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India's Number 1 Education App

## MATHS

## BOOKS - NCERT MATHS (ENGLISH)

## SETS

Short Answers Type Questions

1. Write the following sets in the roaster from.
(i) $A=\{x: x \in R, 2 x+11=15\}$
(ii) $B=\left\{x \mid x^{2}=x, x \in R\right\}$
$\mathrm{C}=\{x \mid x$ is a positive factor of a prime number p$\}$
2. If $Y=\left\{x \mid x\right.$ is a positive factor of the number $2^{p-1}\left(2^{p}-1\right)$ where $2^{p}-1$ is a prime number\} Write Y in roaster form.

## D Watch Video Solution

3. If $L=\{1,2,3,4\}, M=\{3,4,5,6\}$ and $N=\{1,3,5\}$, then verify that $L-(M \cup N)=(L-M) \cap(L-N)$.

## D Watch Video Solution

4. If $A$ and $B$ are subsets of the universal set $U$, then slow that
(i) $A \subset A \cup B$, (ii) $A \subset B \Leftrightarrow A \cup B=B$
(iii) $(A \cap B) \subset A$

## (D) Watch Video Solution

5. Give that $N=\{1,2,3, \ldots \ldots \ldots, 100\}$. The, write
(i) the subset of N whose elements are even numbers.
(ii) the subset of N whose elements are perfect square numbers.

## - Watch Video Solution

6. If $X=\{1,2,3\}$, if n represents any member of X , write the following sets containing all numbers represented by
(i) $4 n$, (ii) $n+6$, (iii) $\frac{n}{2}$, (iv) $n-1$

## D Watch Video Solution

7. If $y=\{1,2,3, \ldots \ldots, 10\}$ and a represents any element of Y , write the following sets, containing all the elements satisfying the given conditions,
(i) $a \in Y$ but $a^{2} \notin Y$
(ii) $a+1=6, a \in Y$
(iii) a is less than 6 and $a \in Y$

## D Watch Video Solution

8. A, B and C are subsets of universal set U . If $A=\{2,4,6,8,12,20\}$, $B=(3,6,9,12,15\}, C=\{5,10,15,20\}$ and $U$ is the set of all whole numbers, draw a Venn diagram showing the relation of $\mathrm{U}, \mathrm{A}, \mathrm{B}$ and C .

## D Watch Video Solution

9. Let $U$ be the set of all boyes and girls in a school, $G$ be the set of all girls in the school, B be the set of all boys in the school and $S$ be the set of all students in the school who take swimming. Some but not all, students in the school take swimming. Draw a Venn diagram
showing one of the possible interrelationship among sets $\mathrm{U}, \mathrm{G}, \mathrm{B}$ and
S.

## (D) Watch Video Solution

$$
\begin{aligned}
& \text { 10. For all sets } \mathrm{A}, \mathrm{~B} \text { and C show that } \\
& (A-B) \cap(A-C)=A-(B \cup C)
\end{aligned}
$$

## (D) Watch Video Solution

11. For all sets A and $\mathrm{B},(A-B) \cup(A \cap B)=A$.

D Watch Video Solution
12. For all sets A, B and $C, A-(B-C)=(A-B)-C$.
13. For all sets $A, B$ and C , if $A \subset B$, then $A \cap C \subset B \cap C$.

## D Watch Video Solution

14. For all sets $A, B$ and C , if $A \subset B$, then $A \cup C \subset B \cup C$.

## D Watch Video Solution

15. For all sets $\mathrm{A}, \mathrm{B}$ and C , if $A \subset C$ and $B \subset C$, then $A \cup B \subset C$.

## D Watch Video Solution

16. For all sets A and B , show that, $A \cup(B-A)=A \cup B$.
17. For any two sets $A$ and $B$ prove the following: $A-(A-B)=A \cap B$

- Watch Video Solution

18. For all sets A and $\mathrm{B}, A-(A \cap B)$ is equal to .........

## D Watch Video Solution

19. For all set A and $\mathrm{B},(A \cup B)-B=A-B$.

## D Watch Video Solution

20. Let $T=\left\{x \left\lvert\, \frac{x+5}{x-7}-5=\frac{4 x-40}{13-x}\right.\right\}$. Is $T$ an empty set ? Justify your answer.

## Long Answers Type Questions

1. If $A, B$ and $C$ be sets. Then, show that $A \cap(B \cup C)=(A \cap B) \cup(A \cap C)$.

## D Watch Video Solution

2. Out of 100 students 15 passed in English 12 in Mathematics, 8 in Science 6 in English and Mathematics 7 in Mathematics and Science 4 in English and science and 4 in all the three .Find how many students passed
(a) in English and Mathmatics but not in science
(b) in Mathematics and science but not in English
(c) in Mathematics only
(d) in more than one subujects
3. In Dr. Steve's math class, 12 students play the piano and 17 students play the guitar. If a total of 19 students play only one of these two instruments, how many students play both instruments?

## D Watch Video Solution

4. In a survey of 200 students of higher secondary school, it was found that 120 studied Mathematics, 90 studies Physics and 70 studied Chemistry, 40 studied Mathematics and Physics, 3 studied Physics and Chemistry, 50 studied Chemistry and Mathematics and 20 studied none of these subjects. Find the number of students who studied all the three subjects.
5. In a town of 10000 families, it was found that $40 \%$ families buy newspaper A, 20\% families buy newspaper B, 10 \% families buy newspaper C, $5 \%$ families buy $A$ and $B, 3 \%$ buy $B$ and $C$ and $4 \%$ buy a and C. If $2 \%$ families buy all the three newspaper. Find
(i) the number of families which buy newspaper A only.
(ii) the number of families which buy none of $\mathrm{A}, \mathrm{B}$ and C .

## D Watch Video Solution

6. In a group of 50 students, the number of students studying French, English, Sanskrit were found to be as follows French = 17,

English = 13, Sanskrit = 15 French and English = 09, English and Sanskrit $=4$, French and Sanskrit $=5$, English , French and Sanskrit $=3$.

Find the number of students who study
(i) only French, (ii) only English.
(iii) only Sanskrit., (iv) English and Sanskrit but not French.
(v) French and Sanskrit but not English.
(vi) French and English but not Sanskrit.
(vii) atleast one of the three languages.
(viii) none of the three languages.

## ( Watch Video Solution

## Objective Type Questions

1. Suppose, $A_{1}, A_{2}, \ldots \ldots$. . $A_{30}$ are thirty sets each having 5 elements and $B_{1}, B_{2}, B_{n}$ sets each with 3 elements, let $\bigcup_{i=1}^{30} A_{i}=\bigcup_{j=1}^{n} B_{j}=S$ and each element of $S$ belongs to exactly 10 of the $A_{i}$ 's and exactly 9 of the $B_{j}{ }^{\prime} s$. Then, n is equal to
A. 15
B. 3
C. 45
D. 35

## D Watch Video Solution

2. Two infinite sets have $m$ and $n$ elements. The number of subsets of the first set is 112 more than that of the second set. The values of $m$ and $n$ are, respectively.(a) 4,7 (b) $7,4(c) 4,4(d) 7,7$
A. 4,7
B. 7,4
C. 4,4
D. 7, 7

Answer: B
3. The set $\left(A \cup B^{\prime}\right)^{\prime} \cup(B \cap C)$ is equal to $A^{\prime} \cup B \cup C$ b. $A^{\prime} \cup B$
c. $A^{\prime} \cup C^{\prime}$ d. $A^{\prime} \cap B$
A. $A^{\prime} \cup B \cup C$
B. $A^{\prime} \cup B$
C. $A^{\prime} \cup C^{\prime}$
D. $A^{\prime} \cap B$

## Answer: B

## D Watch Video Solution

4. Let $F_{1}$ be the set of parallelograms $F_{2}$ the set of recteangles $F_{3}$ be the set of rhombuses $F_{4}$ be the set of squares and $F_{5}$ be the set of trapezium in a plane .Then $F_{1}$ may be equal to
A. $F_{2} \cap F_{3}$
B. $F_{3} \cap F_{4}$
C. $F_{2} \cup F_{5}$
D. $F_{2} \cup F_{3} \cup F_{4} \cup F_{1}$

## Answer: D

## - Watch Video Solution

5. Let $S=$ set of point inside the sqare, $T=$ set of points inside the triangles and $C=$ the set of point inside the circle, if the triangle and circle intersect each other are contained in the square, then (a) $\quad S \cap T \cap C=\phi(\mathrm{b}) S \cup T \cup C=C(\mathrm{c}) \quad S \cup T \cup C=S$ $(d) S \cup T=S \cap C$
A. $S \cap T \cap C=\phi$
B. $S \cup T \cup C=C$
C. $S \cup T \cup C=S$
D. $S \cup T=S \cap C$

Answer: C

## - Watch Video Solution

6. Let $R$ be set of points inside a rectangle of sides $a$ and $b$ $(a, b>1)$ with two sides along the positive direction of x -axis and y axis(a)

$$
R=\{(x, y): 0 \leq x \leq a, 0 \leq y \leq b\}(\mathrm{b})
$$

$R=\{(x, y): 0 \leq x<a, 0 \leq y \leq b\}(c)$
$R=\{(x, y): 0 \leq x \leq a, 0<y<b\}(\mathrm{d})$
$R=\{(x, y): 0<x<a, 0<y<b\}$
A. $R=\{(x, y): 0 \leq x \leq a, 0 \leq y \leq b\}$
B. $R=\{(x, y): 0 \leq x<a, 0 \leq y \leq b\}$
C. $R=\{(x, y): 0 \leq x \leq a, 0<y<b\}$
D. $R=\{(x, y): 0<x<a, 0<y<b\}$

## Answer: D

## - Watch Video Solution

7. In a town of 840 persons, 450 persons read Hindi, 300 read English and 200 read both. Then, the number of persons who read neither, is
A. 210
B. 290
C. 180
D. 260

Answer: B
8. If $X=\left\{8^{n}-7 n-1 \mid n \in N\right\}$ and $Y=\{49 n-49 \mid n \in N\}$. Then
A. $X \subset Y$
B. $Y \subset X$
C. $X=Y$
D. $X \cap Y=\phi$

## Answer: A

## D Watch Video Solution

9. A survey shows that $63 \%$ of the people watch a news channel whereas $76 \%$ watch another channel. If $x \%$ of the people watch both channel then(a) $\mathrm{x}=35(b) x=63(\mathrm{c}) 39 \leq x \leq 63(d) \mathrm{x}=39^{`}$

$$
\text { A. } x=35
$$

B. $x=63$
C. $39 \leq x \leq 63$
D. $x=39$

## Answer: C

## (D) Watch Video Solution

10. If set $A$ and $B$ are defined as
$A=\left\{(x, y) \left\lvert\, y=\frac{1}{x}\right., 0 \neq x \in R\right\}, B=\{(x, y) \mid y=-x, x \in R$,
.Then (a) $A \cap B=A(b) A \cap B=B(c) A \cap B=\phi(d) A \cup B=A$
A. $A \cap B=A$
B. $A \cap B=B$
C. $A \cap B=\phi$
D. $A \cup B=A$

## D Watch Video Solution

11. If A and B are two sets then prove $A=A \cap(A \cup B)$.
A. A
B. B
C. $\phi$
D. $A \cap B$

## Answer: A

## D Watch Video Solution

12. If $A=\{1,3,5,7,9,11,13,15,17\}, B=\{2,4, \ldots \ldots, 18\}$ and $N$ the set of natural numbers is the universal set, then
$A^{\prime} \cup\left\{(A \cup B) \cap B^{\prime}\right\}$ is (a) $\phi$ (b)N (c) A (d) B
A. $\phi$
B. N
C. A
D. $B$

## Answer: B

## - Watch Video Solution

13. If $S=\{x: x$ is a positive multiple of 3 less than 100$\}$ and $P=\{x: x$ is a prime number less than 20$\}$. Then, $n(S)+n(P)$ is equal to (a) 34 (b) 31 (c) 33 (d) 41
A. 34
B. 31
C. 33
D. 41

## Answer: D

## - Watch Video Solution

14. If $A$ and $B$ are two sets, then $A \cap(A \cup B)^{\prime}$ is equal to - A (b) B (c) $\phi(d) A \cap B$ '
A. $A$
B. $B$
C. $\phi$
D. $A \cap B^{`}$

Answer: A

1. The set $\{x \in R: 1 \leq x<2\}$ be written as - Watch Video Solution
2. How many elements has $\mathrm{P}(\mathrm{A})$, if $A=\varphi$ ?

## (D) Watch Video Solution

3. If A and B are finite sets, such that $A \subset B$, then $n(A \cup B)$ is equal to ......... .

- Watch Video Solution

4. If $A$ and $B$ are any two sets, then $A-B$ is equal to ......... .

## D Watch Video Solution

5. Power set of the set $A=\{1,2\}$ is . ........

## D Watch Video Solution

6. If the sets $A=\{1,3,5\}, B=\{2,4,6\}$ and $C=\{0,2,4,6,8\}$.

Then, the universal set of all the three sets A, B and C can be

## D Watch Video Solution

7. 

$U=\{1,2,3,4,5,6,7,8,9,10\}, A=\{1,2,3,5\}, B=2,4,6,7\}$
and $C=\{2,3,4,8\}$. Then
(i) $(B \cup C)^{\prime}$ is
(ii) $(C-A)^{\prime}$ is $\qquad$

## - Watch Video Solution

8. For all sets A and $\mathrm{B}, A-(A \cap B)$ is equal to .........

## D Watch Video Solution

9. Match the following sets for all sets $A, B$ and $C$

|  |  | Column I |  |
| :--- | :--- | :--- | :--- |
| Column II |  |  |  |
| (i) | $\left(\left(A^{\prime} \cup B^{\prime}\right)-A\right)^{\prime}$ | (a) | $A-B$ |
| (ii) | $\left[\left(B^{\prime} \cup\left(B^{\prime}-A\right)\right]^{\prime}\right.$ | (b) | $A$ |
| (iii) | $(A-B)-(B-C)$ | (c) | $B$ |
| (iv) | $(A-B) \cap(C-B)$ | (d) | $(A \times B) \cap(A \times C)$ |
| (v) | $A \times(B \cap C)$ | (e) | $(A \times B) \cup(A \times C)$ |
| (vi) | $A \times(B \cup C)$ | (f) | $(A \cap C)-B$ |

## True And False

1. IF A any set, then $A \subset A$.

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2. If $M=\{1,2,3,4,5.6,7,8,9\}$ and $B=\{1,2,3,4,5.6,7,8,9\}$, then $B \varnothing M$.

## D Watch Video Solution

3. The sets $\{1,2,3,4\}$ and $\{3,4,5,6\}$ are equal

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4. $Q \cup Z=Q$, where Q is the set of rational numbers and Z is the set of integers.

## D Watch Video Solution

5. Let sets $R$ and $T$ be defined as
$R=\{x \in Z \mid x$ is divisible by 2$\}$
$T=\{x \in Z \mid x$ is divisible by 6$\}$. Then, $T \subset R$

## D Watch Video Solution

6. Given $A=[0,, 2], B=[x \in R \mid 0 \leq x \leq 2\}$. Then, $A=B$.

## D Watch Video Solution

