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## MATHS

## BOOKS - NCERT MATHS (ENGLISH)

## INTRODUCTION TO THREE

## DIMENSIONAL GEOMETRY

Short Answer Type Questions

## 1. Locate the following points

$\begin{array}{ll}\text { (i) }(1,-1,3) & \text { (ii) }(-1,2,4)\end{array}$
(iii) $(-2,-4,-7) \quad$ (iv) $(-4,2,-5)$

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2. Name the octant in which each of the following points lie.
(i)(1,2,3), (ii) (4,-2,3)
$(4,-2,-5),(i v)(4,2,-5)$,

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3. If $A, B, C$ be the feet of perpendiculars from a point p on the $\mathrm{X}, \mathrm{Y}$ and Z - axes repsectively, then find the coordinates of $\mathrm{A}, \mathrm{Band} \mathrm{C}$ in each of the following where the point $P$ is
(i) $\mathrm{A}(3,4,2)$ (ii) $\mathrm{B}(-5,3,7)$
(iii) C (4,-3,-5)

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4. If $A, B$, and $C$ be the feet of perpendiculars
from a point $P$ on the $X Y, Y Z$, and $Z X$ - planes
respectively, then find the coordinates of $A, B$
and $C$ in each of the following where the point $P$ is .
(i) $(3,4,5)$ (ii) $(-5,3,7)$
(iii) $(4,-3,-5)$

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5. How far part are the points ( $2,0,0$ ) and $(-3,0,0)$ ?

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## 6. Find the distance from the origin to ( $6,6,7$ ).

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7. Show that, if $x^{2}+y^{2}=1$, then the point $\left(x, y, \sqrt{1-x^{2}-y^{2}}\right)$ is at is distance 1 unit

## form the origin.

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8. Show that the point $A(1,-1,3), B(2,-4,5)$ and $C$
( $5,-13,11$ ) are collinear.

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9. Three consective vertices of a parallelogram
$A B C D$ are $A(6,-2,4), B(2,4,-8)$ and $C(-2,2,4)$.

Find the condinates of the following

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10. Show that the $\Delta A B C$ with vertices $\mathrm{A}(0,4$,
1), $B(2,3,-1)$ and $C(4,5,0)$ is right angled.

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11. find the third vertex of triangle whose centroid is origin and two vertices are $(2,4,6)$ and (0,-2,5)

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12. Find the centroid of the triangle mid points
of whose sides are
$(1,2,-3),(3,0,1)$ and $(-1,1,4)$

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13. The mid points of the sides of a triangle are
$(5,7,11),(0,8,5)$ and $(2,3,-1)$ Find its
vertices and hence find centroid.

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14. If the vertices of a parallelogram $A B C D$ are
$A(1,2,3)$. $B(-1,-2,-1)$ and $C(2,3,2)$ then find the fourth vertex D .

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15. Find the coordinates of the points which trisect the line segment $A B$, given that
$A(2,1,-3)$ and $B(5,-8,3)$

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16. If the origin is the centroid of a triangle

ABC having
$A(a, 1,3), B(-2, b,-5)$ and $C(4,7, c)$
find the values of $a, b, c$.

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17. If $A(2,2,-3) B(5,6,9), C(2,7,9)$ be the vertices of a triangle. The internal bisector of the angle
$A$ meets $B C$ at the point $D$, then find the coordinates of $D$.

## Long Answer Type Questions

1. Show that the three points
$A(2,3,4), B(-1,2,-3)$ and $C(-4,1,-10)$
are collinear and find the ratio in which $C$ divides $A B$.

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2. The mid-points of the sides of a triangle are
$(1,5,-1),(0,4,-2)$ and ( $2,3,4)$. Find its vertices.
3. Prove that the points $(0,-1,7),(2,1,-9)$ and $(6,5,-13)$ are collinear. Find the ratio in which the frist point divides the join of the other two.

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4. What are the coordinate of the vertices of a
cube whose edge is 2 units, one of whose
vertices coincides with the origin and three edge passing through the origin coincides with the positive direction of the axis $\theta$ through the origin.

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## Objective Type Questions

1. The distance of point $p(3,4,5)$ from the YZplane is
A. 3 units
B. 4 units
C. 5 units
D. 15 units

Answer: A

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2. The length of the perpendicular drawn from
the point $P(3,4,5)$ on $y$-axis is
A. $\sqrt{41}$
B. $\sqrt{34}$
C. 5
D. none of these

Answer: B

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3. Distance of the point $(3,4,5)$ from the origin
$(0,0,0)$ is
A. $\sqrt{50}$
B. 3
C. 4
D. 5

Answer: A

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4. If the distance between the points ( $a, 0,1$ )
and $(0,1,2)$ is $\sqrt{27}$ then the value of $a$ is
A. 5
B. $\pm 5$
C. -5
D. none of these

Answer: B

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5. $X$-axis is the intersection of two planes.
A. $X Y$ and $X Z$

## B. YZ and ZX

C. $X Y$ and $Y Z$
D. none of these

Answer: a

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6. Write the equation which represents y axis.
A. $x=0, y=0$
B. $y=0$ and $z=0$

## C. $\mathrm{z}=0, \mathrm{x}=0$

D. none of these

## Answer: c

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## 7. the point ( $-2,-3,-4$ ) lies in the

A. first octant
B. seventh octant
C. second octant
D. eight octant

Answer: B

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8. The plane parallel to YZ- plane is perpendicular to
A. $X$-axis
B. $Y$-axis
C. Z-axis

## D. none of these

## Answer: a

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9. What is the locus of a point $(x, y, z)$ for which $y=0, z=0$ ?
A. equation of $X$ - axis
B. equation of $y$-axis
C. equation at Z-axis

## D. none of these

## Answer: a

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10. The locus of a point for which $\mathrm{x}=0$ is
A. XY - plane
B. YZ-plane
C. ZX- plane
D. none of these

Answer: B

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11. If a parallelopiped is formed by planes drawn through the points ( $5,8,10$ ) and ( $3,6,8$ ) parallel to the coordinate planes, then the length of diagonal of the parallelopiped is
A. $2 \sqrt{3}$
B. $3 \sqrt{2}$
C. $\sqrt{2}$

## D. $\sqrt{3}$

## Answer: a

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12. $L$ is the foot of the perpendicular drawn
from a point $p(3,4,5)$ on the $X Y$ - plane. The coordinates of point $L$ are
A. 3,0,0
B. $0,4,5$
C. 3,0,5
D. none of these

## Answer: D

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13. $L$ is the foot of the perpendicular drawn
from a point $(3,4,5)$ on $X$-axis. The coordinates of $L$ are.
A. 3,0,0
B. $0,4,0$
C. 0,0,5
D. none of these

Answer: A

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## Fillers

1. The three axes $O X, O Y$ and $O Z$ determine
2. The three planes, determine a rectangular parallelopiped which has .......... Of rectangular faces.

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3. The coordiantes of a point are the perpendicular distance from the ..... On the respectives axes.

## View Text Solution

4. The Three coordiantes planes divide the space into ....... Parts.

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5. If a point $P$ lies in YZ- plane, then the coordinates of a point on YZ-plane is the form.

## 6. The equation of YZ- plane is

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7. If the point $P$ lies on $Z$ - axis, then coordinates of $p$ are of the form

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8. The equation of $Z$ - axis , are..............
9. A line is parallel to $X Y$ - plane if all the points on the line have equal

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10. A line is parallel to $X$-axis, if all the points on
the line have equal.

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11. $45 x=a$ represent a plane parallel to

## D View Text Solution

12. A plane is parallel to YZ-plane, so it is perpendicular tio

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13. The length of the longest piece of a string
that can be stetched straight in a rectangular
room whose dimensions are 10,13 and 8 units are

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14. If the distance between the points
$P(a, 2,1)$ and $Q(1,-1,1)$ is 5 units find the value of $a$.

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15. The coordinates of the mid points of sides
$\mathrm{AB}, \mathrm{BC}$ and CA of $A B C$ are
$D(1,2,-3), E(3,0,1)$ and $F(-1,1,-4)$ respectively. Write the coordinates of its centroid.

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16. Match each item given under the column I to its correct answer given under column II.

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| :---: | :---: |
| (1) in-xt-plase | (a) ist octant |
| (a) Pount (2,3,4) lies in the | (b) $r 2$-plane |
| (ii) Locus of the pomets hiving $x$ coordinate 0 is | (c) $z$-coordinste is zero |
| (v) A line is paraliel to $x$-axis if and only | (d) 2 -axis |
| (v) $\quad X=0 \quad y=0$ taken together will represent the | (e) plane parallel to $X Y$-plane |
| (w) $z=6$ represent the plane | (i) Yall the points on the line hive equal y and $z$-coondinutes |
| (vi) Plines $x=0, Y=0$ represent the line | (i) from the point on the respective |
| (vi) Coordinates of a point are the distances from the orign to the feet of perpendiculars | (i) parallet to 2 -ais |
| (ix) A ball is the solid region in the space enclosed by a | (i) cisc |
| (w) Region in the plane enclosed by a circle is lonown as a | (i) sphere |

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