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CLASS - 12



THREE DIMENSIONAL GEOMETRY

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EXERCISE 11.1 - Question No. 1

If a line makes angles 90° , 135° , 45° with the x, y and z-axes

respectively, find its direction cosines.

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EXERCISE 11.1 - Question No. 2

Find the direction cosines of a line which makes equal angles with

the coordinate axes.



EXERCISE 11.1 - Question No. 3

If a line has the direction ratios 18, 12, 4, then what are its

direction cosines?

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EXERCISE 11.1 - Question No. 4

Show that the points (2, 3, 4), (1, 2, 1), (5, 8, 7) are collinear.

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Find the direction cosines of the sides of the triangle whose vertices

are (3, 5, 4), (1, 1, 2) and (5, 5, 2).

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EXERCISE 11.2 - Question No. 1

Show that the three lines with direction cosines

 $\frac{12}{13}, \frac{-3}{13}, \frac{-4}{13}, \frac{4}{13}, \frac{12}{13}, \frac{3}{13}; \frac{3}{13}, \frac{-4}{13}, \frac{12}{13}$ are mutually

perpendicular.

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Show that the line through the points (1, 1, 2), (3, 4, 2) is

perpendicular to the line through the points (0, 3, 2) and (3, 5, 6).

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EXERCISE 11.2 - Question No. 3

Show that the line through the points (4, 7, 8), (2, 3, 4) is parallel

to the line through the points (1, 2, 1), (1, 2, 5).

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Find the equation of the line which passes through the point (1, 2,

3) and is parallel to the vector $3\hat{i}+2\hat{j}-2\hat{k}$.

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EXERCISE 11.2 - Question No. 5

Find the equation of the line in vector and in cartesian form that

passes through the point with position vector $2\hat{i} - \hat{j} + 4\hat{k}$ and is in

the direction $\hat{i}+2\hat{j}-\hat{k}$.

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Find the cartesian equation of the line which passes through the

point (2, 4, 5) and parallel to the line given by

$$rac{x+3}{3} = rac{y-4}{5} = rac{z+8}{6}\,.$$

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EXERCISE 11.2 - Question No. 7

The cartesian equation of a line is
$$\frac{x-5}{3} = \frac{y+4}{7} = \frac{z-6}{2}$$

Write its vector form.

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Find the vector and the cartesian equations of the lines that passes

through the origin and (5, 2, 3).

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EXERCISE 11.2 - Question No. 9

Find the vector and the cartesian equations of the line that passes

through the points (3, 2, 5), (3, 2, 6).

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Find the angle between the following pairs of lines: (i)

$$egin{aligned} &
ightarrow r=2\hat{i}-5\hat{j}+\hat{k}+\lambda\Big(3\hat{i}+2\hat{j}+6\hat{k}\Big) ext{ and } \ &
ightarrow r=7\hat{i}-6\hat{k}+\mu\Big(\hat{i}+2\hat{j}+2\hat{k}\Big) ext{ (ii)} \ &
ightarrow r=3\hat{i}+\hat{j}-2\hat{k}+\lambda\Big(\hat{i}-\hat{j}-2\hat{k}\Big) ext{ and `-} \end{aligned}$$

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EXERCISE 11.2 - Question No. 11

Find the angle between the following pair of lines: (i)

$$\frac{x-2}{2} = \frac{y-1}{5} = \frac{z+3}{-3} \text{ and } \frac{x+2}{-1} = \frac{y-4}{8} = \frac{z-5}{4} \text{ (ii)}$$
$$\frac{x}{2} = \frac{y}{2} = \frac{z}{1} \text{ and } \frac{x-5}{4} = \frac{y-2}{1} = \frac{z-3}{8}$$



perpendicular to each other.

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Find the shortest distance between the lines

$$egin{aligned} &
ightarrow r = \left(\hat{i}+2\hat{j}+\hat{k}
ight)+\lambdaig(\hat{i}-\hat{j}+\hat{k}ig) ext{ and } \ &
ightarrow r = 2\hat{i}-\hat{j}-\hat{k}+\muig(2\hat{i}+\hat{j}+2\hat{k}ig) \end{aligned}$$

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EXERCISE 11.2 - Question No. 15

Find the shortest distance between the lines

$$\frac{x+1}{7} = \frac{y+1}{-6} = \frac{z+1}{1}$$
 and $\frac{x-3}{1} = \frac{y-5}{-2} = \frac{z-7}{1}$

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Find the shortest distance between the lines whose vector equations

$$egin{array}{ll} ext{are} &
ightarrow r = \left(\hat{i} + 2 \hat{j} + 3 \hat{k}
ight) + \lambda \left(\hat{i} - 3 \hat{j} + 2 \hat{k}
ight) ext{ and } \ &
ightarrow r = 4 \hat{i} + 5 \hat{j} + 6 \hat{k} + \mu \left(2 \hat{i} + 3 \hat{j} + \hat{k}
ight). \end{array}$$

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EXERCISE 11.2 - Question No. 17

Find the shortest distance between the lines whose vector equations

are
$$ightarrow r = (1-t)\hat{i} + (t-2)\hat{j} + (3-2t)\hat{k}$$
 and

$$ightarrow r = (s+1) \hat{i} + (2s-1) \hat{j} - (2s+1) \hat{k} \, .$$

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In each of the following cases, determine the direction cosines of

the normal to the plane and the distance from the origin. (a) z = 2

(b) x + y + z = 1 (c) 2x + 3yz = 5 (d) 5y + 8 = 0

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EXERCISE 11.3 - Question No. 2

Find the vector equation of a plane which is at a distance of 7 units

from the origin and normal to the vector $3\hat{i}+5\hat{j}-6\hat{k}$.

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Find the Cartesian equation of the following planes: (a)

$$ightarrow r\hat{i}+\hat{j}-\hat{k}=2~(\mathrm{b})
ightarrow r2\hat{i}+3\hat{j}-4\hat{k}=1~(\mathrm{c})$$

 $ightarrow r(s-2t)\hat{i} + (3-t)\hat{j} + (2s+t)\hat{k} = 15$

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EXERCISE 11.3 - Question No. 4

In the following cases, find the coordinates of the foot of the

perpendicular drawn from the origin. (a) 2x + 3y + 4z12 = 0 (b)

3y + 4z6 = 0 (c) x + y + z = 1 (d) 5y + 8 = 0

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Find the vector and cartesian equations of the planes (a) that passes

through the point (1,0,2) and the normal to the plane is $\hat{i}+\hat{j}-\hat{k}$

(b) that passes through the point (1,4, 6) and the normal vector to

the plane is



EXERCISE 11.3 - Question No. 6

Find the equations of the planes that passes through three points.

(a)(1,1,-1),(6,4,-5),(-4,-2,3)

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Find the intercepts cut off by the plane 2x + yz = 5.

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EXERCISE 11.3 - Question No. 8

Find the equation of the plane with intercept 3 on the y-axis and

parallel to ZOX plane.

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EXERCISE 11.3 - Question No. 9

Find the equation of the plane through the intersection of the planes

3x - y + 2z - 4 = 0 and x + y + z - 2 = 0 and the point (2, 2,



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EXERCISE 11.3 - Question No. 10

Find the vector equation of the plane passing through the

intersection of the planes

$$i \to r2\hat{i} + 2\hat{j} - 3\hat{k} = 7, \ o r2\hat{i} + 5\hat{j} + 3\hat{k} = 9$$
 and through the

point (2, 1, 3).

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Find the equation of the plane through the line of intersection of the

planes x + y + z = 1 and 2x + 3y + 4z = 5 which is

perpendicular to the planexy + z = 0.

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EXERCISE 11.3 - Question No. 12

Find the angle between the planes whose vector equations are

$$\overrightarrow{r}.\left(2\hat{i}+2\hat{j}-3\hat{k}
ight)=5 ext{ and }\overrightarrow{r}.\left(3\hat{i}-3\hat{j}+5\hat{k}
ight)=3 ext{ .}$$

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In the following cases, determine whether the given planes are parallel or perpendicular, and in case they are neither, find the angles between them. (a)

7x + 5y + 6z + 30 = 0 and 3x - y - 10z + 4 = 0 (b)

2x + y + 3z - 2 = 0 and x - 2y + 5z = 0 (c)

2x - 2y + 4z + 5 = 0 and 3x - 3y + 6z - 1 = 0 (d)

2x - y + 3z - 1 = 0 and 2x - y + 3z + 3 = 0 (e)

4x + 8y + z - 3 = 0 and y + z - 4 = 0

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In the following cases, find the distance of each of the given points

from the corresponding given plane. Point Plane (a) (0, 0, 0)

3x4y + 12z = 3 (b) (3, 2, 1) 2xy + 2z + 3 = 0 (c) `(2,

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MISCELLANEOUS EXERCISE - Question No. 1

Show that the line joining the origin to the point (2, 1, 1) is

perpendicular to the line determined by the points (3, 5, 1), (4, 3, 1)



If l_1, m_1, n_1 and l_2, m_2, n_2 are the direction cosines of two

mutually perpendicular lines, show that the direction cosines of the

line perpendicular to both of these are

 $m_1n_2-m_2n_1, n_1l_2-n_2l_1, l_1m_2-l_2m_1$.



MISCELLANEOUS EXERCISE - Question No. 3

Find the angle between the lines whose direction ratios are a, b, c

and bc, ca, ab.

Find the equation of a line parallel to x-axis and passing through

the origin.

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MISCELLANEOUS EXERCISE - Question No. 5

If the coordinates of the points A, B, C, D be (1, 2, 3), (4, 5, 7),

(4, 3, 6) and (2, 9, 2) respectively, then find the angle between the

lines AB and CD.

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MISCELLANEOUS EXERCISE - Question No. 7

Find the vector equation of the line passing through (1, 2, 3) and

perpendicular to the plane
$$\overrightarrow{r}.\left(\hat{i}+2\hat{j}-5\hat{k}
ight)+9=0$$
 .

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Find the equation of the plane passing through (a, b, c) and parallel

to the plane
$$ightarrow r \hat{i} + \hat{j} + \hat{k} = 2$$
 .

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MISCELLANEOUS EXERCISE - Question No. 9

Find the shortest distance between lines

$$egin{aligned} &
ightarrow r=6\hat{i}+2\hat{j}+\hat{k}+\lambda\Big(\hat{i}-2\hat{j}+2\hat{k}\Big) ext{ and } \ &
ightarrow r=\,-4\hat{i}-\hat{k}+\mu\Big(3\hat{i}-2\hat{j}-2\hat{k}\Big)\,. \end{aligned}$$

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Find the coordinates of the point where the line through (5, 1, 6)

and (3, 4, 1) crosses the YZ-plane.

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MISCELLANEOUS EXERCISE - Question No. 11

Find the coordinates of the point where the line through (5, 1, 6)

and (3, 4, 1) crosses the ZX-plane.

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Find the coordinates of the point where the line through (3, 4, 5)

and (2, 3, 1) crosses the plane 2x + y + z = 7.

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MISCELLANEOUS EXERCISE - Question No. 13

Find the equation of the plane passing through the point (1, 3, 2)

and perpendicular to each of the planes x + 2y + 3z = 5 and

3x + 3y + z = 0.

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If the points (1, 1, p) and (3, 0, 1) be equidistant from the plane

$$\overrightarrow{r}\cdot\left(3\hat{i}+4\hat{j}-12\hat{k}
ight)+13=0$$
 , then find the value of p.

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MISCELLANEOUS EXERCISE - Question No. 15

Find the equation of the plane passing through the line of

intersection of the planes $\
ightarrow r \hat{i} + \hat{j} + \hat{k} = 1$ and

 $ightarrow r2\hat{i} + 3\hat{j} - \hat{k} + 4 = 0$ and parallel to x-axis.

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If O be the origin and the coordinates of P be(1, 2, -3), then find

the equation of the plane passing through P and perpendicular to

OP.

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MISCELLANEOUS EXERCISE - Question No. 17

Find the equation of the plane which contains the line of

intersection of the planes

 $\hat{j} \rightarrow r\hat{i} + 2\hat{j} + 3\hat{k} - 4 = 0, \ o r2\hat{i} + \hat{j} - \hat{k} + 5 = 0$ and which

is perpendicular to the plane

Find the distance of the point (1, 5, 10) from the point of

intersection of the line $\rightarrow r = 2\hat{i} - \hat{j} + 2\hat{k} + \lambda \left(3\hat{i} + 4\hat{j} + 2\hat{k}\right)$

and the plane $\
ightarrow r = \left(\hat{i} - \hat{j} + \hat{k}
ight) = 5$.

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MISCELLANEOUS EXERCISE - Question No. 19

Find the vector equation of the line passing through (1, 2, 3) and

parallel to the planes $\
ightarrow r \hat{i} - \hat{j} + 2 \hat{k} = 5$ and

$$ightarrow r3 \hat{i} + \hat{j} + \hat{k} = 6$$
 .

Find the vector equation of the line passing through the point

(1, 2, -4) and perpendicular to the two lines:

$$\frac{x-8}{3} = \frac{y+19}{-16} = \frac{z-10}{7} \text{ and } \frac{x-15}{3} = \frac{y-29}{8} = \frac{z-5}{-5}$$
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MISCELLANEOUS EXERCISE - Question No. 21

Prove that if a plane has the intercepts a, b, c and is at a distance of

p units from the origin, then
$$\frac{1}{a^2} + \frac{1}{b^2} + \frac{1}{c^2} = \frac{1}{p^2}$$

Distance between the two planes: 2x + 3y + 4z = 4 and

4x + 6y + 8z = 12 is (A) 2 units (B) 4 units (C) 8 units (D) $\frac{2}{\sqrt{29}}$

units

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MISCELLANEOUS EXERCISE - Question No. 23

The planes: 2xy + 4z = 5and5x2. 5y + 10z = 6 are (A)

Perpendicular (B) Parallel (C) intersect y-axis (D) passes through

$$\left(0,0,rac{5}{4}
ight)$$

SOLVED EXAMPLES - Question No. 1

If a line makes angle 90o, 60o and 30o with the positive direction

of x, y and z-axis respectively, find its direction cosines.

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SOLVED EXAMPLES - Question No. 2

If a line has direction ratios 2, 1, 2.determine its direction cosines.

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Find the direction cosines of the line passing through the two points

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(2, 4, 5) and (1, 2, 3).
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SOLVED EXAMPLES - Question No. 4

Find the direction cosines of x, y and z-axis.



SOLVED EXAMPLES - Question No. 5

Show that the points A(2, 3, 4), B(1, 2, 3) and C(3, 8, 11) are

collinear.



SOLVED EXAMPLES - Question No. 6

Find the vector and the Cartesian equations of the line through the

point (5,2,4) and which is parallel to the vector $3\hat{i}+2\hat{j}-8\hat{k}$.

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SOLVED EXAMPLES - Question No. 7

Find the vector equation for the line passing through the points

(1, 0, 2) and (3, 4, 6).

The Cartesian equation of a line is $\frac{x+3}{2} = \frac{y-5}{4} = \frac{z+6}{2}$.

Find the vector equation for the line.

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SOLVED EXAMPLES - Question No. 9

Find the angle between the pair of lines given by

$$ec{r}=3\hat{i}+2\hat{j}-4\hat{k}+\lambdaig(\hat{i}+2\hat{j}+2\hat{k}ig)$$
 and $ec{r}=5\hat{i}-2\hat{j}+\muig(3\hat{i}+2\hat{j}+6\hat{k}ig)$.

Find the angle between the pair of lines

$$\frac{x+3}{3} = \frac{y-1}{5} = \frac{z+3}{4}$$
 and $\frac{x+1}{1} = \frac{y-4}{1} = \frac{z-5}{2}$

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SOLVED EXAMPLES - Question No. 11

Find the shortest distance between the lines 11 and 12 whose vector

equations are $\rightarrow r = \hat{i} + \hat{j} + \lambda \left(2\hat{i} - \hat{j} + \hat{k} \right)$ (1) and

$$ightarrow r=2\hat{i}+\hat{j}-k+\mu\Bigl(3\hat{i}-5\hat{j}+2\hat{k}\Bigr)$$
 (2)

Find the distance between the lines l_1 and l_2 given by

$$ightarrow r=\hat{i}+2\hat{j}-4k+\lambda\Big(2\hat{i}+3\hat{j}+6\hat{k}\Big)$$
 and

$$ightarrow r = 3 {\hat i} + 3 {\hat j} - 5 k + \mu \Bigl(2 {\hat i} + 3 {\hat j} + 6 {\hat k} \Bigr) \, .$$

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SOLVED EXAMPLES - Question No. 13

Find the vector equation of the plane which is at a distance of $\frac{6}{\sqrt{29}}$

from the origin and its normal vector from the origin is

 $2\hat{i} - 3\hat{j} + 4\hat{k}$. Also find its cartesian form.

Find the direction cosines of the unit vector perpendicular to the

plane $\rightarrow r6\hat{i} - 3\hat{j} - 2\hat{k} + 1 = 0$ passing through the origin.

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SOLVED EXAMPLES - Question No. 15

Find the distance of the plane 2x3y + 4z6 = 0 from the origin.

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Find the coordinates of the foot of the perpendicular drawn from

the origin to the plane 2x - 3y + 4z - 6 = 0.

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SOLVED EXAMPLES - Question No. 17

Find the vector and cartesian equations of the plane which passes

through the point (5, 2, 4) and perpendicular to the line with

direction ratios (2, 3, 1).

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Find the vector equations of the plane passing through the points

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R(2,5,3), S(2,3,5) and T(5,3,3).
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SOLVED EXAMPLES - Question No. 19

Find the equation of the plane with intercepts 2, 3 and 4 on the x, y

and z-axis respectively.



Find the vector equation of the plane passing through the

intersection of the planes $\
ightarrow r \hat{i} + \dot{\hat{j}} + \hat{k} = 6$ and

$$rac{1}{2} \rightarrow r2\hat{i} + 3\hat{j} + 4\hat{k} = -5$$
 and the point (1, 1, 1).

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SOLVED EXAMPLES - Question No. 21

Show that the lines
$$\frac{x+3}{-3} = \frac{y-1}{1} = \frac{z-5}{5}$$
 and $\frac{x+1}{-1} = \frac{y-2}{2} = \frac{z-5}{5}$ are coplanar.

Find the angle between the two planes 2x + y2z = 5 and

3x6y2z = 7 using vector method.

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SOLVED EXAMPLES - Question No. 23

Find the angle between the two planes 3x6y + 2z = 7 and

2x + 2y2z = 5.

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Find the distance of a point (2, 5, 3) from the plane

$$ightarrow r6 \hat{i} - 3 \hat{j} + 2 \hat{k} = 4$$
 .

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SOLVED EXAMPLES - Question No. 25

Find the angle between the line $\frac{x+1}{2} = \frac{y}{3} = \frac{z-3}{6}$ and the

plane 10x + 2y11z = 3.

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A line makes angles α , β , γ and δ with the diagonals of a cube,

prove that
$$\cos^2 lpha + \cos^2 eta + \cos^2 \gamma + \cos^2 \delta = rac{4}{3}$$

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SOLVED EXAMPLES - Question No. 27

Find the equation of the plane that contains the point (1, 1, 2) and

is perpendicular to each of the planes 2x + 3y2z = 5 and

x + 2y3z = 8.

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Find the distance between the point P(6, 5, 9) and the plane

determined by the points A(3,1,2) , B(5,2,4) and C(1,1,6) .

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 Solved EXAMPLES - Question No. 29

 Show that the lines
$$\frac{x-a+d}{\alpha-\delta} = \frac{y-a}{\alpha} = \frac{z-a-d}{\alpha+\delta}$$
 and $\frac{x-b+c}{\beta-\gamma} = \frac{y-b}{\beta} = \frac{z-b-c}{\beta+\gamma}$ are coplanar.

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Find the coordinates of the point where the line through the points

A (3, 4, 1) and B(5, 1, 6) crosses the XY-plane.

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