}{2}$



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97. If $1, \omega, \omega^2$ are the cube roots of unity and

$\alpha = \omega + 2\omega^2 - 3$, then $\alpha^3 + 12\alpha^2 + 48\alpha + 3$ equals

A. -63

B. -62

C. -61

D. -60



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98. If α, β are the roots of $1 + x + x^2 = 0$, then the value of $\alpha^4 + \beta^4 + \alpha^{-4}\beta^{-4}$ is

A. 0

B. 1

C. -1

D. -2



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99. If $x^2 + x + 1 = 0$, then the value of $\left(x + \frac{1}{x}\right)^2 + \left(x^2 + \frac{1}{x^2}\right)^2 + \dots + \left(x^{27} + \frac{1}{x^{27}}\right)^2$ is

A. 27

B. 72

C. 45

D. 54

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100. If the cube roots of unity are $1, \omega, \omega^2$ then the roots of the equation

$$(x - 1)^3 + 8 = 0 \text{ are}$$

A. $-1, -1 + 2\omega, -1 - 2\omega^2$

B. $-1, -1, -1$

C. $-1, 1 - 2\omega, 1 - 2\omega^2$

D. $-1, 1 + 2\omega, 1 + 2\omega^2$

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101. If α, β are the non-real cube roots of 2, then $\alpha^6 + \beta^6 =$

A. 8

B. 4

C. 2

D. 1



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102. If α is a non-real root of $x^6 - 1 = 0$ then $\frac{\alpha^5 + \alpha^3 + \alpha + 1}{\alpha^2 + 1}$

A. α^2

B. 0

C. $-\alpha^2$

D. α



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103. If α is a non real root of the equation $x^6 - 1 = 0$ then
$$\frac{\alpha^2 + \alpha^3 + \alpha^4 + \alpha^5}{\alpha + 1}$$

A. α

B. 1

C. 0

D. -1



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104. If $1, \alpha_1, \alpha_2, \dots, \alpha_{n-1}$ are the n^{th} roots of unity then
$$(1 - \alpha_1)(1 - \alpha_2) \dots (1 - \alpha_{n-1}) =$$

A. $n-1$

B. n

C. -1

D. 1

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105. If $1, \alpha_1, \alpha_2, \dots, \alpha_{n-1}$ are the n^{th} roots of unity and n is an odd natural number then

$$(1 + \alpha_1)(1 + \alpha_2) \dots (1 + \alpha_{n-1}) =$$

A. 1

B. -1

C. 0

D. none

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106. $1, \alpha_1, \alpha_2, \alpha_3, \dots, \alpha_{n-1}$ are the n^{th} roots of unity and n is an even natural number, then $(1 + \alpha_1)(1 + \alpha_2)(1 + \alpha_3) \dots (1 + \alpha_{n-1}) =$

- A. 1
- B. 0
- C. -1
- D. none



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107. If $1, z_1, z_2, \dots, z_{n-1}$ are the n^{th} roots of unity, then $(1 - z_1)(1 - z_2) \dots (1 - z_{n-1}) =$.

- A. 0
- B. $n-1$
- C. n
- D. 1



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108. If α is an n^{th} root of unity then prove that

$$1 + 2\alpha + 3\alpha^2 + 4\alpha^3 + \dots + n\alpha^{n-1} = -\frac{n}{1-\alpha}$$

A. $\frac{n}{1-\alpha}$

B. $\frac{-n}{1-\alpha}$

C. $\frac{-n}{(1-\alpha)^2}$

D. none



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109. If $1, \alpha, \alpha^2, \dots, \alpha^{n-1}$ are the n^{th} roots of unity, then the value of

$$(3-\alpha)(3-\alpha^2)\dots(3-\alpha^{n-1})$$
 is

A. n

B. 0

C. $(3^n - 1)/2$

D. $(3^n + 1)/2$

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110. Statement-I :

If $x_n = \cos(\pi/2^n) + i \sin(\pi/2^n)$ then $x_1 \cdot x_2 \cdot x_3 \dots = -1$

Statement-II : $x_n = \cos(\pi/4^n) + i \sin(\pi/4^n)$ then

$x_1 \cdot x_2 \cdot x_3 \dots \infty = -1$

A. $x_1 + x_2 + m - 1$

B. $x_1 + x_2 + x_3 m = 0$

C. $x_1 x_2 x_3 m - 1$

D. $x_1 - x_2 + x_3 m = -1$

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111. If $X_n = \cos \frac{\pi}{2^n} + i \sin \frac{\pi}{2^n}$, then $x_1, x_2, x_3 \dots \infty$

A. -1

B. 1

C. $1/\sqrt{2}$

D. $i/\sqrt{2}$



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112. If $x_n = \cos \left(\frac{\pi}{4^n} \right) + i \sin \left(\frac{\pi}{4^n} \right)$, then $x_1, x_2, x_3 \dots \infty$ is equal to

A. $\frac{1 + i\sqrt{3}}{2}$

B. $\frac{-1 + i\sqrt{3}}{2}$

C. $\frac{1 - i\sqrt{3}}{2}$

D. $\frac{-1 - i\sqrt{3}}{2}$



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113. $\sum_{k=1}^6 \left[\sin\left(\frac{2k\pi}{7}\right) - i \cos\left(\frac{2k\pi}{7}\right) \right] =$

A. -1

B. 0

C. $-i$

D. i



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114. If $z_k = \cos\left(\frac{k\pi}{10}\right) + i \sin\left(\frac{k\pi}{10}\right)$, then $z_1 z_2 z_3 z_4$ is equal to

A. -1

B. 1

C. -2

D. 2



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115. The cube roots of $1+i$ are

A. $(i - 1) / \sqrt[3]{2}, \{(i - 1) / \sqrt[3]{2}\}\omega, \{(i - 1) / \sqrt[3]{2}\}\omega^2$

B. $(i - 1) / \sqrt{2}, \{(i - 1) / \sqrt{2}\}\omega, \{(i - 1) / \sqrt[3]{2}\}\omega^3$

C. $(i - 1) / \sqrt{3}, \{(i - 1) / \sqrt{3}\}\omega, \{(i - 1) / \sqrt{3}\}\omega^2$

D. none



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116. The values of $(1 - \sqrt{3}i)^{1/3}$ are

A. $2^{1/5} cis \left[\frac{2k\pi + \pi/3}{3} \right], k = 0, 1, 2$

B. $2^{1/5} cis \left[\frac{2k\pi - \pi/6}{3} \right], k = 0, 1, 2$

C. $2^{1/3} cis \left[\frac{2k\pi - \pi/3}{3} \right], k = 0, 1, 2$

D. none

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117. Find all the values of $(\sqrt{3} + i)^{\frac{1}{4}}$.

A. $2^{1/4} cis \left[\frac{2k\pi + \pi/6}{4} \right], k = 0, 1, 2, 3$

B. $2^{1/4} cis \left[\frac{2k\pi + \pi/3}{4} \right], k = 0, 1, 2, 3$

C. $2^{1/4} cis \left[\frac{2k\pi - \pi/6}{4} \right], k = 0, 1, 2, 3$

D. none

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118. The product of the four values of $\left(\frac{1}{2} + i\frac{\sqrt{3}}{2}\right)^{3/4}$ is

A. -1

B. 1

C. i

D. i



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119. The product of the values of $\left[\cos \frac{\pi}{3} + i \sin \frac{\pi}{3}\right]^{3/4}$ is

A. -1

B. 1

C. i

D. i



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120. The product of the distinct $(2n)^{th}$ roots $1 + i\sqrt{3}$ is

A. 0

B. $-1 - i\sqrt{3}$

C. $1 + i\sqrt{3}$

D. $-1 + i\sqrt{3}$



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121. If $x^6 + 1 = 0$, then $x =$

A. $cis \frac{(3k + 1)\pi}{6}$, $k = 0, 1, 2, 3, 4, 5$

B. $cis \frac{(2k - 1)\pi}{6}$, $k = 0, 1, 2, 3, 4, 5$

C. $cis \frac{(3k + 1)\pi}{6}$, $k = 0, 1, 2, 3, 4, 5$

D. $\text{cis} \frac{(3k-1)\pi}{6}$, $k = 0, 1, 2, 3, 4, 5$



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122. The number of common roots of 15th and of 25th roots of unity are

A. 1

B.

C. 5

D. 6

Answer: A



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123. The common roots of the equation

$$z^3 + 2z^2 + 2z + 1 = 0, z^{2014} + z^{2015} + 1 = 0$$

A. ω, ω^2

B. $1, \omega, \omega^2$

C. $-1, \omega, \omega^2$

D. $-\omega, -\omega^2$



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124. p, q, r are distinct cube roots of non-zero complex number z . Let a, b, c be complex numbers satisfying $ap + bq + cr \neq 0$. Then find the value of
$$\frac{(aq + br + cp)(ar + bp + cq)}{(ap + bq + cr)^2}.$$

A. 1

B. -1

C. i

D. -1



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EXERCISE 2 SET-1

1. $1, \alpha_1, \alpha_2, \alpha_3, \dots, \alpha_{n-1}$ are the n^{th} roots of unity and n is an even natural number, then $(1 + \alpha_1)(1 + \alpha_2)(1 + \alpha_3) \dots (1 + \alpha_{n-1}) =$

- A. only I is true
- B. only II is true
- C. both I and II are true
- D. neither I nor II true



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2. Statement-I :

If $x_n = \cos(\pi/2^n) + i \sin(\pi/2^n)$ then $x_1 \cdot x_2 \cdot x_3 \dots = -1$

Statement-II : $x_n = \cos(\pi/4^n) + i \sin(\pi/4^n)$ then

$$x_1 \cdot x_2 \cdot x_3 \cdot \dots \cdot \infty = -1$$

- A. only I is true
- B. only II is true
- C. both I and II are true
- D. neither I nor II true

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$$3. I: \sum_{k=1}^6 \left[\sin\left(\frac{2k\pi}{7}\right) - i \cos\left(\frac{2k\pi}{7}\right) \right] = i$$

$$II: \sum_{r=1}^8 \left[\sin\left(\frac{2\pi r}{9}\right) + i \cos\left(\frac{2\pi r}{9}\right) \right] = i$$

Which of the above statements are true

- A. only I is true
- B. only II is true
- C. both I and II are true

D. neither I nor II true



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4. Statement-I : If $e^{i\theta} = \cos \theta + i \sin \theta$ then for the $\Delta ABC e^{iA} e^{iB} e^{iC} = -1$

Statement-II : If $(\sqrt{3} + 1)^{100} = 2^{99}(a + ib)$ then $b = 2\sqrt{3}$

A. only I is true

B. only II is true

C. both I and II are true

D. neither I nor II true



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5. I : Value of $i^i = e^{-\frac{\pi}{2}}$

II : $z = i \log(2 + \sqrt{3})$ then $\sin z = 2$

which of above statement is true

- A. only I is true
- B. only II is true
- C. both I and II are true
- D. neither I nor II true

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EXERCISE 2 SET-2

1. The ascending order of the values of

$$z_1 = (1 + i)^4, z_2 = (\sqrt{3} + i)^{12}, z_3 = (1 + i\sqrt{3})^9 + (1 - i\sqrt{3})^9$$

- A. z_1, z_2, z_3

B. z_2, z_3, z_1

C. z_3, z_1, z_2

D. z_1, z_3, z_2



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2. The ascending order of the values of

$$z_1(1+i)^4 + (1-i)^4, z_2 = (\sqrt{3}+i)^{12} + (\sqrt{3}-i)^{12}, z_3 = (1+i\sqrt{3})^9 + (1-i\sqrt{3})^9$$

A. z_1, z_2, z_3

B. z_2, z_3, z_1

C. z_3, z_1, z_2

D. z_1, z_3, z_2



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3. The descending order of the values of

$$z_1 = \left(\frac{\sqrt{3}}{2}i + \frac{1}{2} \right)^6, z_2 = \left(\frac{1}{\sqrt{2}} + \frac{i}{\sqrt{2}} \right)^4, z_3 = \left(\frac{\sqrt{3}}{4} + \frac{i}{4} \right)^6$$

A. z_1, z_2, z_3

B. z_2, z_3, z_1

C. z_3, z_1, z_2

D. z_1, z_3, z_2



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EXERCISE 2 SET-3

1. Match the following.

- I) $(i)^i =$ a) $i\pi/2$
II) $\log_e i =$ b) $i\pi/2 + \log \pi/2$
III) $\log(\log i) =$ c) $\sqrt{2}$
IV) $\sqrt{i} + \sqrt{-i} =$ $e^{-\pi/2}$

A. d, a, c, b

B. b, c, a, d

C. d, a, b, c

D. d, c, b, a



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EXERCISE 2 SET-4

1. A: $(1 + i)^6 + (1 - i)^6 = 0$

R : If n is a positive integer then

$$(1 + i)^n + (1 - i)^n = 2^{(n/2) + 1} \cdot \cos \frac{n\pi}{4}$$

A. Both A and R are true and R is the correct explanation of A

B. Both A and B are true but R is not correct explanation of A

C. A is true but R is false

D. A is false but R is true



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2. A : If $A + B + C = \pi$ and $\operatorname{cis} A = x$, $\operatorname{cis} B = y$, $\operatorname{cis} C = z$, then $xyz = -1$

R: $(\operatorname{cis} \alpha)(\operatorname{cis} \beta) = \operatorname{cis}(\alpha + \beta)$

A. Both A and R are true and R is the correct explanation of A

B. Both A and B are true but R is not correct explanation of A

C. A is true but R is false

D. A is false but R is true



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3. Assertion (A) : If

$$\alpha = \cos\left(\frac{2\pi}{7}\right) + i \sin\left(\frac{2\pi}{7}\right), p = \alpha + \alpha^2 + \alpha^4, q = \alpha^3 + \alpha^5 + \alpha^6$$

then the equation whose roots are p and q is $x^2 + x + 2 = 0$

Reason (R) : If α is a roots of $z^7 = 1$ then $1 + \alpha + \alpha^2 + \dots + \alpha^6 = 0$

- A. Both A and R are true and R is the correct explanation of A
- B. Both A and B are true but R is not correct explanation of A
- C. A is true but R is false
- D. A is false but R is true



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