



India's Number 1 Education App

## MATHS

### BOOKS - DEEPTI MATHS (TELUGU ENGLISH)

### EXPONENTIAL SERIES & LOGARITHMIC SERIES (APPENDIX- 1)

#### Solved Examples

$$1. \frac{1^3}{1!} + \frac{2^3}{2!} + \frac{3^3}{3!} + \frac{4^3}{4!} + \dots =$$

A. e

B. 3e

C. 5e

D.  $e / 5$

Answer: C

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2.  $1 + \frac{2^3}{1!}x + \frac{3^3}{2!}x^2 + \dots =$

A.  $(x^3 - 6x^2 + 7x - 1)e^x$

B.  $(x^2 + 7x + 8)e^x - 8$

C.  $(x^3 + 6x^2 + 7x + 1)e^x$

D.  $(x^2 + 7x + 8)e^x + 8$

**Answer: C**

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3. If  $y = \frac{1}{2x^2 - 1}$  then  $y + \frac{y^3}{3} + \frac{y^5}{5} + \dots =$

A.  $x + \frac{x^3}{3} + \frac{x^5}{5} + \dots$

B.  $2\left(x + \frac{x^3}{3} + \frac{x^5}{5} + \dots\right)$

- C.  $\frac{1}{2} \left( x + \frac{x^3}{3} + \frac{x^5}{5} + \dots \right)$
- D.  $-\frac{1}{2} \left( x + \frac{x^3}{3} + \frac{x^5}{5} + \dots \right)$

**Answer: B**



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4.  $\frac{x}{1.2} + \frac{x^2}{2.3} + \frac{x^3}{3.4} + \dots =$

A.  $1 + \left( \frac{1-x}{x} \right) \log(1-x)$

B.  $1 + \left( \frac{x-1}{x} \right) \log(1-x)$

C.  $1 + \frac{1-x}{x} \log(x-1)$

D.  $1+(x-1)/(x)\log(x-1)$

**Answer: A**



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## Exercise 1 A

$$1 \cdot 1 + \frac{2}{1!} + \frac{4}{2!} + \frac{8}{3!} + \dots =$$

A. e

B.  $e^2$

C.  $e^3$

D.  $1/e$

**Answer: B**



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$$2 \cdot 1 + \frac{4}{1!} + \frac{16}{2!} + \frac{64}{3!} + \dots =$$

A. e

B.  $e^2$

C.  $e^3$

D.  $e^4$

**Answer: D**



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$$3. \sum_{k=1}^{\infty} \frac{1}{k!} \left( \sum_{n=1}^k 2^{n-1} \right) =$$

A.  $e$

B.  $e^2 + e$

C.  $e^2$

D.  $e^2 - e$

**Answer: D**



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$$4. 1 - \frac{2}{1!} + \frac{4}{2!} - \frac{8}{3!} + \dots =$$

A. e

B.  $e^2$

C.  $e^{-1}$

D.  $e^{-2}$

**Answer: D**



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$$5. 1 - \frac{3}{1!} + \frac{9}{2!} - \frac{27}{3!} + \dots =$$

A. e

B.  $e^2$

C.  $e^3$

D.  $e^{-3}$

**Answer: D**



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$$6. \log_e 2 + \frac{(\log_e 2)^2}{2!} + \frac{(\log_e 2)^3}{3!} + \dots =$$

A. 1

B. 2

C. e

D.  $e^2$

**Answer: A**



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$$7. \log_e 3 + \frac{(\log_e 3)^2}{2!} + \frac{(\log_e 3)^3}{3!} + \dots =$$

A. 1

B. 2

C. e

D.  $e^2$

**Answer: B**



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8.  $1 + 2(\log_e a) + \frac{2^2}{2!}(\log_e a)^2 + \frac{2^3}{3!}(\log_e a)^3 + \dots =$

A. e

B. a

C.  $a^2$

D.  $e^2$

**Answer: C**



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9.  $1 + x(\log_e 2) + \frac{x^2}{2!}(\log_e 2)^2 + \frac{x^3}{3!}(\log_e 2)^3 + \dots =$

A.  $e^2$

B.  $x^2$

C.  $e^x$

D.  $2^x$

**Answer: D**



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10.  $x \log_e a + \frac{x^3}{3!}(\log_e a)^3 + \frac{x^5}{5!}(\log_e a)^5 + \dots =$

A.  $\cosh(x \log_e a)$

B.  $\coth(x \log_e a)$

C.  $\sinh(x \log_e a)$

D.  $\tanh(x \log_e a)$

**Answer: C**



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$$11. x \log_e a + \frac{x^3}{3!}(\log_e a)^3 + \frac{x^5}{5!}(\log_e a)^5 + \dots =$$

A.  $\cosh(x \log_e a)$

B.  $\coth(x \log_e a)$

C.  $\sinh(x \log_e a)$

D.  $\tanh(x \log_e a)$

**Answer: C**



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$$12. \left(1 - \frac{3}{1!} + \frac{9}{2!} - \frac{27}{3!} + \dots\right) \left(1 + \frac{3}{1!} + \frac{9}{2!} + \frac{27}{3!} + \dots\right) =$$

A. e

B.  $e^2$

C.  $e^3$

D. 1

**Answer: D**



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$$13. \left(1 - \frac{2}{1!} + \frac{4}{2!} - \frac{8}{3!} + \dots\right) \left(1 + \frac{4}{1!} + \frac{16}{2!} + \frac{64}{3!} + \dots\right) =$$

A. e

B.  $e^2$

C.  $e^3$

D. 1

**Answer: B**



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$$14. e^{3x} =$$

A.  $1 + \frac{3}{1!} + \frac{3^2}{2!} + \frac{3^3}{3!} + \dots$

B.  $1 - \frac{3}{1!} + \frac{3^2}{2!} - \frac{3^3}{3!} + \dots$

C.  $1 + \frac{3x}{1!} + \frac{(3x)^2}{2!} + \frac{(3x)^3}{3!} + \dots$

D.  $1 - \frac{3x}{1!} + \frac{(3x)^2}{2!} - \frac{(3x)^3}{3!} + \dots$

**Answer: C**



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15.  $e^{-2x} =$

A.  $1 + \frac{2}{1!} + \frac{2^2}{2!} + \frac{2^3}{3!} + \dots$

B.  $1 - \frac{2}{1!} + \frac{2^2}{2!} - \frac{2^3}{3!} + \dots$

C.  $1 + \frac{2x}{1!} + \frac{(2x)^2}{2!} + \frac{(2x)^3}{3!} + \dots$

D.  $1 - \frac{2x}{1!} + \frac{(2x)^2}{2!} - \frac{(2x)^3}{3!} + \dots$

**Answer: D**



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$$16. e^{5x} + e^{-5x} =$$

A.  $1 + \frac{5x}{1!} + \frac{(5x)^2}{2!} + \frac{(5x)^3}{3!} + \dots$

B.  $1 - \frac{5x}{1!} + \frac{(5x)^2}{2!} - \frac{(5x)^3}{3!} + \dots$

C.  $1 + \frac{(5x)^2}{2!} + \frac{(5x)^4}{3!} + \dots$

D.  $2 \left[ 1 + \frac{(5x)^2}{2!} + \frac{(5x)^4}{4!} + \dots \right]$

**Answer: D**



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$$17. e^{7x} - e^{-7x} =$$

A.  $1 + \frac{7x}{1!} + \frac{(7x)^2}{2!} + \frac{(7x)^3}{3!} + \dots$

B.  $1 + \frac{(7x)^2}{2!} + \frac{(7x)^4}{3!} + \dots$

C.  $2 \left[ 1 + \frac{(7x)^2}{2!} + \frac{(7x)^4}{4!} + \dots \right]$

$$\text{D. } 2 \left[ \frac{7x}{1!} + \frac{(7x)^3}{3!} + \frac{(7x)^5}{5!} + \dots \right]$$

**Answer: C**



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$$18. \frac{e^{5x} + e^x}{e^{3x}} =$$

$$\text{A. } 2 \left[ 1 + \frac{(5x)^2}{2!} + \frac{(5x)^4}{4!} + \dots \right]$$

$$\text{B. } 2 \left[ 1 + \frac{(3x)^2}{2!} + \frac{(3x)^4}{4!} + \dots \right]$$

$$\text{C. } 2 \left[ 1 + \frac{(2x)^2}{2!} + \frac{(2x)^4}{4!} + \dots \right]$$

$$\text{D. } 2 \left[ 1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots \right]$$

**Answer: C**



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$$19. \frac{e^{7x} - e^x}{e^{4x}} =$$

- A.  $2 \left[ 1 + \frac{(3x)^2}{2!} + \frac{(3x)^4}{4!} + \dots \right]$
- B.  $2 \left[ \frac{3x}{1!} + \frac{(3x)^3}{3!} + \dots \right]$
- C.  $2 \left[ 1 + \frac{(2x)^2}{2!} + \frac{(2x)^4}{4!} + \dots \right]$
- D.  $2 \left[ \frac{2x}{1!} + \frac{(2x)^3}{3!} + \dots \right]$

**Answer: B**



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20. The  $(n + 1)$  term in the expansion of  $e^5$  is

A.  $5!$

B.  $5^n$

C.  $5^n / n$

D.  $5^n / n!$

**Answer: D**



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21. The  $(n + 1)$ th term in the expansion of  $e^{4x}$  is

- A.  $4!$
- B.  $4^n$
- C.  $4^n / n!$
- D.  $(4x)^n / n!$

**Answer: D**



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22. The 12th term in the expansion of  $e^{-3}$  is

- A.  $\frac{3^{11}}{11!}$
- B.  $\frac{-3^{11}}{11!}$
- C.  $\frac{11!}{3^{11}}$

D.  $-\frac{11!}{3^{11}}$

**Answer: B**



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23. The  $(n + 1)th$  term in the expansion of  $e^{-2}$  is

A.  $\frac{3^n}{n!}$

B.  $\frac{(3x)^n}{n!}$

C.  $\frac{(-3x)^n}{n!}$

D.  $\frac{(-2)^n}{n!}$

**Answer: D**



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24. The  $(n + 1)th$  term in the expansion of  $e^{-3x}$  is

- A.  $\frac{3^n}{n!}$
- B.  $\frac{(3x)^n}{n!}$
- C.  $\frac{(-3x)^n}{n!}$
- D.  $\frac{x^n}{n!}$

**Answer: C**



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**25.** The coefficient of  $x^8$  in the expansion of  $e^{3x}$  is

- A.  $3^8$
- B.  $\frac{3^8}{3!}$
- C.  $\frac{3^8}{8!}$
- D. none

**Answer: C**



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**26.** The coefficient of  $x^2$  in the expansion of  $e^{2x+3}$  is

A.  $e^2$

B.  $e^3$

C.  $2e^3$

D.  $3e^2$

**Answer:** C



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**27.** The coefficient of  $x^n$  in the expansion of  $(1 - x)e^x$  is

A.  $\frac{1}{n!}$

B.  $\frac{1}{(n + 1)!}$

C.  $\frac{1 - n}{n!}$

D.  $\frac{n-1}{n!}$

**Answer: C**



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**28.**

$$\frac{1}{e^{3x}}(e^x + e^{5x}) = a_0 + a_1x + a_2x^2 + \dots \Rightarrow 2a_1 + 2^3a_3 + 2^5a_5 + \dots .$$

A. e

B.  $e^{-1}$

C. 1

D. 0

**Answer: D**



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**29.** The coefficient of  $x^n$  in the expansion of  $\frac{e^{7x} + e^x}{e^{3x}}$  is

A.  $\frac{4^n}{n!} - \frac{(-1)^n 2^n}{n!}$

B.  $\frac{(-1)^n}{n!} + \frac{(-1)^{n-1} a}{(n-1)!} + \frac{(-1)^{n-2}}{(n-2)!}$

C.  $\frac{4^n}{n!} + \frac{(-1)^n 2^n}{n!}$

D.  $\frac{(-1)^n}{n!} - \frac{(-1)^{n-1} a}{(n-1)!} + \frac{(-1)^{n-2}}{(n-2)!}$

**Answer: C**



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**30.** The coefficient of  $x^n$  in the expansion of  $\frac{1 + ax + x^2}{e^x}$  is

A.  $\frac{4^n}{n!} - \frac{(-1)^n 2^n}{n!}$

B.  $\frac{(-1)^n}{n!} + \frac{(-1)^{n-1} a}{(n-1)!} + \frac{(-1)^{n-2}}{(n-2)!}$

C.  $\frac{4^n}{n!} + \frac{(-1)^n 2^n}{n!}$

D.  $\frac{(-1)^n}{n!} - \frac{(-1)^{n-1} a}{(n-1)!} + \frac{(-1)^{n-2}}{(n-2)!}$

**Answer: B**



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31. The coefficient of  $x^n$  in the expansion of  $(2 + 3x)(e^{-3x})$  is

A.  $(-1)^n 2^n$

B.  $(-1)^n 2^n \left( \frac{3}{n!} - \frac{1}{(n-1)!} \right)$

C.  $(-1)^n 2^n \left( \frac{3}{n!} + \frac{1}{(n-1)!} \right)$

D.  $(-1)^n 3^n \left( \frac{2}{n!} - \frac{1}{(n-1)!} \right)$

**Answer: D**



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32. Coefficient of  $x^{10}$  in the expansion of  $(2 + 3x)e^{-x}$  is

A.  $\frac{-26}{(10)!}$

B.  $\frac{-28}{(10)!}$

C.  $\frac{-30}{(10)!}$

D.  $\frac{-32}{(10)!}$

**Answer: B**



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33. The coefficient of  $x^n$  in  $\frac{1 - 2x}{e^x}$  is

A.  $\frac{(1 + 2n)}{n!}$

B.  $(-1)^n \cdot \frac{(1 + 2n)}{n!}$

C.  $(-1)^n \cdot \frac{(1 - 2n)}{n!}$

D.  $(-1)^n \cdot \frac{(1 + 4n)}{n!}$

**Answer: B**



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**34.** The coefficient of  $x^5$  in the expansion of  $\frac{1 - 2x + 3x^2}{e^x}$  is

A.  $\frac{71}{120}$

B.  $-\frac{71}{120}$

C.  $\frac{67}{120}$

D.  $-\frac{67}{120}$

**Answer:** B



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**35.** The coefficient of  $x^k$  in the expansion of  $\frac{1 - 2x - x^2}{e^{-x}}$  is

A.  $\frac{1 - k - k^2}{k!}$

B.  $\frac{k^2 + 1}{k!}$

C.  $\frac{1 - k}{k!}$

D.  $\frac{1}{k!}$

**Answer: A**



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36. The coefficient of  $x^n$  in  $\frac{1+x}{1!} + \frac{(1+x)^2}{2!} + \frac{(1+x)^3}{3!} + \dots$

A. e

B.  $n!$

C.  $en!$

D.  $e/n!$

**Answer: D**



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37. The coefficient of  $x^n$  in

$$1 + (ax + b) + \frac{(ax + b)^2}{2!} + \frac{(ax + b)^3}{3!} + \dots$$

- A.  $\frac{e^b a^n}{n!}$
- B.  $\frac{e^a b^n}{n!}$
- C.  $\frac{e^b a^n}{(n - 1)!}$
- D.  $\frac{e^a b^n}{(n - 1)!}$

**Answer: A**



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**38.** The coefficient of  $x^n$  in the expansion of  $\sum_{n=1}^{\infty} (-1)^n \frac{(2+3x)^n}{n!}$  is

- A.  $\frac{(-3)^n}{e^2 \cdot n!}$
- B.  $\frac{(-2)^n}{e^3 \cdot n!}$
- C.  $\frac{(-3)^n}{e^3 \cdot n!}$
- D.  $\frac{(-2)^n}{e^2 \cdot n!}$

**Answer: A**



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39. If  $n$  is odd, coefficient of  $x^n$  in the expansion of

$$\left(1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots\right)^2$$
 is

A.  $\frac{2^n}{n!}$

B.  $\frac{2^{2n}}{(2n)!}$

C. 0

D.  $\frac{2^{n-1}}{n!}$

**Answer: C**



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40. If  $n$  is even, coefficient of  $x^n$  in the expansion of

$$\left(1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots\right)^2$$
 is

A.  $\frac{2^n}{n!}$

B.  $\frac{2^{2n}}{(2n)!}$

C. 0

D.  $\frac{2^{n-1}}{n!}$

**Answer: D**



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41.  $2 - \frac{3^2}{2!} + \frac{3^3}{3!} - \frac{3^4}{4!} + \dots =$

A.  $e^3$

B.  $e^{-3}$

C.  $-e^3$

D.  $-e^{-3}$

**Answer: D**



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$$42. \frac{1}{2!} + \frac{1}{3!} + \frac{1}{4!} + \dots =$$

A. e

B.  $e/2$

C.  $e^{-1}$

D.  $e-2$

**Answer: D**



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$$43. \frac{1}{2!} - \frac{1}{3!} + \frac{1}{4!} - \frac{1}{5!} + \dots =$$

A. e

B.  $e/2$

C.  $e^{-1}$

D.  $e - 2$

**Answer: C**



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**44.**  $-1 + \frac{2^2}{2!} - \frac{2^3}{3!} + \frac{2^4}{4!} - \dots =$

A. e

B.  $e/2$

C.  $e^{-1}$

D.  $e^{-2}$

**Answer: D**



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**45.** Sum of the series  $1 + \frac{3^2}{2!} + \frac{3^4}{4!} + \frac{3^6}{6!} + \dots$  to  $\infty$  is

A.  $e^{-3}$

B.  $e^3$

C.  $\frac{1}{2}(e^3 - e^{-3})$

D.  $\frac{1}{2}(e^3 + e^{-3})$

**Answer: D**



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46.  $\sum_{n=0}^{\infty} \frac{1}{(n+1)!} =$

A. e

B.  $e + 1$

C.  $1 - e$

D.  $e - 1$

**Answer: D**



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$$47. \sum_{n=1}^{\infty} \frac{1}{(2n-1)!} =$$

A.  $\frac{1}{2}(e + e^{-1})$

B.  $\frac{1}{2}(e - e^{-1})$

C.  $e + e^{-1}$

D.  $e - e^{-1}$

**Answer: B**



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$$48. \sum_{n=1}^{\infty} \frac{x^n}{(2n-1)!} =$$

A.  $e^{\sqrt{x}} - e^{-\sqrt{x}}$

B.  $\sqrt{x}(e^{\sqrt{x}} - e^{-\sqrt{x}})$

C.  $\sqrt{x}(e^{\sqrt{x}} + e^{-\sqrt{x}})$

D.  $\sqrt{x}(e^{\sqrt{x}} - e^{-\sqrt{x}})/2$

**Answer: D**



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**49.** The sum of series  $\frac{1}{2!} + \frac{1}{4!} + \frac{1}{6!} + \dots$  is

A.  $\frac{(e^2 - 1)}{2}$

B.  $\frac{(e^2 - 2)}{e}$

C.  $\frac{(e^2 - 1)}{2e}$

D.  $\frac{(e - 1)^2}{2e}$

**Answer: D**



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**50.**  $1 + \frac{1}{3!} + \frac{1}{5!} + \dots =$

A. e

B.  $\frac{e}{2}$

C.  $\frac{1}{2}(e + e^{-1})$

D.  $\frac{1}{2}(e - e^{-1})$

**Answer: D**



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51.  $\frac{2}{1!} + \frac{4}{3!} + \frac{6}{5!} + \dots =$

A.  $e$

B.  $e^2$

C.  $2e$

D.  $1/e$

**Answer: A**



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$$52. \frac{3}{2!} + \frac{5}{4!} + \frac{7}{6!} + \frac{9}{8!} + \dots =$$

A. e

B.  $2e$

C.  $e^{-1}$

D.  $e - 1$

**Answer: D**



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$$53. 2 \left[ 1 + \frac{(\log_e a)^2}{2!} + \frac{(\log_e a)^4}{4!} + \dots \right] =$$

A. a

B.  $a + a^{-1}$

C.  $a^2 + a^{-2}$

D.  $a - a^{-1}$

**Answer: B**



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**54.**  $1 + \frac{2}{3!} + \frac{3}{5!} + \frac{4}{7!} + \dots =$

A.  $e$

B.  $e/2$

C.  $e^{-1}$

D.  $e^{-1}/2$

**Answer: B**



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**55.**  $\frac{2}{3!} + \frac{4}{5!} + \frac{6}{7!} + \dots =$

A.  $e$

B.  $e/2$

C.  $e^{-1}$

D.  $e^{-1}/2$

**Answer: C**



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$$56. \frac{1}{3!} + \frac{2}{5!} + \frac{3}{7!} + \dots =$$

A.  $e$

B.  $e/2$

C.  $e^{-1}$

D.  $e^{-1}/2$

**Answer: D**



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$$57. 1 + \frac{2}{1!} + \frac{3}{2!} + \frac{4}{3!} + \dots =$$

A. e

B.  $2e$

C.  $e^{-1}$

D.  $e^{-1}/2$

**Answer: B**



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$$58. 1 + \frac{3}{1!} + \frac{5}{2!} + \frac{7}{3!} + \dots =$$

A. e

B.  $2e$

C.  $3e$

D.  $e + 2$

**Answer: C**



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**59.**  $\frac{3}{2!} + \frac{5}{3!} + \frac{7}{4!} + \frac{9}{5!} + \dots =$

A. e

B. 2e

C.  $e^{-1}$

D.  $e^{-1}/2$

**Answer: A**



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**60.**  $1 + \frac{4}{2!} + \frac{7}{3!} + \frac{10}{4!} + \dots =$

A. e

B.  $2e$

C.  $3e$

D.  $e + 2$

**Answer: D**



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$$61. \sum_{n=1}^{\infty} \frac{2n}{(2n+1)!} =$$

A.  $\frac{1}{e}$

B.  $\frac{e}{2}$

C. e

D.  $2e$

**Answer: A**



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$$62. \sum_{n=1}^{\infty} \frac{n^2}{(n+1)!} =$$

A. e

B.  $2e$

C.  $3e$

D.  $e - 1$

**Answer: D**



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$$63. \sum_{n=1}^{\infty} (2n^{(2)} + n + 1) / (n!) =$$

A.  $2e - 1$

B.  $2e + 1$

C.  $6e - 1$

D.  $6e + 1$

**Answer: C**



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$$64. \left(1 + \frac{1}{2!} + \frac{1}{4!} + \frac{1}{6!} + \dots\right)^2 - \left(1 + \frac{1}{3!} + \frac{1}{5!} + \frac{1}{7!} + \dots\right)^2 =$$

A. 0

B. 1

C. e

D.  $1/e$

**Answer: B**



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$$65. \left(1 + \frac{a^2x^2}{2!} + \frac{a^4x^4}{4!} + \dots\right)^2 - \left(ax + \frac{a^3x^3}{3!} + \frac{a^5x^5}{5!} + \dots\right)^2 =$$

A. 0

B. 1

C. e

D.  $1/e$

**Answer: B**



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$$66. \frac{1 + \frac{2^2}{2!} + \frac{2^4}{3!} + \frac{2^6}{4!} + \dots}{1 + \frac{1}{2!} + \frac{2}{3!} + \frac{2^2}{4!} + \dots} =$$

A.  $e - 1$

B.  $e^2 - 1$

C.  $e + 1$

D.  $e^2 + 1$

**Answer: B**



**Watch Video Solution**

$$67. \frac{1 + \frac{1}{3!} + \frac{1}{5!} + \dots}{1 + \frac{1}{2!} + \frac{1}{4!} + \dots} =$$

A.  $\frac{e - 1}{e + 1}$

B.  $\frac{e^2 - 1}{e^2 + 1}$

C.  $\frac{e + 1}{e - 1}$

D.  $\frac{e^2 + 1}{e^2 - 1}$

**Answer: B**



**Watch Video Solution**

$$68. \frac{\frac{1}{2!} + \frac{1}{4!} + \frac{1}{6!} + \dots}{1 + \frac{1}{3!} + \frac{1}{5!} + \dots} =$$

A.  $\frac{e - 1}{e + 1}$

B.  $\frac{e + 1}{e - 1}$

C.  $e^{-1}$

D.  $\frac{e^{-1}}{2}$

**Answer: A**



**Watch Video Solution**

$$69. \frac{1}{2} - \frac{1}{3(1!)} + \frac{1}{4(2!)} - \frac{1}{5(3!)} + \dots =$$

A. e

B.  $2/e$

C.  $1 - 1/e$

D.  $1 - 2/e$

**Answer: D**



**Watch Video Solution**

$$70. \frac{1}{1!} + \frac{1+2}{2!} + \frac{1+2+2^2}{3!} + \dots =$$

A. e

B.  $e^2$

C.  $e^2 + e$

D.  $e^2 - e$

**Answer: D**



**Watch Video Solution**

$$71. \frac{1}{1!} + \frac{1+3}{2!} + \frac{1+3+3^2}{3!} + \dots =$$

A.  $e^3 - e$

B.  $\frac{1}{4}(e^3 - e)$

C.  $\frac{1}{3}(e^3 - e)$

D.  $\frac{1}{2}(e^3 - e)$

**Answer: D**



**Watch Video Solution**

$$72. \frac{1}{2!} + \frac{1+2}{3!} + \frac{1+2+3}{4!} + \dots$$

A. e

B. 2e

C.  $e/2$

D.  $1/e$

**Answer: C**



**Watch Video Solution**

$$73. \frac{2}{2!} + \frac{2+4}{3!} + \frac{2+4+6}{4!} + \dots =$$

A.  $e - 2$

B.  $e - 1$

C. e

D.  $e^{-1}$

**Answer: C**



**Watch Video Solution**

$$74. \frac{1}{1!} + \frac{1+3}{2!} + \frac{1+3+3^2}{3!} + \dots =$$

A. e

B. 2e

C.  $e/2$

D.  $1/e$

**Answer: B**



**Watch Video Solution**

$$75. 1^2 + \frac{2^2}{2!} + \frac{3^2}{3!} + \frac{4^2}{4!} + \dots =$$

A. e

B.  $2e$

C.  $e/2$

D.  $1/e$

**Answer: B**



**Watch Video Solution**

$$76. \frac{1^2}{2!} + \frac{2^2}{3!} + \frac{3^2}{4!} + \dots =$$

A.  $e$

B.  $2e$

C.  $e - 1$

D.  $e + 1$

**Answer: C**



**Watch Video Solution**

$$77. \frac{1^2}{1!} + \frac{1^2 + 2^2}{2!} + \frac{1^2 + 2^2 + 3^2}{3!} + \dots =$$

A.  $17e/6$

B.  $6e/17$

C.  $11e/7$

D.  $7e/11$

**Answer: A**



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$$78. \frac{1^2 \cdot 2}{1!} + \frac{2^2 \cdot 3}{2!} + \frac{3^2 \cdot 4}{3!} + \dots =$$

A.  $5e$

B.  $7e$

C.  $11e$

D.  $e/5$

**Answer: B**



**Watch Video Solution**

$$79. \frac{1^2 \cdot 2^2}{1!} + \frac{2^2 \cdot 3^2}{2!} + \frac{3^2 \cdot 4^2}{3!} + \dots =$$

A.  $27e$

B.  $6e - 1$

C.  $7e$

D.  $2e$

**Answer: A**



**Watch Video Solution**

$$80. \sum_{n=1}^{\infty} {}^n C_0 + {}^n C_1 + \frac{{}^n C_2}{{}^n P_n} + \dots + {}^n C_n =$$

A.  $e - 1$

B.  $e + 1$

C.  $e^2 - 1$

D.  $e^2 + 1$

**Answer: C**



[View Text Solution](#)

81.  $1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \frac{x^6}{6!} + \dots =$

A.  $\frac{e^x + e^{-x}}{2}$

B.  $\frac{e^x - e^{-x}}{2}$

C.  $\frac{e^{ix} + e^{-ix}}{2}$

D.  $\frac{e^{ix} - e^{-ix}}{2}$

**Answer: C**



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$$82. \frac{1.2}{1!} + \frac{2.3}{2!} + \frac{3.4}{3!} + \dots =$$

A. e

B. 2e

C. 3e

D.  $e + 2$

**Answer: C**



**Watch Video Solution**

$$83. 1 + \frac{1}{2!} + \frac{1.3}{4!} + \frac{1.3.5}{6!} + \dots =$$

A. e

B. 2e

C.  $1/e$

D.  $\sqrt{e}$

**Answer: D**



**Watch Video Solution**

**84.** If  $S = \frac{1}{1.2} + \frac{1.3}{1.2.3.4} + \frac{1.3.5}{1.2.3.4.5.6} + \dots$  to  $\infty$ , then  $S =$

A.  $e^{1/2} - 1$

B.  $e^{1/2} + e$

C.  $e + 1$

D. none of these

**Answer: A**



**Watch Video Solution**

**85.**  $\frac{4}{1!} + \frac{11}{2!} + \frac{22}{3!} + \frac{37}{4!} + \frac{56}{5!} + \dots =$

A.  $27e$

B.  $6e - 1$

C.  $7e$

D.  $2e$

**Answer: B**



**Watch Video Solution**

86.  $\frac{5}{1!} + \frac{7}{3!} + \frac{9}{5!} + \dots =$

A.  $5e - 3e^{-1}$

B.  $\frac{5e - 3e^{-1}}{2}$

C.  $5e - 3e^{-1}$

D.  $\frac{5e - 3e^{-1}}{2}$

**Answer: B**



**Watch Video Solution**

**87.** The sum of the series  $1 + \frac{1}{4.2!} + \frac{1}{16.4!} + \frac{1}{64.6!} + \dots \infty$  is

A.  $\frac{e - 1}{\sqrt{e}}$

B.  $\frac{e + 1}{\sqrt{e}}$

C.  $\frac{e - 1}{2\sqrt{e}}$

D.  $\frac{e + 1}{2\sqrt{e}}$

**Answer:** D



**Watch Video Solution**

**88.**  $1 + \frac{2x}{1!} + \frac{3x^2}{2!} + \frac{4x^2}{3!} + \dots =$

A.  $(x + 1)e^x$

B.  $(x - 1)e^x$

C.  $xe^x$

D.  $e^x$

**Answer: A**



**Watch Video Solution**

**89.**  $1.2 + \frac{2.3}{1!}x + \frac{3.4}{2!}x^2 + \dots =$

A.  $(x^2 + 4x + 2)e^x$

B.  $(x^2 + 3x + 2)e^x$

C.  $(x^2 - 4x + 2)e^x$

D.  $(x^2 - 3x + 2)e^x$

**Answer: A**



**Watch Video Solution**

**90.**  $\frac{3.5}{1!}x + \frac{4.6}{2!}x^2 + \frac{5.7}{3!}x^3 + \dots =$

A.  $(x^3 - 6x^2 + 7x - 1)e^x$

B.  $(x^2 + 7x + 8)e^x - 8$

C.  $(x^3 + 6x^2 + 7x + 1)e^x$

D.  $(x^2 + 7x + 8)e^x + 8$

**Answer: B**



**Watch Video Solution**

**91.**

If

$$S = (x + y)(x - y) + \frac{1}{2!}(x + y)(x - y)(x^2 + y^2) + \frac{1}{3!}(x + y)(x - y)(x^2 + y^2)(x - y)$$

then  $S =$

A.  $e^{x^2} - y^2$

B.  $e^{x^2} + e^{y^2}$

C.  $e^{x^2} - e^{y^2}$

D. none of these

**Answer: C**



**92.** The approximate value of  $e^2$  is

A. 7.2

B. 7.3

C. 7.4

D. 7.5

**Answer: C**



**93.**  $x + \frac{x^2}{3!} + \frac{x^3}{5!} + \dots =$

A.  $2\sqrt{x}(e^{\sqrt{x}} + e^{-\sqrt{x}})$

B.  $\sqrt{x}(e^{\sqrt{x}} - e^{-\sqrt{x}})/2$

C.  $\sqrt{x}(e^{\sqrt{x}} + e^{\sqrt{x}})$

D.  $\sqrt{x} \left( e^{\sqrt{x}} - e^{-\sqrt{x}} \right)$

**Answer: B**



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### Exercise 1 B

1. The 7th term of  $\log_e(5/4)$  is

A.  $\frac{1}{7.4^7}$

B.  $-\frac{1}{7.4^7}$

C.  $\frac{1}{7}$

D.  $-\frac{1}{7}$

**Answer: A**



**Watch Video Solution**

**2.** The nth term of  $\log_e 2$  is

A.  $\frac{(-1)^{n-1}}{n \cdot 2^n}$

B.  $\frac{(-1)^{n-1}}{n}$

C.  $\frac{(-1)^{n-1}}{n \cdot 3^n}$

D.  $\frac{(-1)^{n-1}}{n \cdot 4^n}$

**Answer:** B



**Watch Video Solution**

**3.** The nth term of  $\log_2(3/2)$  is

A.  $\frac{(-1)^{n-1}}{n \cdot 2^n}$

B.  $\frac{(-1)^{n-1}}{n}$

C.  $\frac{(-1)^{n-1}}{n \cdot 3^n}$

D.  $\frac{(-1)^{n-1}}{n \cdot 4^n}$

**Answer: A**



**Watch Video Solution**

**4.** The nth term of  $\log_e(4/3)$  is

A.  $\frac{(-1)^{n-1}}{n \cdot 2^n}$

B.  $\frac{(-1)^{n-1}}{n}$

C.  $\frac{(-1)^{n-1}}{n \cdot 3^n}$

D.  $\frac{(-1)^{n-1}}{n \cdot 4^n}$

**Answer: C**



**Watch Video Solution**

**5.**  $\frac{3}{4} + \frac{1}{3}\left(\frac{3}{4}\right)^3 + \frac{1}{5}\left(\frac{3}{4}\right)^5 + \dots =$

A.  $\log_e 3$

B.  $\log_e 4$

C.  $\log_e 7$

D.  $\frac{1}{2} \log_e 7$

**Answer: D**



**Watch Video Solution**

$$6. 2 \left[ \left( \frac{1}{3} \right) + \frac{1}{3} \left( \frac{1}{3} \right)^3 + \frac{1}{5} \left( \frac{1}{3} \right)^5 + \dots \right] =$$

A.  $\log_e 3$

B.  $\log_e 4$

C.  $\log_e 2$

D.  $\log_e 5$

**Answer: C**



**Watch Video Solution**

$$7.2 \left[ \left( \frac{1}{2} \right) + \frac{1}{3} \left( \frac{1}{2} \right)^3 + \frac{1}{5} \left( \frac{1}{2} \right)^5 + \dots \right] =$$

A.  $\log_e 3$

B.  $\log_e 4$

C.  $\log_e 2$

D.  $\log_e 5$

**Answer: A**



Watch Video Solution

$$8.2 \left[ \left( \frac{2}{3} \right) + \frac{1}{3} \left( \frac{2}{3} \right)^3 + \frac{1}{5} \left( \frac{2}{3} \right)^5 + \dots \right] =$$

A.  $\log_e 3$

B.  $\log_e 4$

C.  $\log_e 2$

D.  $\log_e 5$

**Answer: D**



**Watch Video Solution**

$$9. \frac{1}{3} + \frac{1}{3 \cdot 3^3} + \frac{1}{5 \cdot 3^5} + \frac{1}{7 \cdot 3^7} + \dots =$$

A.  $\log 2$

B.  $\frac{1}{2} \log 2$

C.  $2 \log 2$

D.  $\log (1/2)$

**Answer: B**



**Watch Video Solution**

$$10. \frac{1}{5} + \frac{1}{3.5^3} + \frac{1}{5.5^5} + \frac{1}{7.5^7} + \dots =$$

A.  $\log (3/2)$

B.  $\frac{1}{2} \log(3/2)$

C.  $2 \log(3/2)$

D.  $\log(2/3)$

**Answer: B**



**Watch Video Solution**

11.  $1 + \frac{1}{3 \cdot 2^2} + \frac{1}{5 \cdot 2^4} + \frac{1}{7 \cdot 2^6} + \dots =$

A.  $\log_e 2$

B.  $\log_e 3$

C.  $\frac{1}{2} \log_e 2$

D.  $\frac{1}{2} \log_e 3$

**Answer: B**



**Watch Video Solution**

**12.**  $\log_4 2 - \log_8 2 + \log_{16} 2 - \dots =$

- A.  $e^2$
- B.  $\log_2$
- C.  $+\log_e 3$
- D.  $1 - \log_e 2$

**Answer:** D



**Watch Video Solution**

**13.**  $\log_e 2 =$

- A.  $1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots$
- B.  $1 - \frac{1}{2} - \frac{1}{3} - \frac{1}{4} - \dots$
- C.  $\frac{1}{1.2} + \frac{1}{3.4} + \frac{1}{5.6} + \dots$
- D.  $\frac{1}{1.2} + \frac{1}{2.3} + \frac{1}{3.4} + \dots$

**Answer: C**



**Watch Video Solution**

**14.**  $\frac{1}{1.2} + \frac{1}{3.4} + \frac{1}{5.6} + \dots$

A.  $\log_e 2$

B.  $\log_e 3$

C.  $\log_e 5$

D.  $\log_e 2 - 1/2$

**Answer: A**



**Watch Video Solution**

**15.**  $\frac{1}{2.3} + \frac{1}{4.5} + \frac{1}{6.7} + \frac{1}{8.9} + \dots$

A.  $\log\left(\frac{2}{e}\right)$

B.  $\log\left(\frac{e}{2}\right)$

C.  $\log(2e)$

D.  $e - 1$

**Answer: B**



**Watch Video Solution**

16.  $\frac{1}{1.2} - \frac{1}{2.3} + \frac{1}{3.4} - \frac{1}{4.5} + \dots =$

A.  $\log_e 2 - 1$

B.  $2 \log_e 2 - 1$

C.  $2 \log_e 2$

D.  $2 \log_e 2 + 1$

**Answer: B**



**Watch Video Solution**

$$17. \frac{1}{1.3} + \frac{1}{2.5} + \frac{1}{3.7} + \frac{1}{4.9} + \dots =$$

A.  $2 \log_e 2.2$

B.  $2 - 2 \log_e 2$

C.  $2 \log_e 4$

D.  $\log_e 4$

**Answer: B**



**Watch Video Solution**

$$18. \frac{1}{1.2.3} + \frac{1}{3.4.5} + \frac{1}{5.6.7} + \dots$$

A.  $\log_e 2$

B.  $\log_e 3$

C.  $\log_e 5$

D.  $\log_e 2 - 1/2$

**Answer: D**



**Watch Video Solution**

19.  $\frac{5}{1 \cdot 2 \cdot 3} + \frac{7}{3 \cdot 4 \cdot 5} + \frac{9}{5 \cdot 6 \cdot 7} + \dots =$

A.  $\log_e \left( \frac{8}{e} \right)$

B.  $\log_e \left( \frac{2}{e} \right)$

C.  $\log_e \left( \frac{6}{5} \right)$

D.  $2 - \log_e 2$

**Answer: A**



**Watch Video Solution**

20. The sum of the series  $\frac{1}{1 \cdot 3 \cdot 5} + \frac{1}{3 \cdot 5 \cdot 7} + \frac{1}{5 \cdot 7 \cdot 9} + \dots$  is

A.  $3 \log_e x$

B.  $1/8$

C.  $1/9$

D.  $1/12$

**Answer: D**



**Watch Video Solution**

**21.** Sum of the series  $\frac{1}{4.5.6} + \frac{1}{5.6.7} + \frac{1}{6.7.8} + \dots$  upto  $\infty$  is

A.  $\frac{1}{20} \log_e e$

B.  $\frac{1}{10} \log_e e$

C.  $\frac{1}{40} \log_e e$

D. none of these

**Answer: C**



**Watch Video Solution**

$$22. \frac{1}{1.3} + \frac{1}{2}\left(\frac{1}{3.5}\right) + \frac{1}{3}\left(\frac{1}{5.7}\right) + \dots =$$

A.  $\log_e\left(\frac{8}{e}\right)$

B.  $\log_e\left(\frac{2}{e}\right)$

C.  $\log_e\left(\frac{6}{5}\right)$

D.  $2 - \log_e 2$

**Answer: B**



**Watch Video Solution**

$$23. \frac{2}{3} + \frac{1}{2}\left(\frac{2}{3}\right)^2 + \frac{1}{3}\left(\frac{2}{3}\right)^3 + \dots =$$

A.  $\log_e 2$

B.  $\log_e 3$

C.  $\log_e 5$

D.  $\log_e(3/2)$

**Answer: B**



**Watch Video Solution**

**24.**  $\frac{1}{5} + \frac{1}{2.5^2} + \frac{1}{3.5^3} + \frac{1}{4.5^4} + \dots =$

A.  $\log_e\left(\frac{8}{e}\right)$

B.  $\log_e\left(\frac{2}{e}\right)$

C.  $\log_e\left(\frac{5}{4}\right)$

D.  $2 - \log_e 2$

**Answer: C**



**Watch Video Solution**

**25.** The sum of the series  $\frac{1}{2}\left(\frac{1}{5}\right)^2 + \frac{2}{3}\left(\frac{1}{5}\right)^3 + \frac{3}{4}\left(\frac{1}{5}\right)^4 + \dots$  is

A.  $\frac{1}{4} + \log_e\left(\frac{4}{5}\right)$

B.  $\frac{1}{3} + \log_e\left(\frac{2}{3}\right)$

C.  $\frac{1}{2} + \log_e\left(\frac{3}{2}\right)$

D. none of these

**Answer: A**



**Watch Video Solution**

26.  $\frac{1}{2} - \frac{1}{2} \cdot \frac{1}{2^2} + \frac{1}{3} \cdot \frac{1}{2^3} - \frac{1}{4} \cdot \frac{1}{2^4} + \dots =$

A.  $\log_e 2$

B.  $\log_e 3$

C.  $\log_e 5$

D.  $\log_e(3/2)$

**Answer: D**



**Watch Video Solution**

27.  $\frac{1}{2} + \frac{3}{2} \cdot \frac{1}{4} + \frac{5}{3} \cdot \frac{1}{8} + \frac{7}{4} \cdot \frac{1}{16} + \dots =$

A.  $\log_e\left(\frac{8}{e}\right)$

B.  $\log_e\left(\frac{2}{e}\right)$

C.  $\log_e\left(\frac{6}{5}\right)$

D.  $2 - \log_e 2$

**Answer: D**



**Watch Video Solution**

28. Sum of the series

$$\frac{1}{2}\left(\frac{1}{2} + \frac{1}{3}\right) - \frac{1}{4}\left(\frac{1}{2^2} + \frac{1}{3^2}\right) + \frac{1}{6}\left(\frac{1}{2^3} + \frac{1}{3^3}\right) - \dots \text{ is}$$

A.  $\log_e 3$

B.  $\frac{1}{2}\log_e 2$

C.  $\log_e \frac{3}{2}$

D.  $\log_e \frac{2}{3}$

**Answer: B**



**Watch Video Solution**

**29.**  $\frac{a-b}{a} + \frac{1}{2}\left(\frac{a-b}{a}\right)^2 + \frac{1}{3}\left(\frac{a-b}{a}\right)^3 + \dots =$

A.  $\log_e(a/b)$

B.  $\log_e(b/a)$

C.  $\log_e(a+b)$

D.  $\log_e(a-b)$

**Answer: A**



**Watch Video Solution**

**30.**  $(a-1) - \frac{1}{2}(a-1)^2 + \frac{1}{3}(a-1)^3 - \frac{1}{4}(a-1)^4 + \dots =$

A.  $\log a$

B.  $\log(a - 1)$

C.  $\log(1 + a)$

D.  $\log(1 - a)$

**Answer: A**



**Watch Video Solution**

**31.**  $e^{x-1} - \frac{1}{2}(x-1)^2 + \frac{1}{3}(x-1)^3 - \frac{1}{4}(x-1)^4 + \dots =$

A.  $\log(x - 1)$

B.  $\log x$

C. x

D. none of these

**Answer: C**



**Watch Video Solution**

**32.** If  $S = \frac{(b-1) - \frac{1}{2}(b-1)^2 + \frac{1}{3}(b-1)^3 - \dots}{(a-1) - \frac{1}{2}(a-1)^2 + \frac{1}{3}(a-1)^3 - \dots}$ , then  $S =$

A.  $\log_e b$

B.  $\log_a b$

C.  $\log_e a$

D.  $\log_b a$

**Answer:** B



**Watch Video Solution**

**33.**  $\frac{1}{x+1} + \frac{1}{2(x+1)^2} + \frac{1}{3(x+1)^3} + \dots =$

A.  $\log\left[\frac{x}{x+1}\right]$

B.  $\log\left[\frac{x+1}{x}\right]$

C.  $\log\left[\frac{x+1}{x-1}\right]$

D.  $\log\left[\frac{x-1}{x+1}\right]$

**Answer: B**



**Watch Video Solution**

$$34. \frac{x}{x+1} + \frac{1}{2} \left( \frac{x}{x+1} \right)^2 + \frac{1}{3} \left( \frac{x}{x+1} \right)^3 + \dots =$$

A.  $\log(1+x)$

B.  $\log(1-x)$

C.  $\log x$

D. none

**Answer: A**



**Watch Video Solution**

$$35. \frac{2ax}{a^2+x^2} + \frac{1}{3} \left( \frac{2ax}{a^2+x^2} \right)^3 + \frac{1}{5} \left( \frac{2ax}{a^2+x^2} \right)^5 + \dots =$$

A.  $\log \frac{a+x}{a-x}$

B.  $\log \frac{a-x}{a+x}$

C.  $\log \frac{x+a}{x-a}$

D.  $\log \frac{x-a}{x+a}$

**Answer: A**



**Watch Video Solution**

36.  $\left( \frac{2n}{n^2+1} \right) + \frac{1}{3} \left( \frac{2n}{n^2+1} \right)^3 + \frac{1}{5} \left( \frac{2n}{n^2+1} \right)^5 + \dots =$

A.  $\log \frac{n+1}{n-1}$

B.  $\log \frac{n-1}{n+1}$

C.  $\log \frac{1+n}{1-n}$

D.  $\log \frac{1-n}{1+n}$

**Answer: A**



**Watch Video Solution**

$$37. \frac{1}{2x-1} + \frac{1}{3} \cdot \frac{1}{(2x-1)^3} + \frac{1}{5} \cdot \frac{1}{(2x-1)^5} + \dots =$$

A.  $\frac{1}{2} \log \cdot \frac{x}{x-1}$

B.  $\frac{1}{2} \log \cdot \frac{x-1}{x}$

C.  $\frac{1}{2} \log \cdot \frac{x}{1-x}$

D.  $\frac{1}{2} \log \cdot \frac{1-x}{2}$

**Answer: A**



**Watch Video Solution**

$$38. \frac{1}{2x+1} + \frac{1}{3} \cdot \frac{1}{(2x+1)^3} + \frac{1}{5} \cdot \frac{1}{(2x+1)^5} + \dots =$$

A.  $\frac{1}{2} \log \cdot \frac{x}{x+1}$

B.  $\log \cdot \frac{x}{x+1}$

C.  $\frac{1}{2} \log \cdot \frac{x}{x-1}$

D.  $\frac{1}{2} \log \cdot \frac{x+1}{x}$

**Answer: D**



**Watch Video Solution**

39.  $\frac{1}{2n^2 - 1} + \frac{1}{3(2n^2 - 1)^3} + \frac{1}{5(2n^2 - 1)^5} + \dots =$

A.  $\log \frac{n^2}{n^2 - 1}$

B.  $\frac{1}{2} \log \frac{n^2}{n^2 - 1}$

C.  $\log \frac{n^2 - 1}{n^2}$

D.  $\frac{1}{2} \log \frac{n^2 - 1}{n^2}$

**Answer: B**



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40. If  $x > 0$  then  $\frac{x - 1}{x + 1} + \frac{1}{2} \frac{x^2 - 1}{(x + 1)^2} + \frac{1}{3} \frac{x^3 - 1}{(x + 1)^3} + \dots =$

A.  $\log(1 + x)$

B.  $\log(1 - x)$

C.  $\log(x - 1)$

D.  $\log x$

**Answer: D**



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**41.**  $\log(1 + x + x^2 + \dots \infty) =$

A.  $x + \frac{x^2}{2} + \frac{x^3}{3} + \frac{x^4}{4} + \dots \infty$

B.  $x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} \dots \infty$

C.  $1 + x + \frac{x^2}{2} + \frac{x^3}{3} + \frac{x^4}{4} + \dots \infty$

D.  $1 - x + \frac{x^2}{2} - \frac{x^3}{3} + \frac{x^4}{4} + \dots \infty$

**Answer: A**



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**42.** If  $|x| < 1$  then  $\frac{1}{2}x^2 + \frac{2}{3}x^3 + \frac{3}{4}x^4 + \dots =$

A.  $\frac{x}{1-x} + \log(1-x)$

B.  $\frac{x}{1-x} + \log(1+x)$

C.  $\frac{x}{1+x} + \log(1+x)$

D.  $\frac{x}{1+x} + \log(1-x)$

**Answer:** A



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**43.**  $\frac{a-1}{a+1} + \frac{1}{3}\left(\frac{a-1}{a+1}\right)^3 + \frac{1}{5}\left(\frac{a-1}{a+1}\right)^5 + \dots =$

A.  $\log a$

B.  $\frac{1}{2}\log a$

C.  $2\log a$

D.  $\log(1/a)$

**Answer: B**



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**44.** If  $|x| < 1$  and  $y = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$ , then  $x =$

A.  $y + \frac{y^2}{2} + \frac{y^3}{3} + \dots$

B.  $y - \frac{y^2}{2} + \frac{y^3}{3} - \frac{y^4}{4} + \dots$

C.  $y + \frac{y^2}{2!} + \frac{y^3}{3!} + \dots$

D.  $y - \frac{y^2}{2!} + \frac{y^3}{3!} - \frac{y^4}{4!} + \dots$

**Answer: C**



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**45.** If  $y = x + \frac{x^2}{2} + \frac{x^3}{3} + \dots \infty$ , then  $x =$

A.  $y - \frac{y^2}{2!} + \frac{y^3}{3!} - \frac{y^4}{4!} +$

- B.  $y + \frac{y^2}{2!} + \frac{y^3}{3!} + \frac{y^4}{4!} +$
- C.  $1 - y + \frac{y^2}{2!} - \frac{y^3}{3!} + \frac{y^4}{4!} - \dots$
- D.  $1 + y + \frac{y^2}{2!} + \frac{y^3}{3!} + \frac{y^4}{4!} + \dots$

**Answer: A**



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46.  $|a| < 1, b = \sum_{k=1}^{\infty} \frac{a^k}{k} \Rightarrow a =$

- A.  $\sum_{k=1}^{\infty} \frac{(-1)^k b^k}{k}$
- B.  $\sum_{k=1}^{\infty} \frac{(-1)^{k-1} b^k}{k!}$
- C.  $\sum_{k=1}^{\infty} \frac{(-1)^k b^k}{(k-1)!}$
- D.  $\sum_{k=1}^{\infty} \frac{(-1)^{k-1} b^k}{(k+1)!}$

**Answer: B**



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**47.** If  $y = \frac{1}{2x^2 - 1}$  then  $y + \frac{y^3}{3} + \frac{y^5}{5} + \dots =$

- A.  $\frac{1}{x^2} + \frac{1}{2x^4} + \frac{1}{3x^6} + \dots$
- B.  $2\left(\frac{1}{x^2} + \frac{1}{2x^4} + \frac{1}{3x^6} + \dots\right)$
- C.  $\frac{1}{2}\left(\frac{1}{x^2} + \frac{1}{2x^4} + \frac{1}{3x^6} + \dots\right)$
- D.  $-\left(\frac{1}{x^2} + \frac{1}{2x^4} + \frac{1}{3x^6} + \dots\right)$

**Answer: C**



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**48.**  $\frac{1}{x^2} + \frac{1}{2x^4} + \frac{1}{3x^6} + \dots =$

- A.  $2 \log x - \log(x + 1) - \log(x - 1)$
- B.  $\log(x + 1) + \log(x - 1) - 2 \log x$
- C.  $2 \log x + \log(x + 1) - \log(x - 1)$
- D.  $2 \log x - \log(x + 1) + \log(x - 1)$

**Answer: A**



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**49.**  $\frac{1}{1 \cdot 3} \cdot \frac{1}{2} + \frac{1}{2 \cdot 4} \cdot \frac{1}{2^2} + \frac{1}{3 \cdot 5} \cdot \frac{1}{2^3} + \dots =$

A.  $\frac{5}{4} + \frac{3}{2} \log \frac{1}{2}$

B.  $\frac{4}{4} + \frac{3}{2} \log 2$

C.  $\frac{4}{5} + \frac{3}{2} \log 2$

D.  $\frac{4}{5} + \frac{2}{3} \log \left( \frac{1}{2} \right)$

**Answer: A**



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**50.**  $3x - \frac{5x^2}{2} + \frac{9x^3}{3} - \frac{17x^4}{4} + \dots + (-1)^{n-1} \frac{(2^n + 1)}{2} x^n + \dots =$

A.  $\log(1 + 4x + 3x^2)$

B.  $\log_e(1 + 3x + 2x^2)$

C.  $\log(1 + 5x + 6x^2)$

D.  $\log_e(1 + 6x + 5x^2)$

**Answer: B**



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51.  $5x - \frac{13}{2}x^2 + \frac{35}{3}x^3 - \frac{97}{4}x^4 + \dots =$

A.  $\log(1 + 4x + 3x^2)$

B.  $(1 + 3x + 2x^2)$

C.  $\log(1 + 5x + 6x^2)$

D.  $(1 + 6x + 5x^2)$

**Answer: C**



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**52.** The coefficient of  $x^n$  in the expansion of  $\log_e(1 + 3x + 2x^2)$  is

A.  $(-1)^{n-1}(1 + 2^n)/n$

B.  $(-1)^n(1 + 2^{n-1})/n$

C.  $(-1)^{n-1}2^n/n$

D.  $(-1)^n(2^n - 1)/n$

**Answer:** A



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**53.** The coefficient of  $x^n$  in the expansion of  $\log(1 - 5x + 6x^2)^2$  is

A.  $\frac{2^n + 3^n}{n}$

B.  $\frac{2^n - 3^n}{n}$

C.  $\frac{3^n - 2^n}{2}$

D.  $\frac{-3^n - 2^n}{n}$

**Answer: D**



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54. If  $n = 3m$  then the coefficient of  $x^n$  in the expansion of  $\log(1 + x + x^2)$  is

A.  $n$

B.  $1/n$

C.  $2/n$

D.  $-2/n$

**Answer: B**



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55. If  $n = 3m$  then the coefficient of  $x^n$  in the expansion of  $\log(1 + x + x^2)$  is

A. n

B.  $1/n$

C.  $2/n$

D.  $-2/n$

**Answer: D**



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56. The expansion of  $\log \frac{1+x+x^2}{1-x+x^2}$  as ascending powers of x is

A.  $x - \frac{2}{3}x^3 + \frac{x^5}{5} + \frac{x^7}{7} - \frac{2}{9}x^9 \dots$

B.  $x + \frac{2}{3}x^3 + \frac{x^5}{5} + \frac{x^7}{7} + \frac{2}{9}x^9 \dots$

C.  $2 \left[ x - \frac{2}{3}x^3 + \frac{x^5}{5} + \frac{x^7}{7} - \frac{2}{9}x^9 \dots \right]$

D.  $2 \left[ x + \frac{2}{3}x^3 + \frac{x^5}{5} + \frac{x^7}{7} + \frac{2}{9}x^9 \dots \right]$

**Answer: C**



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57. If  $|x| < 1$ , the coefficient of  $x^3$  in the expansion of  $\log(1 + x + x^2)$  in ascending power of x, is

A.  $2/3$

B.  $4/3$

C.  $-2/3$

D.  $-4/3$

**Answer: C**



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58. If x is very small and neglecting  $x^3$  and higher powers of x then the expansion of  $\log(1 + x^2) - \log(1 + x) - \log(1 - x)$  as ascending powers of x is

A.  $2x$

B.  $2x^2$

C.  $1 + 2x$

D.  $1 - x^2$

**Answer: B**



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59.  $\frac{x}{1.2} + \frac{x^2}{3.4} + \frac{x^3}{5.6} + \dots =$

A.  $\frac{\sqrt{x}}{2} \log \frac{1 + \sqrt{x}}{1 - \sqrt{x}} + \frac{1}{2} \log(1 - x)$

B.  $\frac{\sqrt{x}}{2} \log \frac{1 - \sqrt{x}}{1 + \sqrt{x}} + \log(1 - x)$

C.  $\frac{\sqrt{x}}{2} \log \frac{1 + \sqrt{x}}{1 - \sqrt{x}} + \log(x - 1)$

D.  $\frac{\sqrt{x}}{2} \log \frac{1 - \sqrt{x}}{1 + \sqrt{x}} + \log(x - 1)$

**Answer: A**



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$$60. \sum_{n=1}^{\infty} \frac{x^n}{n+2} =$$

A.  $\frac{1}{x^2} \log(1-x)$

B.  $\frac{1}{x^2} \log(1+x)$

C.  $-\frac{1}{x^2} \log(1-x) - \frac{1}{x} - \frac{1}{2}$

D.  $\frac{1}{x^2} \log(1+x)$

**Answer: C**



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$$61. \sum_{n=1}^{\infty} \frac{x^{n+1/2}}{n+1} =$$

A.  $\frac{1}{\sqrt{x}} [x + \log(1-x)]$

B.  $-\frac{1}{\sqrt{x}} [x + \log(1-x)]$

C.  $\frac{1}{x} [x + \log(1-x)]$

D.  $-\frac{1}{x} [x + \log(1-x)]$

**Answer: B**



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$$62. \sin^2 \theta + \frac{1}{2} \sin^4 \theta + \frac{1}{3} \sin^6 \theta + \dots =$$

A.  $2 \log \sin \theta$

B.  $2 \log \cos \theta$

C.  $2 \log \sec \theta$

D.  $2 \log \cos ec\theta$

**Answer: C**



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$$63. \cos^2 \theta + \frac{1}{2} \cos^4 \theta + \frac{1}{3} \cos^6 \theta + \dots =$$

A.  $2 \log \sin \theta$

B.  $2 \log \cos \theta$

C.  $2 \log \sec \theta$

D.  $2 \log \cos ec\theta$

**Answer: D**



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$$64. \tan^2 \theta - \frac{1}{2} \tan^4 \theta + \frac{1}{3} \tan^6 \theta - \frac{1}{4} \tan^8 \theta + \dots =$$

A.  $2 \log \sin \theta$

B.  $2 \log \cos \theta$

C.  $2 \log \sec \theta$

D.  $2 \log \cos ec\theta$

**Answer: C**



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$$65. \cos \theta + \frac{1}{3} \cos^3 \theta + \frac{1}{5} \cos^5 \theta + \dots =$$

- A.  $\log \tan \theta$
- B.  $\log \cot \theta$
- C.  $\log \tan(\theta / 2)$
- D.  $\log \cot(\theta / 2)$

**Answer: D**



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$$66. \sin 2\theta + \frac{1}{3} \sin^3 2\theta + \frac{1}{5} \sin^5 2\theta + \dots =$$

- A.  $\log \tan \theta$
- B.  $\log \tan((\pi)/(4)+\theta)'$
- C.  $\log \tan((\pi)/(4)-\theta)'$
- D.  $\log \tan \frac{\theta}{2}$

**Answer: B**



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$$67. \cos 2\theta + \frac{1}{3} \cos^3 2\theta + \frac{1}{5} \cos^5 2\theta + \dots =$$

A.  $\log \tan \theta$

B.  $\log \tan\left(\frac{\pi}{4} + \theta\right)$

C.  $\log \tan\left(\frac{\pi}{4} - \theta\right)$

D.  $\log \cot \theta$

**Answer: D**



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$$68. \tan \theta + \frac{1}{3} \tan^3 \theta + \frac{1}{5} \tan^5 \theta + \dots =$$

A.  $\log \tan \theta$

B.  $\frac{1}{2} \log \tan\left(\frac{\pi}{4} + \theta\right)$

C.  $\frac{1}{2} \log \tan\left(\frac{\pi}{4} - \theta\right)$

D.  $\log \cot \theta$

**Answer: B**



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**69.** The sum of the series  $\log_4 2 - \log_8 2 + \log_{16} 2 - \dots$  is

A.  $e^2$

B.  $\log_2 2 + 1$

C.  $\log_e 3 - 2$

D.  $1 - \log_e 2$

**Answer: D**



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70. If  $x, y, z$  are three consecutive positive integers then

$$\frac{1}{2} \log_e x + \frac{1}{2} \log_e z + \frac{1}{2xz+1} + \frac{1}{3} \left( \frac{1}{2xz+1} \right)^3 + \dots =$$

A.  $\log_e x$

B.  $\log_e y$

C.  $\log_e z$

D. none

Answer: B



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### Exercise 2 Set 1

1. The coefficient of  $x^n$  in  $\frac{1+x}{1!} + \frac{(1+x)^2}{2!} + \frac{(1+x)^3}{3!} + \dots$

A. only I is true

B. only II is true

C. both I and II are true

D. neither I nor II true

**Answer: A**



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$$2. I: \frac{2}{1!} + \frac{4}{3!} + \frac{6}{5!} + \dots = e - 1$$

$$II: \frac{3}{2!} + \frac{5}{4!} + \frac{7}{6!} + \frac{9}{8!} + \dots = e - 1$$

A. only I is true

B. only II is true

C. both I and II are true

D. neither I nor II true

**Answer: B**



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$$3. I: \frac{1}{1!} + \frac{1+2}{2!} + \frac{1+2+2^2}{3!} + \dots = e^2 - e$$

$$II: \frac{2}{2!} + \frac{2+4}{3!} + \frac{2+4+6}{4!} + \dots = e$$

- A. only I is true
- B. only II is true
- C. both I and II are true
- D. neither I nor II true

**Answer: C**



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$$4. I: 2 \left[ \left( \frac{1}{3} \right) + \frac{1}{3} \left( \frac{1}{3} \right)^3 + \frac{1}{5} \left( \frac{1}{3} \right)^5 + \dots \right] = \log_e 2$$

$$II: 2 \left[ \left( \frac{1}{2} \right) + \frac{1}{3} \left( \frac{1}{2} \right)^3 + \frac{1}{5} \left( \frac{1}{2} \right)^5 + \dots \right] = \log_e 2$$

- A. only I is true
- B. only II is true

C. both I and II are true

D. neither I nor II true

**Answer: A**



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$$5. I: \frac{1}{1.2} + \frac{1}{3.4} + \frac{1}{5.6} + \dots \log_e 2$$

$$II: \frac{1}{1.2} - \frac{1}{2.3} + \frac{1}{3.4} - \frac{1}{4.5} + \dots = 2 \log_e 2 - 1$$

A. only I is true

B. only II is true

C. both I and II are true

D. neither I nor II true

**Answer: C**



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6. I : If  $y = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$  then  $x = y + \frac{y^2}{2!} + \frac{y^3}{3!} + \dots$

II : If  $y = x + \frac{x^2}{2} + \frac{x^3}{3} + \dots \infty$ , then  $x = y - \frac{y^2}{2!} + \frac{y^3}{3!} - \frac{y^4}{4!} + \dots$

- A. only I is true
- B. only II is true
- C. both I and II are true
- D. neither I nor II true

**Answer: B**



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## Exercise 2 Set 2

1.

If

$$1 + \frac{2}{1!} + \frac{4}{2!} + \frac{8}{3!} + \dots = e^a, 1 + \frac{4}{1!} + \frac{16}{2!} + \frac{64}{3!} + \dots = e^b, 1 - \frac{2}{1!} -$$

then the ascending order of a, b, c is

A. a,b,c

B. b,c,a

C. c,a,b

D. a,c,b

**Answer: C**



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**2.**

If

$$1^2 + \frac{2^2}{2!} + \frac{3^2}{3!} + \frac{4^2}{4!} + \dots = ae, \quad \frac{1^2 \cdot 2}{1!} + \frac{2^2 \cdot 3}{2!} + \frac{3^2 \cdot 4}{3!} + \dots = be, \quad \frac{1}{2!} + \frac{1}{3!} + \dots = ce$$

then the descending order of a,b,c is

A. a,b,c

B. b,a,c

C. c,a,b

D. a,c,b

**Answer: C**



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**3.** If  $a, b, c$  are the fifth terms of  $\log_e(3/2), \log_e(4/3), \log_e(6/5)$  then the ascending order of  $a, b, c$  is

A. a,b,c

B. b,c,a

C. c,a,b

D. a,c,b

**Answer: A**



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**4.**

$$\frac{3}{4} + \frac{1}{3} \left(\frac{3}{4}\right)^3 + \frac{1}{5} \left(\frac{3}{4}\right)^5 + \dots = \log_e a, \quad \frac{1}{3} + \frac{1}{3 \cdot 3^3} + \frac{1}{5 \cdot 3^5} + \frac{1}{7 \cdot 3^7} + \dots$$

If

$1 + \frac{1}{3.2^2} + \frac{1}{5.2^4} + \frac{1}{7.2^6} + \dots = \log_e c$  then the ascending order of a, b, c is

A. a,b,c

B. b,a,c

C. c,a,b

D. a,c,b

**Answer: B**



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5.  $\frac{1}{1.3} + \frac{1}{2}\left(\frac{1}{3.5}\right) + \frac{1}{3}\left(\frac{1}{5.7}\right) + \dots =$

A. a,b,c

B. b,c,a

C. c,a,b

D. a,c,b

**Answer: B**



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## Exercise 2 Set 3

### 1. Match the following

- |  |                         |
|--|-------------------------|
| I. The $(n + 1)$ th term in the expansion of $e^x$ is      | a) $\frac{(-3x)^n}{n!}$ |
| II. The $(n + 1)$ th term in the expansion of $e^{4x}$ is  | b) $\frac{(-2)^n}{n!}$  |
| III. The $(n + 1)$ th term in the expansion of $e^{-2}$ is | c) $\frac{(4x)^n}{n!}$  |
| IV. The $(n + 1)$ th term in the expansion of $e^{-3x}$ is | d) $\frac{5^n}{n!}$     |

A. c,d,a,b

B. b,a,d,c

C. c,a,b,d

D. d,c,b,a

**Answer: D**



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## 2. Match the following

I.  $1 + \frac{1}{2!} + \frac{1}{4!} + \frac{1}{6!} + \dots =$

a)  $\frac{1}{2}(e - e^{-1})$

II.  $1 - \frac{1}{3!} + \frac{1}{5!} - \dots =$

b)  $\frac{1}{2}(e - e^{-1})$

III.  $\frac{3}{2!} + \frac{5}{4!} + \frac{7}{6!} + \frac{9}{8!} + \dots =$

c)  $\frac{e}{2}$

IV.  $1 + \frac{2}{3!} + \frac{3}{5!} + \frac{4}{7!} + \dots =$

d)  $e - 1$

A. c,d,a,b

B. b,a,d,c

C. c,a,b,d

D. d,c,b,a

**Answer: B**



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- 3.
- |   |                            |
|---|----------------------------|
| I. $1 + \frac{2x}{1!} + \frac{3x^2}{2!} + \frac{4x^3}{3!} + \dots =$                          | a) $(x^2 + 7x + 8)e^x - 8$ |
| II. $1 \cdot 2 + \frac{2 \cdot 3}{1!} x + \frac{3 \cdot 4}{2!} x^2 + \dots =$                 | b) $(x + 1)e^x$            |
| III. $\frac{3 \cdot 5}{1!} x + \frac{4 \cdot 6}{2!} x^2 + \frac{5 \cdot 7}{3!} x^3 + \dots =$ | c) $(x^2 + 4x + 2)e^x$     |

A. a,c,b

B. b,c,a

C. c,a,b

D. c,b,a

**Answer: B**



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Match the following.

- 4.
- |  |               |
|--|---------------|
| I. $2 \left[ \left( \frac{1}{3} \right) + \frac{1}{3} \left( \frac{1}{3} \right)^3 + \frac{1}{5} \left( \frac{1}{3} \right)^5 + \dots \right] =$   | a) $\log_e 3$ |
| II. $2 \left[ \left( \frac{1}{2} \right) + \frac{1}{3} \left( \frac{1}{2} \right)^3 + \frac{1}{5} \left( \frac{1}{2} \right)^5 + \dots \right] =$  | b) $\log_e 5$ |
| III. $2 \left[ \left( \frac{2}{3} \right) + \frac{1}{3} \left( \frac{2}{3} \right)^3 + \frac{1}{5} \left( \frac{2}{3} \right)^5 + \dots \right] =$ | c) $\log_e 2$ |

A. a,c,b

B. b,c,a

C. c,a,b

D. c,b,a

**Answer: C**



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- Match the following.
5. I.  $\frac{1}{1 \cdot 3} + \frac{1}{2} \left( \frac{1}{3 \cdot 5} \right) + \frac{1}{3} \left( \frac{1}{5 \cdot 7} \right) + \dots =$       a)  $\frac{1}{2} \log_e 2$   
II.  $\frac{1}{2} \left( \frac{1}{5} \right)^2 + \frac{2}{3} \left( \frac{1}{5} \right)^3 + \frac{3}{4} \left( \frac{1}{5} \right)^4 + \dots$       b)  $\log_e \left( \frac{2}{e} \right)$   
III.  $\frac{1}{2} \left( \frac{1}{2} + \frac{1}{3} \right) - \frac{1}{4} \left( \frac{1}{2^2} + \frac{1}{3^2} \right) + \frac{1}{6} \left( \frac{1}{2^3} + \frac{1}{3^3} \right) - \dots$       c)  $\frac{1}{4} + \log_e \left( \frac{4}{5} \right)$

A. a,c,b

B. b,c,a

C. c,a,b

D. c,b,a

**Answer: B**



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## Exercise 2 Set 4

1. A : The value of e lies between 2 and 3.

$$R : e = 1 + \frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \dots$$

- A. Both A and R are true and R is the correct explanation of A
- B. Both A and R are true but R is not correct explanation of A
- C. A is true but R is false
- D. A is false but R is true

Answer: A



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$$2. A : \log_e 3 + \frac{(\log_e 3)^2}{2!} + \frac{(\log_e 3)^3}{3!} + \dots = 2$$

R : If

$$x, a \in R \text{ and } a > 0 \text{ then } a^x = 1 + x \log_e a + \frac{x^2}{2!} (\log_e a)^2 + \frac{x^3}{3!} (\log_e a)^3$$

- A. Both A and R are true and R is the correct explanation of A
- B. Both A and R are true but R is not correct explanation of A
- C. A is true but R is false
- D. A is false but R is true

**Answer: A**



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3. A :  $(3^2)/(2!) + (3^4)/(4!) + (3^6)/(6!) + \dots = \cosh 3 - 1.$ " "R:  $\cosh x = 1 + (x^2)/(2!) + (x^4)/(4!) + \dots$

- A. Both A and R are true and R is the correct explanation of A
- B. Both A and R are true but R is not correct explanation of A

C. A is true but R is false

D. A is false but R is true

**Answer: A**



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4. A:  $\frac{1}{2} - \frac{1}{2} \cdot \frac{1}{2^2} + \frac{1}{3} \cdot \frac{1}{2^3} - \frac{1}{4} \cdot \frac{1}{2^4} + \dots = \log_e\left(\frac{3}{2}\right)$

R :  $\log_e(1 + x) = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$

A. Both A and R are true and R is the correct explanation of A

B. Both A and R are true but R is not correct explanation of A

C. A is true but R is false

D. A is false but R is true

**Answer: A**



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$$5. A : \frac{a-b}{a} + \frac{1}{2} \left( \frac{a-b}{a} \right)^2 + \frac{1}{3} \left( \frac{a-b}{a} \right)^3 + \dots = \log_e \left( \frac{a}{b} \right)$$
$$R : \log_e(1-x) = -x - \frac{x^2}{2} - \frac{x^3}{3} - \frac{x^4}{4} - \dots$$

- A. Both A and R are true and R is the correct explanation of A
- B. Both A and R are true but R is not correct explanation of A
- C. A is true but R is false
- D. A is false but R is true

**Answer:** A



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