

## **CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS**

## **Chapter 1. RELATIONS AND FUNCTIONS**

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1 - 10540	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
	Let $T$ be the set of all triangles in a plane with $R$ as relation in $T$
	given by $\mathrm{R}=\left\{\left(\mathrm{T}_1,\left(ackslash\mathrm{T} ight)_2 ight)\!:\!\left(ackslash\mathrm{T} ight)_1\cong\mathrm{T}_2 ight\}$ . Show that $\mathrm{R}$ is
	an equivalence relation.
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2 - 10547	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
	If $f(x)$ is an invertible function, find the inverse of $f(x)=\dfrac{3x-2}{5}$
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3 - 10583	If $\mathrm{f(x)}=x+7$ and $g(x)=x-7,\;x\;R,\;\mathrm{find}\;(fog)(7)$
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4 - 10601	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS

	If $f:R\div R$ be defined by $f(x)=\left(3-x^3 ight)^{1/3},$ then find
	fof(x)
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5 - 10613	Prove that the relation $R$ on the set $A=\{1,2,3,4,5\}$ given by
	$R=\{(a,b)\colon  a-b   ext{ is even}\}$ , is an equivalence relation.
	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
	Let $A=R-\{3\}$ and $B=R-[1]$ Consider the function
6 - 10644	$f{:}\overrightarrow{AB}$ defined by $f(x)=\left(rac{x-2}{x-3} ight)$ . Show that $f$ is one-one
	and onto and hence find $f^{-1}$
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7 - 10716	Let * be a binary operation of $N$ given by a $a\cdot b=LCM\left(a,b ight)$
	for all $a,b \in N$ . Find $5 \cdot 7$ .
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Let\* be a binary operation on N given by a\*b = HCF

(a, b) a, b N. Write the value of 22\*4.

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9 - 10746

 $R = \{a,b\}$  :  $a \leq b^2\}$  is neither reflexive, nor symmetric, nor transitive

Show that the relation R in the set of real numbers, defined as

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Show that the relation S in the set  $A=\{x \mid Z: 0 \leq x \leq 12\}$ 

given by  $S=\{(a,b)\colon a,\ b\ Z,\ |a-b|\ ext{is divisible by }4\}$  is an

equivalence relation. Find the set of all elements related to 1.

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Show that  $f: N\stackrel{\longrightarrow}{N}$ , given by  $f(x) = \{x + ,$  $ext{if} \quad x \ is \ oddx - 1, \quad ext{if} \quad x \ is \ even$ is both one-one and onto. OCIICK to watch Free Video Solution of this question on Doubtnut Get Solutions as Click Here to TYPE & ASK o doubtnut CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS What is the range of the function  $f(x) = \frac{|x-1|}{(x-1)}$ ? 12 - 10770 Click to watch Free Video Solution of this question on Doubtnut CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS Find the intervals in which the function f given by 13 - 10796  $f(x) = x^3 + rac{1}{x^3} \; , \; x \; 
eq 0 \; ext{is (i) increasing (ii) decreasing.}$ OClick to watch Free Video Solution of this question on Doubtnut 14 - 10803 CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS Consider  $f:R_+ \overset{\longrightarrow}{4,\infty}$  given by  $f(x)=x^2+4$  . Show that f is invertible with the inverse  $f^{\,-\,1}$  of f given by

	$\int f^{-1}(y) = \sqrt{y-4}, $ where $R_+$ is the set of all non-negative
	real numbers.
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15 - 10813	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
	State the reason for the relation R in the set {1, 2, 3} given by R=
	{(1, 2), (2, 1)} not to be transitive.
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	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
16 - 10838	If the binary operation $st$ on the set of integers $Z,$ is defined by
	$a\cdot b=a+3b^2,  ext{ then find the value of } 2\cdot 4$
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17 - 10853	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
	If $f\!:\!R o R$ is defined by $f(x)=3x+2,$ define $f\left[f(x) ight]_{\cdot}$
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18 - 10864	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS

	What is the domain of the function $\sin^{-1}x$ ?
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19 - 10865	If ' $f$ ' is an invertible function, defined as $f(x)=rac{3x-4}{5},$ write $f^{-1}(x)$
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20 - 10897	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS $Let \ f\colon N \overrightarrow{N} \ be \ defined \ by$ $f(n) = \left\{\frac{n+1}{2}, \ \text{if} \ n \ \text{is} \setminus \text{o} \ \text{d} \ \frac{n}{2}, \ \text{if} \setminus \ n \ \text{is} \setminus \text{even} \ f \ \text{or} \right.$ $\left. all \ n \ N \right\}$ Find whether the function $f$ is bijective.
21 - 10918	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS

If  $f(x)=rac{4x+3}{6x-4},\;x
eqrac{2}{3},\;$  show that fof(x)=x for all  $x
eqrac{2}{3}.$  What is the inverse of f?

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Let  $A = N \ x \ N$  and \* be a binary operation and A defined by

 $(a,b)\cdot(c,d)=(a+c,\ b+d)$ . Show that \* is commutative

and associative. Also, find the identity element for  ${}^{\star}$  on A , if any.

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Consider  $f\!:\!R o[\,-5,\infty)$  given by  $f(x)=9x^2+6x-5$  .

Show that f is invertible with  $f^{-1}(y) = \left( \dfrac{\sqrt{y+6}-1}{3} \right)$  .

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	Consider the binary operation* on the set {1, 2, 3, 4, 5} defined by
	a * b=min. {a, b}. Write the operation table of the operation *.
	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
	A binary operation * on the set {0,1,2,3,4,5} is defined as:
25 - 10984	$egin{aligned} a \cdot b &= \{a + ba + b - 6 \setminus \setminus \setminus \mathrm{if} \setminus a + b < 6 \setminus \setminus \setminus \mathrm{if} \ a + b \ \geq 6 \end{aligned}$
	Show that zero is the identity for this operation and each element
	a of the set is invertible with 6a, being the inverse of a.
	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
26 - 10985	Let $f\!:\!R o R$ be defined as $f(x)=10x+7.$ Find the
	function $g\!:\!R o R$ such that $gof=fog=I_R$ .
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27 - 11003	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
	Consider $f\!:\!R_+ o [4,\infty]$ given by $f(x)=x^2+4.$ Show that
	$f$ is invertible with the inverse $\left(f^{-1} ight)$ of $f$ given by
	$\int f^{-1}\left(y ight)=\sqrt{y-4}$ , where $R_{+}$ is the set of all non-negative
	real numbers.





Let  $A = \{1, 2, 3\}, B = \{4, 5, 6, 7\}$  and let

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 $f = \{(1,4),\ (2,5),\ (3,6)\}$  be a function from A to B . State

whether f is one-one or not.

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Show that the function f in  $A=\mid R-\left\{rac{2}{3}
ight\}$  defined as  $f(x)=rac{4x+3}{6x-4}$  is one-one and onto. Hence find  $f^{-1}$ .

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If the binary operation \* on the set Z of integers is defined by

 $a \, \cdot \, b = a + b \, - \, 5$  , then write the identity element for the

operation \* in Z.

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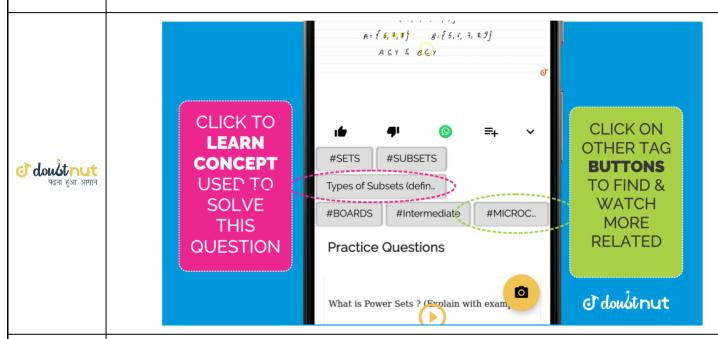
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Prove that the relation R in the set  $A=\{5,6,7,8,9\}$  given by

 $R = \{(a,b): |a-b|, \text{ is divisible by 2}\}$ , is an equivalence

relation. Find all elements related to the element 6.

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Consider the binary operations\*:  $R \times R \rightarrow$  and  $o: R \times R \rightarrow$ 

defined as a  $\cdot$  b=|a-b| and aob=a for all  $a,\ b\ \in R_{\cdot}$ 

Show that  $^*$  is commutative but not associative,  $^\prime o^\prime$  is associative

but not commutative.

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CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS

If the binary operation \*, defined on Q, is defined as

 $a\cdot b=2a+b-ab, \ {
m for \ all} \ a*\ b \ Q, \ {
m find \ the \ value \ of} \ 3*4$ 

32 - 11073

33 - 11078

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34 - 11089	Let $Z$ be the set of all integers and $R$ be the relation on $Z$ defined as $R=\{(a,b);a,\ b\in Z,\  ext{and}\ (a-b)\  ext{is divisible by }5.\}$ . Prove that $R$ is an equivalence relation.
35 - 13227	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
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36 - 13241	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS Let $f,g\colon RR$ be two functions defined as $f(x)= x +x$ and $g(x)= x -x$ , for all $xR$ . Then find fog and gof.

Find the intervals in which the function given by

$$f(x)=rac{3}{10}x^4=rac{4}{5}x^3-3x^2+rac{36}{5}x+11$$
 is  $(a)$  strictly

increasing (b) strictly decreasing.

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Let  $A=\{1,2,3,\cdot,9\}$  and R be the relation in AxA defined by

(a,b)R(c,d) if a+d=b+c for (a,b),(c,d) in AxA. Prove

that R is an equivalence relation. Also obtain the equivalence class [(2,5)].

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Let \* be a binary operation, on the set of all-zero real numbers,

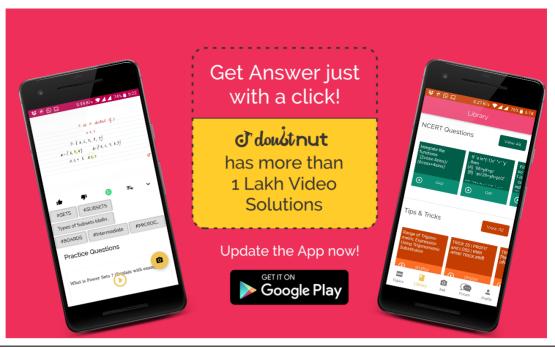
given by a  $a\cdot b=\frac{ab}{5}$  for all  $a,bR-\{0\}$  . Find the value of x given that  $2\cdot (x\cdot 5)=10$ .

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39 - 13263



Let R be the equivalence relation in the set

 $A=\{0,1,2,3,4,5\}$  given by  $R=\{(a,b)\!:\!divides(a-b)\}$  .

Write the equivalence class [0].

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Let S be the set of all rational number except 1 and  $^{\star}$  be defined

on S by  $a \cdot b = a + b - ab$ , for all a, bS. Prove that (i) \* is a

binary operation on `( i i ) \* is commutative as well as associative.

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Let  $R = \{a, a^3\}$ : a is a prime number less than  $5\}$  be a relation.

Find the range of R.

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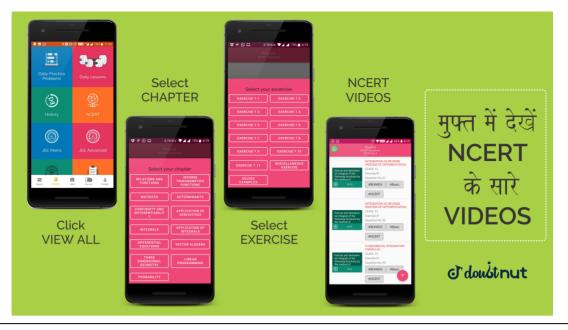
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CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1, RELATIONS AND FUNCTIONS Let  $f\!:\!W\overrightarrow{W}$  , be defined as f(x)=x1 , if x is odd and f(x) = x + 1 , if x is even. Show that f is invertible. Find the 43 - 13329 inverse of f , where W is the set of all whole numbers. OCIICK to watch Free Video Solution of this question on Doubtnut Click Get an o doubt n Picture of Answer QUESTION & doubtnut CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS Show that the relation R in the set  $A = \{1, 2, 3, 4, 5\}$  given by  $R = \{1, 2, 3, 4, 5\}$  $\{(a, b) : |a - b| \text{ is divisible by 2}\}\$  is an equivalence relation. Write all 44 - 13343 the quivalence classes of R. Olick to watch Free Video Solution of this question on Doubtnut 45 - 13377 CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1, RELATIONS AND FUNCTIONS Let  $A = R \times R$  and \* be the binary operation on A defined by (a, b) \* (c, d) = (a + c, b + d). Show that \* is commutative and

associative. Find the identity element for \* on A. Olick to watch Free Video Solution of this question on Doubtnut CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS Let  $f\!:\!N\overset{
ightarrow}{R}$  be a function defined as  $f(x)=4x^2+12x+15.$ Show that  $f\!:\!N\overset{\longrightarrow}{S}$  , where S is the range of f , is invertible. Also 46 - 13399 find the inverse of fO Click to watch Free Video Solution of this question on Doubtnut CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS Show that the binary operation \* on  $A=R-\{\,-\,1\}$  defined as  $a \cdot b = a + b + ab$  for all a, bA is commutative and associative 47 - 13458 on A. Also find the identity element of  $\cdot$  in A and prove that every element of A is invertible. Olick to watch Free Video Solution of this question on Doubtnut Get Solutions as Click Here to TYPE & ASK o doubtnut 48 - 13462 CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1, RELATIONS AND FUNCTIONS

	Let $f\!:\!\overrightarrow{N}$ be a function defined as $f(x)=9x^2+6x-5.$ Show
	that $f\!:\!N\overset{ ightarrow}{S},$ where $S$ is the range of $f,$ is invertible. Find the
	inverse of $f$ and hence $f^{-1}(43) \ { m and} \ f^{-1}(163)$
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	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
49 - 13505	If $f,: R \overset{ ightarrow}{R}$ be two functions defined as $f(x) =  x  + x$ and
	$g(x) =  x  - x, \ orall xR, \  ext{Then find } fog  ext{ and } gof.$ Hence find
	fog(-3), fog(5) and $gof(-2)$
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50 - 228051	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
	Discuss the commutativity and associativity of binary operation *
	defined on $Q$ by the rule $a\cdot b=a-b+ab$ for all $a,b\in Q$
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51 - 228164	CLASS 12 BOARDS: MOST IMPORTANT QUESTIONS - Chapter 1. RELATIONS AND FUNCTIONS
	Consider f $R  o \left\{ -rac{4}{3}  ight\}  o R - \left\{ rac{4}{2}  ight\}$ given by
	$f(x)=rac{4x+3}{3x+4}$ Show that f is bijective. Find the inverse of f and
	hence find $f^{-1}(0) \  ext{and} \ x$ such that $f^{-1}(x)=2$ .
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Let  $A=R-\{3\}, B=R-\{1\}, \ ext{and let } f\!:\!A\overrightarrow{B}$  be defined by  $f(x)=rac{x-2}{x-3}$  is f invertible? Explain.

If a \* b, denoted the larger of 'a' and 'b' and if  $aob = a \cdot b + 3$  ,

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then write the value of (5)o(10), where \* and o are binary operations.

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Let  $A=\{x\in Z\colon 0\leq x\leq 12\}$ . Show that

 $R=\{(a,b)\!:\!a,b\in A,|a-b| ext{ is divisible by 4}\}$  is an

equivalence relation. Find the set of all elements related to 1. Also

write the equivalence class

